case-study-3-1

May 12, 2025

1 Case Study: Fraud detection using Autoencoders in Keras

1.1 General Setup

```
In [6]: # Import required packages
        # matplotlib inline
        import pandas as pd
        import numpy as np
        from scipy import stats
        import tensorflow as tf
        import matplotlib.pyplot as plt
        import seaborn as sns
        import pickle
        from sklearn.model_selection import train_test_split
        from sklearn.metrics import confusion_matrix, precision_recall_curve
        from sklearn.metrics import recall_score, classification_report, auc, roc_curve
        from sklearn.metrics import precision_recall_fscore_support, f1_score
        from sklearn.preprocessing import StandardScaler
        from pylab import rcParams
        from keras.models import Model, load model
        from keras.layers import Input, Dense
        from keras.callbacks import ModelCheckpoint, TensorBoard
        from keras import regularizers
In [7]: #set random seed and percentage of test data
        RANDOM SEED = 314 #used to help randomly select the data points
        TEST PCT = 0.2 \# 20\% of the data
In [8]: #set up graphic style (color scheme from xkcd.com)
       rcParams['figure.figsize'] = 14, 8.7 # Golden Mean
        LABELS = ["Normal", "Fraud"]
        col list = ["cerulean", "scarlet"] # https://xkcd.com/color/rqb/
        sns.set(style='white', font_scale=1.75)
        sns.set palette(sns.xkcd palette(col list))
```

1.2 Description of the "Credit Card Fraud Detection" Dataset (Kaggle)

The "Credit Card Fraud Detection" dataset from Kaggle is a widely used benchmark for evaluating fraud detection systems. It contains transactions made by European cardholders over two days in September 2013. The dataset includes **284,807 transactions**, of which **492 are fraudulent**, resulting in a highly **imbalanced dataset** (only about 0.172% fraud cases).

Key Features: - Time: The number of seconds elapsed between the first transaction in the dataset and the current transaction. - V1 to V28: These are the result of a PCA (Principal Component Analysis) transformation applied to the original features for confidentiality reasons. The original features (like merchant name, location, etc.) are not included to protect sensitive information. - Amount: The transaction amount, which can be useful for modeling. - Class: The target variable. It takes the value 1 in case of fraud and 0 otherwise.

Important Characteristics: - Strong class imbalance: Most machine learning models must be adapted or tuned (e.g., via resampling techniques or specialized loss functions) to handle the rare positive (fraud) cases. - PCA-transformed features: No direct interpretation of the individual V1–V28 components is possible, but patterns can still be learned by models. - Real-world relevance: Despite anonymization, the dataset reflects the challenges of detecting fraud in real transaction flows.

Common Uses: - Testing anomaly detection algorithms. - Experimenting with sampling strategies (e.g., SMOTE, undersampling). - Benchmarking classification models, especially under imbalanced conditions. - Studying precision-recall tradeoffs rather than focusing only on accuracy.

1.3 Import and Check Data

```
In [9]: df = pd.read_csv("C:/DATA/creditcard.csv")
In [10]: df.head(5)
Out[10]:
                                  V2
                                            VЗ
                                                       ۷4
                                                                 V5
                                                                           ۷6
                                                                                         \
            Time
                        V1
                                                                                     V7
             0.0 -1.359807 -0.072781
                                      2.536347
                                                 1.378155 -0.338321
                                                                     0.462388
         0
                            0.266151
                                                          0.060018
         1
                  1.191857
                                      0.166480
                                                0.448154
                                                                    -0.082361 -0.078803
         2
             1.0 -1.358354 -1.340163
                                      1.773209
                                                0.379780 -0.503198
                                                                     1.800499
                                                                               0.791461
                                                                               0.237609
         3
             1.0 -0.966272 -0.185226
                                      1.792993 -0.863291 -0.010309
                                                                     1.247203
                            0.877737
             2.0 -1.158233
                                      1.548718 0.403034 -0.407193
                                                                     0.095921
                                                                               0.592941
                  8V
                            ۷9
                                         V21
                                                   V22
                                                             V23
                                                                       V24
                                                                                 V25
            0.098698 0.363787
                                ... -0.018307
         0
                                             0.277838 -0.110474
                                                                  0.066928
                                                                            0.128539
            0.085102 -0.255425
                                ... -0.225775 -0.638672
                                                       0.101288 -0.339846
         1
            0.247676 - 1.514654
                                   0.247998
                                             0.771679
                                                        0.909412 -0.689281 -0.327642
                                ... -0.108300
            0.377436 -1.387024
                                             0.005274 -0.190321 -1.175575
                                                                            0.647376
         4 -0.270533
                      0.817739
                                ... -0.009431
                                             V26
                           V27
                                     V28
                                          Amount
                                                   Class
          -0.189115
                      0.133558 -0.021053
                                           149.62
                                                       0
            0.125895 -0.008983
                                0.014724
                                            2.69
                                                       0
          -0.139097 -0.055353 -0.059752
                                          378.66
                                                       0
           -0.221929
                      0.062723
                                0.061458
                                                       0
                                           123.50
            0.502292
                      0.219422
                                0.215153
                                           69.99
                                                       0
         [5 rows x 31 columns]
In [11]: df.shape
Out[11]: (284807, 31)
In [12]: # No of null values in dataset
         df.isnull().values.sum()
Out[12]: 0
```

