Regression Discontinuity Design (RDD)

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Today's Goal:

- RDD Assumption
- Tutorial
- Replication

Assumption

- Score, Cutoff, Treatment, Outcome
- Continuity Framework: the sole change occurring at the discontinuity point is the shift in the treatment status (de la Cuesta, Brandon; Imai, Kosuke, 2016 (10.1146/annurev-polisci-032015-010115)).
- · Local randomization: as-if randomized assignment of treatment
- Key: No sorting behavior (incentive/ability to change treatment status)
- · Score might correlate with outcomes

Type 1: Winning Margins in Close Elections

- · Endogeneity: elected politicians are not randomly assigned
- Assumption: Indifference between candidates who win/lose close elections
- Violation: electoral frauds (self-sorting behavior)
- · Treatment: Politician characteristics
- Outcomes: Governance/Policy/Budget
 - David Szakonyi, Private Sector Policy Making: Business Background and Politicians' Behavior in Office (https://www.journals.uchicago.edu/doi/10.1086/709297), JOP 2020.
 - Fowler, Garro, Spenkuch, Quid Pro Quo? Corporate Returns to Campaign Contributions (https://www.journals.uchicago.edu/doi/10.1086/707307), JOP 2020.
 - Potentials: Most focus on US/developed democracies
- Critics: Marshall, Can Close Election Regression Discontinuity Designs Identify Effects of Winning Politician Characteristics? (DOI:%2010.1111/ajps.12741), AJPS 2022.
 - Either that the characteristic of interest does not affect candidate vote shares
 - Or that no compensating differential affects the outcome.

Type 2: Age

- Endogeneity: self-selection into policies
- Assumption: age-based policy design
- · Violation: lax enforcement/ noncompliance
- · Treatment: policy eligibility/benefits
- · Examples:

- Age -> Benefits from education reform -> Political participation. Croke et al., Deliberate
 Disengagement: How Education Can Decrease Political Participation in Electoral Authoritarian
 Regimes (doi:10.1017/S0003055416000253), APSR 2016.
- Age -> Public insurance -> Support for public health policies. Lerman and McCabe, Personal Experience and Public Opinion: A Theory and Test of Conditional Policy Feedback (http://dx.doi.org/10.1086/689286), JOP 2017.
- Son's age -> Legislators' pro-conscription voting. McGuirk, Hilger, Miller, No Kin in the Game: Moral Hazard and War in the U.S. Congress (https://www.journals.uchicago.edu/doi/abs/10.1086/724316), JPE 2023.

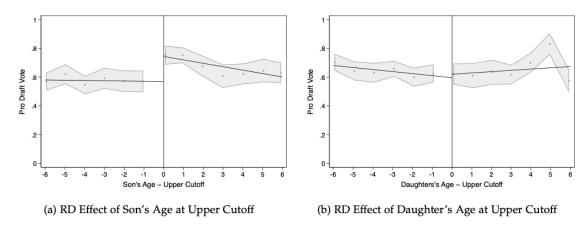


Figure 1: **Regression Discontinuity Plots.** These plots correspond to estimates in Table A10. The estimate for ρ in part (a) is 0.1879 (p<0.05). The placebo estimate in part (b) is -0.0044 (p>0.10).

Type 3: Geography/Boundary (Geographical/Spatial RD)

- · Endogeniety: self-selection into policies
- Assumption: geography-based treatment
- · Violation: population/resource mobility
- Treatment: policies, colonization, natural disaster etc.
- · Examples:
 - North v.s. South Vietnam in history (ruled by Dai Viet before French) -> Economic Growth. Dell, Lane, and Querubin, TheHistorical State, Local Collective Action, and Economic Development in Vietnam (https://doi.org/10.3982/ECTA15122), Econometrica 2018.
 - Japanese colonization -> state building -> township-level governance. Mattingly, Colonial Legacies and State Institutions in China: Evidence From a Natural Experiment (https://doi.org/10.1177/0010414015600465), CPS 2016.

