

# Useful Functions

## Introduction

Below follows a list of the most useful MATLAB functions provided with the Spectral Analysis of Signals textbook. These custom functions follow the notation and definitions in the book. Some useful MATLAB built-in functions are also listed for convenience. For more detailed information regarding each functions, use the `help functionname` command in MATLAB. At least for the custom functions, it is also possible to inspect the code directly.

## Custom functions

- `phi=argamse(gamma,a,L)`  
Generates  $L$  samples of an ARMA spectral density function  $\phi$  from the ARMA coefficients  $\gamma$  and  $a$ .
- `order=armaorder(mvec,sig2,N,nu)`  
Order estimation for a generic ARMA model using: AIC, AICc, GIC, and BIC.
- `phi=armase(b,a,sig2,L)`  
Generates  $L$  samples of an AR(MA) spectral density function  $\phi$  from the AR(MA) polynomial coefficients  $B$  and  $A$ , and the input noise variance  $\sigma^2$ .
- `phi=bartlettse(y,M,L)`  
The Bartlett spectral estimator for estimating the power spectral density (PSD).
- `phi=btse(y,w,L)`  
The Blackman-Tukey spectral estimator for estimating the power spectral density (PSD).
- `phi=capon(y,m,L)`  
The Capon spectral estimator for estimating the power spectral density (PSD).
- `phi=correlogramse(y,L)`  
The correlogram spectral estimator for estimating the power spectral density (PSD).
- `phi=daniellse(y,J,L)`  
The Daniell spectral estimator for estimating the power spectral density (PSD).
- `w=esprit(y,n,m)`  
The ESPRIT method for frequency estimation.
- `[a,varphi]=freqaphi(y,w)`  
Finds the least-squares amplitude and phases for sinusoidal data once the frequencies have been estimated. Uses equation (4.3.8).
- `w=hoyw(y,n,L,M)`  
The Higher-Order Yule-Walker method for frequency estimation.
- `[beta,relMSE,yHat]=lsa(y,w)`  
Computes the complex amplitudes of sinusoidal components given the frequencies by a least-squares fit to the data.

- `[a,sig2]=lsar(y,n)`  
The covariance Least-Squares AR method, given by equation (3.4.12) with  $N_1 = n + 1$  and  $N_2 = N$ .
- `[a,b,sig2]=lsarma(y,n,m,K)`  
The two-stage Least-Squares ARMA method, given in section (3.7.2)
- `w=minnorm(y,n,m)`  
The Root Min-Norm method for frequency estimation.
- `w=music(y,n,m)`  
The Root MUSIC method for frequency estimation.
- `[a,gamma]=mywarma(y,n,m,M)`  
The modified Yule-Walker ARMA method given by equation (3.7.8) together with the AR coefficients estimated using the overdetermined set of equation (3.7.4), where  $W$  is the identity matrix.
- `phi=periodogramse(y,v,L)`  
The windowed periodogram spectral estimator for estimating the power spectral density (PSD).
- `phi=rfb(y,K,L)`  
The statically stable Refined Filter Bank spectral estimator estimating the power spectral density (PSD).
- `order=sinorder(mvec,sig2,N,nu)`  
Order estimation for sinusoidal models using: AIC, AICc, GIC, and BIC.
- `phi=welchse(y,v,K,L)`  
The Welch spectral estimator for estimating the power spectral density (PSD).
- `[a,sig2]=yulewalker(y,n)`  
The Yule-Walker AR method given by equation (3.4.2).

## MATLAB built-in functions

- `Y = fft(X)`  
Computes the discrete Fourier transform (DFT) of  $X$  using a fast Fourier transform (FFT) algorithm.
- `Y = fftshift(X)`  
Rearranges the outputs of `fft`, `fft2`, and `fftn` by moving the zero-frequency component to the center of the array.
- `Y = filter(X)`  
Filters the data in vector  $X$  with the filter described by vectors  $A$  and  $B$  to create the filtered data  $Y$ .
- `X = rand(N,1)`  
Returns an N-by-1 matrix (vector) of uniformly distributed independent random numbers.
- `X = randn(N,1)`  
Returns an N-by-1 matrix (vector) of normally distributed independent random numbers (white Gaussian noise).

- `r = roots(p)`  
Returns the roots of the polynomial represented by the vector  $p$ , as a column vector.
- `subplot(n,m,p)`  
Divides the current figure into an  $m$ -by- $n$  grid and creates an axes for a subplot in the position specified by  $p$ .
- `[U,S,V]=svd(X)`  
Singular value decomposition. Produces a diagonal matrix  $S$ , of the same dimension as  $X$  and with nonnegative diagonal elements in decreasing order, and unitary matrices  $U$  and  $V$  so that  $X = USV^*$ .
- `zplane(b,a)`  
Plots the poles and zeros of a discrete-time system (AR/ARMA etc) in the complex plane. Note that the inputted coefficient vectors must be row vectors.