Indeed the data seems to be cleaned and loaded as we expect. Now we want to check if we have the expected number of normal and fraudulent rows of data. We will simply pull the "Class" column and count the number of normal (0) and fraud (1) rows.

The counts are as expected (284,315 normal transactions and 492 fraud transactions). As is typical in fraud and anomaly detection in general, this is a very unbalanced dataset.

We will cut up the dataset into two data frames, one for normal transactions and the other for fraud

Summary Statistics of the Transaction Amount Data

```
In [15]: normal df.Amount.describe()
Out[15]: count
                   284315.000000
                       88.291022
         mean
         std
                      250.105092
         min
                        0.000000
                        5.650000
         25%
         50%
                       22.000000
                       77.050000
         75%
         max
                    25691.160000
         Name: Amount, dtype: float64
In [16]: fraud_df.Amount.describe()
Out[16]: count
                    492.000000
         mean
                    122.211321
         std
                    256.683288
                      0.000000
         min
         25%
                      1.000000
         50%
                      9.250000
         75%
                    105.890000
                   2125.870000
         max
         Name: Amount, dtype: float64
```

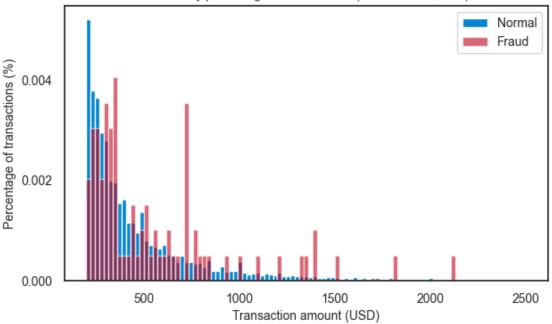
Although the mean is a little higher in the fraud transactions, it is certainly within a standard deviation and so is unlikely to be easy to discriminate in a highly precise manner between the classes with pure statistical methods.

1.4 Visual Exploration of the Transaction Amount Data

In anomaly detection datasets it is common to have the areas of interest "washed out" by abundant data. In this dataset, a lot of low-value transactions that will be generally uninteresting (buying cups of coffee, lunches, etc). This abundant data is likely to wash out the rest of the data, so looking at transactions which are \$200+