Mattingly 439

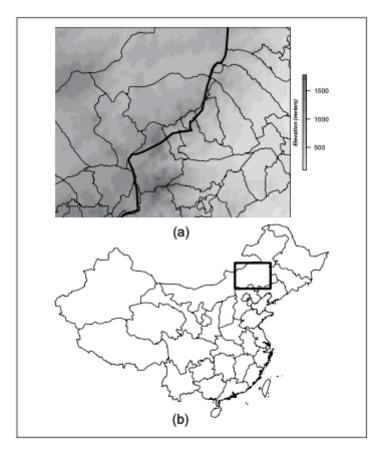


Figure 1. (a) The western border of the Japanese puppet state of Manchukuo, shown with a black line, and (b) The area of detail, which is approximately the size of South Korea.

In Figure 1a, current county borders are shown with lighter black lines, and altitude is shown in the background.

Other Smart Designs:

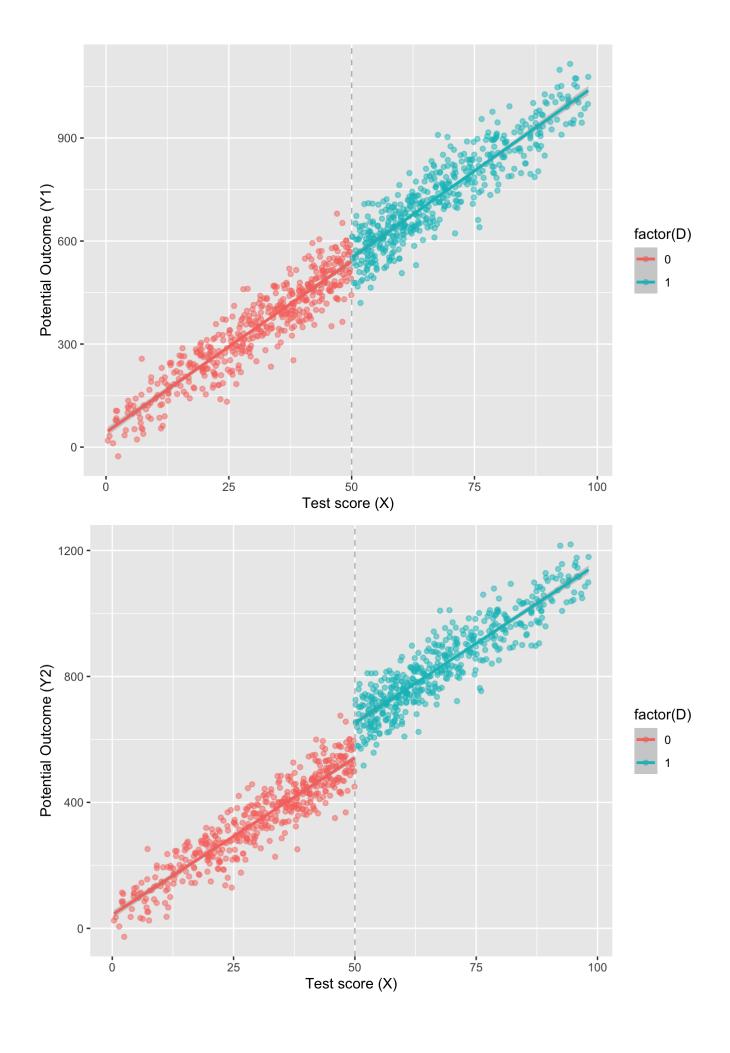
- Timing of unanticipated social events -> Public opinion (weekly survey). Reny and Newman, The Opinion-Mobilizing Effect of Social Protest against Police Violence: Evidence from the 2020 George Floyd Protests (doi:10.1017/S0003055421000460), APSR 2021.
- Exam score -> college education -> political ideology. Apfeld et al., Higher Education and Cultural Liberalism: Regression Discontinuity Evidence from Romania (https://www.journals.uchicago.edu/doi/full/10.1086/720644), JOP 2018.
- Security scores -> military attacks -> economic development. Dell and Querubin, Nation Building Through Foreign Intervention: Evidence from Discontinuities in Military Strategies (https://doi.org/10.1093/qje/qjx037), QJE 2017.

