

Causal Inference TA Section (2): Matching

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Today's Goal

- Calculating Mahalanobis distance
- Propensity Score Matching (*Matching* (<https://cran.r-project.org/web/packages/Matching/index.html>))
- Coarsened Exact Matching (*MatchIt* (<https://cran.r-project.org/web/packages/MatchIt/>))
- Some other resources

Calculating Mahalanobis distance

Mahalanobis Distance_{ij} = $(X_i - X_j)' \Sigma^{-1} (X_i - X_j)$

where Σ stands var-covar matrix of X .

For example, if $X_i = (0, 0)$, $X_j = (1, 0)$, $\Sigma = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

```
mahalanobis(c(0,0), c(1,0), cov=matrix(c(1,0,0,1),2,2))
```

```
## [1] 1
```

Tutorial: Matching

This example is adopted from Jasjeet S. Sekhon. The 2004 Florida Optical Voting Machine Controversy: A Causal Analysis Using Matching (<http://sekhon.berkeley.edu/papers/SekhonOpticalMatch.pdf>).

```
library(Matching)
load("FLOpticalData.RData")
attach(data)
```

The unit of analysis is county in Florida. The treatment is *etouch* i.e. voting machine for electronic voting, the outcome is *bush04*, the vote share for Bush in 2004. We start with looking at the data.

```
dim(data)
```

```
## [1] 67 19
```

```
names(data)
```

```
## [1] "county"      "bush04"      "regTot04.rep" "regTot04.dem"
## [5] "regTot04.ind" "etouch"      "income"       "votePer96.dem"
## [9] "votePer96.rep" "votePer00.dem" "votePer00.rep" "regPer00.dem"
## [13] "regPer00.rep" "turnout00"   "hisp00"       "white00"
## [17] "black00"     "lowEduc00"   "foreignBorn00"
```

These counties are very heterogeneous on many variables: partisanship, races, education, turnout etc.

```
summary(data)
```

```
##      county      bush04      regTot04.rep      regTot04.dem
## Alachua : 1   Min.      :0.2980   Min.      : 260   Min.      : 3323
## Baker   : 1   1st Qu.:0.5326   1st Qu.: 3116   1st Qu.: 8810
## Bay     : 1   Median :0.5861   Median : 25897   Median : 23777
## Bradford: 1   Mean     :0.5952   Mean     : 53536   Mean     : 58451
## Brevard : 1   3rd Qu.:0.6783   3rd Qu.: 72664   3rd Qu.: 64509
## Broward : 1   Max.      :0.7773   Max.      :343772   Max.      :489113
## (Other) :61
## regTot04.ind      etouch      income      votePer96.dem
## Min.      : 97   Min.      :0.0000   Min.      :26032   Min.      :0.2580
## 1st Qu.: 1036   1st Qu.:0.0000   1st Qu.:30029   1st Qu.:0.3909
## Median : 11175   Median :0.0000   Median :33779   Median :0.4304
## Mean     : 24340   Mean     :0.2239   Mean     :35385   Mean     :0.4319
## 3rd Qu.: 23506   3rd Qu.:0.0000   3rd Qu.:40249   3rd Qu.:0.4715
## Max.      :202245   Max.      :1.0000   Max.      :52244   Max.      :0.6627
##
## votePer96.rep      votePer00.dem      votePer00.rep      regPer00.dem
## Min.      :0.2687   Min.      :0.2398   Min.      :0.3093   Min.      :0.2374
## 1st Qu.:0.3920   1st Qu.:0.3715   1st Qu.:0.4974   1st Qu.:0.3997
## Median :0.4417   Median :0.4285   Median :0.5465   Median :0.4834
## Mean     :0.4446   Mean     :0.4261   Mean     :0.5489   Mean     :0.5558
## 3rd Qu.:0.4825   3rd Qu.:0.4785   3rd Qu.:0.6068   3rd Qu.:0.7328
## Max.      :0.6453   Max.      :0.6741   Max.      :0.7370   Max.      :0.9358
##
## regPer00.rep      turnout00      hisp00      white00
## Min.      :0.04424   Min.      :0.4755   Min.      :0.01514   Min.      :0.4158
## 1st Qu.:0.19717   1st Qu.:0.6470   1st Qu.:0.02715   1st Qu.:0.8045
## Median :0.35667   Median :0.6855   Median :0.04888   Median :0.8500
## Mean     :0.31979   Mean     :0.6803   Mean     :0.08533   Mean     :0.8311
## 3rd Qu.:0.42368   3rd Qu.:0.7219   3rd Qu.:0.09394   3rd Qu.:0.8955
## Max.      :0.57081   Max.      :0.8270   Max.      :0.57325   Max.      :0.9558
##
## black00      lowEduc00      foreignBorn00
## Min.      :0.02151   Min.      :0.01762   Min.      :0.01123
## 1st Qu.:0.08187   1st Qu.:0.03470   1st Qu.:0.02404
## Median :0.11600   Median :0.04685   Median :0.05269
## Mean     :0.14186   Mean     :0.05282   Mean     :0.07494
## 3rd Qu.:0.17171   3rd Qu.:0.06493   3rd Qu.:0.09134
## Max.      :0.57358   Max.      :0.14686   Max.      :0.50936
##
```

If we simply looks at the difference in means, using electronical voting decreased Bush's share

```
table(etouch)
```

```
## etouch
## 0 1
## 52 15
```

```
tapply(bush04, etouch, mean)
```

