

# Energy management strategies for reducing a building's electricity costs after a PV installation

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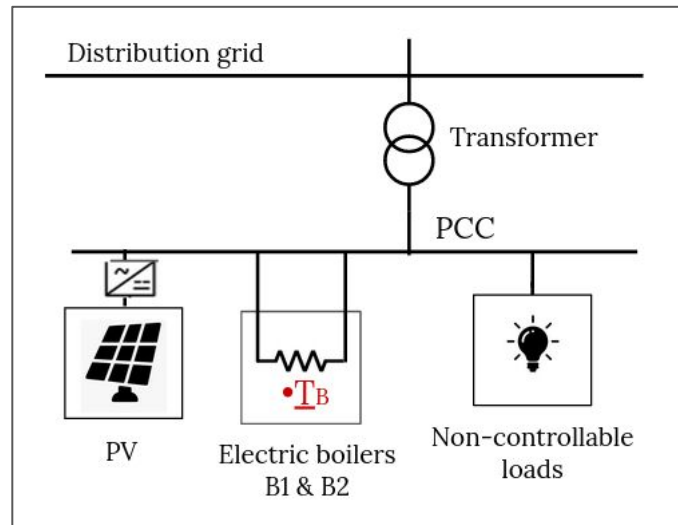
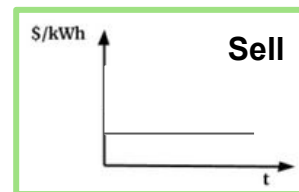
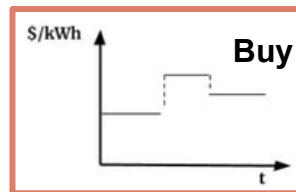
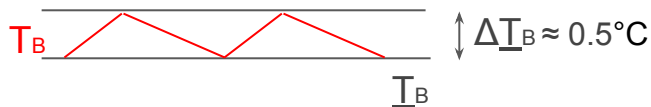
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# Baseline scenario

Assumptions:

- Variable buy price > sell price
- Two electric boilers, controlled by a thermostat fixing their temperature within  $[\underline{T}_B; \underline{T}_B + \Delta T_B]$



# EMS strategies

designed to reduce building's electricity bill.

## Strategy 1: Myopic control of boilers for self-consumption

Rule-based logic : maintain boilers between Temp bounds and supply PV surplus to boilers to the extent possible

at each timestep  $h$ :

**Inputs (5):**  $p_{PCC}$ ,  $T_{B1}$ ,  $p_{B1}$ ,  $T_{B2}$ ,  $p_{B2}$

(set hysteresis state)

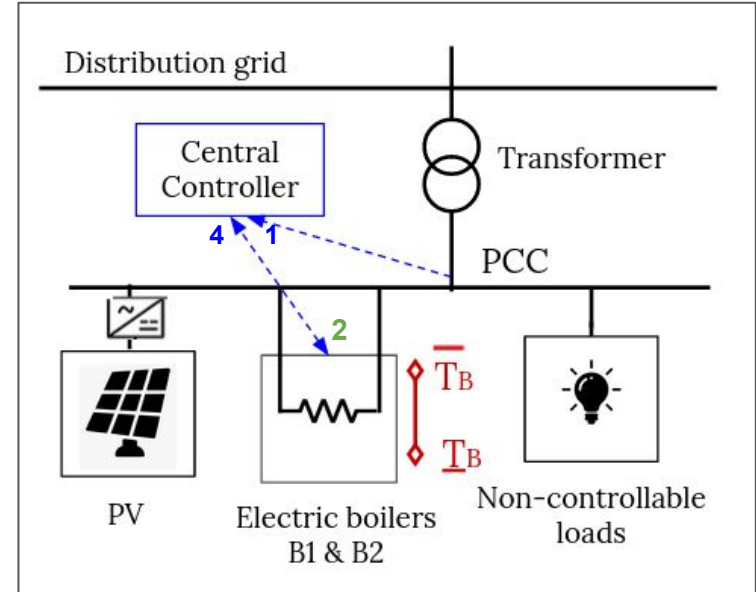
(max supply if boiler at critical state)

(else supply using surplus)

```

 $p_x = p_{PCC}[h] - (p_{B1}[h] + p_{B2}[h])$ 
sort  $T_B[h]$  in ascending order
for each boiler  $k$  do
  set  $s_{B,k}[h]$  ( $T_{B,k}[h]$ ,  $s_{B,k}[h-1]$ )
  if  $s_{B,k}[h] = 1$  then
     $u_{B,k} \leftarrow \bar{P}_k$ 
     $p_x = p_x + u_{B,k}$ 
  else
    if  $p_x > 0$  then
       $e_k^T[h] = \max(0, \bar{T}_{B,k} - T_{B,k}[h])$ 
       $u_{B,k} \leftarrow \max[-C_{B,k} \frac{e_k^T[h]}{\Delta t}, \bar{P}_k, -p_x]$ 
       $p_x = p_x + u_{B,k}$ 
    end
  end
end
    
```

**Outputs (2):**  $u_{B1}$ ,  $u_{B2}$  (boiler commands)



Limitations: 1) myopic approach, 2) boiler model does not account for heat demand, 3) limited flexibility

## Strategy 2: Myopic control of boilers & battery

Same rule-based control for boilers + battery backup:

→ Only charged when boilers at their max Temp or max Power

→ Discharged when negative surplus.

at each timestep  $h$ :

