



Chinese University of Hong Kong, Shenzhen

???

adapted from KTH ACM Contest Template Library

CUHK-SZ

Contest (1)

base.hpp

Description: Somehow type this up before you do anything

<bits/stdc++.h> 16 lines

```
template <class T> using V = vector<T>;
template <class T> using VV = V<V<T>>;
```

```
using ll = int64_t;
```

```
template <class F> struct ycr { // hash-cpp-1
    F f;
    template <class T> explicit ycr(T&& f_) : f(forward<T>(f_
        ↳)) {}
```

```
    template <class... A> decltype(auto) operator()(A&&... as
        ↳) {
        return f(ref(*this), forward<A>(as)...);
    }
};
template <class F> decltype(auto) yc(F&& f) {
    return ycr<decay_t<F>>(forward<F>(f));
} // hash-cpp-1 = 9344860c946665f163f1e784f1305c28
```

extra.hpp

#pragma once 19 lines

#include "contest/base.hpp"

```
using i64 = int64_t;
using u32 = uint32_t;
using u64 = uint64_t;
using i128 = __int128_t;
using u128 = __uint128_t;
```

```
namespace internal {
```

```
inline int next_pow2(int n) {
    int k = 0;
    while ((uint32_t(1) << k) < uint32_t(n)) k++;
    return k;
}
```

```
} // namespace internal
```

bashrc

5 lines

```
setxkbmap -option caps:escape
alias e='vim'
alias cls='clear -x'
alias mv='mv -i'
alias cp='cp -i'
```

Makefile

3 lines

```
CXXFLAGS = -O2 -std=gnu++20 -Wall -Wextra -Wno-unused-
↳result -pedantic -Wshadow -Wformat=2 -Wfloat-equal -
↳Wconversion -Wlogical-op -Wshift-overflow=2 -
↳Wduplicated-cond -Wcast-qual -Wcast-align
DEBUGFLAGS = -D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC -
↳fsanitize=address -fsanitize=undefined -fno-sanitize-
↳recover=all -fstack-protector -D_FORTIFY_SOURCE=2
CXXFLAGS += $(DEBUGFLAGS) # flags with speed penalty
```

vimrc

9 lines

```
set nosp ai bs=2 hls ic is lbr ls=2 mouse=a nu ru sc scs
↳smd so=3 sw=4 ts=4
filetype plugin indent on
syn on
map gA m'ggVG"+y''

set cindent cino=jl,(0,ws,Ws

com -range=% -nargs=1 P exe "<linel>,<line2>!".<q-args> |y|
↳sil u|echom @"
au FileType cpp com! -buffer -range=% Hash <linel>,<line2>P
↳cpp -dD -P -fpreprocessed | tr -d '[:space:]' |
↳md5sum
```

hash-cpp.sh

1 lines

```
cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum
```

fast-input.hpp

Description: Fast scanner implementation based on fread

55 lines

```
namespace fast_input {
```

```
struct Scanner {
    FILE* f;
    Scanner(FILE* f_) : f(f_) {}

    void read() {} // hash-cpp-1
    template <class H, class... T> void read(H& h, T&... t) {
        read_single(h);
        read(t...);
    } // hash-cpp-1 = 1be9d87558b4e70f056af5e4bc8df866

    char buf[1 << 16]; // hash-cpp-2
    size_t s = 0, e = 0;
    char get() {
        if (s >= e) {
            buf[0] = 0;
            s = 0;
            e = fread(buf, 1, sizeof(buf), f);
        }
        return buf[s++];
    } // hash-cpp-2 = 836ba7888edb5fec27c4231ad0b7d2a

    template <class T> void read_single(T& r) { // hash-cpp-3
        char c;
        while ((c = get()) <= ' ') {}
        bool neg = false;
        if (c == '-' ) {
            neg = true;
            c = get();
        }
        r = 0;
        do {
            r = 10 * r + (c & 0x0f);
        } while ((c = get()) >= '0');
        if (neg) r = -r;
    } // hash-cpp-3 = 2a45bc9b396bdcf75005cca881c4efd9
```

```
    void read_single(string& r) { // hash-cpp-4
        char c;
        while ((c = get()) <= ' ') {}
        r = "";
        do {
            r += c;
        } while ((c = get()) <= ' ');
    } // hash-cpp-4 = 7b45a9f3c88601371ddc5e8e9795e764
```

```
void read_single(string& r) { // hash-cpp-4
```

```
    char c;
    while ((c = get()) <= ' ') {}
    r = "";
    do {
        r += c;
```

```
    } while ((c = get()) > ' ');
} // hash-cpp-4 = 7b45a9f3c88601371ddc5e8e9795e764
```

```
void read_single(double& r) { // hash-cpp-5
    string z;
    read_single(z);
    r = stod(z);
} // hash-cpp-5 = 32d080eb6e36c0c1cede9030bbb31fa1
};

} // namespace fast_input
```

Data Structure (2)

hash-map.hpp

Description: Faster and safer hash map.

<ext/pb_ds/assoc.container.hpp> 13 lines

```
struct CustomHash { // hash-cpp-1
    size_t operator()(uint64_t x) const {
        static const uint64_t z = chrono::steady_clock::now().
↳time_since_epoch().count(),
        c = uint64_t(4e18*acos(0))+71;
        return __builtin_bswap64((x^z)*c);
    }
}; // hash-cpp-1 = 6c7374790fb23e010426cdcd0361a13
```

```
template <class K, class V, class Hash = CustomHash> //
↳hash-cpp-2
using HashMap = __gnu_pbds::gp_hash_table<K, V, Hash>; //
↳hash-cpp-2 = 4fe2baba5ae354ac6dd53d37ad221011
```

```
template <class K, class Hash = CustomHash> // hash-cpp-3
using HashSet = HashMap<K, __gnu_pbds::null_type, Hash>; //
↳hash-cpp-3 = 1d899df3bf29329f777189feb8d1944c
```

binary-indexed-tree.hpp

Description: Supports computing partial sum $a_0 + \dots + a_{i-1}$ and incrementing some a_i by v **Time:** Both operations are $\mathcal{O}(\log N)$

44 lines

```
template <class T> struct BIT {
    V<T> x;
    int s;
    BIT(int n) { build(n); }
    BIT(const V<T>& a) { build(a); }

    void build(int n) { // hash-cpp-1
        x.clear();
        x.resize(s = n);
    } // hash-cpp-1 = 47107bdc695b2cbc062915efca897e56
```

```
    void build(const V<T>& a) { // hash-cpp-2
        build(int(a.size()));
        copy(a.begin(), a.end(), x.begin());
        for (int i = 0; i < s; i++) {
            int j = i | (i+1);
            if (j < s) x[j] += x[i];
        }
    } // hash-cpp-2 = ce95cbd55bea652fb39765d7f422ee70
```

```
    void add(int i, T v) { // hash-cpp-3
        for (; i < s; i |= i+1) x[i] += v;
    }
    T sum(int i) {
        T res = 0;
```

```

    for (; i; i &= i-1) res += x[i-1];
    return res;
} // hash-cpp-3 = e7fbe70df2a7ecfa13485bb1c017438a

// Slightly tested; requires s >= 1
int kth(T k) { // hash-cpp-4
    int cur = 0;
    for (int i = 31 - __builtin_clz(s); i >= 0; i--) {
        int nxt = cur + (1 << i);
        if (nxt <= s && x[nxt-1] <= k) {
            k -= x[nxt-1];
            cur = nxt;
        }
    }
    return cur;
} // hash-cpp-4 = c6bf486c9c36a50aae1d2e8d61e4fa7c

int kth_helper(T k, int i = 0) { return kth(k + sum(i));
    ↪ }
};

```

static-range.hpp

Description: Static range composition. You need to specify a composition function f and an identity element e

Time: $\mathcal{O}(N \log N)$ building and $\mathcal{O}(1)$ querying

```

template <class T, class F> struct StaticRange {
    VV<T> d; // hash-cpp-1
    const F f;
    const T e;
    StaticRange(const V<T>& a, F f_, T e_) : f(f_), e(e_) {
        int n = int(a.size());
        int h = 0;
        while ((2 << h) < n) h++;
        d.resize(h+1);
        d[0] = a;
        for (int k = 0; k < h; k++) {
            d[k+1].resize(n, e);
            int s = 1 << (k+1);
            for (int i = s; i < n; i += 2*s) {
                T x = e;
                for (int j = i-1; j >= i-s; j--) {
                    d[k+1][j] = x = f(a[j], x);
                }
                x = e;
                for (int j = i; j < i+s && j < n; j++) {
                    d[k+1][j] = x = f(x, a[j]);
                }
            }
        }
    } // hash-cpp-1 = 2e3ea8128d01a499906df5c7e8758889

    T operator()(int l, int r) const { // hash-cpp-2
        if (l >= r) return e;
        r--;
        if (l == r) return d[0][l];
        int k = __lg(1^r);
        return f(d[k][l], d[k][r]);
    } // hash-cpp-2 = e599b1dcf6ad8f51cef0410a05e23290
};

```

treap.hpp

Description: Randomized Treap with split/merge support. `nodes.size() < nodes.capacity()` must be maintained. One strategy to save space is to refactor everything when the size of nodes is approximating its capacity

Time: $\mathcal{O}(\log N)$ per operation

```

template <class M, bool persistent = false> struct
    ↪ TreapManager {
    using S = typename M::S;
    using F = typename M::F;

    TreapManager(M m_, int alloc = 0) : m(m_) {
        if (alloc > 0) {
            nodes.reserve(alloc);
        } else {
            // make sure to understand what you're doing
            assert(!persistent);
        }

        mt19937_64 mt(chrono::steady_clock::now().
            ↪ time_since_epoch().count());
        for (int z = 0; z < 2; z++) {
            states[z] = uint32_t(mt());
        }
    }

    using Tree = int;

    Tree make_empty() { return Tree(nullptr); }

    Tree make_single(S s) { // hash-cpp-1
        int i = int(nodes.size());
        nodes.push_back(Node{nullptr, nullptr, 1, false, false, s, s,
            ↪ m.id()});
        return i;
    } // hash-cpp-1 = 6c4d20b86ebfc6f60d88165b76573a67

    Tree make_copy(Tree o) { return _make_copy(o); }

    int size(const Tree t) { return _size(t); }
    int reverse(Tree t) { return _reverse(t); }
    int apply(Tree t, F f) { return _apply(t, f); }
    S prod(const Tree& t) { return _prod(t); }

    Tree split_k(Tree& t, int k) { // hash-cpp-2
        Tree o;
        tie(t, o) = _split_k(t, k);
        return o;
    } // hash-cpp-2 = c70f87700806d15a4c4ec662572f17ff

    Tree merge(Tree a, Tree b) { return _merge(a, b); }

    Tree build(const V<S>& a) { // hash-cpp-3
        if (a.empty()) return make_empty();
        return _build(a, 0, int(a.size()));
    } // hash-cpp-3 = 8df775a114f42165c31f42bf4a67d6c7

    V<S> to_array(const Tree& t) { // hash-cpp-4
        V<S> buf;
        buf.reserve(size(t));
        _to_array(t, buf);
        return buf;
    } // hash-cpp-4 = 6addc521e35d79f542267016dc1b5165

private:
    static constexpr int null = -42;
    M m;

    struct Node { // hash-cpp-5
        int li, ri, sz;
        bool rev, app;
    };

```

```

    S a, s;
    F f;
};

V<Node> nodes;
Node& node(int i) { return nodes[i]; }
int _size(int i) { return i == null ? 0 : node(i).sz; }
    ↪ // hash-cpp-5 = c1168dbc9a00419db6a93774a5b0b603

int _make_copy(int o) { // hash-cpp-6
    if constexpr (!persistent) return o;

    if (o == null) return null;
    assert(nodes.size() < nodes.capacity());
    int i = int(nodes.size());
    nodes.push_back(node(o));
    return i;
} // hash-cpp-6 = 26a70edec35d6f656b6f85d49ceb2fc6

int _build(const V<S>& a, int l, int r) { // hash-cpp-7
    if (r - l == 1) {
        return make_single(a[l]);
    }
    int md = (l + r) / 2;
    return _merge(_build(a, l, md), _build(a, md, r));
} // hash-cpp-7 = 6020135dd6f1feb9bee1dc613c54dc2d

void _update(int i) { // hash-cpp-8
    auto& n = node(i);
    n.s = m.op(_prod(n.li), m.op(n.a, _prod(n.ri)));
    n.sz = size(n.li) + size(n.ri) + 1;
} // hash-cpp-8 = c5fb7048740c35c2a720845684e4ff19

int _reverse(int i) { // hash-cpp-9
    if (i == null) return i;
    i = _make_copy(i);
    auto& n = node(i);
    n.rev = !n.rev;
    swap(n.li, n.ri);
    return i;
} // hash-cpp-9 = 266d7203b1c04371492ea0bd85cb281d

S _prod(int i) { return i == null ? m.e() : node(i).s; }

int _apply(int i, F f) { // hash-cpp-10
    if (i == null) return i;
    i = _make_copy(i);
    auto& n = node(i);
    n.s = m.mapping_sz(f, n.s, n.sz);
    n.a = m.mapping_sz(f, n.a, 1);
    n.f = m.composition(f, n.f);
    n.app = true;
    return i;
} // hash-cpp-10 = c1044aa4c9dbe3605f7e255c9ef1131b

int downdate(int i) { // hash-cpp-11
    assert(i != null);
    i = _make_copy(i);
    auto& n = node(i);
    if (n.rev) {
        n.li = _reverse(n.li);
        n.ri = _reverse(n.ri);
        n.rev = false;
    }
    if (n.app) {
        n.li = _apply(n.li, n.f);
        n.ri = _apply(n.ri, n.f);
        n.f = m.id();
        n.app = false;
    }
}

