

图论作业221025

2. 设 T 有 n 个 4 度顶点

$$2x(n+12) = 4n + 9 + 3 \times 3$$

$$n = 2$$

3. 设 T 有 n 片树叶

$$n + \sum_{i=2}^k i n_i = 2x(n + \sum_{i=2}^k n_i - 1)$$

$$\sum_{i=3}^k (i-2) n_i = n - 2$$

$$n = \sum_{i=3}^k (i-2) n_i + 2$$

7. 设 G 的连通分支为 G_1, G_2, \dots, G_k . G_i 是树, $i=1, 2, \dots, k$

对 $G_i, |V(G_i)| = n_i, |E(G_i)| = m_i$

$$n_i = m_i + 1, \sum_{i=1}^k n_i = n = |V(G)|, \sum_{i=1}^k m_i = m = |E(G)|$$

$$n = \sum_{i=1}^k n_i = \sum_{i=1}^k (m_i + 1) = m - k. \text{ 得证}$$