**Inputs (7):**  $p_{bat}$ ,  $x_{bat}$ ,  $p_{PCC}$ ,  $T_{B1}$ ,  $p_{B1}$ ,  $T_{B2}$ ,  $p_{B2}$

$$p_x = p_{PPC}[h] - (p_{B1}[h] + p_{B2}[h] + p_{bat}[h])$$

take care of boilers as usual

if  $p_x \geq 0$  then

$$u_{bat} \leftarrow \max\left[\frac{x_{bat}[h] - \bar{C}_{bat}}{\Delta t}, \bar{P}_{bat}^{ch}, -p_x\right] \quad (\text{charge battery})$$

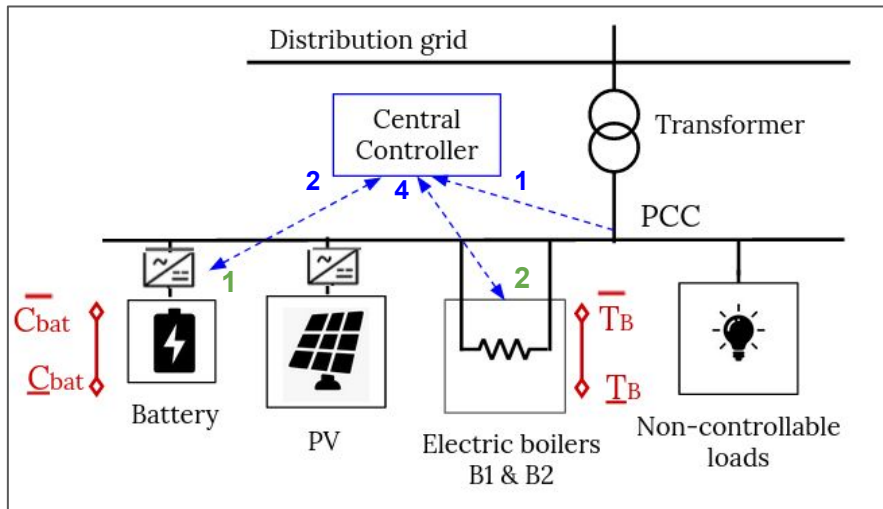
else

$$u_{bat} \leftarrow \min\left[\frac{x_{bat}[h] - \underline{C}_{bat}}{\Delta t}, \bar{P}_{bat}^{disch}, -p_x\right] \quad (\text{discharge battery})$$

end

return Control variables

**Outputs (3):**  $u_{bat}$ ,  $u_{B1}$ ,  $u_{B2}$  (battery & boiler commands)



## Strategy 3: Model Predictive Control with boilers as controllable loads

At each time  $h$ , controller applies the first iteration of the solution of the following OP:

*(Minimize cost)*

$$\min_{\mathbf{u}_B, \mathbf{T}_B, p_g} \sum_{h=t}^{t+H-1} C_{buy}[h] \max(0, +p_g[h]) - C_{sell}[h] \max(0, -p_g[h])$$

*s.t.*

*(Power balance constraint)*

$$p_g[h] + \hat{p}_x[h] + u_{B1}[h] + u_{B2}[h] = 0$$

for  $k = 1, 2 :$

*(Boiler models and power and temperature bounds)*

$$T_{B,k}[h+1] = T_{B,k}[h] - A u_{B,k}[h] + B \frac{\hat{E}_{B,k}[h]}{T_{B,k}[h]} - C \hat{E}_{B,k}[h]$$

$$\bar{P}_{B,k} \leq u_{B,k}[h] \leq 0$$

$$\underline{T}_{B,k} \leq T_{B,k}[h] \leq \bar{T}_{B,k}$$

# Strategy 4: Model Predictive Control with battery & boilers as controllable loads

At each time  $h$ , controller applies the first iteration of the solution of the following OP:

*(Minimize cost)*

*(Power balance constraint)*

*(Battery model and power and SoC bounds)*

*(Boiler models and power and temperature bounds)*

$$\min_{\mathbf{u}_B, \mathbf{T}_B, u_{bat}, x_{bat}} \sum_{h=t}^{t+H-1} C_{buy}[h] \max(0, +p_g[h]) - C_{sell}[h] \max(0, -p_g[h])$$

s.t.

$$p_g[h] + \hat{p}_x[h] + u_{B1}[h] + u_{B2}[h] + u_{bat}[h] = 0$$

$$x_{bat}[h+1] = x_{bat}[h] + u_{bat}[h]\Delta t$$

$$\underline{C}_{bat} \leq x_{bat}[h] \leq \overline{C}_{bat}$$

$$\overline{P}_{bat}^{ch} \leq u_{bat}[h] \leq \overline{P}_{bat}^{disch}$$

for  $k = 1, 2$ :

$$T_{B,k}[h+1] = T_{B,k}[h] - A u_{B,k}[h] + B \frac{\hat{E}_{B,k}[h]}{T_{B,k}[h]} - C \hat{E}_{B,k}[h]$$

$$\overline{P}_{B,k} \leq u_{B,k}[h] \leq 0$$

$$\underline{T}_{B,k} \leq T_{B,k}[h] \leq \overline{T}_{B,k}$$

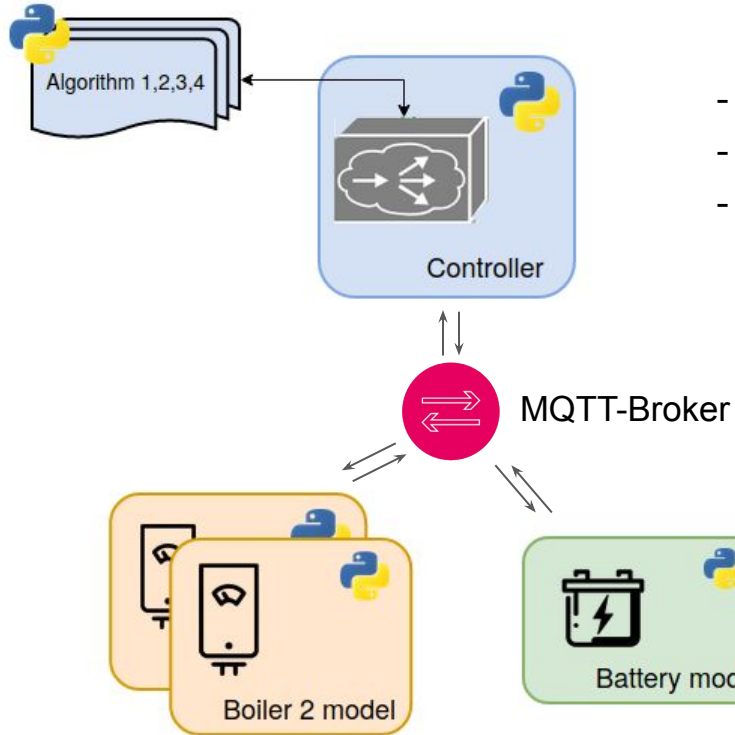
Limitations: 1) need for forecasts (PV, loads, heat demand), 2) need for more computing time



# Simulation framework

to allow us to compare all of the controller algorithms in the same building conditions.

## Software implementation



- *Listen* to units sensors
- *Run* algorithm
- *Publish* control commands

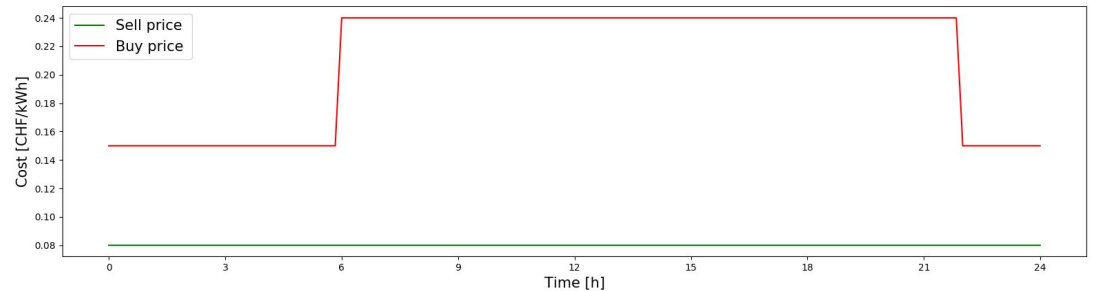
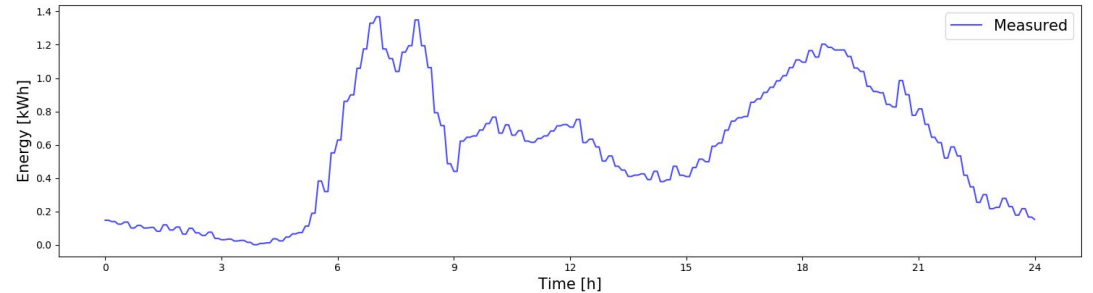
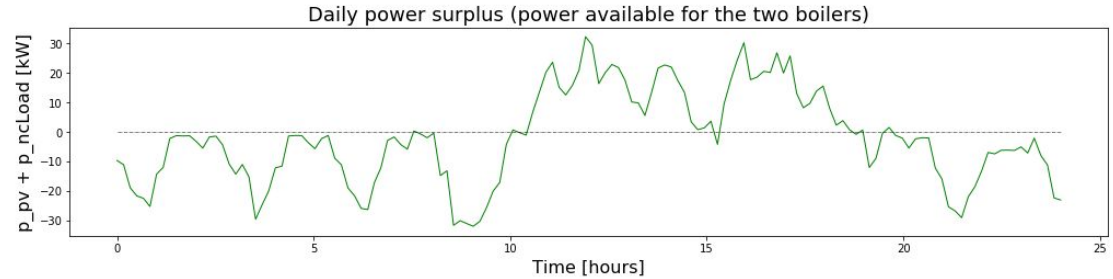
- *Simulate* entities state evolution
- *Publish* Power and Temp/Soc
- *Listen* to controller's commands

## Building case

- Building's power profile (without accounting for boilers)
- two 800L boilers ( $P_{\max} = -7.6$  kW)
  - [40°C; 50°C]
  - [30°C; 60°C]

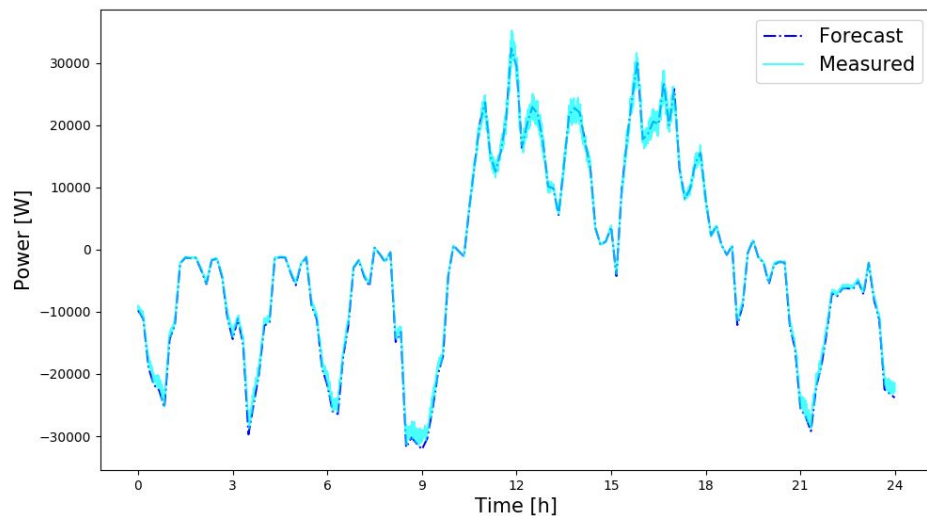
Boiler's heat demand for water usage:

- 5 kWh battery ( $P_{\max/\min} = \pm 5$  kW)
- Time-of-Use tariff:

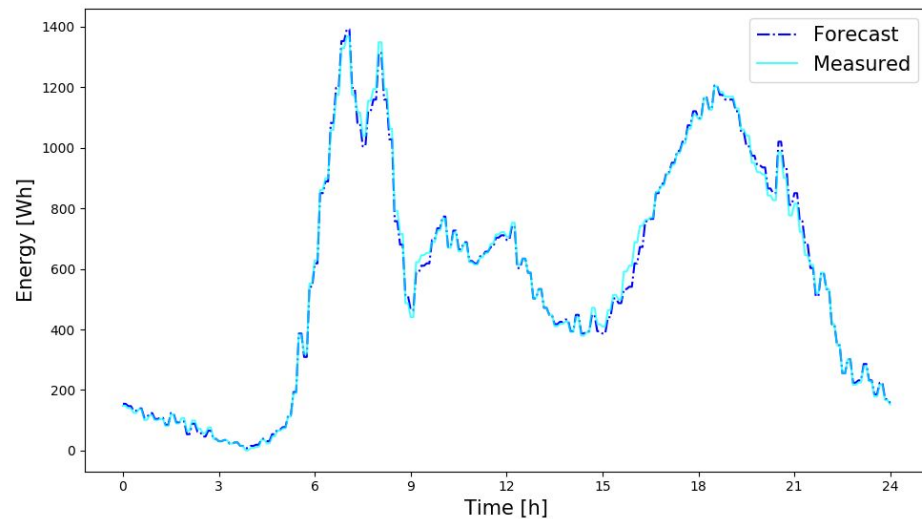


## Forecasts and disturbances

Building power state



Building heat demand

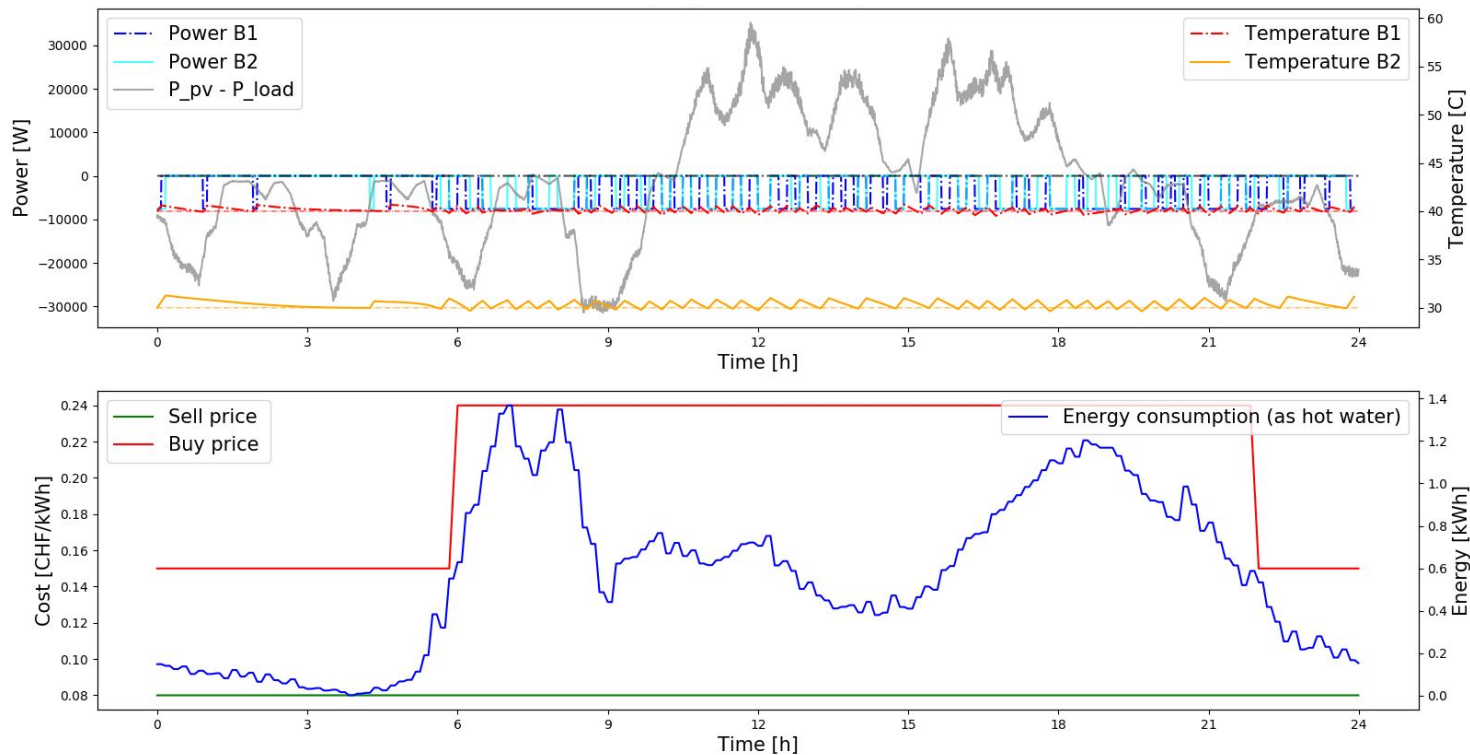


# Results

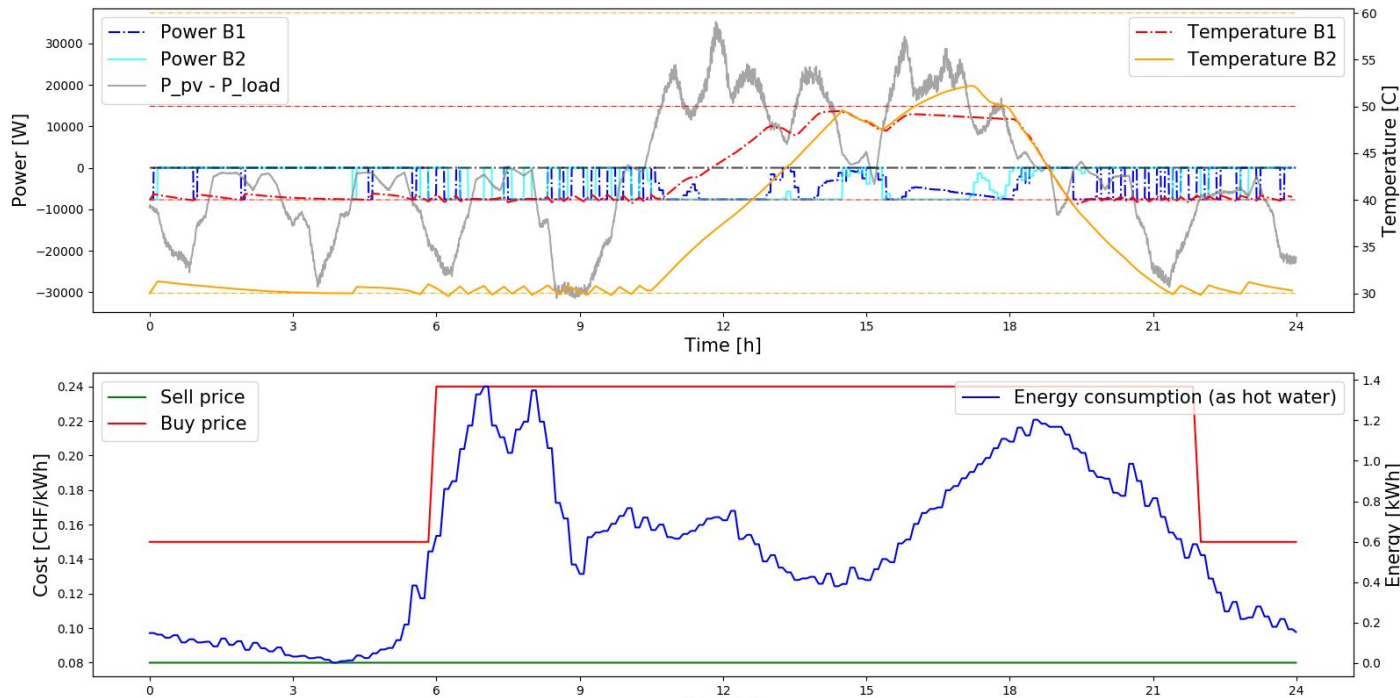
Comparing behaviour and cost reduction of all four strategies

