

University of British Columbia  
Department of Electrical & Computer Engineering  
EECE 487 (Winter 2012-2013): Introduction to Robotics  
Assignment #2, due Thursday Feb 7<sup>th</sup>

**Exercise # 1:**

A rigid motion  $\underline{y} = \underline{\rho} + \underline{d} + \underline{Q}(\underline{x} - \underline{\rho})$  mapping a point  $\underline{x}$  to another point  $\underline{y}$  changes the point coordinates (with respect to  $\{\underline{\rho}, \underline{C}\}$ ) from  $x$  to  $y$  according to

$$\begin{bmatrix} y \\ 1 \end{bmatrix} = \begin{bmatrix} Q & d \\ 0^T & 1 \end{bmatrix} \begin{bmatrix} x \\ 1 \end{bmatrix}$$

What is the inverse of this transformation? Does this inverse always exist? Explain.

**Exercise # 2:**

What is the acceleration of a point with coordinates  $y(t) = d(t) + Q(t)x(t)$ , where  $Q(t)$  is a rotation matrix?

**Exercise # 3:**

The Puma 560 shown in Figure 1 has a reach of approximately 0.92m, and a payload capacity of 2.3kg. This makes it ideal for medium-to-lightweight assembly, welding, materials handling, packaging and inspection applications.



Figure 1: Photo of a 500 series Puma robot.

Using the schematic of Figure 2, do the following:

DH Parameter	$\theta_i$ (deg)	$d_i$ (mm)	$a_i$ (mm)	$\alpha_i$ (deg)
Link 1				
Link 2				
Link 3				
Link 4				
Link 5				
Link 6				

Table 1: DH Parameters for the Puma 560

- Directly on the schematic, assign coordinate frames by means of the Denavit-Hartenberg convention. Assume  $\underline{C}_0$  and  $\underline{C}_6$  are as illustrated in the “home” position. Fill in Table 1 the values of the DH-parameters. For each joint, consider the positive rotation to be in the *right-handed sense* (NB: These are different from what is in the notes).
- Compose a chain of transformations that will give you the relationship between the base frame,  $\{\underline{\rho}_0, \underline{C}_0\}$ , and the end-effector frame  $\{\underline{\rho}_6, \underline{C}_6\}$  (use notation from Salcudean notes as was done for example 2.5 on p 31).
- Write a Matlab m-file which prompts the user for the sequence of 6 joint angles in degrees (for example, the user might type “45,-45,45,0,-30,90”), then *outputs the resulting homogeneous transformation matrix* relating the base and end effector frames. As well, graphically plot the location of each link origin (e.g., using Matlab’s “plot3” function, indicate each origin with an “\*”) for the given joint angles.
- Use your code to compute base-to-gripper transformations and display your results and the locations of the link origins for the following sets of joint configurations:  $\underline{q} = [0^\circ \ 0^\circ \ 0^\circ \ 0^\circ \ 0^\circ \ 0^\circ]^T$ ,  $\underline{q} = [0^\circ \ 0^\circ \ -90^\circ \ 0^\circ \ 0^\circ \ 180^\circ]^T$ ,  $\underline{q} = [45^\circ \ -45^\circ \ 45^\circ \ 0^\circ \ -30^\circ \ 90^\circ]^T$ ,  $\underline{q} = [15^\circ \ 30^\circ \ -30^\circ \ -30^\circ \ 15^\circ \ -15^\circ]^T$

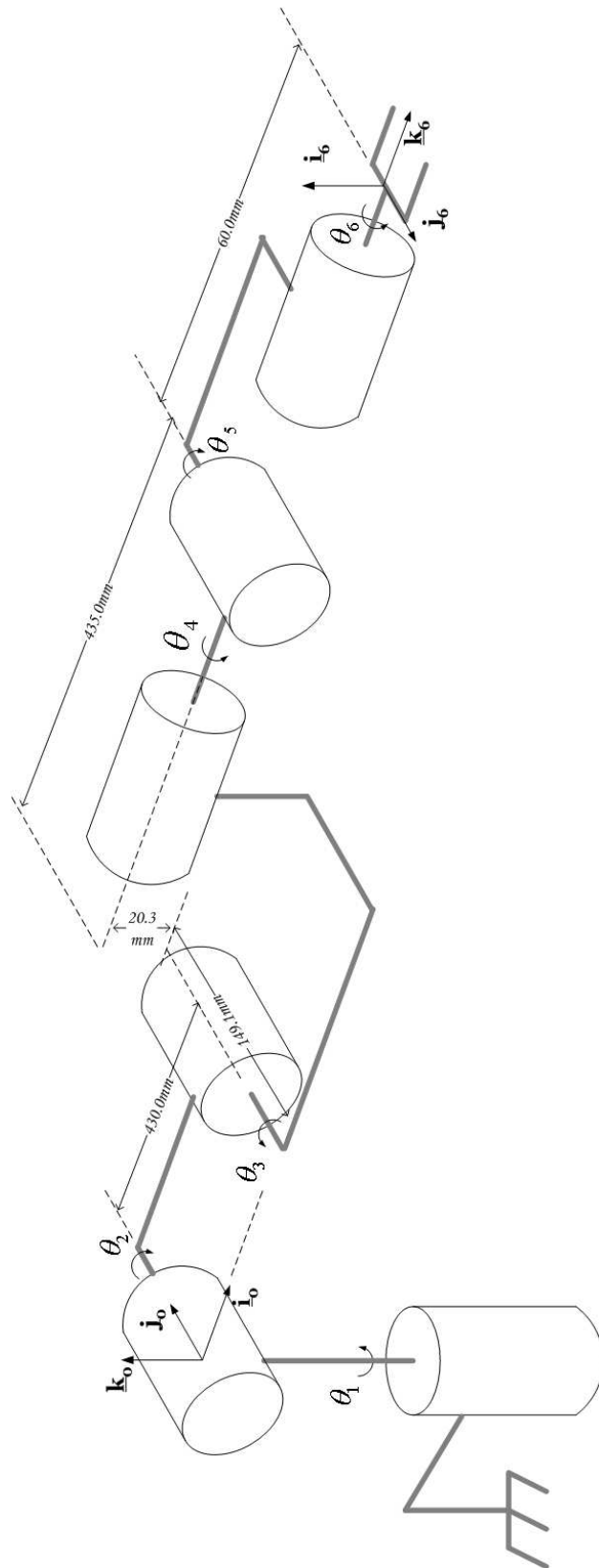


Figure 2: The Puma 560 robot schematic (not to scale).