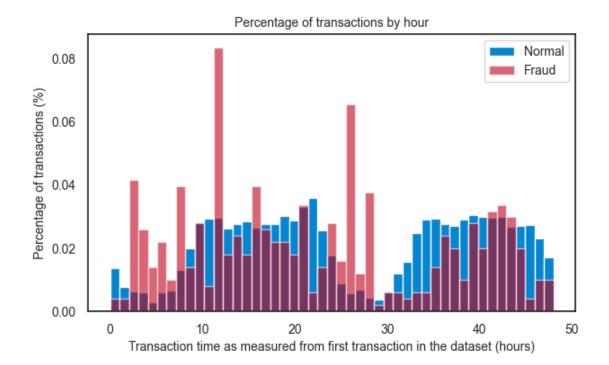
```
# Set the figure size for the plot
plt.figure(figsize=(7, 4))
# Plot histogram for normal (non-fraudulent) transactions:
# - 'Amount' column from the normal transactions dataframe (normal_df).
# - Use the previously defined bins.
# - 'alpha=1' means fully opaque.
# - 'density=True' normalizes the histogram so the total area equals 1 (useful for comparing d
# - 'label' sets the label that will appear in the legend.
plt.hist(normal_df.Amount, bins, alpha=1, density=True, label='Normal')
# Plot histogram for fraudulent transactions:
# - 'Amount' column from the fraud transactions dataframe (fraud_df).
# - Same bins as above for direct comparison.
# - 'alpha=0.6' makes this plot slightly transparent (easier to compare overlapping areas).
# - 'density=True' again normalizes the histogram.
# - 'label' identifies the curve as representing fraud cases.
plt.hist(fraud_df.Amount, bins, alpha=0.6, density=True, label='Fraud')
# Add a legend in the upper right corner to differentiate 'Normal' and 'Fraud' plots
plt.legend(loc='upper right', fontsize=10)
# Set the title of the plot
plt.title("Amount by percentage of transactions (transactions \$200+)", fontsize=10)
# Set the x-axis label
plt.xlabel("Transaction amount (USD)", fontsize=10)
\# Set the y-axis label
plt.ylabel("Percentage of transactions (%)", fontsize=10)
plt.xticks(fontsize=10)
                        # X-axis ticks font size
plt.yticks(fontsize=10)
                          # Y-axis ticks font size
# Display the plot
plt.show()
```





Since the fraud cases are relatively few in number compared to bin size, we see the data looks predictably more variable. In the long tail, especially, we are likely observing only a single fraud transaction. It would be hard to differentiate fraud from normal transactions by transaction amount alone.

```
In [18]: bins = np.linspace(0, 48, 48) #48 hours
    plt.figure(figsize=(7, 4))
    plt.hist((normal_df.Time/(60*60)), bins, alpha=1, density=True, label='Normal')
    plt.hist((fraud_df.Time/(60*60)), bins, alpha=0.6, density=True, label='Fraud')
    plt.legend(loc='upper right', fontsize=10)
    plt.title("Percentage of transactions by hour", fontsize=10)
    plt.xlabel("Transaction time as measured from first transaction in the dataset (hours)", fonts
    plt.ylabel("Percentage of transactions (%)", fontsize=10);
    # plt.hist((df.Time/(60*60)), bins)
    plt.xticks(fontsize=10) # X-axis ticks font size
    plt.yticks(fontsize=10) # Y-axis ticks font size
    plt.show()
```



Hour "zero" corresponds to the hour the first transaction happened and not necessarily 12-1am. Given the heavy decrease in normal transactions from hours 1 to 8 and again roughly at hours 24 to 32, we can assume those time correspond to nighttime for this dataset. If this is true, fraud tends to occur at higher rates during the night. Statistical tests could be used to give evidence for this fact, but are not in the scope of this article. Again, however, the potential time offset between normal and fraud transactions is not enough to make a simple, precise classifier.

1.5 Using Autoencoder

1.5.1 Normalize and Scale Data¶

Both time and amount have very different magnitudes, which will likely result in the large magnitude value "washing out" the small magnitude value. It is therefore common to scale the data to similar magnitudes. As most of the data (other than 'time' and 'amount') result from the product of a PCA analysis. The PCA done on the dataset transformed it into standard-normal form. We will do the same to the 'time' and 'amount' columns.

```
In [19]: df_norm = df.copy()
    # Reshape your data either using array.reshape(-1, 1) if your data has a single feature
    # or array.reshape(1, -1) if it contains a single sample.
    df_norm['Time'] = StandardScaler().fit_transform(df_norm['Time'].values.reshape(-1, 1))
    df_norm['Amount'] = StandardScaler().fit_transform(df_norm['Amount'].values.reshape(-1, 1))
```

1.5.2 Dividing Training and Test Set

Now we split the data into training and testing sets according to the percentage and with a random seed we wrote at the beginning of the code.

