# **Getting Started with Uclid5**

January 2018

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# 1. Introduction

UCLID5 is a modeling language that supports verification and synthesis. The UCLID5 toolchain aims to:

- 1. Enable modeling of finite and infinite state transition systems.
- 2. Verification of safety and hypersafety (k-safety) properties on these systems.
- 3. Allow syntax-guided synthesis of models and model invariants on these transitions systems.

This document serves as introduction to the UCLID5 modeling language and toolchain.

# 1.1. Getting Started: A Simple Uclid5 Model

```
1 module main {
    // Part 1: System description.
    var a, b : int;
     init {
      a = 0;
      b = 1;
    next {
9
     a, b = b, a + b;
10
11
12
    // Part 2: System specification.
13
    invariant a_le_b: a <= b;</pre>
14
15
    // Part 3: Proof script.
16
17
     control {
      unroll (3);
19
      check;
      print _results;
20
21
22 }
```

Example 1.1.: A UCLID5 model that computes the Fibonacci sequence.

A simple UCLID5 module that computes the Fibonacci sequence is shown in Example 1.1. We will now walk through each line in this model to understand the basics of UCLID5.

#### 1. Introduction

The top-level syntactic structure in UCLID5 is a module. All modeling, verification and synthesis code in UCLID5 is contained within modules. In Example 1.1, we have defined one module named main. This module starts on line 1 and ends on line 18. The module can be conceptually split into three parts: a system model, a specification and proof script. In the example, these three conceptual parts are also kept separate in the code. The following subsections will describe each of these sections of the module.

#### The System Model

This part of a UCLID5 module describes the functionality of the transition system that is being modeled: it tells us what the system does.

The first item of interest within the module main are *state variables*. These are declared using the var keyword. The module main declares two state variables: a and b on line 2. These are both of type int, which corresponds to mathematical integers.<sup>2</sup>

The init block appears next and spans lines 4 to 7. It defines the initial values of the states variables in the module. We see that a is initialized to 0 while b is initialized to 1.

The next block appears after this and it defines the transition relation of the module. In the figure, the next statement spans from lines 8 to 10; a is assigned to the (old) value of b, while b is assigned to the value a + b.

#### The System Specification

The specification answers the question: what is the system supposed to do?.

In our example, we have a single invariant that comprises that entire specification. Line 12 defines this invariant. It is named a\_le\_b and as the name suggests, it states that a must be less than or equal to b for every reachable state of the system.

#### The Proof Script

The third and final part of the UCLID5 module is a set of commands to the UCLID5 verification engine. These tell how we should go about proving<sup>3</sup> that the system satisfies itself specification.

The proof script is contained within the control block. The commands here execute the system for 3 steps and check whether all of the systems properties (in this case, we only have one invariant: a\_le\_b) are satisfied for each of these steps.

The command unroll executes the system for 3 steps. This execution generates four proof obligations. These proof obligations ask whether the system satisfies the invariant a\_le\_b in the initial state and in each of the 3 states reached next. The check

<sup>&</sup>lt;sup>1</sup>This is not required by the UCLID5 syntax but is a good design practice.

<sup>&</sup>lt;sup>2</sup>Mathematical integer types, as opposed to the machine integer types present in languages like C/C++ and Java, do not have a fixed bit-width and do not overflow.

<sup>&</sup>lt;sup>3</sup>Note we are using a very broad definition of the word prove here to refer to any systematic method that gives us assurance that the specification is (perhaps partially) satisfied.

command *checks* whether these proof obligations are satisfied and the print\_results prints out the results of these checks.

## 1.2. Installing Uclid5

Public releases of the UCLID5 can be obtained at: https://github.com/uclid-org/uclid/releases. For the impatient, the short version of the installation instructions is: download the archive with the latest release, unzip the archive and add the 'bin/' subdirectory to your PATH.

More detailed instructions for installation are as follows.

#### 1.2.1. Prerequisites

UCLID5 has two prerequisites.

- 1. UCLID5 requires that the Java<sup>TM</sup> Runtime Environment be installed on your machine. You can download the latest Java Runtime Environment for your platform from https://www.java.com.com.
- 2. UCLID5 uses the Z3 SMT solver. You can install Z3 from: https://github.com/Z3Prover/z3/releases. Make sure the 'z3' or 'z3.exe' binary is in your path after Z3 installed. Also make sure, the shared libraries for libz3 and libz3java are in the dynamic library load path (LD LIBRARY PATH on Unix-like systems).