```

```

    }
    return i;
} // hash-cpp-11 = de62225a6441397fe26f3bdae0f19423

template <class F> pair<int, int> _split(int i, F go_left
    ↪) { // hash-cpp-12
    if (i == null) return {null, null};
    i = downdate(i);
    auto& n = node(i);
    int li = n.li, ri = n.ri;
    int x, y;
    if (go_left(li, ri)) {
        y = i;
        tie(x, n.li) = _split(n.li, go_left);
    } else {
        x = i;
        tie(n.ri, y) = _split(n.ri, go_left);
    }
    _update(i);
    return {x, y};
} // hash-cpp-12 = 3162351f3f2db4155104ab28b68b8e49

pair<int, int> _split_k(int i, int k) { // hash-cpp-13
    return _split(i, [&](int li, int) -> bool {
        int lsz = size(li);
        if (k <= lsz) {
            return true;
        } else {
            k -= lsz + 1;
            return false;
        }
    });
} // hash-cpp-13 = 21661461b27eeb90e1e770dacc49c006

// Use std::mt19937_64 if performance is not an issue
// https://prng.di.unimi.it/xoroshiro64star.c
inline uint32_t rotl(const uint32_t x, int k) { // hash-
    ↪cpp-14
    return (x << k) | (x >> (32 - k));
}

uint32_t states[2];
uint32_t rng() {
    const uint32_t s0 = states[0];
    uint32_t s1 = states[1];
    const uint32_t res = s0 * 0x9E3779BB;
    s1 ^= s0;
    states[0] = rotl(s0, 26) ^ s1 ^ (s1 << 9);
    states[1] = rotl(s1, 13);
    return res;
} // hash-cpp-14 = 31b4c34fabff6176394fc53b9ec44499

int _merge(int a, int b) { // hash-cpp-15
    if (a == null) return b;
    if (b == null) return a;
    int r;
    uint32_t sa = size(a), sb = size(b);
    if (rng() % (sa + sb) < sa) {
        r = downdate(a);
        node(r).ri = _merge(node(r).ri, b);
    } else {
        r = downdate(b);
        node(r).li = _merge(a, node(r).li);
    }
    _update(r);
    return r;
} // hash-cpp-15 = d2175413493f2a811c2e26771feabcd8

void _to_array(int i, V<S>& buf) { // hash-cpp-16

```

```

    if (i == null) return;
    downdate(i);
    auto& n = node(i);
    _to_array(n.li, buf);
    buf.push_back(n.a);
    _to_array(n.ri, buf);
} // hash-cpp-16 = d330cf42ee4c55689bcc44e8d63a6333
};

```

queue-aggregation.hpp

Description: A queue that supports querying the composition of all elements

45 lines

```

template <class T, class F> struct QueueAggregation {
    const F f; // hash-cpp-1
    const T e;
    V<T> as, bs, ae, be;
    T vs, ve;
    QueueAggregation(F f_, T e_) : f(f_), e(e_), vs(e), ve(e)
        ↪ {} // hash-cpp-1 = e0f918d3b739972ea1a01alc8960f816

    void push_s(const T& x) { // hash-cpp-2
        as.push_back(x), bs.push_back(vs = f(x, vs));
    }
    void push_e(const T& x) {
        ae.push_back(x), be.push_back(ve = f(ve, x));
    }
    void reduce() {
        while (!ae.empty()) {
            push_s(ae.back()), ae.pop_back();
        }
        while (!be.empty()) be.pop_back();
        ve = e;
    } // hash-cpp-2 = 6d2c0367633d89637a8235162683cf9e

    bool empty() const { // hash-cpp-3
        return as.empty() && ae.empty();
    }
    int size() const {
        return int(as.size()) + ae.size();
    } // hash-cpp-3 = b5166973f8a1e060551da48002d67335

    void push(const T& x) { // hash-cpp-4
        if (as.empty()) {
            push_s(x), reduce();
        } else {
            push_e(x);
        }
    }
    void pop() {
        assert(!empty());
        if (as.empty()) reduce();
        as.pop_back(), bs.pop_back();
        vs = (bs.empty() ? e : bs.back());
    }
    T prod() const {
        return f(vs, ve);
    } // hash-cpp-4 = 0b46cd5fba53f4c166094224da58ee1c
};

```

line-container.hpp

Description: Container where you can add lines of the form $y = kx + m$, and query maximum values at given points. Useful for dynamic programming (“convex hull trick”)

Time: $O(\log N)$ with a large constant factor

39 lines

```

namespace line_container {

struct Line { // hash-cpp-1
    mutable ll k, m, p;
    bool operator < (const Line& o) const { return k < o.k; }
    bool operator < (ll x) const { return p < x; }
}; // hash-cpp-1 = 7e3ecf95828aa19c1006717961ebf6c7

struct LineContainer : multiset<Line, less<>> {
    using I = iterator; // hash-cpp-2
    // (for doubles, use inf = 1/.0, div(a,b) = a/b)
    static const ll inf = numeric_limits<ll>::max();
    static ll div(ll a, ll b) {
        return a / b - ((a ^ b) < 0 && a % b);
    } // hash-cpp-2 = cc33661adfbf09f701ba00fae3589d48
    bool isect(I x, I y) { // hash-cpp-3
        if (y == end()) return x->p = inf, 0;
        if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
        else x->p = div(y->m - x->m, x->k - y->k);
        return x->p >= y->p;
    } // hash-cpp-3 = 2b98c40c29f240ca9a861a8267ad00e5
    void add(ll k, ll m) { // hash-cpp-4
        auto z = insert({k, m, 0}), y = z++, x = y;
        while (isect(y, z)) z = erase(z);
        if (x != begin() && isect(--x, y)) {
            isect(x, y = erase(y));
        }
        while ((y = x) != begin() && (--x->p >= y->p) {
            isect(x, erase(y));
        }
    } // hash-cpp-4 = 2810198878e0dfc44ef39381376b7731
    ll query(ll x) { // hash-cpp-5
        assert(!empty());
        auto l = *lower_bound(x);
        return l.k * x + l.m;
    } // hash-cpp-5 = d21e2fde3c73a41bd894e185d7d18d1e
};

} // namespace line_container

```

persistent-array.hpp

Description: Persistent array based on persistent segtrees

69 lines

```

template <class D> struct PersistentArray {
    union N { // hash-cpp-1
        D v;
        array<int, 2> c;
        N(const D& a) : v(a) {}
        N(int a, int b) : c{a, b} {}
    };
    V<N> x;
    int s, h;
    // Modify this so that it can reserve memory for x
    PersistentArray() {} // hash-cpp-1 = 521
        ↪ fef167012ec972f1c84f879a34735

    // All arrays share the same layout (length)
    int build(int n) { // hash-cpp-2
        x.clear();
        s = 1, h = 0;
        while (s < n) {
            s *= 2;
            h++;
        }
        int rt = make_leaf(D());
        for (int l = 0; l < h; l++) {
            rt = make_node(rt, rt);
        }
    }
};

```

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```

    }
    return rt;
} // hash-cpp-2 = 07caee6062571a915772221c203141f3

int make_leaf(const D& a) { // hash-cpp-3
    x.emplace_back(a);
    return int(x.size())-1;
}
int make_node(int a, int b) {
    x.emplace_back(a, b);
    return int(x.size())-1;
} // hash-cpp-3 = 1fee63ccaf8114c5295fe73f218cc786

int set(int rt, int i, const D& a) { // hash-cpp-4
    static int buf[40];
    for (int l = 0; l < h; l++) {
        buf[l] = rt;
        if ((i >> (h-1-l)) & 1) {
            rt = x[rt].c[l];
        } else {
            rt = x[rt].c[0];
        }
    }
    int res = make_leaf(a);
    for (int l = h-1; l >= 0; l--) {
        int j = buf[l];
        if ((i >> (h-1-l)) & 1) {
            res = make_node(x[j].c[0], res);
        } else {
            res = make_node(res, x[j].c[l]);
        }
    }
    return res;
} // hash-cpp-4 = ce571ab8758dbbaf6d393f0545a71302

D get(int rt, int i) { // hash-cpp-5
    for (int l = h-1; l >= 0; l--) {
        if (i & (1 << l)) {
            rt = x[rt].c[l];
        } else {
            rt = x[rt].c[0];
        }
    }
    return x[rt].v;
} // hash-cpp-5 = 3a880dd33ae85a7becf12470a5ee22d6
};

```

fast-set.hpp

Description: A set for insertion, removal and querying the predecessor/successor of some element

76 lines

```

struct FastSet {
    using U = uint64_t; // hash-cpp-1
    int n, h;
    VV<U> x;
    FastSet(int n_ = 0) : n(n_) {
        int m = (n ? n : 1);
        do {
            x.push_back(V<U>((m + 63) >> 6));
            m = (m + 63) >> 6;
        } while (m > 1);
        h = int(x.size());
    } // hash-cpp-1 = e00a026f56355ee04eb312a72ab65ae0

    bool empty() const { // hash-cpp-2
        return !x[h-1][0];
    }
}

```

```

bool operator [] (int i) const {
    return (x[0][i >> 6] >> (i & 63)) & 1;
} // hash-cpp-2 = e7139f9a9d939bcdaea656a0e3dcb204

void set(int i) { // hash-cpp-3
    for (int d = 0; d < h; d++) {
        int q = i >> 6, r = i & 63;
        x[d][q] |= U(1) << r;
        i = q;
    }
} // hash-cpp-3 = 3319dfe2dcef21686104393ed36b8705

void reset(int i) { // hash-cpp-4
    for (int d = 0; d < h; d++) {
        int q = i >> 6, r = i & 63;
        if ((x[d][q] &= ~(U(1) << r))) break;
        i = q;
    }
} // hash-cpp-4 = 1f4723e2daf4308e36bca9899dfea88c

// min active j s.t. j >= i
int next(int i) const { // hash-cpp-5
    if (i >= n) return n;
    i = max(i, 0);
    for (int d = 0; d < h; d++) {
        int q = i >> 6, r = i & 63;
        if (q >= int(x[d].size())) break;
        U up = x[d][q] >> r;
        if (up) {
            i += __builtin_ctzll(up);
            for (int e = d-1; e >= 0; e--) {
                i = i << 6 | __builtin_ctzll(x[e][i]);
            }
            return i;
        }
        i = q+1;
    }
    return n;
} // hash-cpp-5 = 2a01cef716336e62e563b5d73eaaaf40

// max active j s.t. j <= i
int prev(int i) const { // hash-cpp-6
    if (i < 0) return -1;
    i = min(i, n-1);
    for (int d = 0; d < h; d++) {
        if (i < 0) break;
        int q = i >> 6, r = i & 63;
        U lo = x[d][q] << (63-r);
        if (lo) {
            i -= __builtin_clzll(lo);
            for (int e = d-1; e >= 0; e--) {
                i = i << 6 | (63 - __builtin_clzll(x[e][i]));
            }
            return i;
        }
        i = q-1;
    }
    return -1;
} // hash-cpp-6 = f8f01973030c47d09562f7ad1e93b4cc
};

```

Ad Hoc (3)

tree-dp.hpp

Description: “Solving for all roots” abstraction. This seems to bear some huge constant factor, so try out ad-hoc implementations if you get TLs

44 lines

```

template <class D, class E> struct TreeDP {
    using S = typename D::S;
    const VV<E>& g;
    int n;
    V<S> dp, dp2, res;
    V<E> par;

    TreeDP(D d, const VV<E>& g_) : g(g_), n(int(g.size())),
        dp(n), dp2(n), res(n), par(n) {
        assert(n >= 1);
        V<S> up(n), pref(n);

        yc([&](auto self, int v, int p) -> void { // hash-cpp-1
            up[v] = d.make(v);
            for (auto& e : g[v]) {
                if (e != p) {
                    self(e, v);
                    pref[e] = up[v];
                    up[v] = d.op(up[v], up[e]);
                } else {
                    par[v] = e;
                }
            }
            dp[v] = up[v];
            if (p != -1) {
                up[v] = d.up(up[v], par[v]);
            }
        })(0, -1); // hash-cpp-1 =
        aa0d20033a045bc0718a9e3f3544a0fb

        yc([&](auto self, int v, int p, S f) -> void { // hash-
            cpp-2
            for (int j = int(g[v].size())-1; j >= 0; j--) {
                auto& e = g[v][j];
                if (e == p) continue;
                dp2[e] = d.op(f, pref[e]);
                self(e, v, d.up(dp2[e], e));
                f = d.op(f, up[e]);
            }
            res[v] = f;
        })(0, -1, d.make(0)); // hash-cpp-2 = 605
        a3d440cbc2fdd18703cae2d61373e

        const S& operator [] (int i) const {
            return res[i];
        }
    };
}

```

monotone-minima.hpp

Description: Given an $N \times M$ matrix A , returns $m_i = \operatorname{argmin}_j A_{i,j}$ given that m_0, \dots, m_{N-1} is non-decreasing

16 lines