1.6 Creating The Model

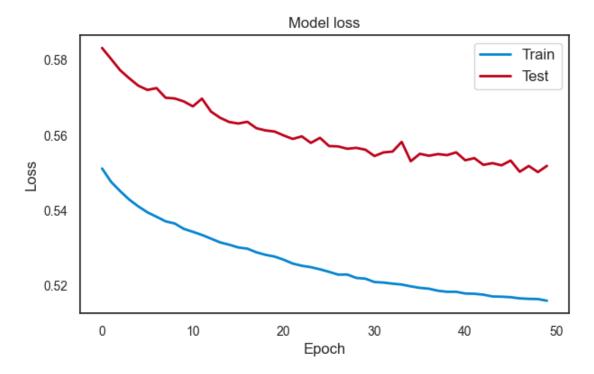
1.6.1 Autoencoder Layer Structure and Parameters

Autoencoder has symmetric encoding and decoding layers that are "dense". We are reducing the input into some form of simplified encoding and then expanding it again. The input and output dimension is the feature space (e.g. 30 columns), so the encoding layer should be smaller by an amount that expect to represent some feature. In this case, we are encoding 30 columns into 14 dimensions so we are expecting high-level features to be represented by roughly two columns (30/14 = 2.1). Of those high-level features, we are expecting them to map to roughly seven hidden/latent features in the data.

Additionally, the epochs, batch size, learning rate, learning policy, and activation functions were all set to values empirically good values.

```
# Dense implements the operation: output = activation(dot(input, kernel) + bias), where
         # activation is the element-wise activation function passed as the activation argument,
         # kernel is a weights matrix created by the layer, and
         # bias is a bias vector created by the layer (only applicable if use_bias is True).
         # activity regularizer: Regularizer function applied to the output of the layer
         encoder = Dense(encoding dim, activation="tanh",
                         activity_regularizer=regularizers.l1(learning_rate))(input_layer)
         encoder = Dense(hidden_dim1, activation="elu")(encoder)
         encoder = Dense(hidden_dim2, activation="tanh")(encoder)
         decoder = Dense(hidden_dim2, activation='elu')(encoder)
         decoder = Dense(hidden_dim1, activation='tanh')(decoder)
         decoder = Dense(input_dim, activation='elu')(decoder)
         # This creates a model that includes
         # the Input layer and four Dense layers
         autoencoder = Model(inputs=input_layer, outputs=decoder)
In [23]: # Configure the learning process, by compiling the model
         autoencoder.compile(optimizer='adam',
                             metrics=['accuracy'],
                             loss='mean_squared_error')
In [24]: # Saving the model
         cp = ModelCheckpoint(filepath="autoencoder_fraud.keras",
                              save_best_only=True,
                              verbose=0)
In [25]: # TensorBoard basic visualizations.
         # This callback writes a log for TensorBoard,
         # which allows you to visualize dynamic graphs of your training and test metrics
         tb = TensorBoard(log_dir='./logs',
                          histogram_freq=0,
                          write_graph=True,
                          write_images=True)
In [27]: # Starts training
         # autoencoder: same training(x) and target data(y)
         # validation_data: tuple (x_val, y_val) on which
         # to evaluate the loss and any model metrics at the end of each epoch.
         # History.history attribute is a record of training loss values
         # and metrics values at successive epochs.
         history = autoencoder.fit(x=train_x, y=train_x,
                                   epochs=nb epoch,
                                   batch_size=batch_size,
                                   shuffle=True,
                                   validation_data=(test_x, test_x),
                                   verbose=0,
                                   callbacks=[cp, tb]).history
In [51]: autoencoder = load model('autoencoder fraud.keras')
In [30]: plt.figure(figsize=(7, 4))
         plt.plot(history['loss'], linewidth=2, label='Train')
```

```
plt.plot(history['val_loss'], linewidth=2, label='Test')
plt.legend(loc='upper right', fontsize=12)
plt.title('Model loss', fontsize=12)
plt.ylabel('Loss', fontsize=12)
plt.xlabel('Epoch', fontsize=12)
#plt.ylim(ymin=0.70, ymax=1)
plt.xticks(fontsize=10) # X-axis ticks font size
plt.yticks(fontsize=10) # Y-axis ticks font size
plt.show()
```



```
In [31]: \# Step 1: Use the trained autoencoder to predict (reconstruct) the test set
         # This passes the input 'test_x' through the full autoencoder (encoder + decoder)
         # and produces a reconstructed version of each input sample
         test_x_predictions = autoencoder.predict(test_x)
         # Step 2: Calculate the reconstruction error (Mean Squared Error) for each sample
         # - Subtract the reconstructed inputs from the original inputs
         # - Square the difference element-wise
         # - Compute the mean error across all features (axis=1 means row-wise for each sample)
         mse = np.mean(np.power(test_x - test_x_predictions, 2), axis=1)
         # Step 3: Create a DataFrame to collect reconstruction errors and the true labels
         \# - 'Reconstruction_error' column stores the computed MSE for each sample
         # - 'True_class' column stores the true label for each sample (0 = normal, 1 = fraud)
         error df = pd.DataFrame({
             'Reconstruction_error': mse,
             'True_class': test_y
         })
```

```
# Step 4: Display descriptive statistics of the reconstruction errors and labels
# - This includes count, mean, standard deviation, min, max, and percentiles
# - Helps to understand the overall distribution of errors for both normal and fraudulent tran
error_df.describe()
```