Tutorial

We start with simulating data. C is the confounder, X is the running variable (affected by C), the cutoff is at 25. Y1 is the outcome without a jump at the cutoff and Y2 are affected by the treatment. The real treatment effect is 100.

```
library(ggplot2)
library(tidyverse)
set.seed(2023)
dat <- tibble(
    C = rnorm(1000, 10, 5),
    X = 5*C + rnorm(1000, 0, 10),
    D = if_else(X > 50, 1, 0),
    Y1 = 0     * D + 30*C + 5     * X + rnorm(1000, 0, 5),
    Y2 = 100     * D + 30*C + 5     * X + rnorm(1000, 0, 5))
dat<- subset(dat,X>0&X<100)</pre>
```

Here shows the relationship between X and Y1/Y2. Graphically, we can see that Y2 has a jump at the cutoff (X=50) but not Y1.



Estimation

· We then estimate the effect of D on Y2 using OLS.

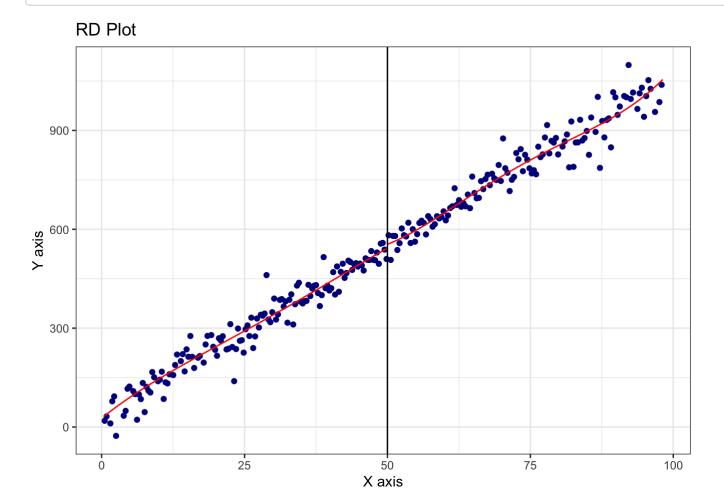
```
m0<- lm(Y2~D,dat)
m1<- lm(Y2~D+X,dat)
m2<- lm(Y2~D+X+C,dat)
stargazer::stargazer(m0,m1,m2,type='text',digits = 2,omit.stat = 'f')</pre>
```

```
##
##
                     Dependent variable:
##
             _____
##
                          Y2
##
                 (1)
                          (2)
                                    (3)
## ------
               490.78***
                        110.21***
                                  100.00***
## D
                                   (0.58)
##
               (9.09)
                          (6.47)
##
## X
                         10.04***
                                   4.98***
##
                          (0.14)
                                   (0.02)
##
## C
                                   30.15***
##
                                   (0.09)
##
              344.42***
                        40.97***
## Constant
                                   -0.14
##
               (6.47)
                         (5.00)
                                   (0.46)
##
## -----
## Observations
                          939
                939
                                    939
                                   1.00
## R2
                0.76
                          0.96
## Adjusted R2
                0.76
                          0.96
## Residual Std. Error 139.30 (df = 937) 55.27 (df = 936) 4.96 (df = 935)
## Note:
                          *p<0.1; **p<0.05; ***p<0.01
```

We then estimate the effect with rdrobust.

```
## Covariate-adjusted Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                                    939
## BW type
                                  mserd
## Kernel
                             Triangular
## VCE method
                                     NN
## Number of Obs.
                                    463
                                                  476
## Eff. Number of Obs.
                                    212
                                                  244
## Order est. (p)
                                      1
                                                    1
## Order bias (q)
                                      2
                                                    2
## BW est. (h)
                                 16.325
                                               16.325
                                 26.406
## BW bias (b)
                                               26.406
## rho (h/b)
                                                0.618
                                  0.618
## Unique Obs.
                                    463
                                                  476
##
##
##
                      Coef. Std. Err.
                                                      P> | z |
           Method
                                                                  [ 95% C.I. ]
##
##
     Conventional
                      -0.299
                                 0.942
                                           -0.317
                                                      0.751
                                                                [-2.145, 1.548]
                                                                [-2.560 , 1.871]
##
           Robust
                                           -0.305
                                                      0.760
```

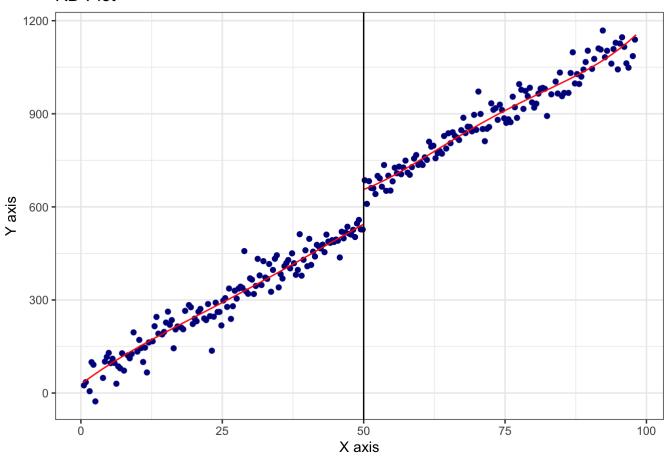
rdplot(y=Y1,x=X,c=50)



```
## Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                      939
## BW type
                     mserd
## Kernel
                 Triangular
## VCE method
                       NN
##
## Number of Obs.
                      463
                               476
## Eff. Number of Obs.
                      147
                               177
## Order est. (p)
                       1
                                1
                        2
## Order bias (q)
                                2
## BW est. (h)
                    11.256
                            11.256
## BW bias (b)
                    18.098
                             18.098
## rho (h/b)
                     0.622
                            0.622
## Unique Obs.
                               476
                      463
##
##
       Method
             Coef. Std. Err.
                              Z
                                  P> | z |
                                        [ 95% C.I. ]
Conventional 113.214 15.550
                                  0.000 [82.736 , 143.691]
##
                          7.281
##
                           6.404
                                        [81.668 , 153.711]
       Robust
                                  0.000
```

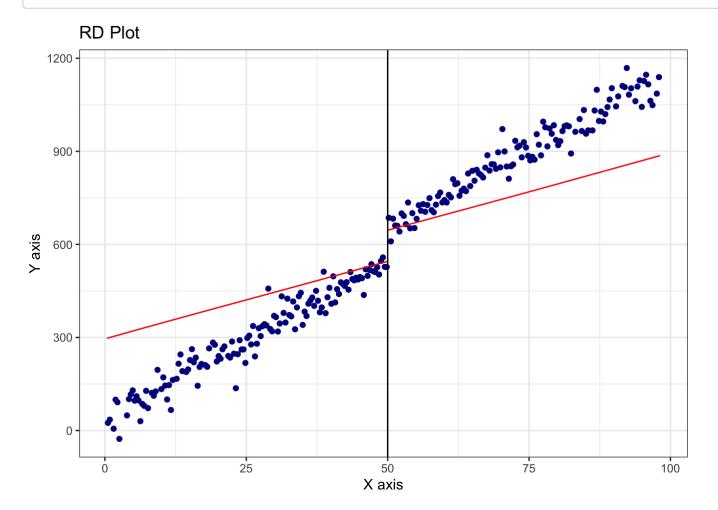
```
rdplot(y=Y2,x=X,c=50)
```





```
## Covariate-adjusted Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                                    939
## BW type
                                  mserd
## Kernel
                             Triangular
## VCE method
                                     NN
## Number of Obs.
                                    463
                                                  476
## Eff. Number of Obs.
                                    173
                                                  205
## Order est. (p)
                                      1
                                                    1
## Order bias (q)
                                       2
                                                    2
## BW est. (h)
                                 13.060
                                               13.060
## BW bias (b)
                                 21.431
                                               21.431
## rho (h/b)
                                                0.609
                                  0.609
## Unique Obs.
                                                  476
                                    463
##
##
                       Coef. Std. Err.
                                                      P> | z |
##
           Method
                                                                  [ 95% C.I. ]
##
##
     Conventional
                    100.674
                                 1.182
                                           85.167
                                                      0.000
                                                                [98.357 , 102.991]
                                                                [98.260 , 103.735]
##
           Robust
                                           72.320
                                                      0.000
```

rdplot(y=Y2,x=X,c=50,covs = C)



Replication

David Szakonyi, Private Sector Policy Making: Business Background and Politicians' Behavior in Office (https://www.journals.uchicago.edu/doi/10.1086/709297), JOP 2020

- · Research Question: Do businessperson politicians actually govern differently?
- · Empirical evidence: mayor elections and outcomes in Russia
- · Argument: Pro-business policies, government efficiency
- · Research Design: RDD on margin of victory

