

#### DIPARTIMENTO DI

#### SCIENZE STATISTICHE "PAOLO FORTUNATI"



#### 2 - Recurrent Neural Network

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# Sequential Data

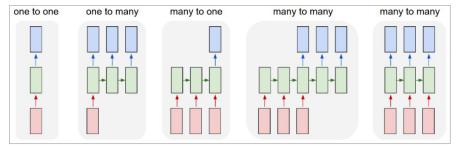
### What are Sequential Data

- Sequential data refers to data that has a natural ordering to it, meaning that each data point is dependent on the data that came before it. In other words, the sequence of the data matters.
- Examples of sequential data include time series data such as stock prices, weather data, or audio signals, where each point in time is dependent on the previous point. Other examples include text data such as sentences or paragraphs, where the meaning of each word is dependent on the context of the words that came before it.
- Sequential data can be modeled and analyzed using various techniques, including Hidden Markov Models (HMMs), and autoregressive models such as ARIMA.

### What are Sequential Data

- In the context of machine learning, sequential data presents unique challenges because the order of the data is important and traditional machine learning models such as decision trees and linear regression do not take this into account.
- Models such as RNNs (Recurrent Neural Network) are specifically designed to handle sequential data by processing the data one element at a time and retaining information about the previous elements to make predictions about future elements in the sequence.

### What are Sequential Data



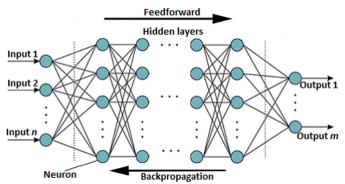
Each rectangle is a vector and arrows represent functions (e.g. matrix multiply). Input vectors are in red, output vectors are in blue and green vectors hold the RNN's state (more on this soon). From left to right: (1) Vanilla mode of processing without RNN, from fixed-sized input to fixed-sized output (e.g. image classification). (2) Sequence output (e.g. image captioning takes an image and outputs a sentence of words). (3) Sequence input (e.g. sentiment analysis where a given sentence is classified as expressing positive or negative sentiment). (4) Sequence input and sequence output (e.g. Machine Translation: an RNN reads a sentence in English and then outputs a sentence in French). (5) Synced sequence input and output (e.g. video classification where we wish to label each frame of the video). Notice that in every case are no pre-specified constraints on the lengths sequences because the recurrent transformation (green) is fixed and can be applied as many times as we like.

What are Recurrent Neural Networks,

### What are Recurrent Neural Networks

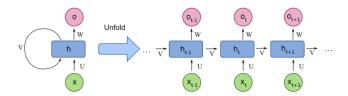
#### What are Recurrent Neural Networks

- A major characteristic of all neural networks you have seen so far, such as densely connected networks and convnets, is that they have no memory.
- Each input shown to them is processed independently, with no state kept in between inputs.

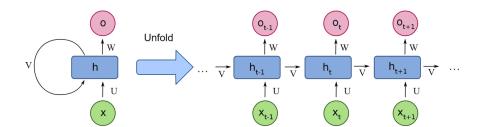


#### What are Recurrent Neural Networks

- A recurrent neural network (RNN) processes sequences by iterating through the sequence elements and maintaining a state containing information relative to what it has seen so far.
- In effect, an RNN is a type of neural network that has an internal loop: the network internally loops over sequence elements.

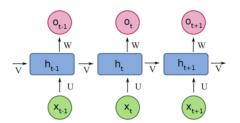


### What are Recurrent Neural Network



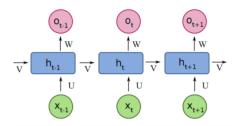
#### What are Recurrent Neural Network

- In the picture, there are some distinct components, from which the most important are:
- x: The input. It can be a word in a sentence or some other type of sequential data
- O: The output. For instance, what the network thinks the next word on a sentence should be given the previous words



#### What are Recurrent Neural Network

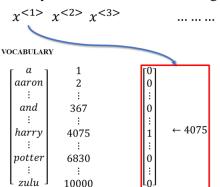
- In the picture, there are some distinct components, from which the most important are:
- h: The main block of the RNN. It contains the weights and the activation functions of the network
- V: Represents the communication from one time-step to the other.



### Words to Vectors

- Word embedding is a technique in natural language processing (NLP) and deep learning that represents words as continuous vector representations in a high-dimensional space.
- These vector representations, often referred to as word vectors or word embeddings, are designed to capture semantic and syntactic relationships between words, making them a fundamental component of various NLP applications.
- One popular type of word embedding is the one-shot vector representation, which is also known as "one-hot encoding" or "one-hot vectors."