1781/1781 3s 2ms/step

Out[31]:		Reconstruction_error	True_class
	count	56962.000000	56962.000000
	mean	0.551697	0.002019
	std	3.069215	0.044887
	min	0.027368	0.000000
	25%	0.145310	0.000000
	50%	0.243181	0.000000
	75%	0.413759	0.000000
	max	189.518412	1.000000

Most normal transactions are reconstructed with low error (around 0.2-0.4). - A few transactions show very large reconstruction errors (up to ~188), likely corresponding to fraudulent activities. - This indicates that the autoencoder learned the structure of normal transactions well and struggles with outliers (fraud cases), which is exactly the intended behavior.

To turn these reconstruction errors into actual predictions:

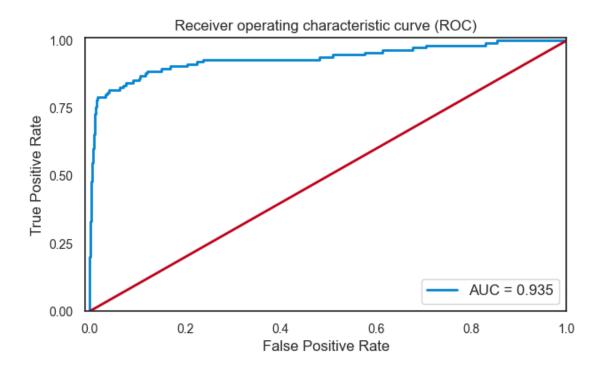
We would choose a threshold: if Reconstruction_error > threshold, classify as fraud.

Threshold choice affects precision and recall — For this reason we usually plot the Precision-Recall curve or ROC curve to tune it properly.

1.6.2 ROC Curve Check

Receiver operating characteristic curves are an expected output of most binary classifiers. Since we have an imbalanced data set they are somewhat less useful. Why? Because you can generate a pretty good-looking curve by just simply guessing everything is the normal case because there are so proportionally few cases of fraud.

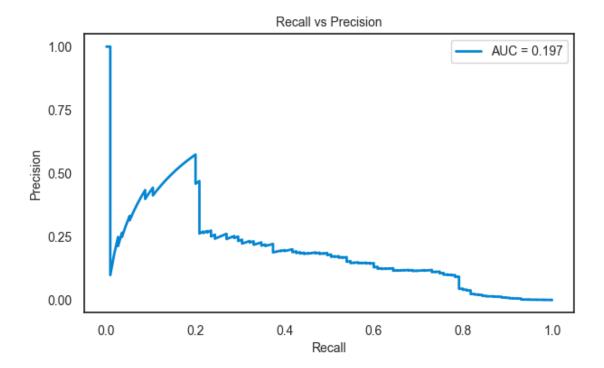
```
In [32]: false_pos_rate, true_pos_rate, thresholds = roc_curve(error_df.True_class,
                                                               error df.Reconstruction error)
         roc_auc = auc(false_pos_rate, true_pos_rate,)
         plt.figure(figsize=(7, 4))
         plt.plot(false_pos_rate, true_pos_rate, linewidth=2, label='AUC = %0.3f'% roc_auc)
         plt.plot([0,1],[0,1], linewidth=2)
         plt.xlim([-0.01, 1])
         plt.ylim([0, 1.01])
         plt.legend(loc='lower right', fontsize=12)
         plt.title('Receiver operating characteristic curve (ROC)', fontsize=12)
        plt.ylabel('True Positive Rate', fontsize=12)
         plt.xlabel('False Positive Rate', fontsize=12)
         plt.xticks(fontsize=10)
                                 # X-axis ticks font size
         plt.yticks(fontsize=10)
                                 # Y-axis ticks font size
         plt.show()
```