```

// f(i, j, k) := [A_{i,j} <= A_{i,k}], given j < k
template <class F> V<int> monotone_minima(int n, int m, F f)
    -> {
    V<int> res(n);
    yc([&](auto self, int s, int e, int l, int r) -> void {
        if (s == e) return;
        int i = (s+e)/2;
        int b = l;
        for (int k = l+1; k < r; k++) {

```

```

    if (!f(i, b, k)) b = k;
}
res[i] = b;
self(s, i, l, b+1);
self(i+1, e, b, r);
})(0, n, 0, m);
return res;
} // hash-cpp-all = b68cfb2b91d32e7fe615c192a9e42207

```

min-plus-convex.hpp

Description: Given a_0, \dots, a_{N-1} and a_0, \dots, a_{M-1} such that $a_{i+1} - a_i \leq a_{i+2} - a_{i+1}$, returns $c_0, \dots, c_{(N-1)+(M-1)}$ such that $c_k = \min_{i+j=k} a_i + b_j$

```

"monotone-minima.hpp" 17 lines
// a convex and b arbitrary
template <class T> V<T> min_plus_convex(const V<T>& a,
    ↪ const V<T>& b) {
    int n = int(a.size());
    int m = int(b.size());
    if (!n || !m) return {};
    auto x = monotone_minima(n+m-1, m, [&](int i, int j, int
        ↪ k) -> bool {
        if (i < k) return true;
        if (i-j >= n) return false;
        return a[i-j] + b[j] <= a[i-k] + b[k];
    });
    V<T> res(n+m-1);
    for (int i = 0; i < n+m-1; i++) {
        int j = x[i];
        res[i] = a[i-j] + b[j];
    }
    return res;
} // hash-cpp-all = 159ba36d66ee6a803173143ca4bd9e1d

```

floor-ceil-range.hpp

Description: TODO

```

28 lines
inline void floor_range(ll n, function<void(ll, ll, ll)> f)
    ↪ {
    int rt = int(sqrtl(n)); // hash-cpp-1
    int num = (rt * rt + rt <= n ? rt : rt - 1);
    ll prv = n + 1;
    for (int q = 1; q <= num; q++) {
        ll x = ll(double(n) / (q + 1)) + 1;
        f(q, x, prv);
        prv = x;
    }
    for (int l = rt; l >= 1; l--) {
        f(ll(double(n) / l), l, l+1);
    } // hash-cpp-1 = c69e74e7c069a0d06122a6a63965f401
}

inline void ceil_range(ll n, function<void(ll, ll, ll)> f)
    ↪ {
    int rt = int(sqrtl(n)); // hash-cpp-2
    ll prv = numeric_limits<ll>::max();
    for (int q = 1; q <= rt; ++q) {
        ll x = ll(double(n + q - 1) / q);
        f(q, x, prv);
        prv = x;
    }
    int num = (n <= rt * rt + rt ? rt : rt + 1);
    if (n == rt * rt) --num;
    for (int l = num; l >= 1; --l) {
        f(ll(double(n + l - 1) / l), l, l+1);
    } // hash-cpp-2 = 30b46f7614a037477901bd82f7a3055d

```

```

}

```

palindromic-decomp-dp.hpp

Description: CF932G DP

```

"string/eertree.hpp" 56 lines
// dp[j] := sum_{i s.t. [i, j] is palindromic} {dp[i] * x}
template <class S, int sigma, bool even = false>
V<S> palindromic_decomp_dp(const V<int>& a,
    function<S(S, S)> add, S add_e,
    function<S(S)> mul_x, S mul_e) {
    int n = int(a.size()); // hash-cpp-1
    V<int> locs(n);
    Eertree<sigma> et(n);
    for (int i = 0; i < n; i++) {
        assert(0 <= a[i] && a[i] < sigma);
        locs[i] = et.append(a[i]);
    } // hash-cpp-1 = 86aa49dc74a7c758bf25b91980da41e1

    int nnodes = et.size();
    V<int> nxt(nnodes);
    nxt[0] = -1;
    if constexpr (even) {
        assert(n % 2 == 0);
        for (int v = 1; v < nnodes; v++) {
            nxt[v] = (et[v].len() % 2 == 0 ? v : nxt[et[v].fail])
                ↪;
        }
    } else {
        iota(nxt.begin()+1, nxt.end(), 1);
    }

    V<int> diff(nnodes, 1e9); // hash-cpp-2
    V<pair<int, int>> top(nnodes);
    for (int v = 2; v < nnodes; v++) {
        int w = nxt[et[v].fail];
        int d = et[v].len() - et[w].len();
        diff[v] = d;
        top[v] = (diff[v] == diff[w] ? top[w] : pair<int, int>(
            ↪ w, 0));
        top[v].second++;
    } // hash-cpp-2 = b5ac0ab709517fecf2e6bec5fc8ceeeef

    V<S> dp(n+1, add_e), gdp = dp; // hash-cpp-3
    dp[0] = mul_e;
    for (int j = 0; j < n; j++) {
        int v = nxt[locs[j]];
        int i = (j+1) - et[v].len();
        while (v >= 2) {
            int d = diff[v];
            auto [p, s] = top[v];
            if (s == 1) {
                gdp[i] = dp[i];
            } else {
                gdp[i] = add(gdp[i], dp[i + d * (s-1)]);
            }
            dp[j+1] = add(dp[j+1], mul_x(gdp[i]));
            i += d * s;
            v = p;
        }
    } // hash-cpp-3 = 2c842efa6722d1a05670a98723570137

    return dp;
}

```

Algebra (4)

modint.hpp

Description: Frees you from writing %mod stuff. This only works with prime modulo numbers that are determined during compile-time

```

47 lines
template <class T> T pow(T a, ll b) {
    assert(b >= 0);
    T r = 1;
    while (b) {
        if (b & 1) r *= a;
        a *= a;
        b >>= 1;
    }
    return r;
}

template <uint32_t mod> struct mint {
    using U = uint32_t;

    static constexpr U m = mod; // hash-cpp-1
    U v;
    constexpr mint() : v(0) {}
    constexpr mint(ll a) { s(U(a % m + m)); }
    constexpr mint& s(U a) { v = a < m ? a : a-m; return *
        ↪ this; }
    friend mint inv(const mint& n) { return pow(n, m-2); } //
        ↪ hash-cpp-1 = 7ae46e1707847d7dc77452080ea79898

    mint operator- () const { // hash-cpp-2
        mint res;
        res.v = v ? m-v : 0;
        return res;
    } // hash-cpp-2 = 682e0bd616a7a1b4efedf0025fd9946a

    friend bool operator == (const mint& a, const mint& b) {
        ↪ return a.v == b.v; } // hash-cpp-3
    friend bool operator != (const mint& a, const mint& b) {
        ↪ return !(a == b); } // hash-cpp-3 = 747
        ↪ b64cd3779b0e594a5a9027b3c39d1

    mint& operator += (const mint& o) { return s(v + o.v); }
        ↪ // hash-cpp-4
    mint& operator -= (const mint& o) { return s(v + m - o.v)
        ↪; }
    mint& operator *= (const mint& o) { v = U(uint64_t(v) * o
        ↪ .v % m); return *this; }
    mint& operator /= (const mint& o) { return *this *= inv(o
        ↪); } // hash-cpp-4 =
        ↪ d2801243cd92c4bf423b4d808c532236

    friend mint operator + (const mint& a, const mint& b) {
        ↪ return mint(a) += b; } // hash-cpp-5
    friend mint operator - (const mint& a, const mint& b) {
        ↪ return mint(a) -= b; }
    friend mint operator * (const mint& a, const mint& b) {
        ↪ return mint(a) *= b; }
    friend mint operator / (const mint& a, const mint& b) {
        ↪ return mint(a) /= b; } // hash-cpp-5 = 0
        ↪ d3449609c465ca434b9110ef55a1bbb

    static constexpr U get_mod() { return m; }
    static constexpr mint get_root() {
        if (m == 998244353) return 3;
        if (m == 1053818881) return 2789;
        assert(false);
    }
};

```

CUHK-SZ

nft.hpp

Description: NTT; mostly the same with fft.hpp?

"contest/extra.hpp" 58 lines

```
template <class T> void nft(V<T>& a, int n) {
    static V<int> rev = {0, 1}; // hash-cpp-1
    static V<T> rt(2, 1);
    if (int(r.size()) < n) {
        rev.resize(n);
        for (int i = 0; i < n; i++) {
            rev[i] = (rev[i>>1] | ((i&1)*n)) >> 1;
        }
        rt.reserve(n);
        for (int k = int(r.size()); k < n; k *= 2) {
            rt.resize(2*k);
            T z = pow(T::get_root(), (T::get_mod()-1) / (2*k));
            for (int i = k/2; i < k; i++) {
                rt[2*i] = rt[i];
                rt[2*i+1] = rt[i] * z;
            }
        }
    } // hash-cpp-1 = 0317970f6407858d30d9ac8d7c912632
    int s = __builtin_ctz(int(rev.size()) / n); // hash-cpp-2
    for (int i = 0; i < n; i++) {
        int j = rev[i] >> s;
        if (i < j) swap(a[i], a[j]);
    }
    for (int k = 1; k < n; k *= 2) {
        for (int i = 0; i < n; i += 2*k) {
            auto it1 = a.begin() + i;
            auto it2 = it1 + k;
            for (int j = 0; j < k; j++, ++it1, ++it2) {
                T t = rt[j+k] * *it2;
                *it2 = *it1 - t;
                *it1 += t;
            }
        }
    } // hash-cpp-2 = f44c0c7afb36c49ec3de1f45f36c18fb
}
```

```
template <class T> void inft(V<T>& a, int n) { // hash-cpp
    ↪-3
    T d = inv(T(n));
    for (int i = 0; i < n; i++) a[i] *= d;
    reverse(a.begin()+1, a.begin()+n);
    nft(a, n);
} // hash-cpp-3 = 70f478c2abbc15c2d18bdf1b0781f931
```

```
template <class T> V<T> multiply(V<T> a, V<T> b) { // hash-
    ↪cpp-4
    int n = int(a.size()), m = int(b.size());
    if (!n || !m) return {};
    int s = 1 << internal::next_pow2(n + m - 1);
    a.resize(s), nft(a, s);
    b.resize(s), nft(b, s);
    T is = inv(T(s));
    for (int i = 0; i < s; i++) {
        a[i] *= b[i] * is;
    }
    reverse(a.begin() + 1, a.end());
    nft(a, s);
    a.resize(n + m - 1);
    return a;
} // hash-cpp-4 = ebb669e117a71af44f842cf79631bd1d
```

matrix.hpp

Description: Gaussian elimination and stuff. solve_lineareq returns the pair (some particular solution, a basis of the null space).

"algebra/modint.hpp" 116 lines

```
namespace matrix {

template <class T>
using F_better = function<bool(T, T)>;
```

```
template <class T>
using F_zero = function<bool(T)>;
```

```
template <bool rref = false, class T>
```

```
pair<int, T> sweep(VV<T>& a,
    F_better<T> fb, F_zero<T> fz,
    int c = -1) {
    int h = int(a.size());
    if (!h) return {0, 0};
    int w = int(a[0].size());
```

```
    if (c == -1) c = w; // hash-cpp-1
    int r = 0;
    T det = 1;
    for (int j = 0; j < c; j++) {
        int p = -1;
        for (int i = r; i < h; i++) {
            if (p == -1 || fb(a[i][j], a[p][j])) p = i;
        }
        if (p == -1 || fz(a[p][j])) {
            det = 0;
            continue;
        }
        if (r != p) {
            det = -det;
            swap(a[r], a[p]);
        }
        auto& ar = a[r];
        det *= ar[j]; // hash-cpp-1 = 68409
        ↪b9e970dd293b0fbdda0e682d0c9
```

```
    int is; // hash-cpp-2
    T d = T(1) / ar[j];
    if constexpr(rref) {
        for (int k = j; k < w; k++) {
            ar[k] *= d;
        }
        d = 1;
        is = 0;
    } else {
        is = r+1;
    } // hash-cpp-2 = 2e7107ced9297d66963c63feb0f864a8
```

```
    for (int i = is; i < h; i++) { // hash-cpp-3
        if (i == r) continue;
        auto& ai = a[i];
        if (!fz(ai[j])) {
            T e = ai[j] * d;
            for (int k = j; k < w; k++) {
                ai[k] -= ar[k] * e;
            }
        }
    }
    r++;
} // hash-cpp-3 = bf314b34183f0c8f2f977a8def861fab
return {r, det};
}
```