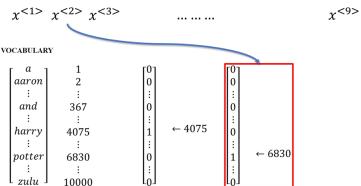
#### x : Harry Potter and Hermione Granger invented a new spell



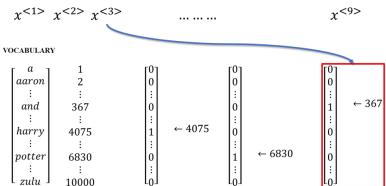
In a one-shot vector representation, each word in a vocabulary is represented by a binary vector of fixed length, where all elements are zero except for one element, which is set to one. This single non-zero element corresponds to the position of the word in the vocabulary.

x<9>

x : Harry Potter and Hermione Granger invented a new spell



x : Harry Potter and Hermione Granger invented a new spell



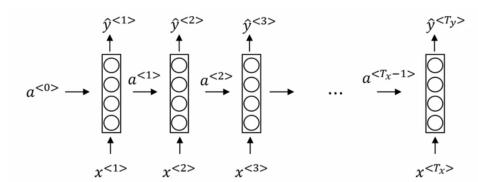
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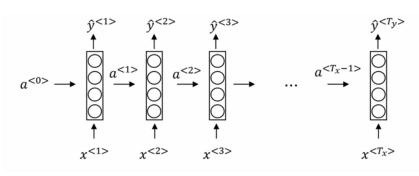
#### VOCABULARY

| a aaron : and : harry : potter : zulu | 1<br>2<br>::<br>367<br>::<br>4075<br>::<br>6830<br>::<br>10000 | [0]<br>0<br>::<br>0<br>::<br>1<br>::<br>0<br>::<br>0 | 4075 $\begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ \vdots \\ 0 \\ \vdots \\ 1 \\ \vdots \\ 0 \end{bmatrix}$ | ← 6830 | [0]<br>0<br>:<br>1<br>:<br>0<br>:<br>0<br>: | ← 367 |  |
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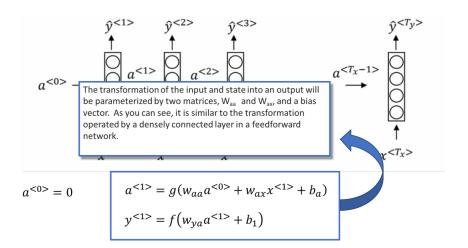
- One-shot vectors are sparse because most elements are zero, and they have a dimensionality equal to the size of the vocabulary.
- As the vocabulary grows, so does the dimensionality of the vectors.
- More advanced word embeddings techniques, on the other hand, represent words as dense vectors of real numbers in a continuous vector space.
- Unlike one-shot vectors, word embeddings are not binary and can take on a range of real values.
- We'll talk a lot about word embeddings in the next chapters ...

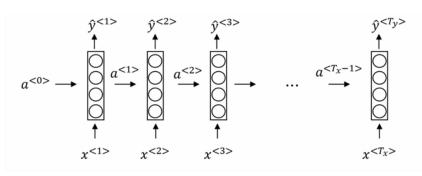




$$a^{<0>} = 0$$
  $a^{<1>} = g(w_{aa}a^{<0>} + w_{ax}x^{<1>} + b_a)$   $y^{<1>} = f(w_{ya}a^{<1>} + b_1)$ 





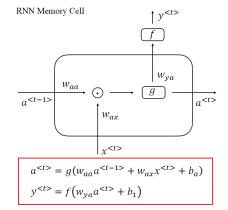


$$a^{<0>} = 0 a^{} = g(w_{aa}a^{} + w_{ax}x^{} + b_a)$$
 
$$y^{} = f(w_{ya}a^{} + b_1)$$



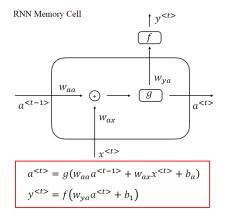
### Memory Cell

- Is very useful for educational purposes, introduce the idea of Memory Cell
- A memory cell refers to a fundamental component within an RNN unit that is designed to store and maintain information over time as the network processes sequential data.



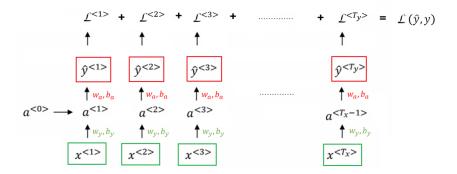
### Memory Cell

 Memory cells are a key feature of RNNs, and they play a central role in allowing these networks to capture and remember information from previous time steps.



# Backpropagation Through Time

### Backpropagation Through Time



### Backpropagation Through Time

DA TERMINARE

### Conclusions

### Advantages of RNN

- Due to their shortterm memory RNNs can handle sequential data and identify patterns in the historical data.
- Moreover, RNNs are able to handle inputs of varying length.



# Disadvantages of RNN

- The RNN suffers from the vanishing gradient descent.
- In this, the gradients that are used to update the weights during backpropagation become very small.
- Multiplying weights with a gradient that is close to zero prevents the network from learning new weights.
- This stopping of learning results in the RNN forgetting what is seen in longer sequences.
- The problem of vanishing gradient descent increases the more layers the network has.

### Disadvantages of RNN

- As the RNN only keeps recent information, the model has problems to consider observations which lie far in the past.
- The RNN, thus, tends to loose information over long sequences as it only stores the latest information.
- Hence, the RNN has only a short-term but not a long-term memory.