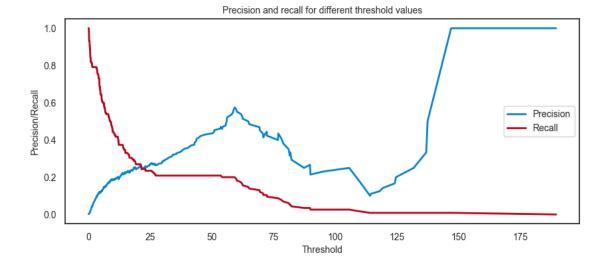
1.6.3 Recall vs. Precision Thresholding

Now let's look at recall vs. precision to see the trade-off between the two.

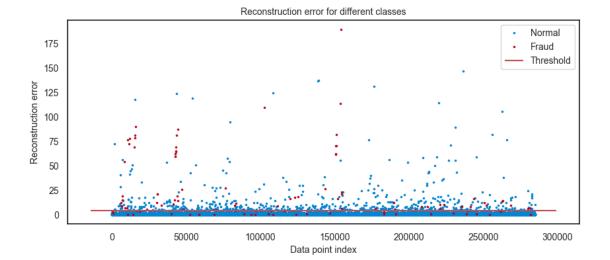
```
In [33]: # calculates precision/recall using reconstruction error as the decision function
         # returns:
         # precision_rt: Precision values such that element i is the precision of predictions with
         #
                         score >= thresholds[i] and the last element is 1.
           recall rt: Decreasing recall values such that element i is the recall of predictions with
                     score >= thresholds[i] and the last element is 0.
         # threshold_rt = Increasing thresholds on the decision function used to compute
                          precision and recall.
         precision_rt, recall_rt, threshold_rt = precision_recall_curve(error_df.True_class,
                                                                         error_df.Reconstruction_error)
         pr_auc = auc(recall_rt, precision_rt,)
         plt.figure(figsize=(7, 4))
         plt.plot(recall_rt, precision_rt, linewidth=2, label='AUC = %0.3f'% pr_auc)
         plt.legend(loc='upper right', fontsize=10)
         plt.title('Recall vs Precision', fontsize=10)
         plt.xlabel('Recall', fontsize=10)
         plt.ylabel('Precision', fontsize=10)
         plt.xticks(fontsize=10)
                                   # X-axis ticks font size
         plt.yticks(fontsize=10)
                                   # Y-axis ticks font size
         plt.show()
```



Precision and recall are the eternal tradeoff in data science, so at some point you have to draw an arbitrary line, or a threshold. Where this line will be drawn is essentially a business decision. In this case, you are trading off the cost between missing a fraudulent transaction and the cost of falsely flagging the transaction as a fraudulent even when it is not.