UCLID5 has been tested with Java $^{\rm TM}$  SE Runtime Environment version 1.8.0 and Z3 versions 4.5.1 and 4.6.0.

#### 1.2.2. Detailed Installation Instructions

First, down the platform independent package from https://github.com/uclid-org/uclid/releases.

Next, follow these instructions which are provided for the bash shell running on a Unix-like platform. Operations for Micosoft Windows, or a different shell should be similar.

- Unzip the archive.
  - \$ unzip uclid-0.9.zip.
- Add the uclid binary to your path.
  - \$ export PATH=\$PATH:\$PWD/uclid-0.9/bin/
- Check that the uclid works.
  - \$ uclid

This should produce output similar to the following.

#### 1. Introduction

```
$ uclid

Usage: uclid [options] filename [filenames]
Options:
    -h/--help : This message.
    -m/--main : Set the main module.
    -d/--debug : Debug options.

Error : Unable to find main module.
```

#### 1.2.3. Running Uclid5

Invoke UCLID5 on a model is easy. Just run the uclid binary and provide the model as a command-line argument. When invoked, UCLID5 looks for a module named main and executes the commands in its control block.<sup>4</sup> If no main module is found, UCLID5 will exit with an error, as we saw in the previous section when uclid was invoked without arguments.

Example 1.1 is part of the UCLID5 distribution in the examples/tutorial/ sub-directory. You can run UCLID5 on this model as:

```
$ uclid examples/tutorial/ex1-fib-module.ucl4
```

This should produce the following output.

```
4 assertions passed.
0 assertions failed.
0 assertions indeterminate.
```

# 1.3. Looking Forward

This chapter has provided an brief overview of UCLID5's features and toolchain. The rest of this tutorial will take a more detailed looked at more of UCLID5's features.

<sup>&</sup>lt;sup>4</sup>The --main command line argument can be used to specify a different name for the "main" module.

# 2. Basics: Types and Statements

This chapter will provide an overview of UCLID5's type system and modelling features. Let us start with Example 2.1, a model of a simple arithmetic logic unit (ALU).

## 2.1. Types in Uclid5

Types supported by UCLID5 are of the following kinds:

- 1. int: the type of mathematical integers.
- 2. bool: the Boolean type. This type has two values: true and false.
- 3. by W: The family of bit-vector types parameterized by their width (W).
- 4. enum: enumerated types.
- 5. Tuples and records.
- 6. Array types.

An enumerated type is used in line 4 of Example 2.1. This declares a *type synonym*: cmd\_t is an alias for the enumerated type consisting of three values: add, sub and mov\_imm. The input cmd is then declared to be of type cmd\_t in line 9.

The input valid is of type bool. Register indices r1 and r2 are bit-vectors of width 3 (bv3), while immed, result, r1val and r2val are bit-vectors of width 8 (bv8).

Line 7 declares a type synonym for a record. It declares result\_t as being a record consisting of two fields: a Boolean field valid and a bit-vector field value. The output result is declared to be of type result\_t on Line 13.

The final point-of-interest, type-wise, in Example 2.1 is line 15. The state variable regs is declared to be of type array: indices to the array are of type bv3 and elements of the array are of type bv8. This is used to model an 8-entry register file, where each register is a bit-vector of width 8.

#### 2.2. Statements in Uclid5

Example 2.1 also provides examples of the most commonly used statements in UCLID5.

```
1 // Model of an ALU
2 module main
3 {
     // Synonym for an enumerated type.
4
    type cmd_t = enum { add, sub, mov_imm };
5
     // Synonym for a record type.
6
     type result_t = record { valid : bool, value : bv8 };
9
    input valid
                       : bool;
10
    input cmd
                        : cmd_t;
11
    input r1, r2
                        : bv3;
    input immed
                        : bv8;
13
    output result
                        : result_t;
                        : [bv3]bv8;
    var regs
16
    // Temporary var to hold register values.
17
    var r1val, r2val : bv8;
18
19
    // Variable for the test harness.
20
     var cnt
                       : bv8;
21
22
     init {
23
24
      // All registers initialized to one.
25
       for i in range (0 \text{ bv}3, 7 \text{bv}3) {
       regs[i] = 1bv8;
26
27
      cnt = 1bv8;
28
       result.value = 1bv8;
29
30
31
     next {
32
      // Do we have a valid command?
33
       if (valid) {
34
35
         r1val = regs[r1];
         r2val = regs[r2];
36
         // Case-split on the operation to be performed.
37
         case
38
                             : \{ regs[r1] = r1val + r2val; \}
           (cmd == add)
39
                             : \{ regs[r1] = r1val - r2val; \}
           (cmd = sub)
40
           (cmd = mov_imm) : \{ regs[r1] = immed; \}
41
42
         // Set the output result.
         result.valid = true;
         result.value = regs[r1];
45
46
       } else {
         result.valid = false;
47
48
       // This code is only for testing this module.
49
50
      cnt = cnt + cnt;
51
52
    // Specification.
53
                                  (r1 = 0bv3 \&\& r2 = 0bv3);
    assume regindex_zero:
54
    assume cmd_is_add:
                                  (cmd = add);
    assume cmd_is_valid:
                                  (valid);
56
    invariant result_eq_cnd: (cnt == result.value);
57
58
    // Proof script.
59
    control {
60
      f = unroll (5);
61
      check;
62
63
      print _results;
64
65 }
```

Example 2.1.: Model of a simple ALU

#### 2.2.1. For Loops

The init block uses a for loop to initialize each value in the array regs to the bit-vector value 1.<sup>1</sup> The loop iterates over the values between 0 and 7 (both-inclusive).

#### 2.2.2. If and Case Statements

Also worth pointing out are the if statement that appears on line 34, and the case statement that appears on line 38. Syntax for if statements should be familiar.

case statements are delimited by case and esac and contain within them a list of boolean expressions and associated statement blocks. These expressions are evaluated in the order in which appear, and if any of them evaluate to true, the corresponding block is executed. If none of the case-expressions evaluate to true, then nothing is executed. The keyword default can be used as a "catch-all" case like in C/C++.

#### 2.2.3. Expressions

The syntax for expressions in UCLID5 is similar to languages like C/C++/Java. Index i of array regs is accessed using the syntax regs[i]. Field value in the record result is accessed as result.value.

# 2.3. Computation/Verification Model

We now describe how the computation specified by Example 2.1 is specified.

#### 2.3.1. Initialization

"Execution" of the model in Example 2.1 starts with the init block. This block assigns initial values to regs, cnt and result.value. The other variables (e.g. r1val and r2val) are not assigned to in the init block and will be initialized non-deterministically.

#### 2.3.2. Next State Computation

The next state of each state variable in the model is computed according to the next block. Any variables not assigned to in the next block retain their "old" values.

The input variables of the model are assigned non-deterministic values for each step of the transition system. These values can be controlled by using assumptions. Indeed, the model uses the three assumptions on lines 54, 55 and 56 to constrain the input to the ALU to always be an add operation, where both operands refer to register index 0.

<sup>&</sup>lt;sup>1</sup>1bv8 here refers to the bit-vector value 1 of width 8.

## 2.3.3. Verification

As in Example 1.1, the verification script in Example 2.1 unrolls the transition system for 5 steps and checks if the invariant on line 57 is violated in any of these steps.

# 3. Verification Techniques

# 4. Compositional Verification: Procedures and Modules

# A. Appendix: Uclid5 Grammar

This appendix describes UCLID5's grammar.

### A.1. Grammar of Modules and Declarations

**A model** consist of a list of modules. Each module consists of a list of declarations followed by an optional control block.

```
 \langle Model \rangle & ::= \langle Module \rangle^* \\ \langle Module \rangle & ::= module \langle Id \rangle \quad `` \{' \ \langle Decl \rangle^* \ \langle ControlBlock \rangle? \ `` \}'
```

**Declarations** can be of the following types.

```
 \langle Decl \rangle & ::= \langle TypeDecl \rangle \\ & | \langle InputsDecl \rangle \\ & | \langle OutputsDecl \rangle \\ & | \langle VarsDecl \rangle \\ & | \langle ConstsDecl \rangle \\ & | \langle Shared VarsDecl \rangle \\ & | \langle FuncDecl \rangle \\ & | \langle FuncDecl \rangle \\ & | \langle InstanceDecl \rangle \\ & | \langle InitDecl \rangle \\ & | \langle NextDecl \rangle \\ & | \langle SpecDecl \rangle \\ \end{aligned}
```

**Type declarations** declare either a type synonym or an uninterpreted type.

```
 \langle \mathit{TypeDecl} \rangle \qquad \qquad ::= \ \mathsf{type} \ \langle \mathit{Id} \rangle \ \text{`='} \ \langle \mathit{Type} \rangle \ \text{`;'} \\ | \ \mathsf{type} \ \langle \mathit{Id} \rangle \ \text{`;'}
```

Variable declarations can refer to inputs, outputs, state variables or shared variables.

```
\langle InputsDecl \rangle ::= input \langle IdList \rangle ':' \langle Type \rangle ';' \langle OutputsDecl \rangle ::= output \langle IdList \rangle ':' \langle Type \rangle ';' \langle VarsDecl \rangle ::= var \langle IdList \rangle ':' \langle Type \rangle ';'
```

#### A. Appendix: UCLID5 Grammar

```
\langle ConstsDecl \rangle ::= const \langle IdList \rangle ':' \langle Type \rangle ';' \langle SharedVarsDecl \rangle ::= sharedvar \langle IdList \rangle ':' \langle Type \rangle ';'
```

**Function declarations** refer to uninterpreted functions.

```
\langle FuncDecl \rangle ::= function \langle Id \rangle '(' \langle IdTypeList \rangle ')' ':' \langle Type \rangle ';'
```

**Procedure declarations** consist of a formal parameter list, a list of return values and types, followed by optional pre-/post-conditions and the list of state variables modified by procedure.

```
 \langle ProcedureDecl\rangle & ::= \operatorname{procedure} \langle Id\rangle \text{ ('} \langle IdTypeList\rangle \text{ ')'} \langle ProcReturnArg\rangle ? \\ & \langle RequireExprs\rangle \langle EnsureExprs\rangle \langle ModifiesExprs\rangle \\ & ` \{' \langle VarsDecls\rangle^* \langle Statement\rangle^* \text{ '}\}' \\ \\ \langle ProcReturnArg\rangle & ::= \operatorname{returns} \text{ ('} \langle IdTypeList\rangle \text{ '})' \\ \\ \langle RequireExprs\rangle & ::= (\operatorname{requires} \langle Expr\rangle \text{ '}; \text{'})^* \\ \\ \langle EnsureExprs\rangle & ::= (\operatorname{ensures} \langle Expr\rangle \text{ '}; \text{'})^* \\ \\ \langle ModifiesExprs\rangle & ::= (\operatorname{modifies} \langle IdList\rangle \text{ '}; \text{'})^* \\ \end{aligned}
```

**Instance declarations** allow the instantiation (duh!) of other modules. It consists of the instance name, the name of the module being instantiated and the list of mappings for the instances' inputs, output and shared variables.

```
 \langle InstanceDecl \rangle & ::= instance \langle Id \rangle \text{ `:' } \langle Id \rangle \langle ArgMapList \rangle \text{ `;'} 
 \langle ArgMapList \rangle & ::= \text{`('')'} 
 | \text{`('} \langle ArgMap \rangle \text{`,'} \langle ArgMap \rangle \text{`)'} 
 \langle ArgMap \rangle & ::= \langle Id \rangle \text{`:'} \text{`('')'} 
 | \langle Id \rangle \text{`:'} \text{`('} \langle Expr \rangle \text{')'}
```

**Axioms** refer to assumptions while a **specification declaration** refers to design invariants. Note axiom and assume are synonyms, as are property and invariant.

```
 \langle AxiomDecl\rangle & ::= \langle AxiomKW\rangle \langle Id\rangle `:` \langle Expr\rangle `;` \\ | \langle AxiomKW\rangle \langle Expr\rangle `;` \\ | \langle AxiomKW\rangle & ::= axiom | assume \\ | \langle SpecDecl\rangle & ::= \langle PropertyKW\rangle \langle Id\rangle `:` \langle Expr\rangle `;` \\ | \langle PropertyKW\rangle \langle Expr\rangle `;` \\ | \langle PropertyKW\rangle & ::= property | invariant \\ | \textbf{Init} \text{ and } \textbf{next} \text{ blocks consist of lists of statements.} \\ | \langle InitDecl\rangle & ::= init `\{` \langle Statement\rangle^* `\}` \\ | \langle NextDecl\rangle & ::= next `\{` \langle Statement\rangle^* `\}`
```

#### A.2. Statement Grammar

**Statements** are the following types, most of which should be familiar. Note the support for simultaneous assignment à la Python. The keyword next allows for synchronous scheduling of instantiated modules.

```
 \langle Statement \rangle & ::= \text{skip';'} \\ & | \text{assert } \langle Expr \rangle \text{';'} \\ & | \text{assume } \langle Expr \rangle \text{';'} \\ & | \text{havoc } \langle Id \rangle \text{';'} \\ & | \langle LhsList \rangle \text{'='} \langle ExprList \rangle \text{';'} \\ & | \text{call'('} \langle LhsList \rangle \text{')''='} \langle Id \rangle \langle ExprList \rangle \text{';'} \\ & | \text{next'('} \langle Id \rangle \text{')'';'} \\ & | \langle IfStmt \rangle \\ & | \langle CaseStmt \rangle \\ & | \langle ForLoop \rangle
```

**Assignments** and **call** statements refer to the nonterminal  $\langle LhsList \rangle$ . As the name suggests, this is a list of syntactic forms that can appear on the left hand side of an assignment.  $\langle Lhs \rangle$  are of four types: (i) identifiers, bitvector slices within identifiers, (iii) array indices, and (iv) fields within records.

```
\langle LhsList \rangle \qquad ::= \langle Lhs \rangle \ (`,`\langle Lhs \rangle)^* 
\langle Lhs \rangle \qquad ::= \langle Id \rangle 
| \langle Id \rangle \ `[`\langle Expr \rangle \ `:`\langle Expr \rangle \ `]`
| \langle Id \rangle \ `[`\langle ExprList \rangle \ `]'
| \langle Id \rangle \ (`.`\langle Id \rangle) +
```

If statements are as per usual. "Braceless" if statements are not permitted.

```
\langle \mathit{IfStmt} \rangle \qquad ::= \text{if `('} \langle \mathit{IfExpr} \rangle \text{ `)' `` \{' \langle \mathit{Statement} \rangle * \text{ `} \}'} \\ = \text{lse `\{' \langle \mathit{Statement} \rangle * \text{ `} \}'} \\ | \text{if `('} \langle \mathit{IfExpr} \rangle \text{ `)' `` \{' \langle \mathit{Statement} \rangle * \text{ `} \}'} \\ \langle \mathit{IfExpr} \rangle \qquad ::= \langle \mathit{Expr} \rangle \mid *
```

**Case** statements are as follows.

```
\langle CaseStmt \rangle ::= case \langle CaseBlock \rangle^* esac \langle CaseBlock \rangle ::= \langle Expr \rangle ':' '{' \langle Statement \rangle^* '}' default ':' '{' \langle Statement \rangle^* '}'
```

For loops allow iteration over a statically defined range of values.

```
\langle ForLoop \rangle ::= for \langle Id \rangle in range '(' \langle Number \rangle ',' \langle Number \rangle ')' 
 `{' \langle Statement \rangle* '}'
```

## A.3. Expression Grammar

Let us turn to **expressions**, which may be quantified.

$$\langle Expr \rangle$$
 ::=  $\langle E1 \rangle$ 

The usual logical and bitwise operators are allowed.

$$\langle E2 \rangle$$
 ::=  $\langle E3 \rangle$  '<==>'  $\langle E2 \rangle$  |  $\langle E3 \rangle$ 

$$\langle E3 \rangle$$
 ::=  $\langle E4 \rangle$  '==>'  $\langle E3 \rangle$  |  $\langle E4 \rangle$ 

As are relational operators, bitvector concatentation (++) and arithmetic.

$$\langle E5 \rangle$$
 ::=  $\langle E6 \rangle$   $\langle RelOp \rangle$   $\langle E6 \rangle$ 

$$\langle RelOp \rangle$$
 ::= '>' | '<' | '=' | '!=' | '>=' | '<='

$$\langle E6 \rangle$$
 ::=  $\langle E7 \rangle$  '++'  $\langle E6 \rangle$ 

$$\langle E7 \rangle$$
 ::=  $\langle E8 \rangle$  '+'  $\langle E7 \rangle$ 

$$\langle E8 \rangle$$
 ::=  $\langle E9 \rangle$  '-'  $\langle E9 \rangle$ 

$$\langle E9 \rangle$$
 ::=  $\langle E10 \rangle$  '\*'  $\langle E10 \rangle$ 

The unary operators are arithmetic negation (unary minus), logical negation and bitwise negation of bitvectors.

$$\langle E10 \rangle = \langle UnOp \rangle \langle E11 \rangle | \langle E11 \rangle$$

$$\langle UnOp \rangle$$
 ::= '-' | '!' | '~'