Replication

We start with a simple model without any setting

```
## Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                       1662
## BW type
                       mserd
## Kernel
                   Triangular
## VCE method
                         NN
## Number of Obs.
                       1299
                                 363
## Eff. Number of Obs.
                        478
                                 188
## Order est. (p)
                         1
                                   1
## Order bias (q)
                         2
                                  2
## BW est. (h)
                       0.284
                                0.284
                                0.460
## BW bias (b)
                       0.460
## rho (h/b)
                       0.616
                                0.616
## Unique Obs.
                       1295
                                 363
##
 ______
##
       Method
              Coef. Std. Err.
                                    P> | z |
##
   Conventional
              -0.185
                      0.063
                            -2.941
                                    0.003
                                          [-0.309, -0.062]
                                          [-0.341, -0.055]
##
       Robust
                            -2.714
                                    0.007
 ______
```

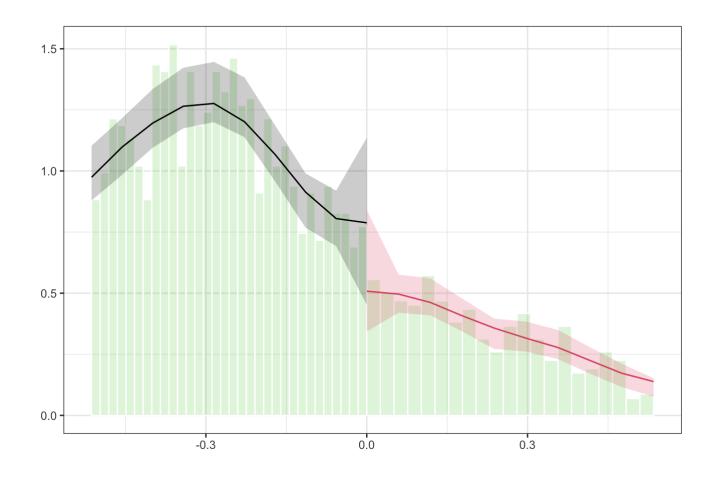
- We then replicate the results and see what were set in the specification
 - BW=.05
 - Kernel='uni'
 - p=1

```
## Covariate-adjusted Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                          1662
## BW type
                        Manual
## Kernel
                       Uniform
## VCE method
                           NN
##
## Number of Obs.
                          1299
                                    363
## Eff. Number of Obs.
                           58
                                     43
## Order est. (p)
                            1
                                      1
                            2
                                      2
## Order bias (q)
                         0.050
                                   0.050
## BW est. (h)
## BW bias (b)
                         0.050
                                   0.050
## rho (h/b)
                         1.000
                                   1.000
## Unique Obs.
                          1299
                                    363
##
               Coef. Std. Err.
##
        Method
                                       P> | z |
                                                [ 95% C.I. ]
                                   Z
Conventional
               -0.323
                                        0.002
                                              [-0.528, -0.119]
                       0.104
                               -3.096
## Bias-Corrected
                       0.104 -3.408
               -0.356
                                       0.001
                                              [-0.561, -0.151]
##
                                               [-0.742, 0.030]
        Robust
               -0.356
                       0.197
                               -1.808
                                       0.071
```

Test of Manipulation

Is there any self-sorting behavior?

```
#Density Test
library(rddensity)
rdd<- rddensity(X = vrn_b$businesswinmargin)
rddplot<- rdplotdensity(rdd,X = vrn_b$businesswinmargin)</pre>
```