```
template <class T>
pair<V<T>, VV<T>> solve_lineareq(VV<T> a, V<T> b,
    F_better<T> fb, F_zero<T> fz) {
    int h = int(a.size());
    assert(h);
    int w = int(a[0].size());
    for (int i = 0; i < h; i++) a[i].push_back(b[i]); // hash
    ↪-cpp-4
    int r = sweep<true>(a, fb, fz, w).first;
    for (int i = r; i < h; i++) {
        if (!fz(a[i][w])) return {};
    }
    V<T> x(w);
    V<int> pivot(w, -1);
    int z = 0;
    for (int i = 0; i < r; i++) {
        while (fz(a[i][z])) z++;
        x[z] = a[i][w], pivot[z] = i;
    } // hash-cpp-4 = fed9f2cf91f51c7f7f691143a21b1d45
    VV<T> ker; // hash-cpp-5
    for (int j = 0; j < w; j++) {
        if (pivot[j] == -1) {
            V<T> v(w);
            v[j] = 1;
            for (int k = 0; k < j; k++) {
                if (pivot[k] != -1) v[k] = -a[pivot[k]][j];
            }
            ker.push_back(v);
        }
    } // hash-cpp-5 = d82658f1eb1a359e4c0319403ac44cce
    return {x, ker};
}
```

```
template <class T> VV<T> mat_inv(VV<T> a,
    F_better<T> fb, F_zero<T> fz) { // hash-cpp-6
    int n = int(a.size());
    VV<T> m(n, V<T>(2*n));
    for (int i = 0; i < n; i++) {
        copy(begin(a[i]), end(a[i]), begin(m[i]));
        m[i][n+i] = 1;
    }
    if (sweep<true>(m, fb, fz, n).first != n) return {};
    VV<T> b(n);
    for (int i = 0; i < n; i++) {
        copy(begin(m[i]) + n, end(m[i]), back_inserter(b[i]));
    }
    return b;
} // hash-cpp-6 = 243823cb5b0f3f38377baf672f6d7276
```

```
template <class T> T mat_det(VV<T> a,
    F_better<T> fb, F_zero<T> fz) { // hash-cpp-7
    return sweep<false>(a, fb, fz).second;
} // hash-cpp-7 = fa5f2046eelbe299cee6c7f1f558ba9f

} // namespace matrix
```

Graph (5)

eulerian-trail.hpp

Description: Eulerian undirected/directed trail algorithm. Returns a list of (vertex, edge)'s in the trail with src at the start, or std::nullopt if there is no trail. Note that choosing the starting vertex can be somewhat ad-hoc.)

Time: $\mathcal{O}(V + E)$

84 lines

```
namespace eulerian_trail {
```



```

// (vertex, edge)
// For the returned list,
// edge is the preceding edge of that vertex
using E = pair<int, int>;
template <bool cyc_only = false>
optional<V<E>> go(int nv, const VV<E>& g, int ne, int src =
    ↪ 0) {
    assert(nv == int(g.size()));
    assert(0 <= src && src < nv);

    V<V<E>::const_iterator> its(nv); // hash-cpp-1
    for (int i = 0; i < nv; i++) its[i] = g[i].begin();
    V<int> state(nv);
    if constexpr (!cyc_only) state[src]++;
    V<bool> seen(ne);
    V<E> res, stk = {E(src, -1)}; // hash-cpp-1 = 1
    ↪ e5089ad863eb917ca8416c84758c980

    while (!stk.empty()) { // hash-cpp-2
        auto [i, p] = stk.back();
        auto& it = its[i];
        if (it == g[i].end()) {
            res.emplace_back(i, p);
            stk.pop_back();
            continue;
        }
        auto [j, e] = *(it++);
        if (!seen[e]) {
            state[i]--, state[j]++;
            stk.emplace_back(j, e);
            seen[e] = true;
        }
    }
    if (int(res.size()) != ne+1) return {};
    for (int s : state) if (s < 0) return {};
    return V<E>{res.rbegin(), res.rend()}; // hash-cpp-2 =
    ↪ ae20d810f8feef21197961bf6c241e0d
}

template <bool cyc_only = false>
optional<V<E>> trail_undirected(int nv, const V<pair<int,
    ↪ int>>& edges) {
    assert(nv > 0);

    VV<E> g(nv);
    int e = 0;
    for (auto [a, b] : edges) {
        g[a].emplace_back(b, e);
        g[b].emplace_back(a, e);
        e++;
    }

    int src = 0; // hash-cpp-3
    for (int i = 0; i < nv; i++) {
        if (!g[i].empty()) src = i;
    }
    for (int i = 0; i < nv; i++) {
        if (g[i].size() % 2 == 1) src = i;
    } // hash-cpp-3 = 8f0c0499edac02a8775d04f38f6b519e
    return go<cyc_only>(nv, g, int(edges.size()), src);
}

template <bool cyc_only = false>
optional<V<E>> trail_directed(int nv, const V<pair<int, int
    ↪ >>& edges) {
    assert(nv > 0);

```

```

VV<E> g(nv);
V<int> indeg(nv);
int e = 0;
for (auto [a, b] : edges) {
    g[a].emplace_back(b, e);
    indeg[b]++;
    e++;
}

int src = 0; // hash-cpp-4
for (int i = 0; i < nv; i++) {
    if (!g[i].empty()) src = i;
}
for (int i = 0; i < nv; i++) {
    if (indeg[i] < int(g[i].size())) src = i;
} // hash-cpp-4 = 78a6497411685fe139d007ac0cce4a8b
return go<cyc_only>(nv, g, int(edges.size()), src);
}

} // namespace eulerian_trail

```

bipartite.hpp

Description: Hopcroft–Karp algorithm that gives a maximum bipartite matching. edges should be a sequence of edges (a_i, b_i) such that $a_i \in [n_l]$ and $b_i \in [n_r]$

Time: $\mathcal{O}(E\sqrt{V})$

83 lines

```

struct Bipartite {
    int nl, nr;
    VV<int> g;
    V<int> mtl, mtr, lvl;
    V<bool> seen;
    Bipartite(int nl_, int nr_, const V<pair<int, int>>&
        ↪ edges)
        : nl(nl_), nr(nr_),
          g(nl, mtl(nl, -1), mtr(nr, -1), lvl(nl), seen(nr) {
        for (auto [i, j] : edges) {
            g[i].push_back(j);
        }
        V<int> q; q.reserve(nl);
        while (true) {
            q.clear(); // hash-cpp-1
            for (int i = 0; i < nl; i++) {
                if (mtl[i] == -1) {
                    lvl[i] = 0;
                    q.push_back(i);
                } else {
                    lvl[i] = -1;
                }
            }
            // If there is an alternating path that
            // leads to some unmatched left-side vertex
            bool f = false;
            for (int z = 0; z < int(q.size()); z++) {
                int i = q[z];
                for (int j : g[i]) {
                    int o = mtr[j];
                    if (o == -1) {
                        f = true;
                    } else if (lvl[o] == -1) {
                        lvl[o] = lvl[i] + 1;
                        q.push_back(o);
                    }
                }
            }
            if (!f) {

```

```

        for (int i : q) for (int j : g[i]) seen[j] = true;
        break;
    } // hash-cpp-1 = 3c672de70b8adeba7d37b4685bbebca6

    V<bool> done(nl); // hash-cpp-2
    for (int s = 0; s < nl; s++) {
        if (mtl[s] != -1) continue;

        yc([&](auto self, int i) -> bool {
            if (done[i]) return false;
            done[i] = true;
            for (int j : g[i]) {
                int o = mtr[j];
                if (o == -1 || (lvl[i]+1 == lvl[o] && self(o)))
                    ↪ {
                    mtl[i] = j, mtr[j] = i;
                    return true;
                }
            }
            return false;
        })(s);
    } // hash-cpp-2 = 18358a31be7e4bd4afa0cafb536586d8
}

V<pair<int, int>> matching() { // hash-cpp-3
    V<pair<int, int>> res;
    for (int i = 0; i < nl; i++) {
        int j = mtl[i];
        if (j != -1) res.emplace_back(i, j);
    }
    return res;
} // hash-cpp-3 = 9f6badbc0263844183d9e375f20ae28e

pair<V<int>, V<int>> vertex_cover() { // hash-cpp-4
    V<int> lvs, rvs;
    for (int i = 0; i < nl; i++) {
        if (lvl[i] == -1) lvs.push_back(i);
    }
    for (int j = 0; j < nr; j++) {
        if (seen[j]) rvs.push_back(j);
    }
    return {lvs, rvs};
} // hash-cpp-4 = fcdd34794a59dc336b8edfabd350b490
};

```

hld.hpp

Description: Heavy-light decomposition with derived functionalities

179 lines

```

struct HLD {
    int n;
    V<int> ord, st, en, depth;
    V<pair<int, int>> heavy;
    HLD() {}
    HLD(const V<int>& par, int rt = -1) { build(par, rt); }

    void build(const V<int>& par, int rt = -1) {
        n = int(par.size()); // hash-cpp-1
        ord.resize(n);
        st.resize(n);
        en.resize(n);
        depth.resize(n);
        heavy.resize(n);
        VV<int> ch(n);
        for (int i = 0; i < n; i++) {
            if (par[i] != -1) ch[par[i]].push_back(i);
        } // hash-cpp-1 = 8ae787897663a0b8ad2c988fae1184b0
    }

```



```

int i = 0;
V<int> sub(n);
auto go = [&](int g) -> void {
    yc([&](auto self, int v, int d = 0) -> void { // hash
        ↪-cpp-2
        sub[v] = 1;
        depth[v] = d;
        for (int& w : ch[v]) {
            self(w, d+1);
            sub[v] += sub[w];
            if (sub[ch[v][0]] < sub[w]) swap(ch[v][0], w);
        }
    })(g); // hash-cpp-2 =
        ↪f85fc1f8fd7047a905e24720a59d1d8b

    yc([&](auto self, int v, bool r = true) -> void { //
        ↪hash-cpp-3
        ord[st[v]] = i++; v;
        if (r) {
            heavy[st[v]] = {par[v] == -1 ? -1 : st[par[v]],
                ↪1};
        } else {
            heavy[st[v]] = heavy[st[v]-1];
            heavy[st[v]].second++;
        }
        bool cr = false;
        for (int w : ch[v]) {
            self(w, cr);
            cr = true;
        }
        en[v] = i;
    })(g); // hash-cpp-3 =
        ↪f1d1da4b4153cfda08dc6ef0502deaf4
};

if (rt == -1) {
    // rooted forest
    for (int v = 0; v < n; v++) {
        if (par[v] == -1) go(v);
    }
} else {
    // rooted at rt
    assert(0 <= rt && rt < n);
    go(rt);
}

assert(i == n);
}

bool in_subtree(int a, int v) const {
    return st[a] <= st[v] && st[v] < en[a];
}

int get_ancestor(int a, int k) const { // hash-cpp-4
    assert(k >= 0);
    a = st[a];
    while (a != -1 && k) {
        if (k >= heavy[a].second) {
            k -= heavy[a].second;
            a = heavy[a].first;
        } else {
            a -= k;
            k = 0;
        }
    }
    if (a == -1) return -1;
    else return ord[a];
}

```

```

} // hash-cpp-4 = 38c66b004fd349c93647d7943f36251f

int lca(int a, int b) const { // hash-cpp-5
    a = st[a], b = st[b];
    while (true) {
        if (a > b) swap(a, b);
        if (a > b - heavy[b].second) {
            return ord[a];
        }
        b = heavy[b].first;
        if (b == -1) return -1;
    }
} // hash-cpp-5 = 9ee75bf6da246fa444c875c297d5c9a7

int jump(int s, int t, int d) const { // hash-cpp-6
    int w = lca(s, t);
    if (d <= depth[s] - depth[w]) {
        return get_ancestor(s, d);
    } else {
        d = (depth[s] + depth[t] - 2 * depth[w]) - d;
        return d >= 0 ? get_ancestor(t, d) : -1;
    }
} // hash-cpp-6 = 278341587908508d2f5cabb88ab56ed1

V<array<int, 2>> extract(int s, int t) { // hash-cpp-7
    static V<array<int, 2>> res;
    res.clear();
    s = st[s], t = st[t];
    while (true) {
        if (t > s - heavy[s].second) {
            res.push_back({s, t+1});
            break;
        }
        res.push_back({s, s - heavy[s].second + 1});
        s = heavy[s].first;
    }
    return res;
} // hash-cpp-7 = 273a0339e602dbb257c2354c8177ac96

template <bool vertex = true, class F> void apply(int s,
    ↪int t, F f) { // hash-cpp-8
    int a = lca(s, t);
    for (auto& [x, y] : extract(s, a)) {
        f(x+1, y);
    }
    if constexpr (vertex) {
        f(st[a], st[a]+1);
    }
    auto des = extract(t, a);
    reverse(des.begin(), des.end());
    for (auto& [x, y] : des) {
        f(y, x+1);
    }
} // hash-cpp-8 = c27280d29b591909807fe89e7034137c

// NOT TESTED
template <class F> int get_lowest(int a, F f) const { //
    ↪hash-cpp-9
    a = st[a];
    while (a != -1) {
        int t = a - heavy[a].second + 1;
        if (!f(ord[t])) {
            a = heavy[a].first;
            continue;
        }
        int mi = t, ma = a+1;
        while (ma - mi > 1) {
            int md = (mi + ma) / 2;

```

```

            if (f(ord[md])) mi = md;
            else ma = md;
        }
        return ord[mi];
    }
    return -1;
} // hash-cpp-9 = b254f08e7b14254b490de927443e62ac