Array select, update and bitvector select operators are defined à la Boogie.

$$\langle E11 \rangle \qquad ::= \langle E12 \rangle \text{ `['} \langle Expr \rangle \text{ (','} \langle Expr \rangle) * \text{`]'} \\ | \langle E12 \rangle \text{ `['} \langle Expr \rangle \text{ (','} \langle Expr \rangle) * = \langle Expr \rangle \text{ `]'} \\ | \langle E12 \rangle \text{ `['} \langle Expr \rangle \text{ `:'} \langle Expr \rangle \text{ `]'} \\ | \langle E12 \rangle \end{cases}$$

Function invocation, record selection, and access to variables in instantiated modules is as follows.

#### A. Appendix: UCLID5 Grammar

$$\langle E12 \rangle \qquad ::= \langle E13 \rangle \text{ (',' } \langle ExprList \rangle \text{ ')'}$$

$$| \langle E13 \rangle \text{ (', ',' } \langle Id \rangle) +$$

$$| \langle E13 \rangle \text{ (', ->' } \langle Id \rangle) +$$

And finally, we have the terminal symbols, identifiers, tuples and the if-then-else operator.

```
\langle E12 \rangle \qquad ::= \text{false} \mid \text{true} \mid \langle Number \rangle \\ \mid \langle Id \rangle \mid \langle Id \rangle \text{ `: '} \langle Id \rangle \\ \mid \text{`` {'}} \langle Expr \rangle \text{ (`, '} \langle Expr \rangle) * \text{`} \text{'} \text{'} \\ \mid \text{ite `('} \langle Expr \rangle \text{ ', '} \langle Expr \rangle \text{', '} \langle Expr \rangle \text{') '} \end{cases}
```

## A.4. Types

```
\langle \mathit{Type} \rangle \qquad ::= \langle \mathit{PrimitiveType} \rangle \\ | \langle \mathit{EnumType} \rangle \\ | \langle \mathit{TupleType} \rangle | \langle \mathit{RecordType} \rangle \\ | \langle \mathit{ArrayType} \rangle \\ | \langle \mathit{SynonymType} \rangle \\ | \langle \mathit{ExternalType} \rangle
```

Supported primitive types are Booleans, integers and bit-vectors. Bit-vector types are defined according the regular expression 'bv[0-9]+' and the number following 'bv' is the width of the bit-vector.

```
\langle PrimitiveType \rangle ::= bool | int | \langle BitVectorType \rangle
```

Enumerated types are defined using the enum keyword.

```
\langle EnumType \rangle ::= enum '{' \langle IdList \rangle '}'
```

Tuple types are declared using curly brace notation.

$$\langle Tuple Type \rangle ::= `\{` \langle Type \rangle (`, ` \langle Type \rangle) * `\}`$$

Record types use the keyword record.

```
\langle Record type \rangle ::= record '{' \langle IdTypeList \rangle '}'
```

Array types are defined using square brackets. The list of types within square brackets defined the array's index type.

$$\langle Array Type \rangle$$
 ::= '['  $\langle Type \rangle$  (', '  $\langle Type \rangle$ )\* ']'  $\langle Type \rangle$ 

Type synonyms are just identifiers, while external types refer to synonym types defined in a different module.

```
\langle SynonymType \rangle ::= \langle Id \rangle
```

$$\langle ExternalType \rangle ::= \langle Id \rangle `:: ` \langle Id \rangle$$

## A.5. Control Block

**The control block** consists of a list of commands. A command can have an optional result object, an optional argument object, an optional list of command parameters and finally an optional list of argument expressions.

#### A.6. Miscellaneous Nonterminals

 $\langle IdList \rangle$ ,  $\langle IdTypeList \rangle$  and  $\langle ExprList \rangle$  are non-empty, comma-separated list of identifiers, identifier/type tuples and expressions respectively.

$$\langle IdList \rangle \qquad ::= \langle Id \rangle \\ | \langle Id \rangle \text{ ', '} \langle IdList \rangle \\ \langle IdTypeList \rangle \qquad ::= \langle Id \rangle \text{ ': '} \langle Type \rangle \\ | \langle Id \rangle \text{ ': '} \langle Type \rangle \text{ ', '} \langle IdTypeList \rangle \\ \langle ExprList \rangle \qquad ::= \langle Expr \rangle \\ | \langle Expr \rangle \text{ ', '} \langle ExprList \rangle$$