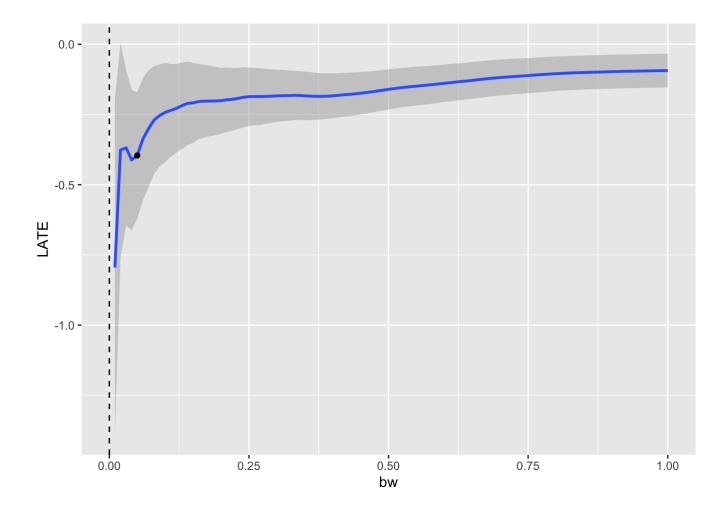
summary(rdd)

```
##
## Manipulation testing using local polynomial density estimation.
##
## Number of obs =
                        2260
## Model =
                        unrestricted
## Kernel =
                        triangular
## BW method =
                        estimated
## VCE method =
                        jackknife
##
## c = 0
                        Left of c
                                             Right of c
## Number of obs
                        1751
                                             509
## Eff. Number of obs
                        330
                                             198
## Order est. (p)
                        2
                                             2
## Order bias (q)
                        3
                                             3
## BW est. (h)
                        0.171
                                             0.178
##
## Method
                                            P > |T|
## Robust
                        -0.9534
                                             0.3404
##
##
## P-values of binomial tests (H0: p=0.5).
## Window Length / 2
                                           P>|T|
                             <c
                                    >=c
## 0.014
                              22
                                     20
                                           0.8776
## 0.028
                              46
                                      41
                                           0.6683
## 0.042
                              68
                                     56 0.3232
## 0.056
                              97
                                     69
                                           0.0358
## 0.070
                             124
                                    83 0.0053
## 0.084
                             154
                                     97
                                           0.0004
## 0.098
                             178
                                     112
                                           0.0001
## 0.112
                             205
                                     130 0.0000
## 0.126
                             228
                                     147
                                           0.0000
## 0.141
                                     166
                                            0.0000
                             257
```

Test of Sensitivity (BW Select)

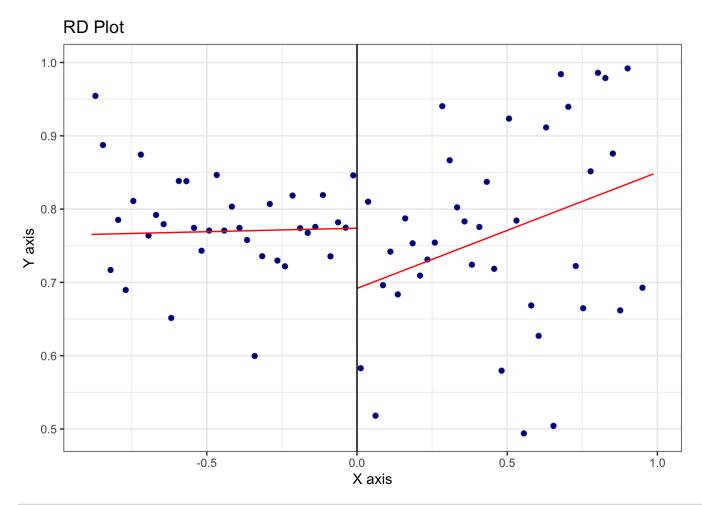
• Is the effect unique to the bandwidth choice (h=.05)?

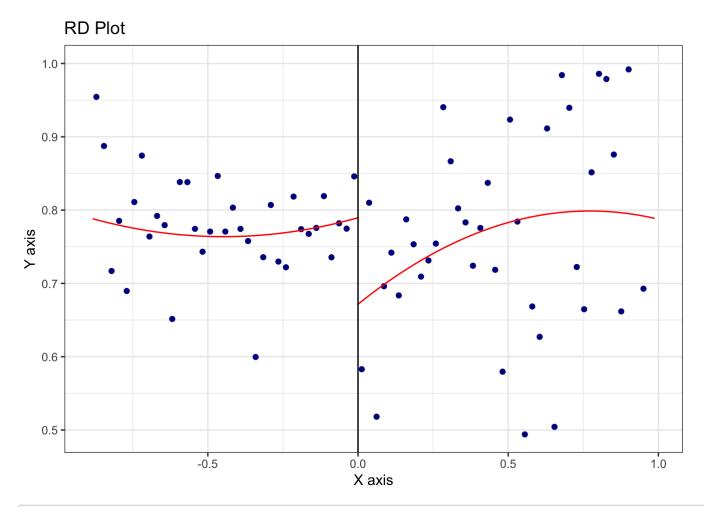
```
library(rddtools)
dat2 <- rdd_data(y = vrn_b$competitive_construction,x = vrn_b$businesswinmargin,cutpoint
= 0)
m1<- rdd_reg_np(rdd_object=dat2,bw=0.05)
plotSensi(m1, from = 0.01, to = 1, by = 0.01)</pre>
```



