Algorithm Lab 4

Supta Philip Philip

October 17, 2022

1 Pre-Requisite in C++

- 1. Function
- 2. Pointer
- 3. Array / Dynamic Array
- 4. Dynamic Array 2D/ Matrix
- 5. Random number
- 6. File Operation
- 7. Standard Template Library(STL)

2 Recursive Function

- 1. Fibonacci
- 2. Factorial
- 3. Euclid's algorithm for GCD

Algorithm 1 Fibonacci

```
1: procedure FIBONACCI(n)

2: if n \le 1 then

3: return n

4: else

5: return FIBONACCI(n-1)+FIBONACCI(n-2)

6: end if

7: end procedure
```

Algorithm 2 Factorial

```
1: procedure Factorial(n)
2: if n \le 0 then
3: return 1
4: else
5: return n*Factorial(n-1)
6: end if
7: end procedure
```

Algorithm 3 Euclid's algorithm [Recursive]

```
1: procedure GCD(n, m)
2:
     if n = m then
        {\bf return}\ m
3:
     else if n \geq m then
4:
        return GCD(n-m,m)
5:
6:
     else
        return GCD(n, m-n)
7:
     end if
8:
9: end procedure
```

Algorithm 4 Euclid's algorithm for GCD[Iterative]

```
1: procedure GCD(a, b)
                                                                            \triangleright The g.c.d. of a and b
        r \leftarrow a \bmod b
2:
                                                                   \triangleright We have the answer if r is 0
3:
        while r \neq 0 do
             a \leftarrow b
4:
             b \leftarrow r
5:
             r \leftarrow a \bmod b
6:
7:
        end while
                                                                                        \triangleright The gcd is b
        \mathbf{return}\ b
9: end procedure
```

3 Iterative Algorithm

- 1. Linear Search
- 2. Bubble sort
- 3. Selection sort
- 4. Insertion Sort

Algorithm 5 Linear Search

```
1: procedure LINEAR(A, n, item)
2: for i \leftarrow 0, n-1 do
3: if A[i] == item then
4: return i
5: end if
6: end for
7: return -1
8: end procedure
```

${\bf Algorithm~6~Bubble~Sort}$

```
1: procedure BUBBLESORT(A, n)
2: for k \leftarrow 0, n-1 do
3: for i \leftarrow 0, n-1 do
4: if A[i] > A[i+1] then
5: swap(A[i], A[i+1]
6: end if
7: end for
8: end for
9: end procedure
```

Algorithm 7 Selection Sort

```
1: procedure SelectionSort(A, n)
2:
       \mathbf{for}\ i \leftarrow 0, n-1\ \mathbf{do}
3:
           iMin \leftarrow i
           for j \leftarrow i+1, n-1 do
4:
               if A[j] < A[iMin] then
5:
                   iMin = j
6:
7:
               end if
                swap(A[iMin], A[i])
8:
           end for
9:
       end for
10:
11: end procedure
```

Algorithm 8 Insertion Sort

```
1: procedure InsertionSort(A, n)
 2:
        \mathbf{for}\ j \leftarrow 1, n-1\ \mathbf{do}
 3:
            value \leftarrow A[j]
            i \leftarrow j-1
 4:
            while i > 0 \& A[i] > value do
 5:
 6:
                swap(A[i],A[i+1]) \\
 7:
                i \leftarrow i-1
            end while
 8:
            A[i+1] = value
 9:
        end for
10:
11: end procedure
```

4 Divide and Conquer Algorithm

Algorithm 9 Binary Search Recursive algorithm

```
1: procedure BINARYSEARCH(A, low, high, x)
      if low > high then
2:
3:
         return -1
      end if
4:
      mid = (low + high)/2
5:
      if x == A[mid] then
6:
         {\bf return}\ mid
7:
      else if x < A[mid] then
8:
         return BINARYSEARCH(A, low, mid - 1, x)
9:
10:
         return BINARYSEARCH(A, mid + 1, high, x)
11:
      end if
12:
13: end procedure
```

Algorithm 10 Binary Search Iterative algorithm

```
1: procedure BINARYSEARCH(A, n, x)
      low = 0, high = n - 1
2:
3:
      while low < high do
          mid = (low + high)/2
4:
          if x == A[mid] then
5:
             {\bf return}\ mid
6:
7:
          end if
          if x < A[mid] then
8:
             high = mid - 1
9:
          else
10:
             low = mid + 1
11:
          end if
12:
13:
      end while
      return -1
14:
15: end procedure
```

Algorithm 11 Merge Two Arrays

```
1: procedure MERGE(A, B, n, m)
2:
       i \leftarrow 0, j \leftarrow 0, k \leftarrow 0
       while i \le n - 1 \& j \le m - 1 do
3:
           if A[i] > B[j] then
4:
               C[k++] \leftarrow B[j++]
5:
6:
           else
               C[k++] \leftarrow A[i++]
7:
           end if
8:
       end while
9:
       while i \le n-1 do
10:
           C[k++] \leftarrow A[i++]
11:
       end while
12:
       while j \le m-1 do
13:
           C[k++] \leftarrow B[j++]
14:
       end while
15:
16: end procedure
```

Algorithm 12 Merge

```
1: procedure MERGE(A, left, mid, right)
        n1 = mid - left + 1
 2:
        n2 = right - mid
 3:
         L[1...n1] and R[1...n2]
        for i \leftarrow 0, n1 - 1 do
 4:
            L[i] \leftarrow A[left+i]
 5:
        end for
 6:
 7:
        for j \leftarrow 0, n2 - 1 do
            R[j] \leftarrow A[mid + 1 + j]
 8:
        end for
 9:
        i \leftarrow 0, j \leftarrow 0, k \leftarrow left
10:
11:
        while i \le n1 - 1 \& j \le n2 - 1 \text{ do}
            if L[i] < R[j] then
12:
                A[k++] \leftarrow L[i++]
13:
            else
14:
                A[k++] \leftarrow R[i++]
15:
            end if
16:
        end while
17:
        while i \le n1 - 1 do
18:
            A[k++] \leftarrow L[i++]
19:
        end while
20:
        while j \le n2 - 1 do
21:
            A[k++] \leftarrow R[j++]
22:
23:
        end while
24: end procedure
```

Algorithm 13 Merge Sort

```
1: procedure MergeSort(A, left, right)
2: if left < right then
3: mid = (left + right)/2
4: MergeSort(A, left, mid)
5: MergeSort(A, mid + 1, right)
6: Merge(A, left, mid, right)
7: end if
8: end procedure
```

Algorithm 14 partition

```
1: procedure PARTITION(A, start, end)
2:
      pivot = A[end]
      pIndex = start
3:
      for i \leftarrow start, end - 1 do
4:
          if A[i] < pivot then
5:
6:
             swap(A[i], A[pIndex])
             pIndex + +
7:
          end if
8:
      end for
9:
      swap(A[pIndex], A[end])
10:
      return pIndex
12: end procedure
```

Algorithm 15 Quick Sort

```
1: procedure QUICKSORT(A, start, end)
2: if start >= end then
3: pIndex = PARTITION(A, start, end)
4: QUICKSORT(A, start, pIndex - 1)
5: QUICKSORT(A, pIndex + 1, end)
6: end if
7: end procedure
```