

TED (15) – 1002

(REVISION — 2015)

Reg. No.....

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**DIPLOMA EXAMINATION IN ENGINEERING/TECHNOLOGY/  
MANAGEMENT/COMMERCIAL PRACTICE — OCTOBER, 2019**

**ENGINEERING MATHEMATICS - I**

[Time : 3 hours]

(Maximum marks : 100)

**PART — A**

(Maximum marks : 10)

Marks

I Answer *all* questions. Each question carries 2 marks.

1. Prove that  $\cos^2 A - \sin^2 A = 2 \cos^2 A - 1$ .
2. Write the expression for  $\sin 3A$ .
3. Prove that in any triangle ABC,  $abc = 4R\Delta$ .
4. If  $y = x \sin x$ , Find  $\frac{dy}{dx}$
5. Find the velocity and acceleration at time 't' of a particle moving according to  $s = 2t^3 - 3t^2 + 1$ . (5×2 = 10)

**PART — B**

(Maximum marks : 30)

II Answer any *five* of the following questions. Each question carries 6 marks.

1. Express  $4 \cos x + 3 \sin x$  in the form  $R \sin(x + \alpha)$  where  $\alpha$  is acute.
2. Prove that  $\sin 10^\circ \sin 50^\circ \sin 70^\circ = \frac{1}{8}$ .
3. Prove that  $(a - b) \cos \frac{C}{2} = c \sin \frac{A-B}{2}$ .
4. Differentiate  $\sin x$  by the method of first principles.
5. Find  $\frac{dy}{dx}$  if  $(x^2 + y^2)^2 = xy$ .
6. Find the equation to the tangent and normal to the curve  $y = 3x^2 + x - 2$  at (1, 2).
7. Prove that  $\sin A + \sin(120^\circ + A) + \sin(240^\circ + A) = 0$ . (5×6 = 30)



## PART — C

Marks

(Maximum marks : 60)

(Answer one full question from each unit. Each full question carries 15 marks.)

## UNIT — I

- III (a) Prove that  $\frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = 2 \operatorname{cosec} \theta$ . 5
- (b) If  $\theta$  is acute and  $\sin \theta = 0.4$ , find the value of  $\sec \theta + \tan \theta$ . 5
- (c) If  $A + B = 45^\circ$ , show that  $(1 + \tan A)(1 + \tan B) = 2$ . 5

OR

- IV (a) Prove that  $\frac{1 + \cos \theta}{\sin \theta} = \frac{\sin \theta}{1 - \cos \theta}$ . 5
- (b) If  $\sin A = \frac{4}{5}$ ,  $\sin B = \frac{12}{13}$ ;  $A, B$  are acute, find  $\sin(A + B)$  and  $\cos(A - B)$ . 5
- (c) The horizontal distance between two towers is 60m and the angle of depression of the first tower as seen from the second which is in 150m height is  $30^\circ$ . Find the height of the first tower. 5

## UNIT — II

- V (a) Prove that  $\frac{\sin 3A}{\sin A} - \frac{\cos 3A}{\cos A} = 2$ . 5
- (b) Prove that  $\tan A + \cot A = 2 \operatorname{cosec} 2A$ . 5
- (c) Show that  $\frac{\sin 2A}{1 + \cos 2A} = \tan A$  and deduce the value of  $\tan 15^\circ$ . 5

OR

- VI (a) Prove that  $\frac{\sin A + \sin 3A + \sin 5A}{\cos A + \cos 3A + \cos 5A} = \tan 3A$  5
- (b) Prove that  $\sin A + \sin 3A + \sin 5A + \sin 7A = 4 \cos A \cos 2A \sin 4A$ . 5
- (c) Solve  $\Delta ABC$ , given  $a = 4\text{cm}$ ,  $b = 5\text{cm}$  and  $c = 7\text{cm}$ . 5

## UNIT — III

- VII (a) Evaluate  $\lim_{x \rightarrow 4} \frac{x^4 - 256}{x^3 - 64}$ . 5
- (b) If  $x = a(\theta - \sin \theta)$ ;  $y = a(1 - \cos \theta)$ , show that  $\frac{dy}{dx} = \cot \frac{\theta}{2}$  5
- (c) If  $y = A \cos px + B \sin px$ , ( $A, B, p$  are constants), Show that  $\frac{d^2y}{dx^2}$  is proportional to  $y$ . 5

OR

- VIII (a) Evaluate (i)  $\lim_{x \rightarrow 0} \frac{1 - \cos 2x}{x^2}$  (ii)  $\lim_{x \rightarrow -1} \frac{x^3 + 1}{x + 1}$  (3+3=6)
- (b) Find  $\frac{dy}{dx}$  if  $y = (x^2 + x + 1)^7 \sin^2 x$ . 4
- (c) If  $y = Ae^{nx} + Be^{-nx}$  (A, B are constants), Show that  $\frac{d^2y}{dx^2} - n^2y = 0$ . 5

## UNIT — IV

- IX (a) A particle is projected vertically upwards and its height 'h' and time 't' are connected by  $h = 60t - t^2$ . Find the greatest height attained. 5
- (b) A balloon is spherical in shape. Gas is escaping from it at the rate of 10cc/sec. How fast is the surface area shrinking when the radius is 15cm. 5
- (c) The deflection of a beam is  $S = 2x^3 - 9x^2 + 12x$ . Find the maximum deflection. 5

OR

- X (a) Find the velocity and acceleration of a particle at  $t = 3$  seconds whose displacement is given by  $S = 3t^3 - t^2 + 9t + 1$ . 5
- (b) A spherical balloon is inflated by pumping 25cc of gas per second. Find the rate at which the radius of the balloon is increasing when the radius is 15cm. 5
- (c) Find the maximum value of  $2x^3 - 3x^2 - 36x + 10$ . 5