V<int> inds; // hash-cpp-10
pair<V<int>, V<int>> compress(V<int> vs) {
    inds.resize(n, -1);
    auto cmp = [&](int a, int b) -> bool {
        return st[a] < st[b];
    };
    sort(vs.begin(), vs.end(), cmp);
    vs.erase(unique(vs.begin(), vs.end(), vs.end()));
    int num = int(vs.size());
    assert(num >= 1);
    for (int z = 1; z < num; z++) {
        vs.push_back(lca(vs[z-1], vs[z]));
    }
    sort(vs.begin(), vs.end(), cmp);
    vs.erase(unique(vs.begin(), vs.end(), vs.end()));
    num = int(vs.size());
    for (int z = 0; z < num; z++) inds[vs[z]] = z;
    V<int> par(num, -1);
    for (int z = 1; z < num; z++) {
        par[z] = inds[lca(vs[z-1], vs[z])];
    }
    return {vs, par};
} // hash-cpp-10 = 28006d54abac0b3eaa7865ad2f55bb70
};

```

enumerate-triangles.hpp

Description: Enumerates all triangles (x, y, z) in an undirected graph
Time: TODO

23 lines

```

template <class F> void triangles(int n, const V<pair<int,
    ↪int>>& edges, F f) {
    V<int> deg(n); // hash-cpp-1
    for (auto& [a, b] : edges) {
        deg[a]++, deg[b]++;
    }
    VV<int> adj(n);
    for (auto [a, b] : edges) {
        if (tie(deg[a], a) > tie(deg[b], b)) swap(a, b);
        adj[a].push_back(b);
    } // hash-cpp-1 = 7f0b6720531a2a2c68c8619dadbfed31

    V<int> ind(n); // hash-cpp-2
    int i = 0;
    for (int x = 0; x < n; x++) {
        ++i;
        for (int y : adj[x]) ind[y] = i;
        for (int y : adj[x]) {
            for (int z : adj[y]) {
                if (ind[z] == i) f(x, y, z);
            }
        }
    } // hash-cpp-2 = bfa178d26a11e8e8875f23e0a1275488
}

```

block-cut.hpp

47 lines

```

template <class E> VV<int> block_cut_tree(int n, const VV<E
    ↪>& g) {

```

```

VV<int> tr(n); // hash-cpp-1
auto add = [&](int b, int v) -> void {
    tr[b].push_back(v);
    tr[v].push_back(b);
}; // hash-cpp-1 = d73420bf298cdd9bb0e5d25c188b4da1

V<int> stk; stk.reserve(n);
V<int> idx(n, -1);
int t = 0;
for (int s = 0; s < n; s++) {
    if (idx[s] != -1) continue;
    yc([&](auto self, int v, int p) -> int {
        stk.push_back(v); // hash-cpp-2
        idx[v] = t++;
        int low = idx[v] = t++;
        int c = 0;
        for (int w : g[v]) {
            if (w == p) continue;
            if (idx[w] == -1) {
                c++;
                auto z = stk.size();
                int nlow = self(w, v);
                low = min(low, nlow);
                if ((p == -1 && c > 1) || (p != -1 && idx[v] <=
                    ↪nlow)) {
                    int b = int(tr.size());
                    tr.resize(b+1);
                    add(b, v);
                    while (z < stk.size()) {
                        add(b, stk.back());
                        stk.pop_back();
                    }
                } else {
                    low = min(low, idx[w]);
                }
            }
        }
        return low; // hash-cpp-2 = 7
        ↪cc064051424c44ab789d52113b58040
    ))(s, -1);
    int b = int(tr.size()); // hash-cpp-3
    tr.resize(b+1);
    for (int v : stk) add(b, v);
    stk.clear(); // hash-cpp-3 = 98651
        ↪a8db6af759650d4c4be638030dd
}

return tr;
}

```

two-sat.hpp

Description: Calculates a valid assignment to boolean variables a, b, c,... to a 2-SAT problem, so that an expression of the type $(a \vee b) \wedge \neg(c \vee d) \wedge \neg(b) \wedge \dots$ becomes true, or reports that it is unsatisfiable. Negated variables are represented by bit-inversions ($\sim x$)

Usage: TwoSat ts(number of boolean variables);
 ts.either(0, ~3); // Var 0 is true or var 3 is false
 ts.set_value(2); // Var 2 is true
 ts.at_most_one({0, ~1, 2}); // ≤ 1 of vars 0, ~1 and 2 are true
 ts.solve(); // Returns true iff it is solvable
 ts.values[0..N-1] holds the assigned values to the vars
Time: $\mathcal{O}(N + E)$

```

struct TwoSat {
    int n;
    VV<int> g;

```

```

TwoSat(int n_ = 0) : n(n_), g(2*n) {}

int add_var() {
    g.emplace_back(), g.emplace_back();
    return n++;
}

void either(int a, int b) { // hash-cpp-1
    a = max(2*a, -1-2*a);
    b = max(2*b, -1-2*b);
    g[a^1].push_back(b);
    g[b^1].push_back(a);
} // hash-cpp-1 = 16e68cfa6a6fc20d6b21bba940571f2

void set_value(int x) {
    either(x, x);
}

void at_most_one(const V<int>& vs) { // hash-cpp-2
    int m = int(vs.size());
    if (m <= 1) return;
    int cur = ~vs[0];
    for (int i = 2; i < m; i++) {
        int nxt = add_var();
        either(cur, ~vs[i]);
        either(cur, nxt);
        either(~vs[i], nxt);
        cur = ~nxt;
    }
    either(cur, ~vs[1]);
} // hash-cpp-2 = 5fb24984002f7bac35e6e8ef6c1b3ce5

optional<V<bool>> solve() { // hash-cpp-3
    V<int> idx(2*n, -1), comp(2*n, -1), stk;
    int tm = 0;
    V<char> r(n, -1); // hash-cpp-3 = 572
        ↪ebd2509c5c93c519ae4ff99a396d0

    for (int s = 0; s < 2*n; s++) { // hash-cpp-4
        if (comp[s] != -1) continue;

        yc([&](auto self, int i) -> int {
            int low = idx[i] = tm++;
            stk.push_back(i);
            for (auto& j : g[i]) {
                if (comp[j] != -1) continue;
                low = min(low, idx[j] == -1 ? self(j) : idx[j]);
            }
            tm++;
            if (low == idx[i]) {
                while (true) {
                    int z = stk.back(); stk.pop_back();
                    comp[z] = tm;
                    if (r[z>>1] == -1) r[z>>1] = !(z&1);
                    if (i == z) break;
                }
            }
            return idx[i] = low;
        })(s);
    } // hash-cpp-4 = 2a4eba424a97524adeb7fdf28a595304

    for (int i = 0; i < n; i++) { // hash-cpp-5
        if (comp[2*i] == comp[2*i+1]) return {};
    }
    V<bool> res(n);
    for (int i = 0; i < n; i++) res[i] = bool(r[i]);
    return res; // hash-cpp-5 = 46
        ↪f2074bbd0b6aeff35c156aabe39e19

```

```

}
};

```

Number Theory (6)

factor.hpp

Description: Returns prime factors in ascending order (e.g. 2299 -> {11, 11, 19})

Time: $\mathcal{O}(n^{1/4})$

"contest/extra.hpp", <random> 91 lines

```

namespace factor {

template <class T> T pow_mod(T a, u64 b, T m) { // hash-cpp
    ↪-1
    T r = 1;
    while (b) {
        if (b & 1) r = r * a % m;
        a = a * a % m;
        b >>= 1;
    }
    return r;
} // hash-cpp-1 = 8153dd104c95c28bf40b51ccfa359c28

template <class T> bool is_prime(T n) { // hash-cpp-2
    if (n <= 1 || n % 2 == 0) return (n == 2);
    int s = __builtin_ctzll(n-1);
    T d = (n-1) >> s;
    for (u128 a : {2, 325, 9375, 28178, 450775, 9780504,
        ↪1795265022}) {
        a %= n;
        if (a == 0) continue;
        a = pow_mod<u128>(a, d, n);
        if (T(a) == 1 || T(a) == n-1) continue;
        for (int i = 0; i < s-1; i++) {
            a = a * a % n;
            if (T(a) == n-1) break;
        }
        if (T(a) != n-1) return false;
    }
    return true;
} // hash-cpp-2 = 91830792ecc62049005cfc63ebf602cb

// Fake pollard-rho, which does not guarantee
// to return a nontrivial divisor of n
template <class T> T pollard(T n) {
    assert(n >= 2);
    if (n % 2 == 0) return 2;
    static mt19937_64 rng(chrono::steady_clock::now().
        ↪time_since_epoch().count());
    T c = uniform_int_distribution<T>(1, n-1)(rng);
    T y = uniform_int_distribution<T>(1, n-1)(rng);
    auto f = [&](T a) -> T { // hash-cpp-3
        return T((u128(a) * a + c) % n);
    };
    for (int s = 1; s * s == 2) {
        T x = y, d = 1;
        for (int i = 0; i < s; i++) y = f(y);
        static constexpr int block = 256;
        for (int i = 0; i < s; i += block) {
            T yb = y;
            for (int j = 0; j < block && j < s-i; j++) {
                y = f(y);
                d = T(u128(d) * (y-x+n) % n);
            }
            d = __gcd(n, d);

```

```

    if (d == 1) continue;
    if (d == n) {
        for (d = 1, y = yb; d == 1; ) {
            y = f(y);
            d = __gcd(n, y-x+n);
        }
        return d;
    }
} // hash-cpp-3 = af034d23976b39357fd911349e573172

// Returns prime factors in ascending order
template <class T> V<T> factorize(T n) { // hash-cpp-4
    if (n == 1) return {};
    if (is_prime(n)) return {n};
    T f = pollard(n);
    auto a = factorize(f), b = factorize(n / f);
    V<T> c(a.size() + b.size());
    merge(a.begin(), a.end(), b.begin(), b.end(), c.begin());
    return c;
} // hash-cpp-4 = 14092f0d69169ca846474fdcaf0c8fcf

template <class T> T primitive_root(T p) {
    assert(is_prime(p));
    auto f = factorize(p-1);
    while (true) {
        static mt19937_64 rng(chrono::steady_clock::now().
            ↪time_since_epoch().count());
        T c = uniform_int_distribution<T>(1, p-1)(rng);
        if ([&]() -> bool { // hash-cpp-5
            for (T d : f) {
                if (pow_mod<ul128>(c, (p-1) / d, p) == 1) return
                    ↪false;
            }
            return true;
        }()) return c; // hash-cpp-5 = 5
        ↪ecb7c7d20c0e216abf8992272cb47d9
    }
}

} // namespace factor

```

int-kth-root.hpp

Description: Computes $[a^{1/k}]$

```

18 lines
template <class I = uint64_t> I int_kth_root(I a, I k) {
    if (k == 1) return a;
    if (k >= 64) return (a == 0 ? 0 : 1);

    using T = __uint128_t;
    auto works = [&](T x) -> bool {
        T r = 1;
        for (int n = int(k); n; n >>= 1) {
            if (n & 1) r *= x;
            x *= x;
        }
        return r <= a;
    };
    if (a == I(-1)) a--;
    I rt = I(pow(a, nextafter(1 / double(k), 0)));
    while (works(rt+1)) rt++;
    return rt;
} // hash-cpp-all = 62ef9e78cc4292fd7c7b21aa1c80b9a3

```

eratosthenes.hpp

Description: Prime sieve for generating all primes up to a certain limit
n

```

17 lines
inline V<int> prime_enumerate(int n) {
    V<bool> sieve(n/3+1, true); // hash-cpp-1
    int qe = int(sieve.size());
    int n2 = int(sqrt(n));
    for (int p = 5, d = 4, i = 1; p <= n2; p += d = 6-d, i++)
        ↪{
            if (!sieve[i]) continue;
            for (int q = p * p / 3, r = d * p / 3 + (d * p % 3 ==
                ↪2), s = 2*p; q < qe; q += r = s-r) {
                sieve[q] = false;
            }
        } // hash-cpp-1 = 7a03caac557d3e6836e8cbcd82397b1e
    V<int> res{2, 3}; // hash-cpp-2
    for (int p = 5, d = 4, i = 1; p <= n; p += d = 6-d, i++)
        ↪{
            if (sieve[i]) res.push_back(p);
        }
    while (!res.empty() && res.back() > n) res.pop_back();
    return res; // hash-cpp-2 = 9
        ↪d7ac632394009547a94300c97b43d20
}

```

multiplicative-sum.hpp

Description: Blackbox sieve. Modify f(v, p, c) to fit your wish

```

188 lines
namespace multiplicative_sum {

    inline ll isqrt(ll n) {
        return ll(sqrt(n));
    }

    inline ll icbrt(ll n) {
        return ll(cbrt(n));
    }

    inline ll sq(ll a) {
        return a * a;
    }

    inline ll sump(int k, ll n) {
        if (k == 0) {
            return n;
        } else assert(false);
    }