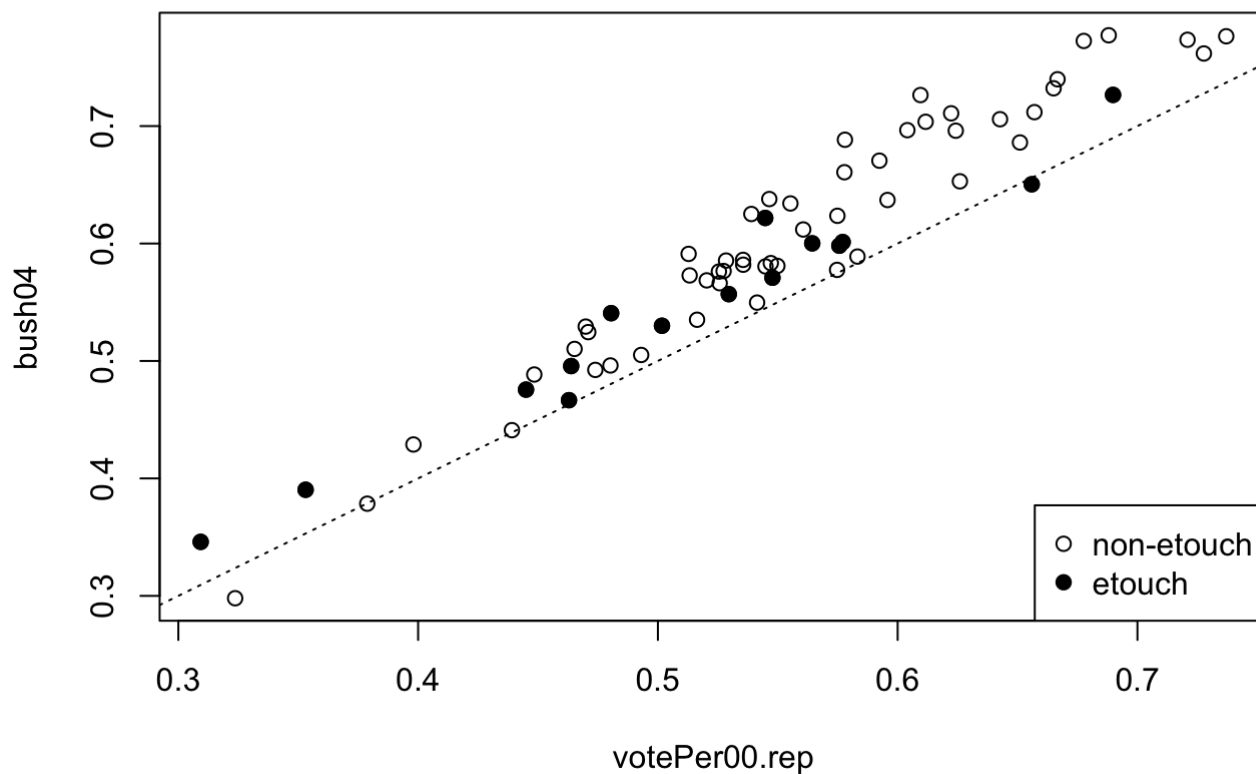
```
##          0          1
## 0.6097499 0.5447324
```

```
summary(lm(bush04 ~ etouch))
```

```
##
## Call:
## lm(formula = bush04 ~ etouch)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.311761 -0.054553 -0.004049  0.077816  0.181817
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.60975    0.01441  42.327  <2e-16 ***
## etouch      -0.06502    0.03045  -2.136   0.0365 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1039 on 65 degrees of freedom
## Multiple R-squared:  0.06556,    Adjusted R-squared:  0.05118
## F-statistic:  4.56 on 1 and 65 DF,  p-value: 0.03649
```

What if we add some covariates given the heterogeneity among counties. Let's start with vote shares for Bush in 2000.

```
plot(bush04 ~ votePer00.rep)
points(bush04[etouch==1] ~ votePer00.rep[etouch==1], pch=19)
abline(0,1, lty=3)
legend("bottomright", c("non-etouch", "etouch"), pch=c(1,19))
```



```
summary(lm(bush04 ~ etouch + votePer00.rep))
```

```
##
## Call:
## lm(formula = bush04 ~ etouch + votePer00.rep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.052780 -0.017312  0.000566  0.021303  0.060632
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.01215    0.02124  -0.572   0.5692
## etouch        -0.01417    0.00815  -1.739   0.0868 .
## votePer00.rep  1.11227    0.03739  29.748 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02719 on 64 degrees of freedom
## Multiple R-squared:  0.937, Adjusted R-squared:  0.935
## F-statistic: 475.8 on 2 and 64 DF, p-value: < 2.2e-16
```

