

Introduction to MATLAB

Week 2 Lecture 2

Polina Cherepanova

cherepanova@princeton.edu

Matrix operations: Addition and subtraction

```
>> mat_1=[6:2:10;20:-2:16]  
      mat_2=[3:5;-5:-3]
```

```
mat_1 =
```

```
6   8  10  
20  18 16
```

```
mat_2 =
```

```
3   4   5  
-5 -4 -3
```

```
>> mat_add=mat_1+mat_2
```

```
mat_add =
```

```
9 12 15  
15 14 13
```

```
>> mat_sub=mat_1 - mat_2
```

```
mat_sub =
```

```
3   4   5  
25 22 19
```

Matrix operations: Scalar multiplication

```
>> mat_3 = [1:2:5; 5:-2:1]
>> scalar_3 = 5
>> scalar_mult = mat_3 * scalar_3
```

```
>> mat_3=[1:2:5; 5:-2:1]
scalar_3=5
scalar_mult=mat_3*scalar_3
```

mat_3 =

1	3	5
5	3	1

scalar_3 =

5

scalar_mult =

5	15	25
25	15	5

Matrix operations: Matrix (or vector) multiplication

Keep in mind the dimension of the two matrices for vector multiplication

$$[A]_{m \times n} \times [B]_{n \times m} = [C]_{m \times m}$$

For example:

	>> mat_4 =	>> mat_5 =	>> vector_mult =
>> mat_4=[3:5; 5:7]	3 4 5	2 3	52 64
>> mat_5=[2:3; 4:5; 6:7]	5 6 7	4 5	76 94
>> vector_mult=mat_4*mat_5		6 7	

Matrix operations: Element-wise multiplication

Both the matrices should be of the same size.

For example:

```
>> mat_6=[3:5; 5:7]
```

```
>> mat_7=[2:4; 4:6]
```

```
>> element_by_element_mult=mat_6.*mat_7
```

```
>> mat_6 =
```

```
3  4  5  
5  6  7
```

```
>> mat_7 =
```

```
2  3  4  
4  5  6
```

```
>> element_by_element_mult =
```

```
6  12  20  
20  30  42
```

Matrix operations: Transpose of a matrix

Flips the dimensions of the matrix

$$[A]_{m \times n} \rightarrow [B]_{n \times m}$$

```
>> mat_8=[3:5; -7:-5]  
>> mat_9=mat_8'
```

```
>> mat_8 =
```

```
3    4    5  
-7   -6   -5
```

```
>> mat_9 =
```

```
3    -7  
4    -6  
5    -5
```

Concatenating matrices: Horizontal

- Combine two matrices horizontally
- If you have 2 matrices A and B then to horizontally concatenate them:

$C=[A \ B]$ or $C=\text{horzcat}(A, B)$

```
>> mat_10=ones(3,2)*4  
>> mat_11=randi(7,3,2)  
>> horz_cat_1=[mat_10 mat_11]  
>> horz_cat_2=horzcat(mat_10,mat_11)
```

```
>> mat_10 =
```

```
4  4  
4  4  
4  4
```

```
>> mat_11 =
```

```
6  7  
7  5  
1  1
```

```
>> horz_cat_1 =
```

```
4  4  6  7  
4  4  7  5  
4  4  1  1
```

```
>> horz_cat_2 =
```

```
4  4  6  7  
4  4  7  5  
4  4  1  1
```

Concatenating matrices: Vertical

- Combine two matrices vertically
- If you have 2 matrices A and B then to horizontally concatenate them:

$C=[A; B]$ or $C=\text{vertcat}(A, B)$

```
>> mat_12=ones(2,3)*4  
>> mat_13=randi(7,2,3)  
>> vert_cat_1=[mat_12; mat_13]  
>> vert_cat_2=vertcat(mat_12,mat_13)
```

>> mat_12 =

4	4	4
4	4	4

>> mat_13 =

7	6	3
4	1	7

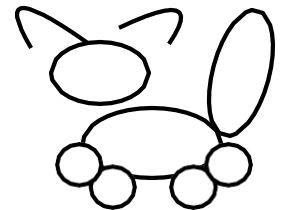
>>vert_cat_1 =

4	4	4
4	4	4
7	6	3
4	1	7

>>vert_cat_2 =

4	4	4
4	4	4
7	6	3
4	1	7

$\text{cat}(\text{DIM}, A, B)$



mean of an array

```
>> new_matrix= [2:2:16; 10:-2:-5; 3:3:24];
```

```
>> new_matrix =
```

```
2   4   6   8  10  12  14  16
10   8   6   4   2   0  -2  -4
3   6   9  12  15  18  21  24
```

By default, MATLAB takes
mean across each column

2	4	6	8	10	12	14	16
10	8	6	4	2	0	-2	-4
3	6	9	12	15	18	21	24

```
mean(new_matrix)
```

```
ans =
```

```
5 6 7 8 9 10 11 12
```

What if you want to find the
mean across each row?

```
mean(new_matrix,2)
```

```
ans =
```

```
9
```

```
3
```

```
13.5
```

2=across each row

1=across each column

2	4	6	8	10	12	14	16
10	8	6	4	2	0	-2	-4
3	6	9	12	15	18	21	24

sort

- To sort an array, you can use the inbuilt MATLAB function sort
- `mat_14 = [10 5 2 3 6 7 0 -1 -12 7 6]`
- `sort(mat_14)`

`ans =`

`[-12 -1 0 2 3 5 6 6 7 7 10]`

Can sort in descending order with: `sort(mat_14, 'descend')`

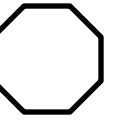
unique

- Sometimes your goal is to find the unique elements in an array
- For e.g. in the previous example 6 and 7 appeared twice.
- To find the unique elements, use the function 'unique'.
- `mat_14=[10 5 2 3 6 7 0 -1 -12 7 6]`
- `unique(mat_14)`
- `ans =`

-12 -1 0 2 3 5 6 7 10

Note that the 'unique' function also sorts the output

reshape



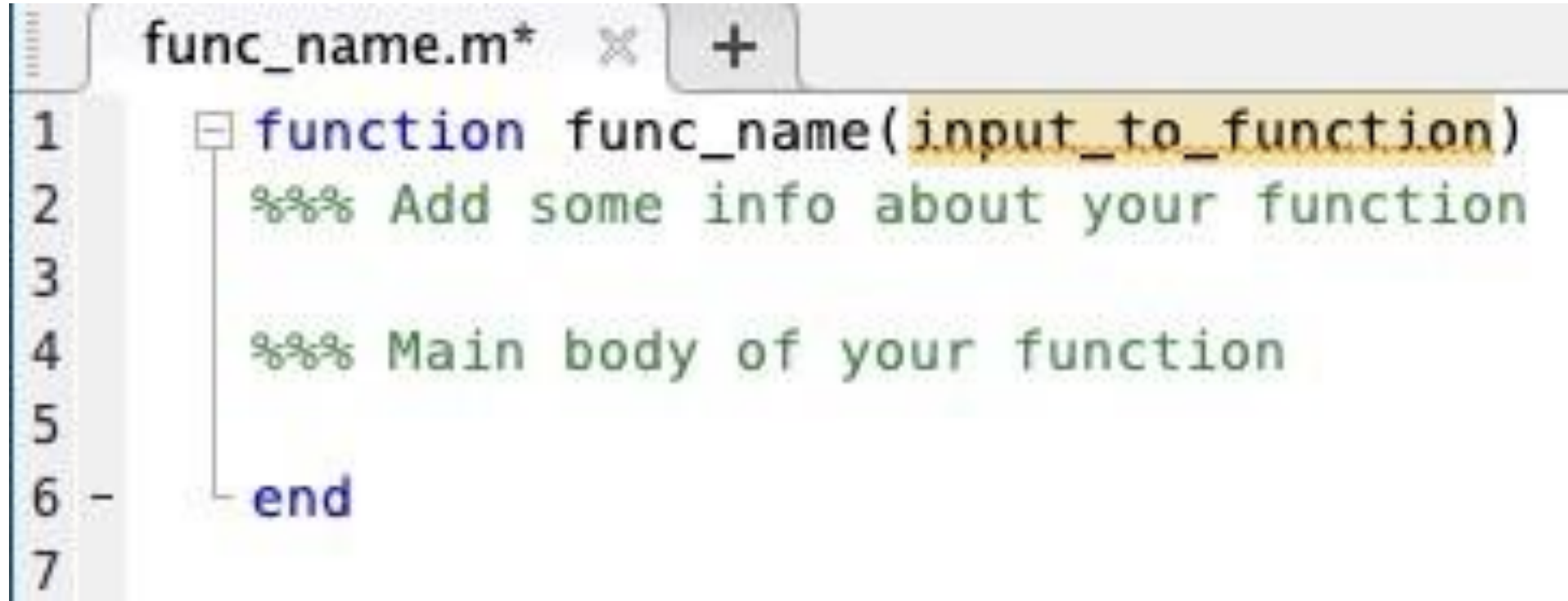
- Using reshape function, we can reshape a matrix to another size
- `to_reshape_array=[1:10]`
- `reshape(to_reshape_array, [5, 2])`
- `ans =`

1	6
2	7
3	8
4	9
5	10

Functions in MATLAB

- You have already used many in-built MATLAB functions such as:
 - sort
 - length
 - mean
 - unique
 - disp
- You can also make your own functions in MATLAB pretty easily

Syntax for functions

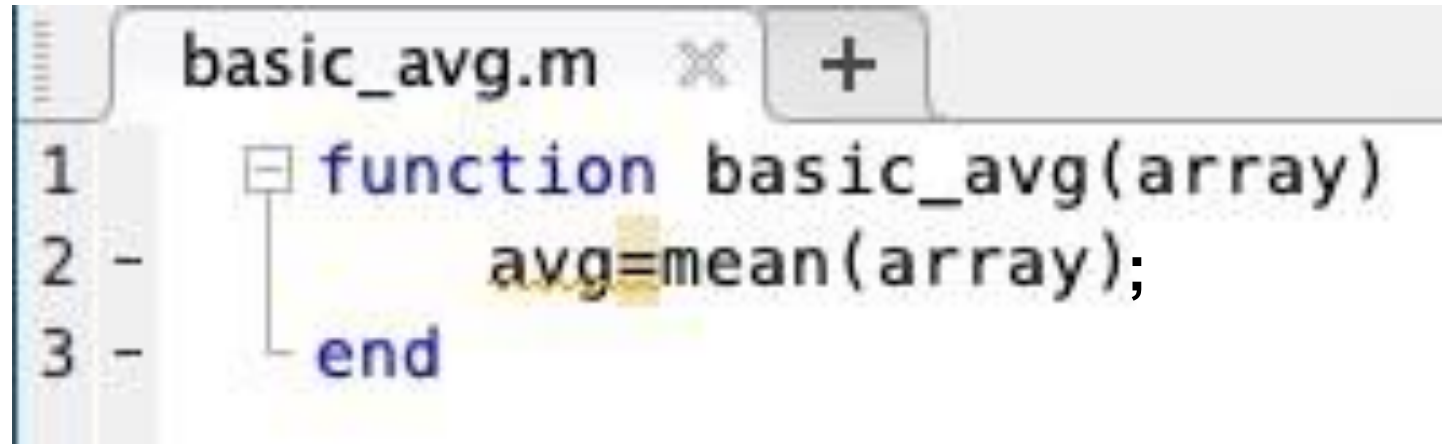
A screenshot of a MATLAB editor window titled 'func_name.m*'. The window shows a function definition starting with 'function' on line 1, followed by the function name 'func_name' and its input argument 'input_to_function' in parentheses. Line 2 contains a comment '%%% Add some info about your function'. Line 4 contains another comment '%%% Main body of your function'. Line 6 ends with 'end'. A vertical line connects the 'function' keyword to the 'end' keyword. The input argument 'input_to_function' is highlighted in yellow. The editor has a line number margin on the left with numbers 1 through 7. A minus sign is visible next to line 6.

```
1 function func_name(input_to_function)
2     %%% Add some info about your function
3
4     %%% Main body of your function
5
6 - end
7
```

Important:

- 1) Rules for naming a function are same as rules for naming a variable
- 2) Functions go at the bottom of MATLAB scripts

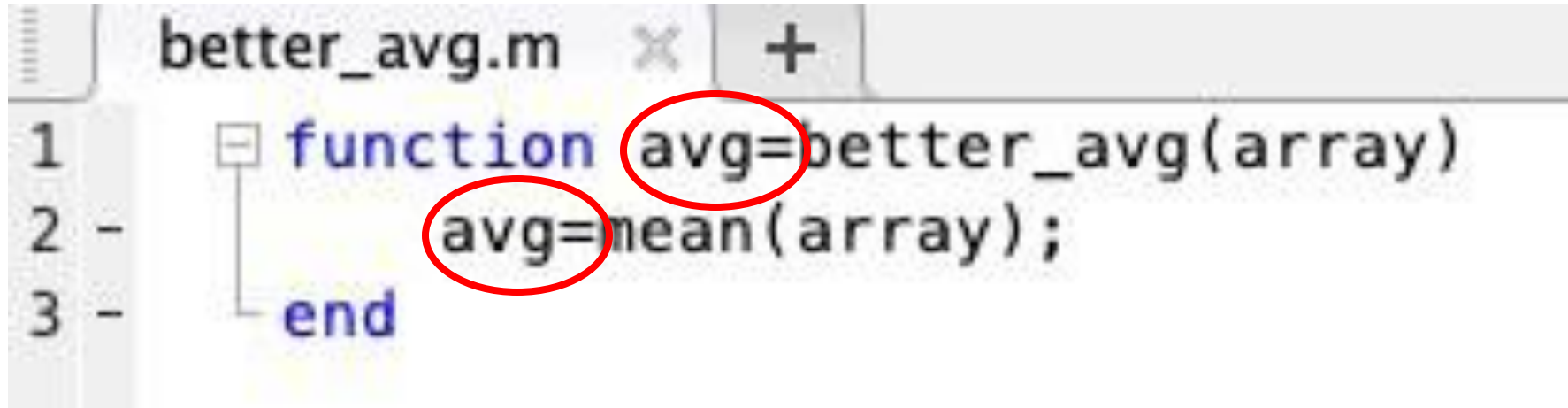
Example: basic_average



```
basic_avg.m  ✕  +  
1  function basic_avg(array)  
2  -      avg=mean(array);  
3  -  end
```

Drawback: The output of this function is not stored as a separate variable, and so we can't access it after running the function.

Store output of the function as a variable



The image shows a MATLAB code editor window titled 'better_avg.m'. The code defines a function 'better_avg' that takes an 'array' as input and returns its mean value. The function is defined as follows:

```
1 function avg=better_avg(array)
2 -     avg=mean(array);
3 - end
```

In the code, the variable 'avg' is circled in red in both the function signature and the assignment statement, highlighting its role as the output variable.

```
>> avg_result = better_avg([9 2 4 6 7 10 11 1 0]);
```


Exercise 1: Write a function to calculate the circumference of a circle

$$\text{circumference} = 2 * \pi * \text{radius}$$

Make a function that takes in the radius of a circle and returns its circumference

```
>> circumference = calc_circ(4.6);  
>> circumference
```

```
circumference =
```

```
28.90
```

Custom functions can call built-in MATLAB functions

```
1 [-] function avgx3 = mean_times_three(array)
2
3     avg = mean(array);
4     avgx3 = avg * 3;
5
6 end
```

Exercise 2: Write the following function:

Make a function that takes in a vector of elements and returns the sum of its unique elements

```
>> output = sum_unique([1 2 2 3 5 1 10 9]);
```

```
>> output
```

```
output =
```

```
30
```

Functions can generate multiple outputs

```
min_max.m  ×  +  
1  function [min_num,max_num]=min_max(array)  
2  -         min_num=min(array);  
3  -         max_num=max(array);  
4  -     end
```

```
>> [min_n, max_n] = min_max([1 2 3 5 6 1 10 7]);
```

```
>> [~, max_n] = min_max([1 2 3 5 6 1 10 7]);
```

Exercise 3: Write a function to return the results of five operations

Make a function that takes in a vector of elements and returns its mean, standard deviation, min, max, and unique elements, all as separate variables.

```
>> [avg, stand_dev, mini, maxi, uniq] = operations([1 2 2 3 5 1 10 9]);
```

```
>> stand_dev
```

```
mini =
```

```
1
```

Exercise 4: Temperature conversion

$$C = \frac{5}{9} (F - 32)$$

$$K = C + 273.15$$

Write a function that takes in a temperature in Fahrenheit and returns two outputs: the converted temperature in Celsius and the converted temperature in Kelvin

Custom functions can call other custom functions

```
1 function avgx3 = mean_times_three(array)
2
3     avg = mean(array);
4     avgx3 = avg * 3;
5
6 end
```

```
1 function avgx3_plus5 = mean_times_three_plus_five(array)
2
3     avgx3 = mean_times_three(array);
4     avgx3_plus5 = avgx3 + 5;
5
6 end
```

Exercise 5:

Write a function that takes in an array of temperatures in Fahrenheit and returns both the average and the range of these temperatures in Celsius.

Hint: call the temperature conversion function you just wrote when coding this new function

```
>> [avg_C, range_C] = temp_operations([65 22 89]);
```