    // Somehow precompute small primes and store them in ps[]
    static V<int> ps;

    template <class T, int K> struct counting_primes {
        using A = array<T, K>; // hash-cpp-1
        void add(A& a, const A& b) {
            for (int k = 0; k < K; k++) a[k] += b[k];
        }
        void sub(A& a, const A& b) {
            for (int k = 0; k < K; k++) a[k] -= b[k];
        }
        const ll n;
        const int n2, n3, n6;
        int s;
        V<ll> vs;
        V<A> sum, fw;
        A pref; // hash-cpp-1 = 71768c8f1f85c90f2649977a31dbf3dd

        A getpows(T p) { // hash-cpp-2
            A res;

```

```

        res[0] = 1;
        for (int k = 1; k < K; k++) {
            res[k] = res[k-1] * p;
        }
        return res;
    } // hash-cpp-2 = 1282c5b86030aad73569a7ce5b1492b8

```

```

void trans(int i, int p) { // hash-cpp-3
    A w = getpows(p);
    int j = get_idx(vs[i] / p);
    for (int k = 0; k < K; k++) {
        sum[i][k] -= (sum[j][k] - pref[k]) * w[k];
    }
} // hash-cpp-3 = 1b75b45369ff775f2ea7ab66bf8c1726

```

```

void trans2(int i, int p) { // hash-cpp-4
    A w = getpows(p);
    int j = get_idx(vs[i] / p);
    A z = sum[j];
    if (j >= n3) {
        j -= n3;
        for (; j < int(fw.size()); j += (j+1) & (-j-1)) {
            add(z, fw[j]);
        }
    }
    for (int k = 0; k < K; k++) {
        sum[i][k] -= (z[k] - pref[k]) * w[k];
    }
} // hash-cpp-4 = 4f7b414359537414dc08ba63b39ad6ec

```

```

void upd(int i, ll cur, bool f) { // hash-cpp-5
    if (!f) {
        A w = getpows(cur);
        for (int j = get_idx(cur)-n3; j >= 0; j -= (j+1) & (-
            ↪j-1)) {
            sub(fw[j], w);
        }
    }
    for (int j = i; cur * ps[j] <= vs[n3]; j++) {
        upd(j, cur * ps[j], false);
    }
} // hash-cpp-5 = a365852e657a6b32c13a96129cd8b444

```

```

counting_primes(ll n_) : n(n_), n2(int(isqrt(n))), n3(int
    ↪(icbrt(n))), n6(int(icbrt(n2))) { // hash-cpp-6
    {
        ll v = n;
        while (v) {
            vs.push_back(v);
            v = n / (n/v+1);
        }
    }
    s = int(vs.size());

    sum.resize(s);
    for (int i = 0; i < s; i++) {
        for (int k = 0; k < K; k++) {
            sum[i][k] = sump(k, vs[i]) - 1;
        }
    }

    int idx = 0;
    pref = {};
    {
        while (ps[idx] <= n6) {
            for (int i = 0; i < s; i++) {
                if (sq(ps[idx]) > vs[i]) break;
                trans(i, ps[idx]);
            }

```

```

    }
    add(pref, getpows(ps[idx]));
    idx++;
}
{
    fw.resize(s-n3);
    while (ps[idx] <= n3) {
        for (int i = 0; i < n3; i++) {
            if (sq(ps[idx]) > vs[i]) break;
            trans2(i, ps[idx]);
        }
        upd(idx, ps[idx], true);
        add(pref, getpows(ps[idx]));
        idx++;
    }
    for (int i = s-n3-1; i >= 0; i--) {
        int j = i + ((i+1) & (-i-1));
        if (j < int(fw.size())) {
            add(fw[i], fw[j]);
        }
    }
    for (int i = 0; i < s-n3; i++) {
        add(sum[i+n3], fw[i]);
    }
}
{
    while (ps[idx] <= n2) {
        for (int i = 0; i < s; i++) {
            if (sq(ps[idx]) > vs[i]) break;
            trans(i, ps[idx]);
        }
        add(pref, getpows(ps[idx]));
        idx++;
    }
}
// hash-cpp-6 = cc14950776f6082996b40e34cfc9052

int get_idx(ll a) { // hash-cpp-7
    return int(a <= n2 ? s-a : n/a-1);
} // hash-cpp-7 = e71b9037098be21e53f8db6ea63d73c3

// f(v)=f(p^c), where p is some prime
// totient function as an example:
T f(ll, int p, int c) {
    T res = p-1;
    for (int z = 0; z < c-1; z++) {
        res *= p;
    }
    return res;
}

```

```

V<T> buf;
T multiplicative_sum() { // hash-cpp-8
    // sum of [p is prime] f(p)
    buf.resize(s);
    for (int i = 0; i < s; i++) {
        buf[i] = sum[i][1] - sum[i][0];
    }

    T ans = 1 + buf[0];
    auto dfs = yc([&](auto self, int i, int c, ll v, ll lim
        ↪, T cur) -> void {
        ans += cur * f(v+ps[i], ps[i], c+1);
        if (lim >= sq(ps[i])) {
            self(i, c+1, v * ps[i], lim/ps[i], cur);
        }
        cur *= f(v, ps[i], c);
    }
}

```

```

    ans += cur * (buf[get_idx(lim)] - buf[get_idx(ps[i])
        ↪]);
    for (int j = i+1; sq(ps[j]) <= lim; j++) {
        self(j, 1, ps[j], lim/ps[j], cur);
    }
});
for (int i = 0; i < int(ps.size()); i++) {
    if (sq(ps[i]) <= n) {
        dfs(i, 1, ps[i], n/ps[i], 1);
    } else {
        break;
    }
}
return ans;
} // hash-cpp-8 = 11adf13473ccebe5d663835ad33e4b7d
};

} // namespace multiplicative_sum

```

String (7)

z-algorithm.hpp

Description: Returns r_0, \dots, r_N such that $s[0..r_i] = s[i..i + r_i]$. In particular, $r_0 = N$ and $r_N = 0$

Time: $\mathcal{O}(N)$

```

template <class S> V<int> z_algo(const S& s) {
    int n = int(s.size());
    V<int> r(n+1);
    for (int i = 1, j = 0; i <= n; i++) {
        int& k = r[i];
        if (j + r[j] <= i) k = 0;
        else k = min(r[j]+j-i, r[i-j]);
        while (i+k < n && s[k] == s[i+k]) k++;
        if (j+r[j] < i+r[i]) j = i;
    }
    r[0] = n;
    return r;
}
// hash-cpp-all = 5f7ecea2b91f34f0c19bf6fd4dlace4e

```

manacher.hpp

Description: Returns maximum lengths of “palindromic” (whatever that means) substring of S centered at each point

Time: $\mathcal{O}(N)$

```

/*
 * eq(i, j): whether [i, j] (inclusive) is palindromic,
 * given that [i+1, j-1] is palindromic.
 * Properties:
 *   * res[i] == i (mod 2)
 *   * k + res[i-k] < res[i] => res[i+k] = res[i-k]
 *   * k + res[i-k] >= res[i] => res[i-k] >= res[i] - k
 *   * [i, j] being palindromic <=> j-i <= res[i+j]
 *   * In particular, res[2*i+1] = -1 states that [i, i] is not
        ↪ palindromic.
 */
template <class E> V<int> manacher(int n, E e) {
    V<int> res(2*n+1);
    int i = 0, a = 0, b = 0;
    while (i <= 2*n) {
        while (0 < a && b < n) {
            if (i-2*a >= -1 && !e(a-1, b)) break;
            a--, b++;
        }
    }
}

```

```

int j = b-a;
res[i] = j;
int k = 1;
while (k < j && k + res[i-k] < j) {
    res[i+k] = res[i-k];
    k++;
}
i += k, a += k;
}
return res;
} // hash-cpp-all = 5c644e1a1f524017b35172cdd50cdee7

```

hashint.hpp

Description: Self-explanatory string hashing structure

39 lines

```

struct HashInt {
    using H = HashInt; // hash-cpp-1
    using T = unsigned long long;
    using L = __uint128_t;
    static constexpr T m = (T(1) << 61) - 1;
    static constexpr T m8 = m * 8;

    T v;
    HashInt() : v(0) {}
    HashInt(T a) : v(a % m * 8) {}
    T get() const { return v == m8 ? 0 : v; } // hash-cpp-1 =
        ↪ 441ee64fd18fdc7b1df56890de357f06

    H& operator += (const H& o) { // hash-cpp-2
        if (__builtin_uaddll_overflow(v, o.v, &v)) v -= m8;
        return *this;
    }
    H& operator -= (const H& o) {
        if (__builtin_usubll_overflow(v, o.v, &v)) v += m8;
        return *this;
    } // hash-cpp-2 = 03a79be35c3f8731c3c4e64a1799cc94

    H& operator *= (const H& o) { // hash-cpp-3
        L t = L(v) * o.v;
        T x = T(t >> 67 << 3);
        T y = T(t << 61 >> 64);
        if (__builtin_uaddll_overflow(x, y, &v)) v -= m8;
        return *this;
    } // hash-cpp-3 = c535ff913f601dd75b6c039556dda31a

    friend H operator + (const H& a, const H& b) { return H(a
        ↪) += b; } // hash-cpp-4
    friend H operator - (const H& a, const H& b) { return H(a
        ↪) -= b; }
    friend H operator * (const H& a, const H& b) { return H(a
        ↪) *= b; }
    friend bool operator == (const H& a, const H& b) { return
        ↪ a.get() == b.get(); } // hash-cpp-4 =
        ↪ b15740d449ec094c54eaf820a3f31571
};

inline HashInt rand_base() {
    static mt19937_64 rng(chrono::steady_clock::now().
        ↪ time_since_epoch().count());
    return 2 * uniform_int_distribution<uint64_t>(4e10, 5e10)
        ↪ (rng) + 1;
}

```

suffix-array.hpp

Description: Builds the suffix array given a string

Time: $\mathcal{O}(N)$ building

117 lines

// Work in progress

```

struct SuffixArray {
    int n;
    V<int> sa;
    V<int> isa;
    V<int> lcp;
    SuffixArray(int n_ : n(n_) {})

    template <class S> static SuffixArray construct(const S&
        ↪s) {
        int n = int(s.size());
        SuffixArray sa(n);

        sa.build_sa_fast(s);

        sa.build_isa();
        sa.build_lcp(s);

        return sa;
    }

    template <class S> void build_sa_fast(S s) {
        sa.resize(n+1);
        // kinda weird
        int sigma = 0;
        for (auto v : s) {
            sigma = max(sigma, int(v));
            assert(int(v) > 0);
        }
        ++sigma;
        s.push_back(0);
        // what exactly should be these sizes?
        V<int> freq(2 * max(n+1, sigma)), lms(2 * (n+1));
        V<char> type(2 * (n+1));
        sais(n, s.data(), sa.data(), sigma, freq.data(), lms.
            ↪data(), type.data());
    }

    template <class S> static void sais(int n, S* s, int* sa,
        ↪ int sigma,
        int* freq, int* lms, char* which) {
        int n2 = -1; // hash-cpp-1
        which[n] = 1;
        for (int i = n-1; i >= 0; i--) {
            which[i] = (s[i] == s[i+1] ? which[i+1] : s[i] < s[i+1])
                ↪+1);
            if (which[i] == 0 && which[i+1] == 1) {
                which[i+1] = 2;
                lms[++n2] = i+1;
            }
        }
        reverse(lms, lms + (n2+1));
        fill(freq, freq + sigma, 0);
        for (int i = 0; i <= n; i++) ++freq[int(s[i])];
        partial_sum(freq, freq + sigma, freq); // hash-cpp-1 =
            ↪cc46481fc435bcf90a6ccb7e296ff9e8

        auto induce = [&](int* v) { // hash-cpp-2
            fill(sa, sa + n+1, 0);
            int* cur = freq + sigma;
            auto pushS = [&](int i) { sa[--cur[int(s[i])]] = i;
                ↪};
            auto pushL = [&](int i) { sa[cur[int(s[i])]]++ = i;
                ↪};

```

```

        copy(freq, freq + sigma, cur);
        for (int i = n2; i >= 0; i--) pushS(v[i]);
        copy(freq, freq + sigma-1, cur + 1);
        for (int i = 0; i <= n; i++) {
            int j = sa[i]-1;
            if (j >= 0 && which[j] == 0) pushL(j);
        }
        copy(freq, freq + sigma, cur);
        for (int i = n; i >= 0; i--) {
            int j = sa[i]-1;
            if (j >= 0 && which[j]) pushS(j);
        }
    }; // hash-cpp-2 = 67f9a319b4923bb284c38a01d1ad54ab

    auto eq = [&](int i, int j) { // hash-cpp-3
        if (s[i] == s[j]) {
            while (s[++i] == s[++j]) {
                if (which[i] == 2) return true;
            }
        }
        return false;
    }; // hash-cpp-3 = 208a2ae3b819fd126c46e4e3a88d30c0

    induce(lms); // hash-cpp-4
    int sigma2 = -1;
    int* s2 = remove_if(sa, sa + n, [&](int i) { return
        ↪which[i] != 2; });
    for (int i = 0; i <= n2; i++) {
        if (sigma2 <= 0 || !eq(sa[i], sa[i-1])) sigma2++;
        s2[sa[i]>>1] = sigma2;
    }
    for (int i = 0; i <= n2; i++) s2[i] = s2[lms[i]>>1];
    ++sigma2;
    if (sigma2 <= n2) {
        sais(n2, s2, sa, sigma2,
            freq + sigma, lms + (n2+1), which + (n+1));
    } else {
        for (int i = 0; i <= n2; i++) sa[s2[i]] = i;
    }
    auto buf = lms + (n2+1);
    for (int i = 0; i <= n2; i++) buf[i] = lms[sa[i]];
    induce(buf); // hash-cpp-4 =
        ↪e9bb7e999f55cac59c9fb7d0a330f760
    }

    void build_isa() { // hash-cpp-5
        isa.resize(n+1);
        for (int i = 0; i <= n; i++) isa[sa[i]] = i;
    } // hash-cpp-5 = bcb546b2fc94176fc80672b20a808f7f

    template <class S> void build_lcp(const S& s) {
        assert(n == int(s.size()));
        lcp.resize(n+1); // hash-cpp-6
        for (int i = 0, k = 0; i < n-1; i++) {
            int r = isa[i]-1, j = sa[r];
            while (k < n - max(i, j) && s[i+k] == s[j+k]) k++;
            lcp[r] = k;
            if (k) k--;
        } // hash-cpp-6 = 85193c3617ced5f805117ffdf20255aa
    }
};

```

eertree.hpp**Description:** Palindrome tree. Call reset() to move back to the root

55 lines

```

// 0, ..., K-1
template <int sigma> struct Eertree {

```

```

struct Node { // hash-cpp-1
    array<int, sigma> ch;
    int fail;
    int l, r; // location of the first ocurrence
    Node(int f_, int l_, int r_) : ch{}, fail(f_), l(l_), r
        ↪(r_) {}
    int len() const { return r-l; }
};
V<Node> x;
V<int> buf;
int cur; // hash-cpp-1 = f5c073ef9f6cdf81ef2d56cb6d2e477
Eertree(int alloc = 0) {
    if (alloc) {
        x.reserve(alloc+2);
        buf.reserve(alloc);
    }
    x.emplace_back(-1, 1, 0);
    x.emplace_back(0, 0, 0);
    reset();
}

void reset() {
    cur = 1;
    buf.clear();
}

int append(int a) { // hash-cpp-2
    int i = int(buf.size());
    buf.push_back(a);
    auto works = [&](int v) -> bool {
        int l = i - x[v].len();
        return l > 0 && buf[l-1] == a;
    };
    for (; !works(cur); cur = x[cur].fail) {}
    if (!x[cur].ch[a]) {
        int par = x[cur].fail;
        if (par != -1) {
            for (; !works(par); par = x[par].fail) {}
        }
        int npar = (par == -1 ? 1 : x[par].ch[a]);
        x[cur].ch[a] = int(x.size());
        x.emplace_back(npar, i - x[cur].len() - 1, i + 1);
    }
    cur = x[cur].ch[a];
    return cur;
} // hash-cpp-2 = 15be9415acd9f07f11b20a59308379a0

int size() const {
    return int(x.size());
}
const Node& operator [] (int i) const {
    return x[i];
}
};

```

Geometry (8)

8.1 2D

base.hpp

Description: Primitive operations

83 lines

namespace geometry {

```

using D = double; // hash-cpp-1
const D EPS = D(1e-9);

```

```

inline int sgn(D a) { return (a > EPS) - (a < -EPS); }
inline int sgn(D a, D b) { return sgn(a - b); } // hash-cpp
↳-1 = eb6175a3f198588d18a518264d1eee5d

const D PI = acos(D(-1));

template <class T = D> struct Point {
    using P = Point; // hash-cpp-2
    T x, y;
    Point(T x_ = T(), T y_ = T()) : x(x_), y(y_) {} // hash-
↳cpp-2 = 6494c3c9bfac161e2c65d414a2c7bc83

P& operator += (const P& p) { x += p.x, y += p.y; return
↳*this; } // hash-cpp-3
P& operator -= (const P& p) { x -= p.x, y -= p.y; return
↳*this; }
friend P operator + (const P& a, const P& b) { return P(a
↳) += b; }
friend P operator - (const P& a, const P& b) { return P(a
↳) -= b; } // hash-cpp-3 = 32704
↳ee5f47251cb7a5a8bcd8b7996e3

P& operator *= (const T& t) { x *= t, y *= t; return *
↳this; } // hash-cpp-4
P& operator /= (const T& t) { x /= t, y /= t; return *
↳this; }
friend P operator * (const P& a, const T& t) { return P(a
↳) *= t; }
friend P operator / (const P& a, const T& t) { return P(a
↳) /= t; } // hash-cpp-4 = 56
↳a8dfabc9e0968b82d5006dda2d4d7e

friend D dot(const P& a, const P& b) { return a.x * b.x +
↳ a.y * b.y; }
friend D crs(const P& a, const P& b) { return a.x * b.y -
↳ a.y * b.x; }

P operator - () const { return P(-x, -y); }

friend int cmp(const P& a, const P& b) { // hash-cpp-5
    int z = sgn(a.x, b.x);
    return z ? z : sgn(a.y, b.y);
} // hash-cpp-5 = 1553bdfc52835908d4fc0bd0a91b7134

friend bool operator < (const P& a, const P& b) { return
↳cmp(a, b) < 0; }
friend bool operator <= (const P& a, const P& b) { return
↳cmp(a, b) <= 0; }

friend D dist2(const P& p) { return p.x * p.x + p.y * p.y
↳; }
friend auto dist(const P& p) { return sqrt(dist2(p)); }

friend P unit(const P& p) { return p / p.dist(); }

friend D arg(const P& p) { return atan2(p.y, p.x); }

friend D rabs(const P& p) { return max(std::abs(p.x), std
↳::abs(p.y)); }

friend bool operator == (const P& a, const P& b) { return
↳sgn(rabs(a - b)) == 0; }
friend bool operator != (const P& a, const P& b) { return
↳!(a == b); }

explicit operator pair<T, T> () const { return pair<T, T
↳>(x, y); }

```

```

static P polar(D m, D a) { return P(m * cos(a), m * sin(a
↳)); }

};
using P = Point<D>;

inline int sgnrcs(const P& a, const P& b) { // hash-cpp-6
    D cr = crs(a, b);
    if (std::abs(cr) <= (rabs(a) + rabs(b)) * EPS) return 0;
    return (cr < 0 ? -1 : 1);
} // hash-cpp-6 = 715f69675680678da17cc8e5d7d2e1f2

// not tested
inline D norm_angle(D a) { // hash-cpp-7
    D res = fmod(a + PI, 2*PI);
    if (res < 0) res += PI;
    else res -= PI;
    return res;
} // hash-cpp-7 = af057ce01a3fcc8e1b04c1504548eb73

// not tested
inline D norm_nonnegative(D a) { // hash-cpp-8
    D res = fmod(a, 2*PI);
    if (res < 0) res += 2*PI;
    return res;
} // hash-cpp-8 = b899a21e5dbdcde83a81a840e5f9e328

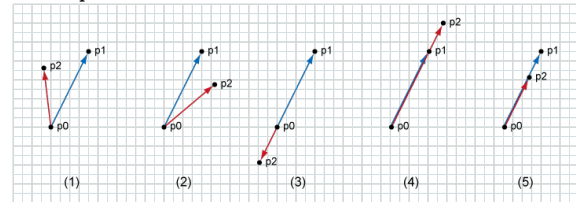
// arg given lengths a, b, c,
// assuming a, b, c are valid
inline D arg(D a, D b, D c) { // hash-cpp-9
    return acos(clamp<D>((a * a + b * b - c * c) / (2 * a * b
↳), -1, 1));
} // hash-cpp-9 = 446a9f9aff310fdad6bafc632c7b5c3c

} // namespace geometry

```

ccw.hpp

Description:



```

"geometry/base.hpp"
22 lines

namespace geometry {

// CGL_1_C
// 1: COUNTER_CLOCKWISE (1)
// -1: CLOCKWISE (2)
// 2: ONLINE_BACK (3)
// -2: ONLINE_FRONT (4)
// 0: ON_SEGMENT (5)
inline int ccw(const P& a, const P& b) { // hash-cpp-1
    int s = sgnrcs(a, b);
    if (s) return s;
    if (!sgn(rabs(b)) || !sgn(rabs(b-a))) return 0;
    if (dot(a, b) < 0) return 2;
    if (dot(-a, b-a) < 0) return -2;
    return 0;
} // hash-cpp-1 = fdf5d91850a67e77c2432a6c81e836eb

inline int ccw(const P& a, const P& b, const P& c) {
    return ccw(b-a, c-a);
}

```

```

}

} // namespace geometry

linear.hpp
Description: Line/segment operations
"geometry/ccw.hpp"
76 lines

namespace geometry {

// Work in progress
struct L { // hash-cpp-1
    P s, t;
    L(P s_ = P(), P t_ = P()) : s(s_), t(t_) {}
    friend P vec(const L& l) { return l.t - l.s; }
    friend auto dist(const L& l) { return dist(vec(l)); }
    friend D arg(const L& l) { return arg(vec(l)); }
}; // hash-cpp-1 = 87c781f4f81ba18dc33d97a7d3de1743

inline P project(const L& l, const P& p) { // hash-cpp-2
    P v = vec(l);
    return l.s + v * dot(v, p - l.s) / dist2(v);
} // hash-cpp-2 = 6c1b8640934518c28805ff8abd24ab79

inline int ccw(const L& l, const P& p) { return ccw(l.s, l.
↳t, p); }

inline bool insSL(const L& s, const L& l) { // hash-cpp-3
    int a = ccw(l, s.s), b = ccw(l, s.t);
    return (a % 2 == 0 || b % 2 == 0 || a != b);
} // hash-cpp-3 = f4cae3c1b1b14b35890348251586bbcc

inline bool insSS(const L& s, const L& t) { // hash-cpp-4
    int a = ccw(s, t.s), b = ccw(s, t.t),
    c = ccw(t, s.s), d = ccw(t, s.t);
    return (a * b <= 0 && c * d <= 0);
} // hash-cpp-4 = a8ed5652fe62541c10c7ea4b729906c4

inline D distLP(const L& l, const P& p) { // hash-cpp-5
    return std::abs(crs(vec(l), p - l.s)) / dist(l);
} // hash-cpp-5 = ec21f2c9fcb170c0b65c7118172e6767

inline D distSP(const L& s, const P& p) { // hash-cpp-6
    P q = project(s, p);
    if (ccw(s, q) == 0) {
        return dist(p - q);
    } else {
        return min(dist(s.s - p), dist(s.t - p));
    }
} // hash-cpp-6 = 1606015a080bef59202968db31b60baa

inline D distSS(const L& s, const L& t) { // hash-cpp-7
    if (insSS(s, t)) return 0;
    return min({
        distSP(s, t.s), distSP(s, t.t), distSP(t, s.s), distSP(
↳t, s.t)
    });
} // hash-cpp-7 = 7213f72dd7063b6226348e3eb1c0dbcc

// TODO: usage
inline int crossLL(const L& l, const L& m, P& r) { // hash-
↳cpp-8
    P vl = vec(l), vm = vec(m);
    D crl = crs(vl, vm), cr2 = crs(vl, l.t - m.s);
    if (sgnrcs(vl, vm) == 0) {
        r = l.s;
        if (sgnrcs(vec(l), l.t - m.s)) return 0;
        return -1;
    }
}

```



```

    }
    r = m.s + vm * cr2 / cr1;
    return 1;
} // hash-cpp-8 = 8518d588ab977248305ed2ff949b418f

// TODO usage
inline int crossSS(const L& l, const L& m, P& r) { // hash-
    ↪cpp-9
    int u = crossLL(l, m, r);
    if (u == 0) return 0;
    if (u == -1) {
        r = max(min(l.s, l.t), min(m.s, m.t));
        P q = min(max(l.s, l.t), max(m.s, m.t));
        return (q < r) ? 0 : (q == r ? 1 : -1);
    }
    if (ccw(l, r) == 0 && ccw(m, r) == 0) return 1;
    return 0;
} // hash-cpp-9 = 57a9b2ceb12937b59727715a7da092c9

} // namespace geometry

```

polygonal.hpp

Description: Polygon operations

"geometry/ccw.hpp", "geometry/linear.hpp" 123 lines

```

namespace geometry {

inline D area2(const V<P>& pol) { // hash-cpp-1
    if (pol.empty()) return 0;
    D res = 0;
    P a = pol.back();
    for (P b : pol) {
        res += crs(a, b);
        a = b;
    }
    return res;
} // hash-cpp-1 = 33dcd4ec795f9208c687cb8f433c0f83

// (1:left) | (2:right) is inside between v[i] -- v[i + 1]
inline V<pair<P, int>> insPolL(const V<P>& pol, const L& l)
    ↪ {
    using Pi = pair<P, int>;
    V<Pi> v;
    P a, b = pol.back();
    for (auto c: pol) {
        a = b; b = c;
        P p;
        if (crossLL({a, b}, l, p) != 1) continue;
        int sa = ccw(l, a) % 2, sb = ccw(l, b) % 2;
        if (sa > sb) swap(sa, sb);
        if (sa != 1 && sb == 1) v.push_back({p, 1});
        if (sa == -1 && sb != -1) v.push_back({p, 2});
    }
    sort(v.begin(), v.end(), [&](Pi x, Pi y){
        auto vl = vec(l);
        return dot(vl, x.first - l.s) < dot(vl, y.first - l.s);
    });
    int m = int(v.size());
    V<Pi> res;
    for (int i = 0; i < m; i++) {
        if (i) v[i].second ^= v[i - 1].second;
        if (!res.empty() && res.back().first == v[i].first) res
            ↪.pop_back();
        res.push_back(v[i]);
    }
    return res;
}

```

```

// 0: outside, 1: on line, 2: inside
inline int contains(const V<P>& pol, const P& p) { // hash-
    ↪cpp-2
    if (!pol.size()) return 0;
    int in = -1;
    P a_, b_ = pol.back();
    for (auto c : pol) {
        a_ = b_, b_ = c;
        P a = a_, b = b_;
        if (ccw(a, b, p) == 0) return 1;
        if (a.y > b.y) swap(a, b);
        if (!(a.y <= p.y && p.y < b.y)) continue;
        if (sgn(a.y, p.y) ? (crs(a - p, b - p) > 0) : (a.x > p.
            ↪x)) in *= -1;
    }
    return in + 1;
} // hash-cpp-2 = d882fa609311ea32e0272dfb7687c2a4

// pol: sorted and distinct
inline V<P> convex_lower(const V<P>& pts) { // hash-cpp-3
    assert(pts.size() >= 2);
    V<P> res;
    for (P d : pts) {
        while (res.size() > 1) {
            //if (ccw(res.end()[-2], res.end()[-1], d) != -1)
                ↪break;
            if (ccw(res.end()[-2], res.end()[-1], d) == 1) break;
            res.pop_back();
        }
        res.push_back(d);
    }
    return res;
} // hash-cpp-3 = 29c9b3dace98447e753933bbbf3e5763

inline V<P> convex(V<P> pts) { // hash-cpp-4
    sort(pts.begin(), pts.end());
    pts.erase(unique(pts.begin(), pts.end()), pts.end());
    if (pts.size() <= 1) return pts;
    V<P> lo = convex_lower(pts);
    reverse(pts.begin(), pts.end());
    V<P> up = convex_lower(pts);
    lo.insert(lo.begin(), up.begin() + 1, up.end() - 1);
    return lo;
} // hash-cpp-4 = 0f6a15113e7873dcabbdf471463886c2

inline V<P> convex_cut(const V<P>& pol, const L& l) { //
    ↪hash-cpp-5
    if (pol.empty()) return {};
    V<P> q;
    P a, b = pol.back();
    for (auto c : pol) {
        a = b, b = c;
        if ((ccw(l, a) % 2) * (ccw(l, b) % 2) < 0) {
            P buf;
            crossLL(l, L(a, b), buf);
            q.push_back(buf);
        }
        if (ccw(l, b) != -1) q.push_back(b);
    }
    return q;
} // hash-cpp-5 = 78abfe09b6be0a372cc416265f50ab8e

// pol: convex
inline D diameter(const V<P>& pol) { // hash-cpp-6
    int n = int(pol.size());
    if (n == 2) return dist(pol[1] - pol[0]);
    int x = 0, y = 0;
    for (int i = 1; i < n; i++) {

```

```

        if (pol[i] < pol[x]) x = i;
        if (pol[y] < pol[i]) y = i;
    }
    D ans = 0;
    int sx = x, sy = y;
    while (sx != y || sy != x) {
        ans = max(ans, dist(pol[x] - pol[y]));
        int nx = (x + 1 < n) ? x + 1 : 0, ny = (y + 1 < n) ? y
            ↪+ 1 : 0;
        if (crs(pol[nx] - pol[x], pol[ny] - pol[y]) < 0) {
            x = nx;
        } else {
            y = ny;
        }
    }
    return ans;
} // hash-cpp-6 = eaebe0c1913a759ddff9fda7a63a058f

} // namespace geometry

```

circular.hpp

Description: Circle operations

"geometry/base.hpp", "geometry/linear.hpp" 96 lines

```

namespace geometry {

struct C {
    P c;
    D r;
    C(P c_ = P(), D r_ = D()) : c(c_), r(r_) {}

    friend P eval(const C& a, const D& angle) {
        return a.c + P::polar(a.r, angle);
    }
};

// NOT TESTED
// 0: outside; 1: on; 2: inside
inline int contains(const C& c, const P& p) { // hash-cpp-1
    return sgn(c.r - dist(p - c.c)) + 1;
} // hash-cpp-1 = ccabefbce6d3385cda996d3900448a5a

// 0-apart; 1-coincide;
// 2-a<b; 3-a<=b;
// 4-a>b; 5-a>=b;
// 6-a touches b; 7-a cross b
inline int insCC(const C& a, const C& b){ // hash-cpp-2
    D c = dist(a.c - b.c);
    if (sgn(c) == 0 && sgn(a.r, b.r) == 0) return 1;
    int d = sgn(c + a.r - b.r);
    if (d <= 0) return d+3;
    int e = sgn(c + b.r - a.r);
    if (e <= 0) return e+5;
    int f = sgn(c - a.r - b.r);
    if (f <= 0) return -f+6;
    return 0;
} // hash-cpp-2 = 2a53c987ff805b98279648263ce5ede1

inline C incircle(const P& a, const P& b, const P& c) { //
    ↪hash-cpp-3
    D da = dist(b - c);
    D db = dist(a - c);
    D dc = dist(a - b);
    D s = da + db + dc;
    return C(
        (a * da + b * db + c * dc) / s,
        std::abs(crs(b-a, c-a)) / s
    );
}

```



```

} // hash-cpp-3 = 16141c15a9d73bdab9db92783059d6e0

inline C outcircle(const P& a, P b, P c) { // hash-cpp-4
    b -= a, c -= a;
    D bb = dist2(b) / 2;
    D cc = dist2(c) / 2;
    D g = crs(b, c);
    D x = (bb * c.y - b.y * cc) / g;
    D y = (b.x * cc - bb * c.x) / g;
    D r = sqrt(x * x + y * y);
    x += a.x, y += a.y;
    return C(P(x, y), r);
} // hash-cpp-4 = d6b82a105b9f1236f464e5b79f797623

inline int crossCL(const C& c, const L& l, array<P, 2>& res
    ↪) { // hash-cpp-5
    D u = distLP(l, c.c);
    int t = sgn(u, c.r);
    if (t == 1) return 0;
    P v = project(l, c.c);
    P d = (t == 0 ? P(0, 0) : vec(l) * (sqrt(c.r * c.r - u *
        ↪u) / dist(l)));
    res = {v - d, v + d};
    return 1 - t;
} // hash-cpp-5 = 033bf3aca850b39d8c71d57d5423d700

// args of two intersections r, l seen by a.c,
// assuming two circles cross
inline pair<D, D> crossCC_args(const C& a, const C& b) { //
    ↪ hash-cpp-6
    P diff = b.c - a.c;
    D c = arg(diff);
    D d = arg(a.r, dist(diff), b.r);
    return {c - d, c + d};
} // hash-cpp-6 = f5d8208d16adc5736be6be6763db3c6e

inline int crossCC(const C& a, const C& b, array<P, 2>& res
    ↪) { // hash-cpp-7
    int t = insCC(a, b);
    if (t == 0 || t == 1 || t == 2 || t == 4) return 0;
    auto [l, r] = crossCC_args(a, b);
    res = {eval(a, l), eval(a, r)};
    return 2 - (t == 3 || t == 5 || t == 6);
} // hash-cpp-7 = 5e1c3c99c88d87a73b0fde2410a0b514

inline int tangent(const C& c, const P& p, array<P, 2>& res
    ↪) { // hash-cpp-8
    P diff = p - c.c;
    D dd = dist(diff);
    int t = sgn(c.r, dd);
    if (t == 1) return 0;
    D d = acos(min<D>(c.r / dd, 1));
    D a = arg(diff);
    res = {eval(c, a - d), eval(c, a + d)};
    return 1 - t;
} // hash-cpp-8 = 95201751eafe5e2b3c829248ef6b020b

} // namespace geometry

```

closest-pair.hpp

Description: Given a set of points, returns the squared distance between the closest pair(s)

Time: $\mathcal{O}(N \log^2 N)$ but practically fast

"geometry/base.hpp" 31 lines

```
namespace geometry {
```

```
inline D closest_pair(V<P> pts) { // hash-cpp-1
```

```

assert(pts.size() > 1);
sort(pts.begin(), pts.end(), [](const P& a, const P& b)
    ↪-> bool {
    return a.x < b.x;
});
D best = dist2(pts[0] - pts[1]);
yc([&](auto self, int l, int r) -> void {
    if (l+1 == r) return;
    int md = (l+r)/2;
    self(l, md), self(md, r);
    V<P> cnds;
    for (int i = l; i < r; i++) {
        D dx = (pts[i] - pts[md-1]).x;
        if (sgn(dx * dx, best) <= 0) cnds.push_back(pts[i]);
    }
    sort(cnds.begin(), cnds.end(), [](const P& a, const P&
        ↪b) -> bool {
        return a.y < b.y;
    });
    int nc = int(cnds.size());
    for (int i = 0; i < nc; i++) {
        for (int j = i+1; j < i+7 && j < nc; j++) {
            best = min(best, dist2(cnds[i] - cnds[j]));
        }
    }
    return best;
}) (0, int(pts.size()));
} // hash-cpp-1 = 1a5bf1bc99163c021c24ffe0faef418c

} // namespace geometry

```

Appendix (9)

techniques.txt	159 lines	
Recursion		Combinatorics
Divide and conquer		Computation of binomial coefficients
Finding interesting points in N log N		Pigeon-hole principle
Algorithm analysis		Inclusion/exclusion
Master theorem		Catalan number
Amortized time complexity		Pick's theorem
Greedy algorithm		Number theory
Scheduling		Integer parts
Max contiguous subvector sum		Divisibility
Invariants		Euclidean algorithm
Huffman encoding		Modular arithmetic
Graph theory		* Modular multiplication
Dynamic graphs (extra book-keeping)		* Modular inverses
Breadth first search		* Modular exponentiation by squaring
Depth first search		Chinese remainder theorem
* Normal trees / DFS trees		Fermat's little theorem
Dijkstra's algorithm		Euler's theorem
MST: Prim's algorithm		Phi function
Bellman-Ford		Frobenius number
Konig's theorem and vertex cover		Quadratic reciprocity
Min-cost max flow		Pollard-Rho
Lovasz toggle		Miller-Rabin
Matrix tree theorem		Hensel lifting
Maximal matching, general graphs		Vieta root jumping
Hopcroft-Karp		Game theory
Hall's marriage theorem		Combinatorial games
Graphical sequences		Game trees
Floyd-Warshall		Mini-max
Euler cycles		Nim
Flow networks		Games on graphs
* Augmenting paths		Games on graphs with loops
* Edmonds-Karp		Grundy numbers
Bipartite matching		Bipartite games without repetition
Min. path cover		General games without repetition
Topological sorting		Alpha-beta pruning
Strongly connected components		Probability theory
2-SAT		Optimization
Cut vertices, cut-edges and biconnected components		Binary search
Edge coloring		Ternary search
* Trees		Unimodality and convex functions
Vertex coloring		Binary search on derivative
* Bipartite graphs (=> trees)		Numerical methods
* 3^n (special case of set cover)		Numeric integration
Diameter and centroid		Newton's method
K'th shortest path		Root-finding with binary/ternary search
Shortest cycle		Golden section search
Dynamic programming		Matrices
Knapsack		Gaussian elimination
Coin change		Exponentiation by squaring
Longest common subsequence		Sorting
Longest increasing subsequence		Radix sort
Number of paths in a dag		Geometry
Shortest path in a dag		Coordinates and vectors
Dynprog over intervals		* Cross product
Dynprog over subsets		* Scalar product
Dynprog over probabilities		Convex hull
Dynprog over trees		Polygon cut
3^n set cover		Closest pair
Divide and conquer		Coordinate-compression
Knuth optimization		Quadrees
Convex hull optimizations		KD-trees
RMQ (sparse table a.k.a 2^k-jumps)		All segment-segment intersection
Bitonic cycle		Sweeping
Log partitioning (loop over most restricted)		Discretization (convert to events and sweep)
		Angle sweeping
		Line sweeping
		Discrete second derivatives
		Strings
		Longest common substring
		Palindrome subsequences
		Knuth-Morris-Pratt
		Tries
		Rolling polynomial hashes
		Suffix array
		Suffix tree
		Aho-Corasick
		Manacher's algorithm
		Letter position lists
		Combinatorial search
		Meet in the middle
		Brute-force with pruning
		Best-first (A*)
		Bidirectional search
		Iterative deepening DFS / A*
		Data structures
		LCA (2^k-jumps in trees in general)
		Pull/push-technique on trees
		Heavy-light decomposition
		Centroid decomposition
		Lazy propagation
		Self-balancing trees
		Convex hull trick (wcipeg.com/wiki/Convex_hull_trick)
		Monotone queues / monotone stacks / sliding queues
		Sliding queue using 2 stacks
		Persistent segment tree