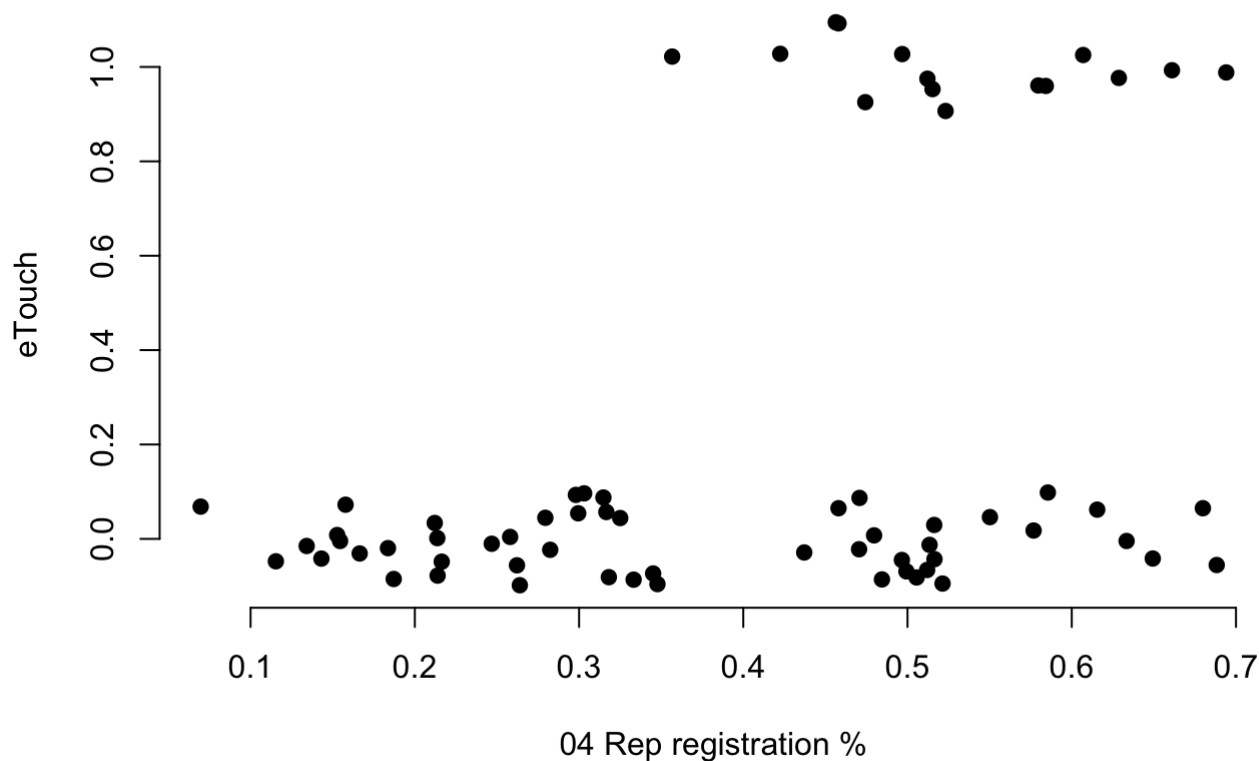
We then create variables for the share of both parties in 2004 registration and add them into the model:

```
reg2pty04.rep <- regTot04.rep / (regTot04.rep + regTot04.dem)
reg2pty04.dem <- regTot04.dem / (regTot04.rep + regTot04.dem)
summary(lm(bush04 ~ etouch + votePer00.rep + reg2pty04.rep))
```

```
##
## Call:
## lm(formula = bush04 ~ etouch + votePer00.rep + reg2pty04.rep)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.060715 -0.012574  0.000669  0.018052  0.044165
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -0.0034137  0.0196353  -0.174 0.862536
## etouch       -0.0002508  0.0084093  -0.030 0.976298
## votePer00.rep  1.1453036  0.0354938  32.268 < 2e-16 ***
## reg2pty04.rep -0.0745826  0.0206343  -3.614 0.000599 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02494 on 63 degrees of freedom
## Multiple R-squared:  0.9478, Adjusted R-squared:  0.9453
## F-statistic: 381.3 on 3 and 63 DF,  p-value: < 2.2e-16
```

Note that p value is 0.98, which indicates a super strong **nonfinding**. The changes in the significance of etouch suggest the results are very model-based. Matching might help, for

```
par(mfrow=c(1,1))
plot(reg2pty04.rep, jitter(etouch, factor=.5), pch=19,
      ylab="eTouch", bty="n", xlab="04 Rep registration %")
```

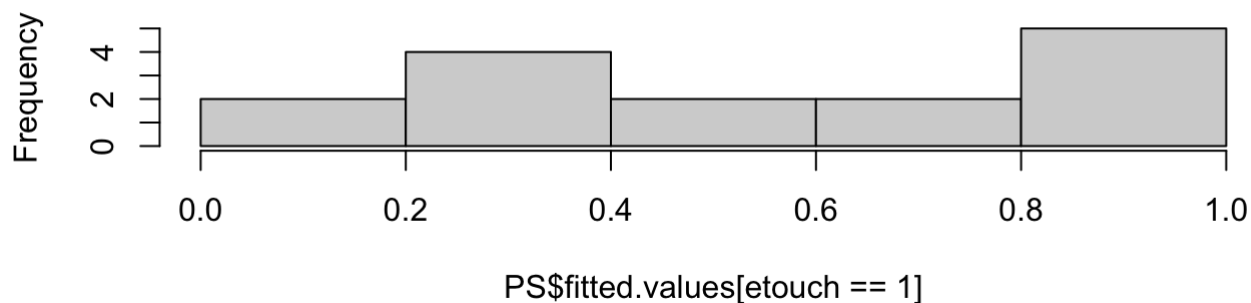
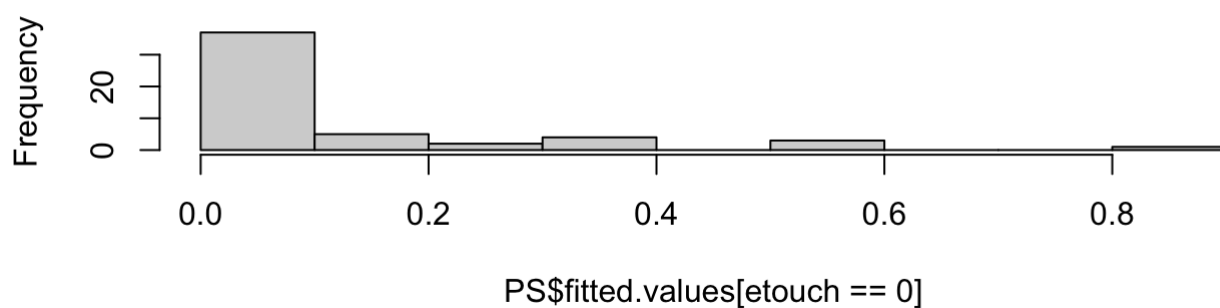


Propensity Score Matching

- Run a logit/probit model to estimate propensity scores for each observation
- Matching treated and control groups based on the propensity scores
- Show balance of your matching
- Estimate the treatment effects (ATT)

We start with calculating the propensity of each county to employ voting machines using logistic regression. Here we use the share of each party in voter registration in 2004 and the population structure (share of each race). The distributions look quite different. Treated groups are those that very likely to be treated and control groups are those unlikely to be treated.

```
PS <- glm(etouch ~ regTot04.dem + regTot04.rep + regTot04.ind + hisp00 + white00 + black
00, family=binomial(link="logit"))
par(mfrow=c(2,1))
hist(PS$fitted.values[etouch==1], main="eVoting")
hist(PS$fitted.values[etouch==0], main="non-eVoting")
```

eVoting**non-eVoting**

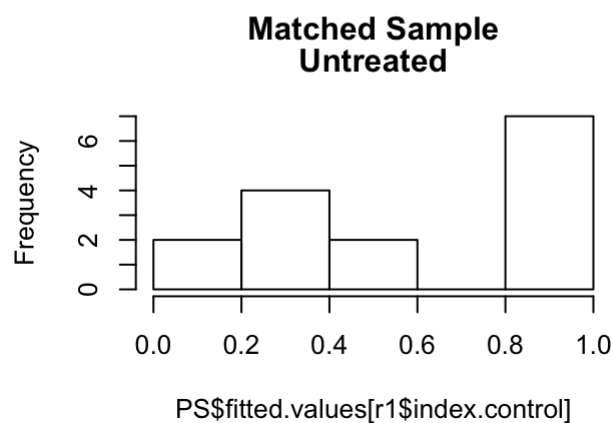
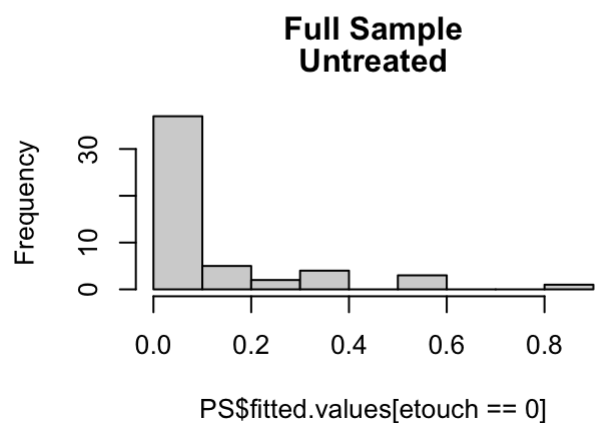
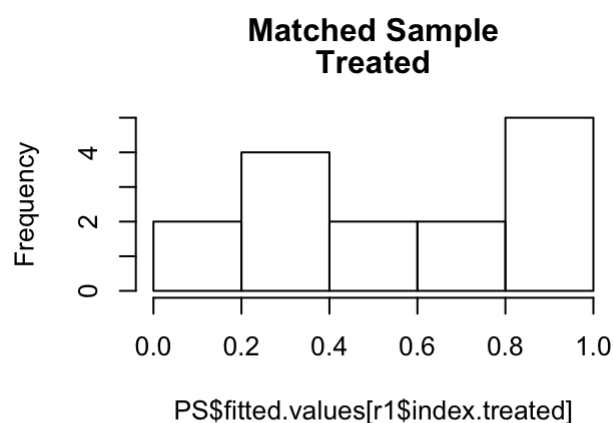
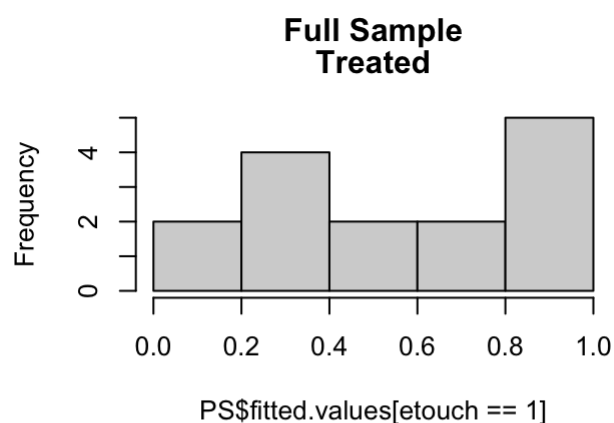
We then match the sample based on propensity scores and estimate the treatment effect (By default, it uses 1:1 matching. All weights=1). The result remains insignificant.

```
r1 <- Match(Y=bush04, Tr=etouch, X=PS$fitted.values)
summary(r1)
```

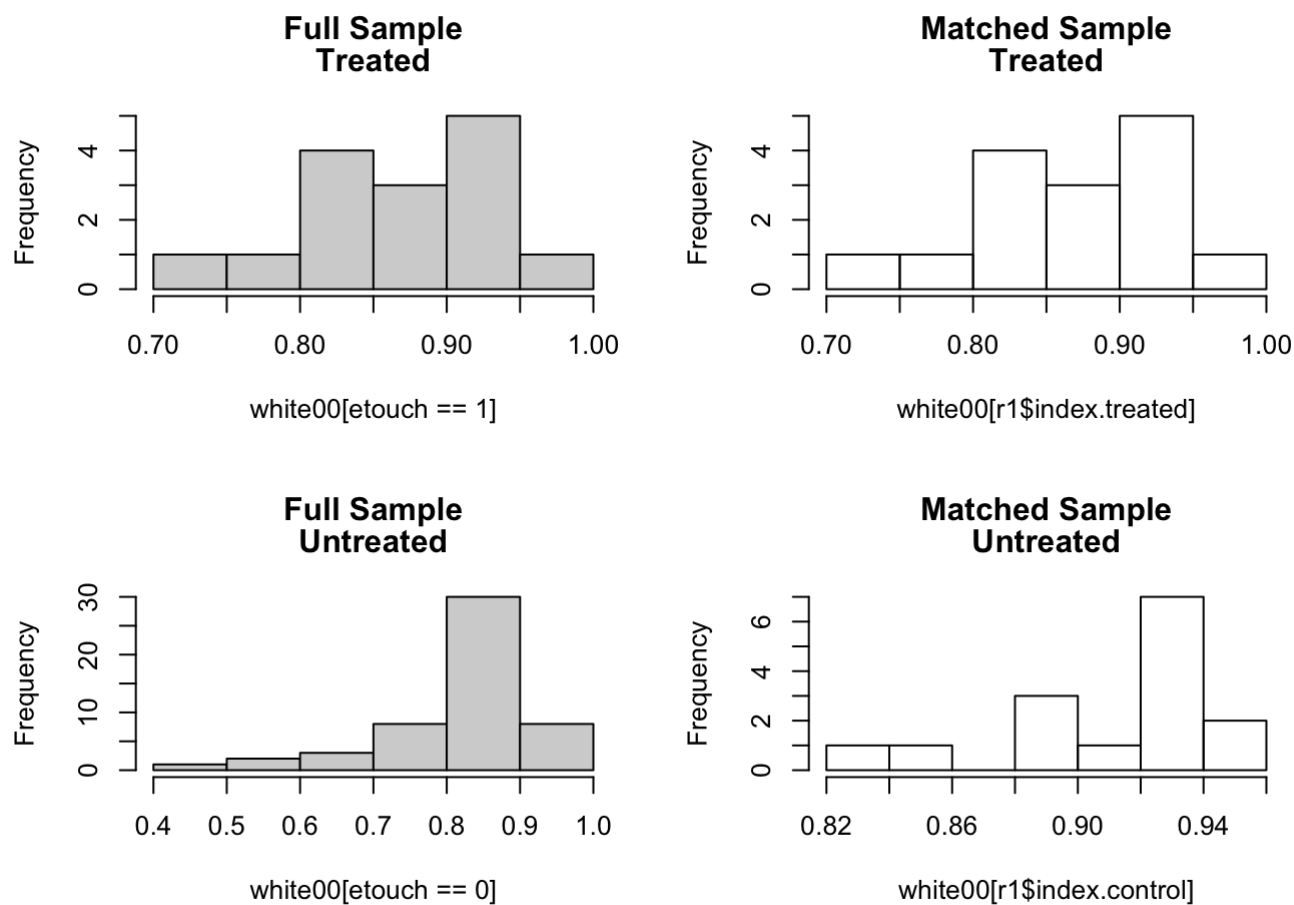
```
##
## Estimate...   -0.01594
## AI SE.....  0.043608
## T-stat..... -0.36552
## p.val.....  0.71472
##
## Original number of observations..... 67
## Original number of treated obs..... 15
## Matched number of observations..... 15
## Matched number of observations (unweighted). 15
```

Let check the balance of matching. We take two examples: the propensity and the population structure.

```
library(weights)
par(mfcol=c(2,2))
hist(PS$fitted.values[etouch==1],
     main=c("Full Sample", "Treated"))
hist(PS$fitted.values[etouch==0],
     main=c("Full Sample", "Untreated"))
wtd.hist(PS$fitted.values[r1$index.treated],
         weight=r1$weights,
         main=c("Matched Sample", "Treated"))
wtd.hist(PS$fitted.values[r1$index.control],
         weight=r1$weights,
         main=c("Matched Sample", "Untreated"))
```



```
par(mfcol=c(2,2))
hist(white00[etouch==1],
     main=c("Full Sample", "Treated"))
hist(white00[etouch==0],
     main=c("Full Sample", "Untreated"))
wtd.hist(white00[r1$index.treated],
         weight=r1$weights,
         main=c("Matched Sample", "Treated"))
wtd.hist(white00[r1$index.control],
         weight=r1$weights,
         main=c("Matched Sample", "Untreated"))
```

We can also see some tables and stats if needed.

```
mb <- MatchBalance(etouch ~ regTot04.dem + regTot04.rep + regTot04.ind + hisp00 + white00 + black00, match.out=r1)
```

```

##
## ***** (V1) regTot04.dem *****
##
##          Before Matching          After Matching
## mean treatment.....      139111      139111
## mean control.....        35184        63915
## std mean diff.....       67.161       48.594
##
## mean raw eQQ diff.....     99234        87584
## med  raw eQQ diff.....     39829        20301
## max  raw eQQ diff.....    294024       373341
##
## mean eCDF diff.....        0.29615      0.14242
## med  eCDF diff.....        0.3141      0.13333
## max  eCDF diff.....        0.48077      0.33333
##
## var ratio (Tr/Co).....     12.041        20.212
## T-test p-value.....        0.021589     0.062429
## KS Bootstrap p-value..        0.01        0.294
## KS Naive p-value.....     0.0057459     0.37521
## KS Statistic.....         0.48077      0.33333
##
##
## ***** (V2) regTot04.rep *****
##
##          Before Matching          After Matching
## mean treatment.....     124571      124571
## mean control.....       33046        84398
## std mean diff.....      88.941       39.038
##
## mean raw eQQ diff.....     90564        57546
## med  raw eQQ diff.....     79045        27428
## max  raw eQQ diff.....    174632       202169
##
## mean eCDF diff.....        0.33718      0.13636
## med  eCDF diff.....         0.35      0.13333
## max  eCDF diff.....        0.57821      0.33333
##
## var ratio (Tr/Co).....      5.3691        5.5937
## T-test p-value.....     0.0041597     0.093614
## KS Bootstrap p-value..        0.002        0.286
## KS Naive p-value.....     0.0003795     0.37521
## KS Statistic.....         0.57821      0.33333
##
##
## ***** (V3) regTot04.ind *****
##
##          Before Matching          After Matching
## mean treatment.....       61518        61518
## mean control.....       13615        32768
## std mean diff.....      72.752       43.663
##
## mean raw eQQ diff.....     45249        40340
## med  raw eQQ diff.....     20246        18329
## max  raw eQQ diff.....    146108       150973

```

```

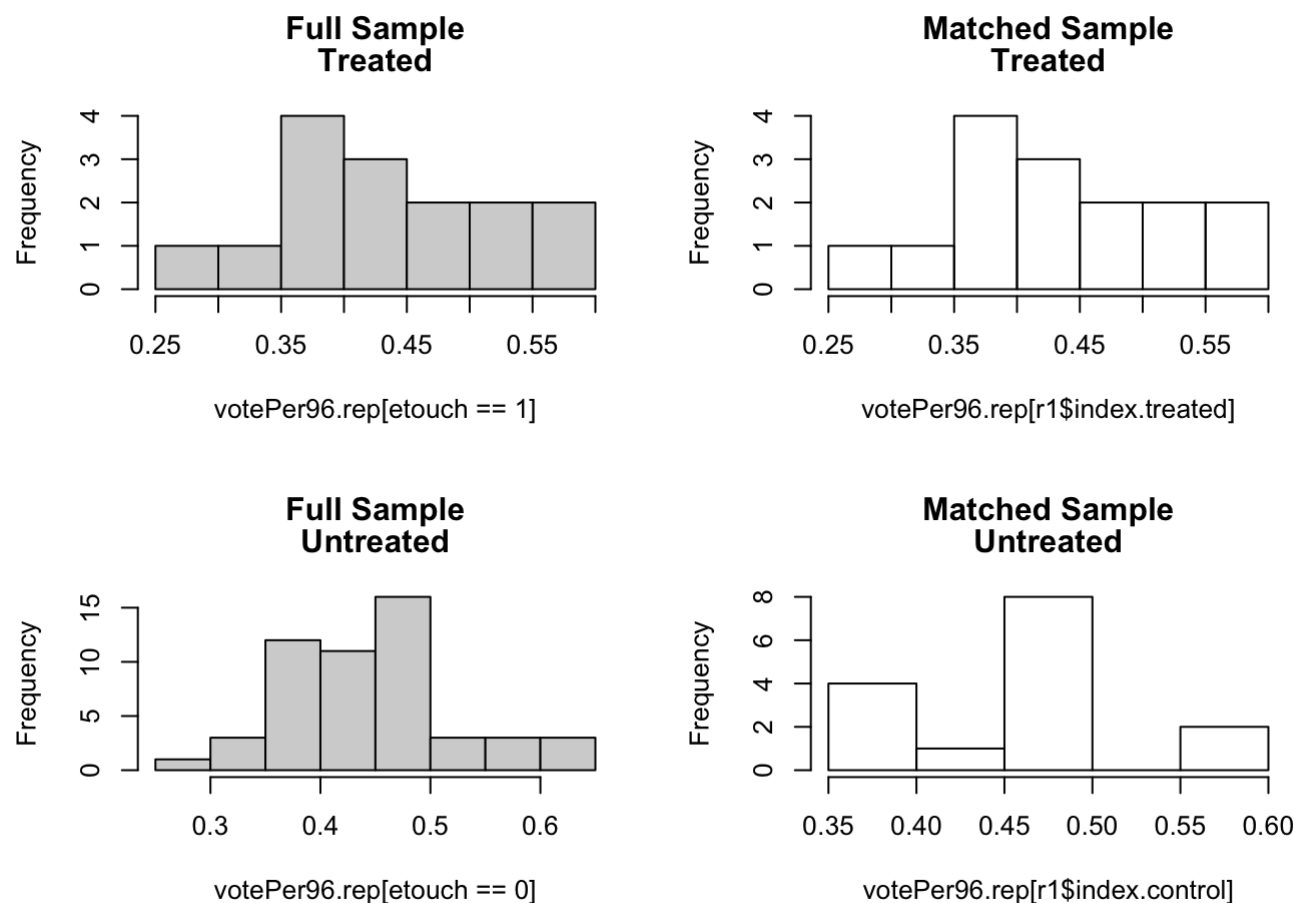
##
## mean eCDF diff..... 0.32505      0.16364
## med eCDF diff..... 0.34231      0.13333
## max eCDF diff..... 0.54872      0.4
##
## var ratio (Tr/Co)..... 11.279      17.074
## T-test p-value..... 0.014141      0.082163
## KS Bootstrap p-value.. < 2.22e-16      0.134
## KS Naive p-value..... 0.0018047      0.1813
## KS Statistic..... 0.54872      0.4
##
##
## ***** (V4) hisp00 *****
##
##          Before Matching      After Matching
## mean treatment..... 0.12191      0.12191
## mean control..... 0.074775      0.068197
## std mean diff..... 34.627      39.459
##
## mean raw eQQ diff..... 0.04384      0.054206
## med raw eQQ diff..... 0.032182      0.031623
## max raw eQQ diff..... 0.17734      0.17734
##
## mean eCDF diff..... 0.2061      0.26667
## med eCDF diff..... 0.20256      0.3
## max eCDF diff..... 0.44359      0.6
##
## var ratio (Tr/Co)..... 2.5494      2.2167
## T-test p-value..... 0.22053      0.22473
## KS Bootstrap p-value.. 0.018      0.004
## KS Naive p-value..... 0.013913      0.0090332
## KS Statistic..... 0.44359      0.6
##
##
## ***** (V5) white00 *****
##
##          Before Matching      After Matching
## mean treatment..... 0.86834      0.86834
## mean control..... 0.82038      0.91283
## std mean diff..... 72.623      -67.36
##
## mean raw eQQ diff..... 0.06333      0.046525
## med raw eQQ diff..... 0.034532      0.043789
## max raw eQQ diff..... 0.3273      0.085413
##
## mean eCDF diff..... 0.14545      0.25758
## med eCDF diff..... 0.12821      0.26667
## max eCDF diff..... 0.36026      0.53333
##
## var ratio (Tr/Co)..... 0.40098      2.8571
## T-test p-value..... 0.038725      0.031501
## KS Bootstrap p-value.. 0.074      0.026
## KS Naive p-value..... 0.070883      0.028057
## KS Statistic..... 0.36026      0.53333

```

```
##
##
## ***** (V6) black00 *****
##
##          Before Matching      After Matching
## mean treatment.....    0.10768      0.10768
## mean control.....    0.15173      0.067459
## std mean diff.....    -72.421      66.116
##
## mean raw eQQ diff.....    0.050061      0.042927
## med  raw eQQ diff.....    0.024652      0.041538
## max  raw eQQ diff.....    0.35486      0.075748
##
## mean eCDF diff.....    0.12979      0.23333
## med  eCDF diff.....    0.13205      0.2
## max  eCDF diff.....    0.28333      0.53333
##
## var ratio (Tr/Co).....    0.33124      2.6379
## T-test p-value.....    0.046802      0.032147
## KS Bootstrap p-value..    0.246      0.026
## KS Naive p-value.....    0.24759      0.028057
## KS Statistic.....    0.28333      0.53333
##
##
## Before Matching Minimum p.value: < 2.22e-16
## Variable Name(s): regTot04.ind  Number(s): 3
##
## After Matching Minimum p.value: 0.004
## Variable Name(s): hisp00  Number(s): 4
```

Do matching affect other variables? Seems not

```
par(mfcol=c(2,2))
hist(votePer96.rep[etouch==1],
     main=c("Full Sample", "Treated"))
hist(votePer96.rep[etouch==0],
     main=c("Full Sample", "Untreated"))
wtd.hist(votePer96.rep[r1$index.treated],
         weight=r1$weights,
         main=c("Matched Sample", "Treated"))
wtd.hist(votePer96.rep[r1$index.control],
         weight=r1$weights,
         main=c("Matched Sample", "Untreated"))
```



Matching on variables

```
r2 <- Match(Y=bush04, Tr=etouch, X=data[,c(3:5, 15:17)])
summary(r2)
```

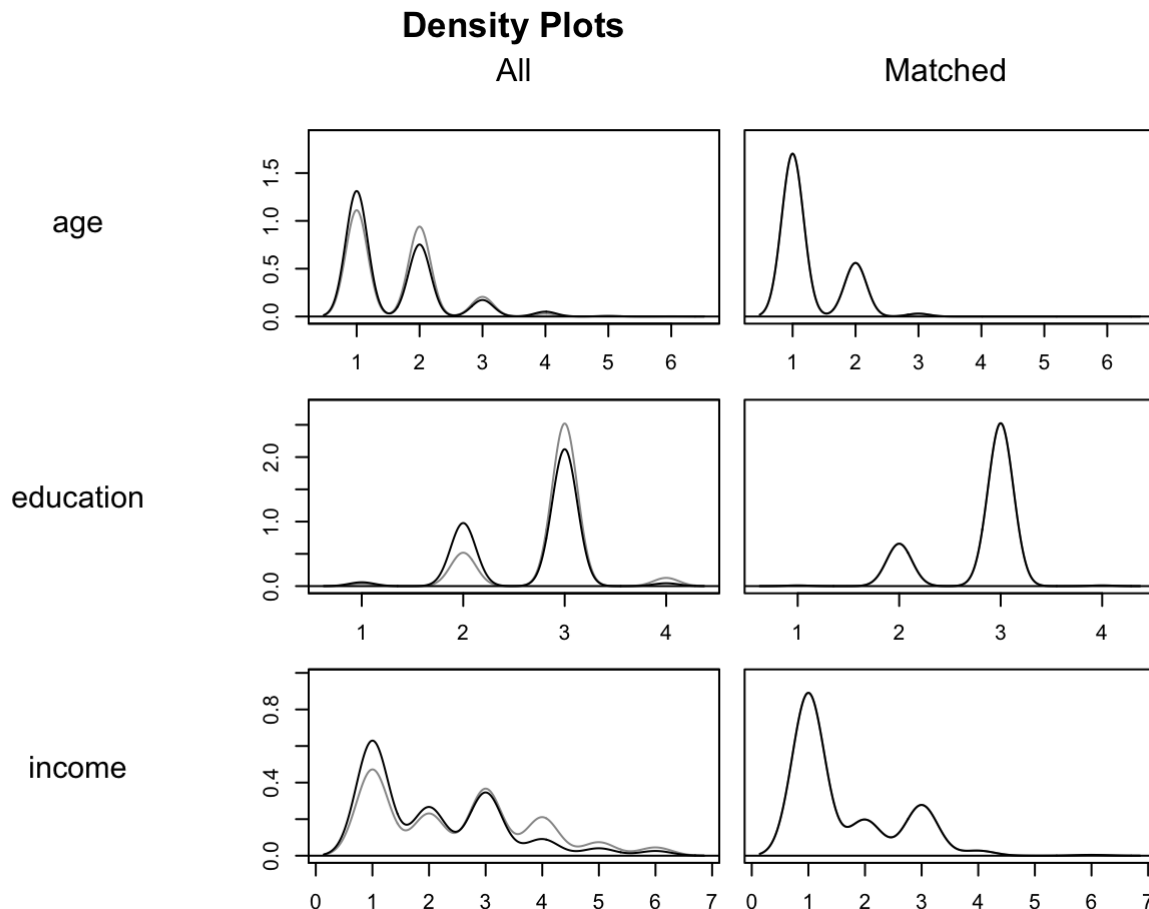
```
##
## Estimate... -0.035793
## AI SE..... 0.032596
## T-stat..... -1.0981
## p.val..... 0.27217
##
## Original number of observations..... 67
## Original number of treated obs..... 15
## Matched number of observations..... 15
## Matched number of observations (unweighted). 15
```

Coarsened Exact Matching

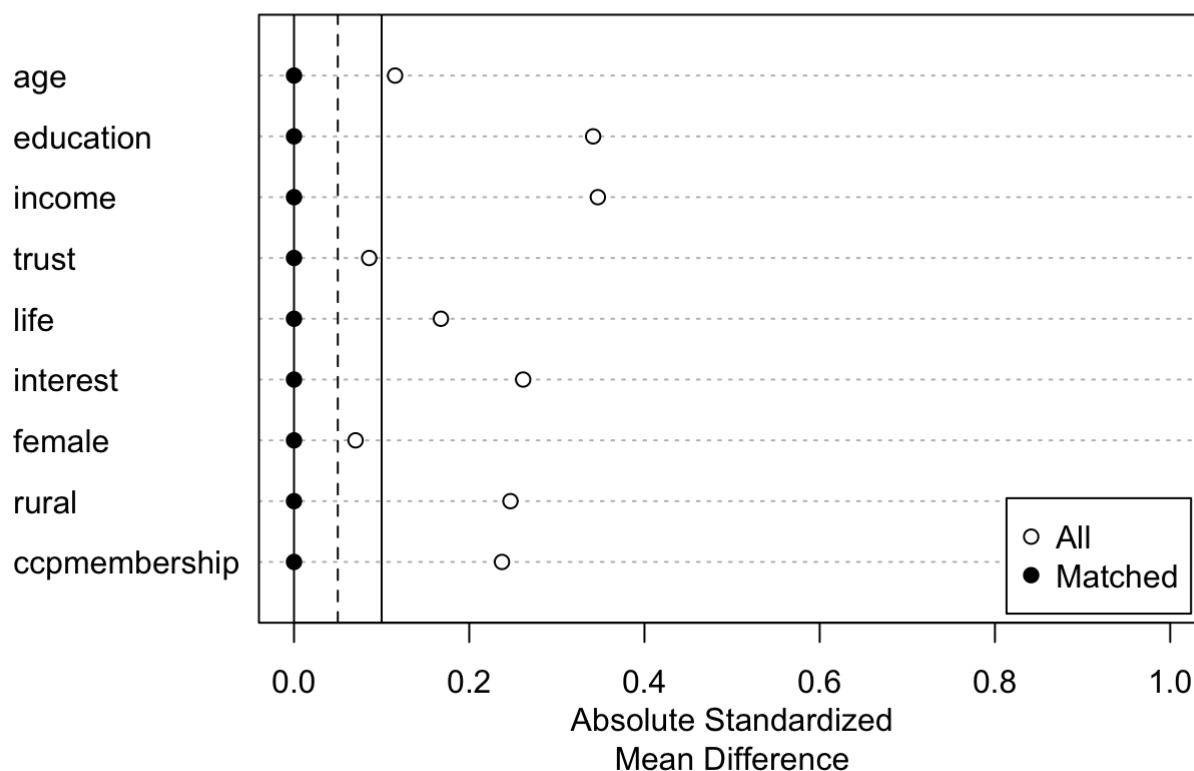
- Select covariates for matching (and the cutoff/threshold, if needed)
- Matching the treated and control groups based on the covariates
- Show balance
- Estimate the effects

In addition to Propensity Score Matching, another widely used method of matching is coarsened exact matching. We use package “MatchIt (<https://kosukeimai.github.io/MatchIt/index.html>)” to replicate results from Wang and Huang 2020, CPS, When “Fake News” Becomes Real: The Consequences of False Government Denials in an Authoritarian Country (<https://doi.org/10.1177/0010414020957672>).

```
library(haven)
library(MatchIt)
Data <- read_dta("cps-wave2_clean.dta")
cem1<- matchit(experience~age+education+income+trust+life+interest+female+rural+ccpmembe
rship,method = 'cem',data=Data)
plot(cem1, type = "density", interactive = FALSE,which.xs = ~age+education+income)
```



```
plot(summary(cem1),xlim=c(0,1))
```



```
mdata<- match.data(cem1)
summary(lm(rumor~experience,data=mdata))
```

```
##
## Call:
## lm(formula = rumor ~ experience, data = mdata)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -47.261 -27.006   2.994  27.994  52.994
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   47.006     1.727   27.215  <2e-16 ***
## experience     1.255     2.504    0.501    0.616
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 31.75 on 643 degrees of freedom
## Multiple R-squared:  0.0003904, Adjusted R-squared:  -0.001164
## F-statistic: 0.2512 on 1 and 643 DF, p-value: 0.6164
```

Other resources

1. Many studies now use matching as a robustness check and leave most details of matching process in the appendix. But some does use mataching as a main specification and published in top journal. E.g., Agerberg and Sohlberg, CPS 2021, Personal Proximity and Reactions to Terrorism (<https://doi.org/10.1177/0010414021997162>). (codes are based on Stata).
2. Most studies use matching in cross-sectional data. For time-series cross-sectional data, see Imai, Kim, and Wang (2021) *PanelMatch* (<https://cran.r-project.org/web/packages/PanelMatch/index.html>):