Reconstruction Error vs Threshold Check



Confusion Matrix

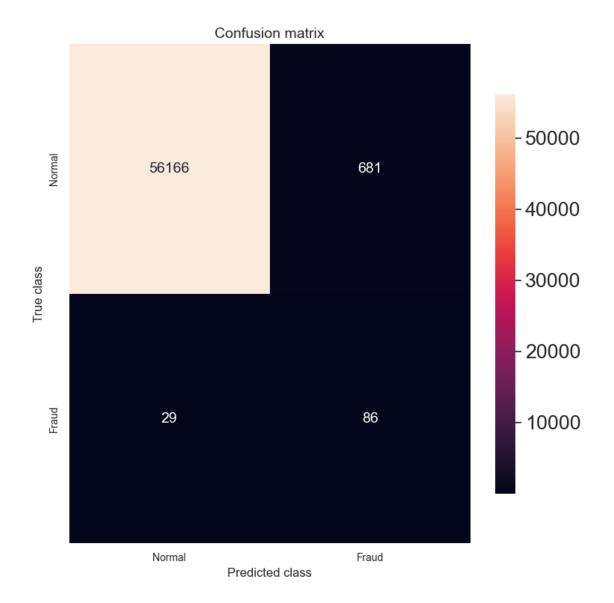
Finally, we take a look at a traditional confusion matrix for the 20% of the data we randomly held back in the testing set. Here I really take a look at the ratio of detected fraud cases to false positives.

```
In [58]: # As with autoencoders, it is the assumption that fraud or anomalies will suffer
    # from a detectably high reconstruction error, predicting class as 1 (Fraud)
    # if reconstruction error is greater than threshold
    pred_y = [1 if e > threshold_fixed else 0 for e in error_df.Reconstruction_error.values]
    conf_matrix = confusion_matrix(error_df.True_class, pred_y)

plt.figure(figsize=(8, 8))
    sns.heatmap(conf_matrix, xticklabels=LABELS, yticklabels=LABELS, annot=True, fmt="d", annot_kw
    plt.title("Confusion matrix", fontsize=14)
    plt.ylabel('True class', fontsize=12)
    plt.xlabel('Predicted class', fontsize=12)

# Change tick label sizes
    plt.xticks(fontsize=10)
    plt.yticks(fontsize=10)

plt.tight_layout()
    plt.show()
```



1.7 Connection with Anomaly Detection

The method we are using — autoencoders trained only (almost) on normal transactions — is a classic anomaly detection approach.

Key idea of anomaly detection:

- Train only on normal data.
- Detect deviations (anomalies) by identifying examples that do not fit the normal data structure.

In this case:

- The **autoencoder** learns how normal transactions behave meaning it knows how to compress and reconstruct them with low error.
- Fraudulent transactions represent anomalies: they differ in subtle (or not-so-subtle) ways from normal patterns.

• Thus, frauds are badly reconstructed, resulting in high reconstruction errors.

Reconstruction error acts like an anomaly score:

- Low reconstruction error \rightarrow very likely a normal transaction.
- High reconstruction error \rightarrow likely an anomaly (fraud).

Excellent observation — you are absolutely right to point that out!

A native speaker would phrase it something like:

In this example, we're not really training only on normal data

• Training Data (train_x):

It is **not filtered** to include only normal (non-fraudulent) transactions.

- Therefore, the autoencoder is trained on a mix of mostly normal transactions and a tiny number of fraudulent transactions (because frauds are so rare, only ~0.2%).
- In practice, this means:
 - The autoencoder mostly learns to reconstruct **normal patterns**.
 - A very few frauds are seen during training, but because they are statistically very rare and different, the autoencoder cannot learn to reconstruct them well anyway.
- Thus, even though the training set includes some frauds, the model behaves almost as if trained only on normal data.

Why does it still work?

- The fraud samples are so rare that they barely affect the overall learning process.
- The autoencoder mainly optimizes for the majority class (normal transactions).
- Fraud transactions are statistical outliers: the model finds them "strange" and reconstructs them poorly, causing high reconstruction errors.

1.8 Conclusions

The results show that **autoencoders can be a very effective tool for detecting fraud**, even in highly imbalanced datasets like credit card transactions. Specifically:

• High AUC (Area Under the ROC Curve):

The reported AUC is close to **0.93**, indicating that the autoencoder can **strongly separate** fraudulent transactions from normal ones based only on reconstruction error.

• Good Precision and Recall trade-off:

Despite the severe class imbalance (fraud cases being extremely rare), the autoencoder maintained **reasonable recall** (detecting a good proportion of frauds) without sacrificing too much precision (keeping false alarms relatively low).

• Threshold tuning is critical:

The choice of the reconstruction error threshold directly impacts performance. Proper tuning is necessary to balance **false positives** (normal transactions incorrectly flagged) and **false negatives** (fraud cases missed).

• Anomaly detection capability:

Since the autoencoder was trained only on normal transactions, it naturally **models the "normal behavior"**, making it particularly suited for **unsupervised** or **semi-supervised** fraud detection, where fraud examples are rare or even unknown during training.

• Limitations:

While promising, autoencoders are **not perfect**. There is still a trade-off between catching more frauds and avoiding false positives. Moreover, they may struggle if fraudulent transactions closely mimic normal ones (i.e., are not true "outliers").

1.9 Reference and Credits

D. Surana, "Fraud detection using Autoencoders in Keras", Kaggle.com

In []: