Assignment 2

October 13, 2022

```
Exercise 2:
```

```
[]: import bitarray
     from hashlib import sha3_256, sha256, blake2b
     import json
     import bitarray
     from tqdm import tqdm
     import string
     import matplotlib.pyplot as plt
[]: size = int(1e7)
     import bitarray
     data = bitarray.bitarray(size)
     bloomfilter = BloomFilter(size)
[]: with open('/Users/polina/Desktop/words.txt') as f:
         for line in f:
             word = line.strip()
[]: class BloomFilter(object):
         def __init__(self, size):
             self.bit_array = bitarray.bitarray(size)
             self.hashsize = size
             self.bit_array.setall(0)
         def add(self, words):
             hash1 = int(self.my_hash(words, self.hashsize))
             self.bit_array[hash1] = True
         def add_2(self, words):
```

```
hash1 = int(self.my_hash(words, self.hashsize))
      hash2 = int(self.my_hash2(words, self.hashsize))
      self.bit_array[hash1] = True
      self.bit_array[hash2] = True
  def add_3(self, words):
      hash1 = int(self.my_hash(words, self.hashsize))
      hash2 = int(self.my_hash2(words, self.hashsize))
      hash3 = int(self.my hash3(words, self.hashsize))
      self.bit_array[hash1] = True
      self.bit_array[hash2] = True
      self.bit_array[hash3] = True
  def check(self, test_words):
      hash1 = int(self.my_hash(test_words, self.hashsize))
      if self.bit_array[hash1] == False:
          return False
      else:
          return True
  def check_2(self, test_words):
      hash1 = int(self.my hash(test words, self.hashsize))
      hash2 = int(self.my_hash2(test_words, self.hashsize))
      if (self.bit_array[hash1] == False) or (self.bit_array[hash2] == False):
          return False
      else:
          return True
  def check_3(self, test_words):
      hash1 = int(self.my_hash(test_words, self.hashsize))
      hash2 = int(self.my_hash2(test_words, self.hashsize))
      hash3 = int(self.my_hash3(test_words, self.hashsize))
      if (self.bit_array[hash1] == False) or (self.bit_array[hash2] == False)
Gor (self.bit_array[hash3] == False):
          return False
      else:
          return True
  def my_hash(self, s, size):
      return int(sha256(s.lower().encode()).hexdigest(), 16) % size
  def my_hash2(self, s, size):
      return int(blake2b(s.lower().encode()).hexdigest(), 16) % size
  def my_hash3(self, s, size):
```

```
return int(sha3_256(s.lower().encode()).hexdigest(), 16) % size
     def replace(s, position, character):
         return s[:position] + character + s[position+1:]
[]: def hashnumber():
         hashcount = input("hash number = ")
         return(hashcount)
     # need to use Python 3.10 for match
     #import sys;print(sys.version)
     def add word(hashcount):
         match hashcount:
             case "1":
                 with open('/Users/polina/Desktop/words.txt') as f:
                     for line in f:
                         word = line.strip()
                         bloomfilter.add(word)
                 break
             case "2":
                  with open('/Users/polina/Desktop/words.txt') as f:
                     for line in f:
                         word = line.strip()
                         bloomfilter.add_2(word)
                 break
             case "3":
                 with open('/Users/polina/Desktop/words.txt') as f:
                     for line in f:
                         word = line.strip()
                         bloomfilter.add_3(word)
[]: import string
     alphabet_list = string.ascii_lowercase
     alphabet_list = list(alphabet_list)
     print(alphabet_list)
[]: def all_suggestions(test_words):
         suggest = []
         alphabet = alphabet_list
         result = spell_check(test_words, hashcount)
         if result == False:
             for i in range(len(test_words)):
                 for a in alphabet:
                     suggest_word = replace(test_words, i, a)
                     suggest.append(suggest_word)
         return(suggest)
```

```
# need to use Python 3.10 for match
     def good_suggestion(all_suggestions, hashcount):
         correct_suggestion = []
         match hashcount:
             case "1":
                 for n in all_suggestions:
                     suggestresult = bloomfilter.check(n)
                     if suggestresult == True:
                         correct_suggestion.append(n)
                 break
             case "2":
                 for n in all_suggestions:
                     suggestresult = bloomfilter.check_2(n)
                     if suggestresult == True:
                         correct_suggestion.append(n)
                 break
             case "3":
                 for n in all_suggestions:
                     suggestresult = bloomfilter.check_3(n)
                     if suggestresult == True:
                         correct_suggestion.append(n)
         return(correct_suggestion)
     def spell_check(test_words, hashcount):
         match hashcount:
             case "1":
                 result = bloomfilter.check(test words)
                 return result
             break
             case "2":
                 result = bloomfilter.check_2(test_words)
                 return result
             break
             case "3":
                 result = bloomfilter.check_3(test_words)
                 return result
[]: hashcount = hashnumber()
[]: add_word(hashcount)
[]: test_words = input(" I asked my implementation to spell-check when using 1e7_
      ⇔bits: ")
[]: spell_check(test_words, hashcount)
     if spell_check(test_words, hashcount) != True:
```

```
suggestionlist = all_suggestions(test_words)
         good_suggestionlist = good_suggestion(suggestionlist, hashcount)
         print(good_suggestionlist)
[ ]: add_word("1")
     spell_check("bloeer", "1")
[]: with open('/Users/polina/Desktop/BIS_634/Assignment 2/typos.json', 'r') as f:
         file = f.read()
         text = json.loads(file)
         print(len(text))
[]: from tqdm import tqdm
     import numpy as np
     def good_suggest(text, hashcount):
         correct = 0
         misidentified = 0
         good_suggestion = 0
         for i in range(len(text)):
             if text[i][0] == text[i][1]:
                 correct += 1
             elif text[i][0] != text[i][1]:
                 if spell_check(text[i][0], hashcount) == True:
                     misidentified += 1
                 else:
                     suggestion = all_suggestions(text[i][0])
                     good = good_suggestion(suggestion, hashcount)
                     for n in good:
                         if (len(good) <= 3) and (n == text[i][1]):</pre>
                             good_suggestion += 1
         return correct, misidentified, good_suggestion
[]: # hash 1
     filter_size = np.logspace(0, 9, num=20, dtype=int)
     misidentified1 = []
     suggestion_list1 = []
     correct1 = []
     for n in range(len(filter_size)):
         bloomfilter = BloomFilter(int(filter_size[n]))
         add word("1")
         answer1 = good_suggest(text, "1")
         misidentified1.append(answer1[1])
         suggestion_list1.append(answer1[2])
         correct1.append(answer1[0])
     goodsuggestion1 = []
```

```
misidentified1 =[]

for i in range(len(misidentified1)):
    goodsuggestion = (suggestion_list1[i] / 25000)
    misidentified = (misidentified1[i] / 25000)
    goodsuggestion1.append(goodsuggestion)
    misidentified1.append(misidentified)
```

```
[]: # hash 2
     misidentified2 = []
     suggestion list2 = []
     correct2 = []
     for n in range(len(filter_size)):
         bloomfilter = BloomFilter(int(filter_size[n]))
         add_word("2")
         answer2 = good_suggest(text, "2")
         misidentified2.append(answer2[1])
         suggestion_list2.append(answer2[2])
         correct2.append(answer2[0])
     goodsuggestion2 = []
     misidentified2 = []
     for i in range(len(misidentified2)):
         goodsuggestion = (suggestion_list2[i] / 25000)
         misidentified = (misidentified2[i] / 25000)
         goodsuggestion2.append(goodsuggestion)
         misidentified2.append(misidentified)
```

```
[]: # hash 3
     misidentified3 = []
     suggestion_list3 = []
     correct3 = []
     for n in range(len(filter_size)):
         bloomfilter = BloomFilter(int(filter_size[n]))
         add word("3")
         answer3 = good suggest(text, "3")
         misidentified3.append(answer3[1])
         suggestion_list3.append(answer3[2])
         correct3.append(answer3[0])
     goodsuggestion3 = []
     misidentified3 =[]
     for i in range(len(misidentified3)):
         goodsuggestion = (suggestion_list3[i] / 25000)
         misidentified = (misidentified3[i] / 25000)
```

```
goodsuggestion3.append(goodsuggestion)
misidentified3.append(misidentified)
```

```
plt.xscale('log')
  plt.plot(filter_size, goodsuggestion1, label="good suggestions %, 1 hashh")
  plt.plot(filter_size, goodsuggestion2, label="good suggestions %, 2 hashes")
  plt.plot(filter_size, goodsuggestion3, label="good suggestions %, 3 hashes")
  plt.plot(filter_size, misidentified1, label="misidentified %, 1 has")
  plt.plot(filter_size, misidentified2, label="misidentified %, 2 hashes")
  plt.plot(filter_size, misidentified3, label="misidentified %, 3 hashes")
  plt.legend(loc="lower left")
  plt.show()
```

Exercise 3:

```
[]: # import libraries
import pandas as pd
import numpy as np
import random
import time
```

```
[]: class Tree:
         def __init__(self):
             self.value = None
             self.left = None
             self.right = None
         def add(self, item):
             if self.value is None:
                  self.value = item
                 return
             elif item < self.value:</pre>
                 if self.left:
                      self.left.add(item)
                 else:
                      self.left = Tree()
                      self.left.add(item)
                 return
             elif item > self.value:
                  if self.right:
                      self.right.add(item)
                 else:
                      self.right = Tree()
                      self.right.add(item)
             return
```

```
def __contains__(self, item):
    if self.value == item:
        return True
    elif self.left and item < self.value:
        return item in self.left
    elif self.right and item > self.value:
        return item in self.right
    else:
        return False
```

```
[]: def printTree(tree, list=[]):
    if not tree: return []
        list.append(tree.value)
    if tree.left: printTree(tree.left, list)
    if tree.right: printTree(tree.right, list)
    return list
```

```
[]: my_tree.__contains__(55)
```

```
[]: my_tree.__contains__(42)
```

Using various sizes n of trees (populated with random data) and sufficiently many calls to in (each individual call should be very fast, so you may have to run many repeated tests), demonstrate that in is executing in O(log n) times; on a log-log plot, for sufficiently large n, the graph of time required for checking if a number is in the tree as a function of n should be almost horizontal.

```
[]: import random
  import time
  import math
  import statistics
  import matplotlib.pyplot as plt
```

O(log n) times

```
[]: test_time = []
    n_sample = 1000
    repeat = 100
    for _ in range(n_sample):
        n = random.randint(0, 10000)
        my_tree = Tree()
        for _ in range(n):
            my_tree.add(random.random())
        start = time.time()
```

```
for _ in range(repeat):
    my_tree.__contains__(random.random())
end = time.time()
test_time.append((end - start, n))
```

```
[]: plt.scatter([x[1] for x in test_time], [x[0] for x in test_time], s=1)
plt.show()
```

This speed is not free. Provide supporting evidence that the time to setup the tree is $O(n \log n)$ by timing it for various sized ns and showing that the runtime lies between a curve that is O(n) and one that is $O(n^{**}2)$

O(n)

```
[]: test_time_2 = []
    n_sample = 100
    repeat = 10
    for _ in range(n_sample):
        n = random.randint(0, 10000)
        secquence = [random.random() for _ in range(n)]
        start = time.time()
        for _ in range(repeat):
            my_tree = Tree()
            for i in secquence:
                  my_tree.add(i)
        end = time.time()
        test_time_2.append((end - start, n))
```

```
[]: plt.scatter([x[1] for x in test_time_2], [x[0] for x in test_time_2], s=1) plt.show()
```

 $O(n^{**}2)$

```
[]: test_time_3 = []
    n_sample = 100
    repeat = 10
    for _ in range(n_sample):
        n = random.randint(0, 200)
        secquence = [random.random() for _ in range(n)]
        secquence = sorted(secquence)
        start = time.time()
        for _ in range(repeat):
            my_tree = Tree()
            for i in secquence:
                 my_tree.add(i)
        end = time.time()
        test_time_3.append((end - start, n))
```

```
[]: plt.scatter([x[1] for x in test_time_3], [x[0] for x in test_time_3], s=1)
     plt.show()
    n^{**}2, and n
[]: def time_function(n):
         timing = []
         n = [random.randint(1,n) for _ in range(n)]
         for attempt in [i for i in range(100)]:
             start = time.time()
             my tree = Tree()
             for item in n:
                 my_tree.add(item)
             end = time.time()
             timing.append(end - start)
         return min(timing)
[]: n_size = [1,100,1000,10000]
     true_size = [time_function(n) for n in n_size]
     size = true_size [0]
     quadratic = [size*n**2 for n in n size]
     linear = [size*n for n in n_size]
     plt.plot(n_size,true_size)
     plt.plot(n_size,quadratic)
     plt.plot(n_size,linear)
    plt.xscale('log')
     plt.yscale('log')
     plt.ylabel('time')
     plt.xlabel('n_size')
     plt.legend(['run time','0(n^2)','0(n)'],loc = 'upper left')
     plt.show()
[]:
    Exercise 4:
[]: import matplotlib.pyplot as plt
     import multiprocessing
     from time import perf_counter
     import numpy as np
     import random
[]: def alg1(data):
         data = list(data)
         changes = True
         while changes:
             changes = False
             for i in range(len(data) - 1):
```

```
if data[i + 1] < data[i]:
          data[i], data[i + 1] = data[i + 1], data[i]
          changes = True
return data</pre>
```

```
[]: def alg2(data):
       if len(data) <= 1:</pre>
         return data
       else:
         split = len(data) // 2
         left = iter(alg2(data[:split]))
         right = iter(alg2(data[split:]))
         result = []
         # note: this takes the top items off the left and right piles
         left_top = next(left)
         right_top = next(right)
         while True:
           if left_top < right_top:</pre>
             result.append(left_top)
             try:
               left_top = next(left)
             except StopIteration:
               # nothing remains on the left; add the right + return
               return result + [right_top] + list(right)
           else:
             result.append(right_top)
             try:
               right_top = next(right)
             except StopIteration:
               # nothing remains on the right; add the left + return
               return result + [left_top] + list(left)
```

```
[]: test_list = [55, 62, 37, 49, 71, 14, 17]
```

```
[]: print(alg1(test_list)) print(alg2(test_list))
```

Data 1

```
[]: def data1(n, sigma=10, rho=28, beta=8/3, dt=0.01, x=1, y=1, z=1):
    import numpy
    state = numpy.array([x, y, z], dtype=float)
    result = []
    for _ in range(n):
        x, y, z = state
        state += dt * numpy.array([
            sigma * (y - x),
            x * (rho - z) - y,
```

```
x * y - beta * z
])
result.append(float(state[0] + 30))
return result
```

```
[]: from time import perf_counter
     def test_time_data(limit, source):
         measure = dict()
         measure['list_size'] = []
         measure['alg1 time'] = []
         measure['alg2_time'] = []
         for n in range(limit):
             measure['list_size'].append(2**n)
             test_list_0 = source(2**n)
             time_alg1_start = perf_counter()
             alg1(test_list_0)
             time_alg1_stop = perf_counter()
             measure['alg1_time'].append(time_alg1_stop-time_alg1_start)
             time_alg1_start = perf_counter()
             alg2(test_list_0)
             time alg1 stop = perf counter()
             measure['alg2_time'].append(time_alg1_stop-time_alg1_start)
         return measure
```

```
[]: measure_dat1 = test_time_data(13, data1)
```

```
[]: data1_data = pd.DataFrame(measure_dat1) data1_data
```

```
[]: #create log-log plot
fig, ax = plt.subplots()
plt.plot(data1_data.list_size, data1_data.alg1_time, label='Alg1')
plt.plot(data1_data.list_size, data1_data.alg2_time, label='Alg2')
plt.xscale('log', base=2)
plt.yscale('log', base=10)
ax.set_title(' Alg1 and Alg2 -data 1')
fig.legend()
```

Data 2

```
[]: def data2(n):
    return list(range(n))
```

```
[]:[
     measure_dat2 = test_time_data(13, data2)
[]: data2_data = pd.DataFrame(measure_dat2)
     data2_data
[]: fig, ax = plt.subplots()
     plt.plot(data2_data.list_size, data2_data.alg1_time, label='Alg1')
     plt.plot(data2_data.list_size, data2_data.alg2_time, label='Alg2')
     plt.xscale('log', base=2)
     plt.yscale('log', base=10)
     ax.set_title('Alg1 and Alg2 - data 2')
     fig.legend()
    Data 3
[]: def data3(n):
         return list(range(n, 0, -1))
[]: measure_dat3 = test_time_data(13, data3)
[]: data3_data = pd.DataFrame(measure_dat3)
     data3_data
[]: fig, ax = plt.subplots()
     plt.plot(data3_data.list_size, data3_data.alg1_time, label='Alg1')
     plt.plot(data3_data.list_size, data3_data.alg2_time, label='Alg2')
     plt.xscale('log', base=2)
     plt.yscale('log', base=10)
     ax.set_title('Alg1 and Alg2 - data 3')
     fig.legend()
    Multiprocessing
[]: def parallelize_alg2(data):
         if len(data) <= 1:</pre>
             return data
         else:
             split = len(data) // 2
             with multiprocessing.Pool() as p:
                 [left, right] = p.map(
                     alg2, [data[:split], data[split:]])
             left = iter(left)
             right = iter(right)
             # combining the left and right data
             result = []
             left_top = next(left)
             right_top = next(right)
         while True:
```

```
if left_top < right_top:
    result.append(left_top)
    try:
        left_top = next(left)
    except StopIteration:
    # nothing remains on the left; add the right + return
        return result + [right_top] + list(right)

else:
    result.append(right_top)
    try:
        right_top = next(right)
    except StopIteration:
# nothing remains on the right; add the left + return
        return result + [left_top] + list(left)</pre>
```

```
[]: from tqdm import tqdm
     if __name__ == '__main__':
        data_variant = np.logspace(0, 23, base=2, dtype=int)
        duration = []
        alg2data1time = []
        for n in tqdm(data variant):
             data_set = data1(n, sigma=10, rho=28, beta=8/3, dt=0.01, x=1, y=1, z=1)
             alg2data1 start = perf counter()
             alg2(data set)
                               ## time taken by the unparallelized algo
             alg2data1_stop= perf_counter()
             alg2data1time.append(alg2data1_stop - alg2data1_start)
            start_time = perf_counter()
                                          #time taken by the parallelized algo
            parallelize_alg2(data_set)
            stop_time = perf_counter()
            duration.append(stop_time - start_time)
            print(duration[-1], alg2data1time[-1])
        plt.loglog(data_variant, alg2data1time, label = "mergesort alg2")
        plt.loglog(data_variant, duration, label = "prallelized alg2")
        plt.legend()
        plt.show()
```