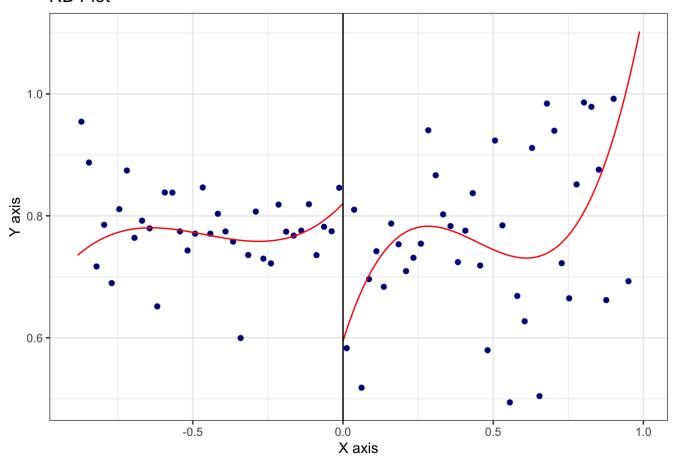
Test of Sensitivity (Order)

• Does the setting of order (p1) matter





RD Plot



```
m_test1<-with(vrn_b, rdrobust(y=competitive_construction,
                          x=businesswinmargin,
                          bwselect="mserd",
                          covs=cbind(factor(unit_type),totalexpend_log_year0),
                          all=TRUE, kernel='uni',p=1,cluster=region,h=.05))
m_test2<-with(vrn_b, rdrobust(y=competitive_construction,</pre>
                          x=businesswinmargin,
                          bwselect="mserd",
                          covs=cbind(factor(unit_type),totalexpend_log_year0),
                          all=TRUE, kernel='uni',p=2,cluster=region,h=.05))
m_test3<-with(vrn_b, rdrobust(y=competitive_construction,</pre>
                          x=businesswinmargin,
                          bwselect="mserd",
                          covs=cbind(factor(unit_type),totalexpend_log_year0),
                          all=TRUE, kernel='uni',p=3,cluster=region,h=.05))
summary(m_test1)
```

```
## Covariate-adjusted Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                          1662
## BW type
                        Manual
## Kernel
                        Uniform
## VCE method
                            NN
##
## Number of Obs.
                          1299
                                     363
## Eff. Number of Obs.
                            58
                                      43
## Order est. (p)
                            1
                                       1
                            2
                                       2
## Order bias (q)
## BW est. (h)
                         0.050
                                   0.050
## BW bias (b)
                         0.050
                                   0.050
## rho (h/b)
                         1.000
                                   1.000
## Unique Obs.
                          1299
                                     363
##
##
                 Coef. Std. Err.
        Method
                                        P> | z |
                                                 [ 95% C.I. ]
##
   Conventional
               -0.323
                        0.104
                               -3.096
                                        0.002
                                               [-0.528, -0.119]
                     0.104
                                        0.001
                                               [-0.561, -0.151]
## Bias-Corrected
               -0.356
                               -3.408
##
        Robust
               -0.356
                       0.197
                               -1.808
                                        0.071
                                              [-0.742, 0.030]
```

summary(m test2)

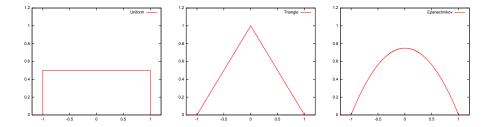
```
## Covariate-adjusted Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                       1662
## BW type
                      Manual
## Kernel
                     Uniform
## VCE method
                         NN
##
## Number of Obs.
                       1299
                                 363
## Eff. Number of Obs.
                        58
                                 43
## Order est. (p)
                         2
                                  2
## Order bias (q)
                         3
                                  3
## BW est. (h)
                      0.050
                               0.050
## BW bias (b)
                      0.050
                                0.050
## rho (h/b)
                      1.000
                                1.000
## Unique Obs.
                       1299
                                 363
##
Coef. Std. Err.
##
       Method
                                    P> | z |
                                           [ 95% C.I. ]
                               7.
[-0.748, 0.034]
   Conventional -0.357
                      0.200
                            -1.789
                                    0.074
                    0.200
## Bias-Corrected
              -0.313
                            -1.570
                                    0.116
                                          [-0.705, 0.078]
##
       Robust
              -0.313
                                          [-0.913, 0.286]
                      0.306
                            -1.024
                                    0.306
```

summary(m_test3)

```
## Covariate-adjusted Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                                1662
## BW type
                             Manual
## Kernel
                             Uniform
## VCE method
                                 NN
##
## Number of Obs.
                               1299
                                             363
## Eff. Number of Obs.
                                 58
                                              43
## Order est. (p)
                                  3
                                              3
## Order bias (q)
                              0.050
                                           0.050
## BW est. (h)
## BW bias (b)
                              0.050
                                           0.050
## rho (h/b)
                               1.000
                                           1.000
## Unique Obs.
                               1299
                                             363
##
##
##
          Method
                    Coef. Std. Err.
                                                P> | z |
                                                           [ 95% C.I. ]
##
##
    Conventional
                   -0.299
                              0.307
                                      -0.972
                                                0.331
                                                         [-0.901, 0.304]
## Bias-Corrected
                                                         [-0.647, 0.557]
                   -0.045
                              0.307
                                      -0.147
                                                0.883
##
          Robust
                   -0.045
                              0.425
                                      -0.107
                                                0.915
                                                         [-0.877, 0.787]
  ______
```

Test of Sensitivity (Kernel)

· How to weight these obs within bandwidth?



```
## Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                      1662
## BW type
                    Manual
## Kernel
                    Uniform
## VCE method
                       NN
##
## Number of Obs.
                      1299
                               363
## Eff. Number of Obs.
                       58
                               43
## Order est. (p)
                        1
                                1
                        2
                                2
## Order bias (q)
## BW est. (h)
                     0.050
                            0.050
## BW bias (b)
                     0.050
                             0.050
## rho (h/b)
                     1.000
                             1.000
## Unique Obs.
                      1299
                               363
##
##
       Method
             Coef. Std. Err. z
                                P> | z |
                                        [ 95% C.I. ]
##
   Conventional
             -0.349
                    0.134
                          -2.615
                                 0.009 [-0.611 , -0.088]
                          -2.167
                                 0.030
                                       [-0.864, -0.043]
##
       Robust
```

```
## Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                     1662
## BW type
                    Manual
               Triangular
## Kernel
## VCE method
                      NN
##
                    1299
## Number of Obs.
                              363
## Eff. Number of Obs.
                     58
                              43
## Order est. (p)
                      1
                               1
## Order bias (q)
                       2
## BW est. (h)
                    0.050
                            0.050
## BW bias (b)
                    0.050
                            0.050
## rho (h/b)
                    1.000
                             1.000
## Unique Obs.
                     1299
                              363
##
##
             Coef. Std. Err.
                         Z
                                P> | z |
      Method
                                       [ 95% C.I. ]
##
 Conventional -0.396 0.153 -2.582
                               0.010 \quad [-0.696, -0.095]
                    - -1.841
##
                                0.066
                                     [-0.863, 0.027]
      Robust
```

```
## Sharp RD estimates using local polynomial regression.
##
## Number of Obs.
                       1662
## BW type
                      Manual
               Epanechnikov
## Kernel
## VCE method
                        NN
##
## Number of Obs.
                       1299
                                363
## Eff. Number of Obs.
                       58
                                 43
## Order est. (p)
                         1
                                  1
## Order bias (q)
                         2
                                  2
## BW est. (h)
                      0.050
                              0.050
## BW bias (b)
                      0.050
                               0.050
## rho (h/b)
                      1.000
                               1.000
## Unique Obs.
                       1299
                                 363
##
##
       Method Coef. Std. Err. z \rightarrow |z| [ 95% C.I. ]
##
   Conventional -0.389 0.148 -2.621
                                    0.009 [-0.680 , -0.098]
                           -1.944
                                    0.052
       Robust -
                                          [-0.864, 0.004]
##
```