# Baseline scenario

Daily cost: **47.91 CHF**



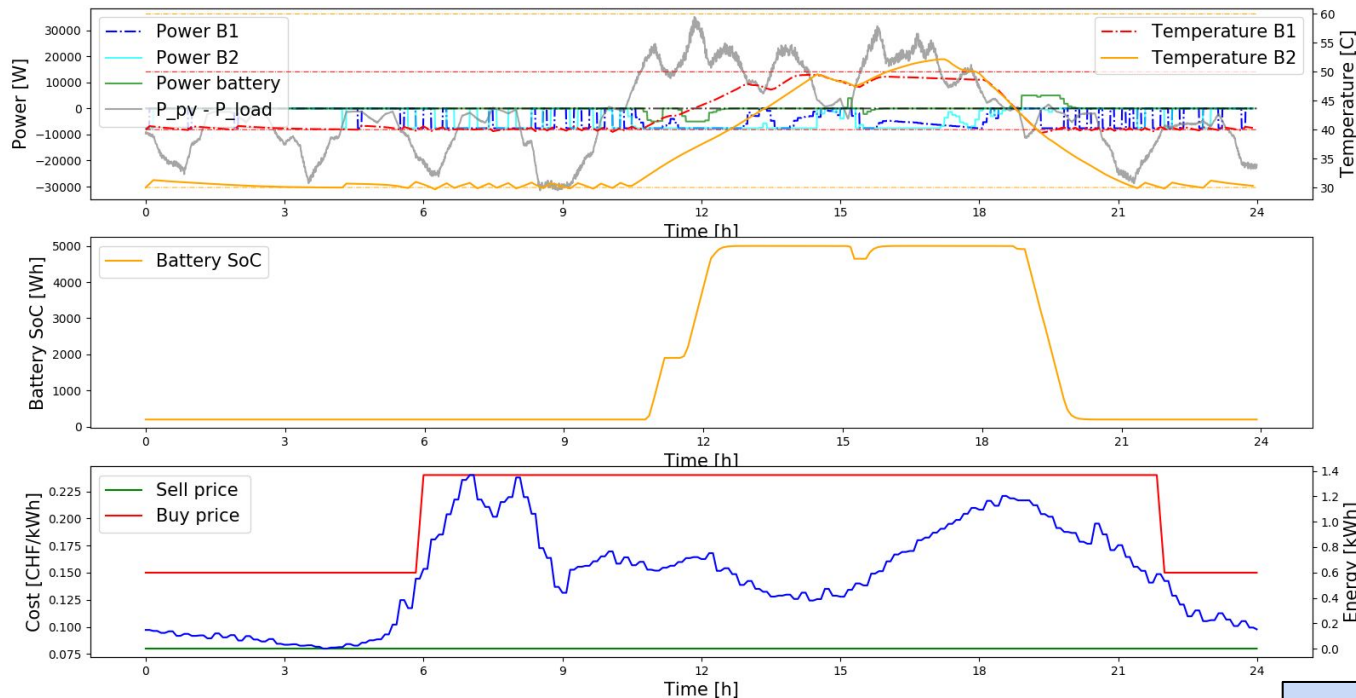
## Strategy 1: myopic control boilers



Daily cost: 45.93 CHF

**-4.13% reduction over Baseline**

## Strategy 2: myopic control of battery & boilers



Daily cost: 45.22 CHF

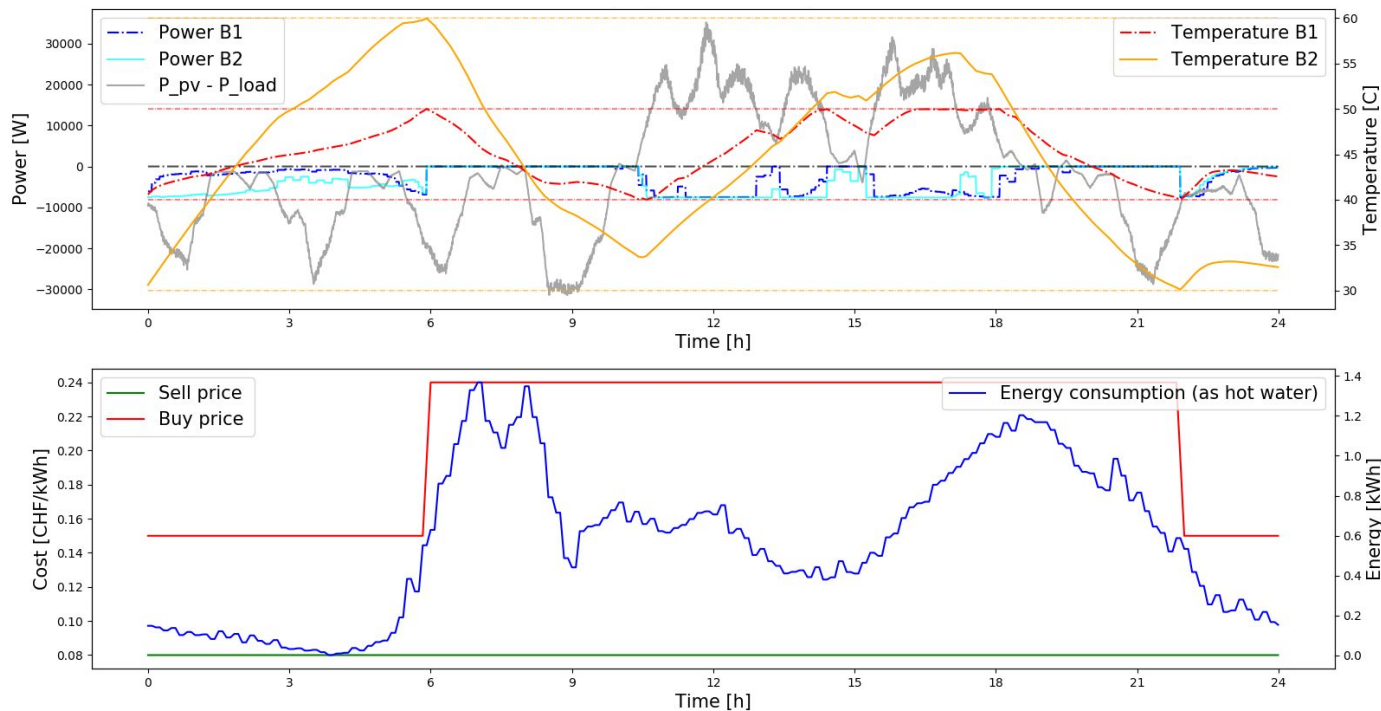
-1.54% over strategy 1

-5.61% over Baseline

6 year battery  
payback time



## Strategy 3: Applying MPC to boilers

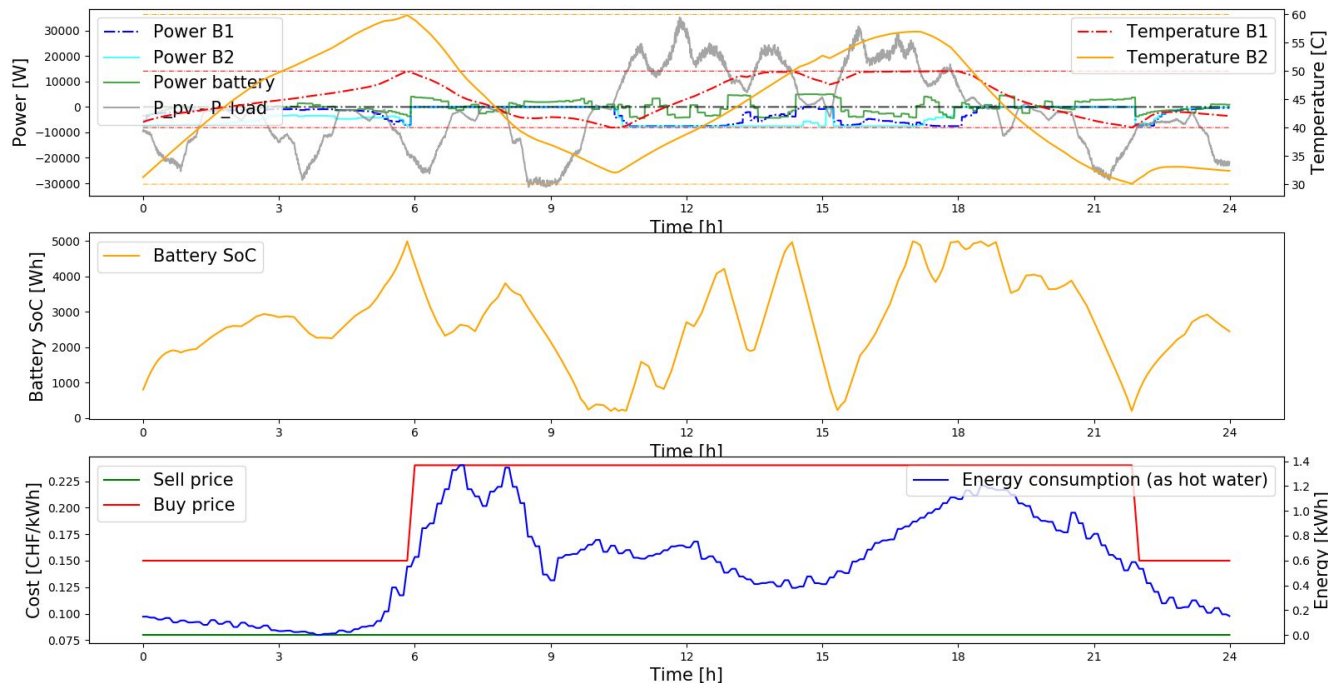


**Daily cost: 39.31 CHF**

**-13.07% over strategy 2**

**-18.0% over Baseline**

## Strategy 4: applying MPC to battery & boilers

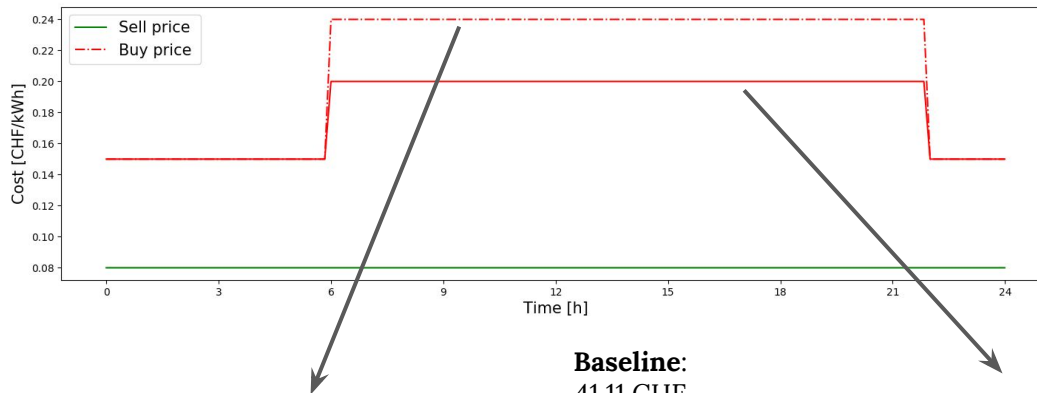


Daily cost: 38.43 CHF

**-2.24% over strategy 3**

**-19.79% over Baseline**

## Reducing price variability



**Baseline:**  
47.91 CHF

	Strategy 1 45.93 CHF	Strategy 2 45.22 CHF	Strategy 3 39.31 CHF	Strategy 4 38.43 CHF
Baseline	4.13%	5.61%	18.0%	19.79%
Strategy 1	×	1.54%	14.41%	16.33%
Strategy 2	×	×	13.07%	15.02%
Strategy 3	×	×	×	2.24%

MPC reduces costs by 14.41%  
over a myopic control of boilers

**Baseline:**  
41.11 CHF

	Strategy 1 40.02 CHF	Strategy 2 39.49 CHF	Strategy 3 35.55 CHF	Strategy 4 35.05 CHF
Baseline	2.65%	3.94%	13.52%	14.74%
Strategy 1	×	1.32%	11.17%	12.42%
Strategy 2	×	×	9.98%	11.24%
Strategy 3	×	×	×	1.41%

MPC reduces costs by 11.17%  
over a myopic control of boilers

# Conclusion

- **4.13%** estimated bill reduction with a primary EMS (communication + microcontroller + myopic algo).
- Battery can bring further savings to such EMS, after **6 years**
- As expected, MPC proves to be more effective (**18%** reduction).
  - MPC implementation computationally costly (100 s per iteration)
  - MPC satisfactory results boosted by:
    - High variability in the pricing structure.
    - High accuracy in forecasts

# Appendix A

## Boiler model

$$T_B[h+1] = T_B[h] - \frac{\Delta t}{C_B} u_B[h] - \frac{E[h]}{C_B} + \frac{E[h] T_{inc}}{C_B} \frac{1}{T_B[h]} \quad (5)$$

The boiler temperature state depends on 1) its present temperature ( $T_B[h]$ ), 2) the temperature increase due to the supplied power ( $\frac{\Delta t}{C_B} u_B[h]$ ), 3) the temperature decrease caused by the energy demanded by the building in terms of hot water ( $\frac{E[h]}{C_B}$ ) and 4) the temperature decrease due to the incoming cold water, whose volume will depend on the energy drained but also on boiler's temperature ( $\frac{E[h] T_{inc}}{C_B} \frac{1}{T_B[h]}$ ).

# Appendix B

## Linearizing MPC formulation

$$\min_{\mathbf{u}_B, \mathbf{T}_B, p_g} \sum_{h=t}^{t+H-1} C_{buy}[h] p_g^+[h] - C_{sell}[h] p_g^-[h]$$

s.t.

$$p_g[h] + \hat{p}_x[h] + u_{B1}[h] + u_{B2}[h] = 0$$

$$p_g^-[h] = \max(0, -p_g[h])$$

$$p_g^+[h] = \max(0, p_g[h])$$

for  $k = 1, 2$ :

$$T_{B,k}[h+1] = T_{B,k}[h] - A u_{B,k}[h] + B \frac{\hat{E}_{B,k}[h]}{\underline{T}_{B,k}[h]} - C \hat{E}_{B,k}[h]$$

$$\bar{P}_{B,k} \leq u_{B,k}[h] \leq 0$$

$$\underline{T}_{B,k} \leq T_{B,k}[h] \leq \bar{T}_{B,k}$$

Nonlinear version

$$\min_{\mathbf{u}_B, \mathbf{T}_B, p_g, \phi, \epsilon_B} \sum_{h=t}^{t+H-1} \phi + w (\epsilon_{B1} + \epsilon_{B2})$$

s.t.

$$p_g[h] + \hat{p}_x[h] + u_{B1}[h] + u_{B2}[h] = 0$$

$$\phi \geq C_{buy}[h] p_g[h]$$

$$\phi \geq C_{sell}[h] p_g[h]$$

for  $k = 1, 2$

$$T_{B,k}[h+1] = T_{B,k}[h] - A u_{B,k}[h] + B \hat{E}_{B,k}[h] \epsilon_{B,k} - C \hat{E}_{B,k}[h]$$

$$\epsilon_{B,k} \geq \tan_i\left(\frac{1}{\underline{T}_{B,k}[h]}\right) \quad \text{for } i \in [\underline{T}_{B,k}; \bar{T}_{B,k}]$$

$$\bar{P}_{B,k} \leq u_{B,k}[h] \leq 0$$

$$\underline{T}_{B,k}[h+1] \leq T_{B,k}[h] \leq \bar{T}_{B,k}[h+1]$$

Linear version

$$\begin{aligned} T_{B,k}[h+1] &= T_{B,k}[h] - A u_{B,k}[h] + B \hat{E}_{B,k}[h] \epsilon_{B,k} - C \hat{E}_{B,k}[h] \\ \epsilon_{B,k} &= \max\left(\tan_i\left(\frac{1}{\underline{T}_{B,k}[h]}\right) \text{ for } i \in [\underline{T}_{B,k}; \bar{T}_{B,k}]\right) \end{aligned}$$

## Strategy 1: Myopic control of boilers

Rule-based logic : at each timestep, maintain boilers between temp bounds and supply PV power surplus to boilers to the extent possible

Inputs: Power PCC,  
B1, B2 power & temp

For each boiler

Setting hysteresis  
state  $s_{B,k}[h]$

Supplying if boiler at  
critical state

Supplying using  
surplus power

Outputs: B1,B2 actions

```

Inputs:  $T_B[h], p_{PCC}[h], p_{B1}[h], p_{B2}[h], s_B[h-1]$ 
Control variables:  $u_B$ 
Initialize: for all  $k$ : if  $(T_{B,k}[0] < T_{\Delta,k})$ :  $s_{B,k}[0] = 1$ , else:  $s_{B,k}[0] = 0$ 
Start
 $u_B \leftarrow 0$ 
 $p_x = p_{PCC}[h] - (p_{B1}[h] + p_{B2}[h])$ 
sort  $T_B[h]$  in ascending order
for each boiler  $k$  do
  if  $T_{B,k}[h] \geq \bar{T}_{B,k} + T_{\Delta,k}$  then
    |  $s_{B,k}[h] = 0$ 
  end
  if  $T_{B,k}[h] \leq \bar{T}_{B,k}$  then
    |  $s_{B,k}[h] = 1$ 
  else
    |  $s_{B,k}[h] = s_{B,k}[h-1]$ 
  end
  if  $s_{B,k}[h] = 1$  then
    |  $u_{B,k} \leftarrow \bar{P}_k$ 
    |  $p_x = p_x + u_{B,k}$ 
  else
    | if  $p_x > 0$  then
      |  $c_k^T[h] = \max(0, \bar{T}_{B,k} - T_{B,k}[h])$ 
      |  $u_{B,k} \leftarrow \max[-C_B \frac{c_k^T[h]}{\Delta t}, \bar{P}_k, -p_x]$ 
      |  $p_x = p_x + u_{B,k}$ 
    end
  end
end
end
return Control variables
    
```

