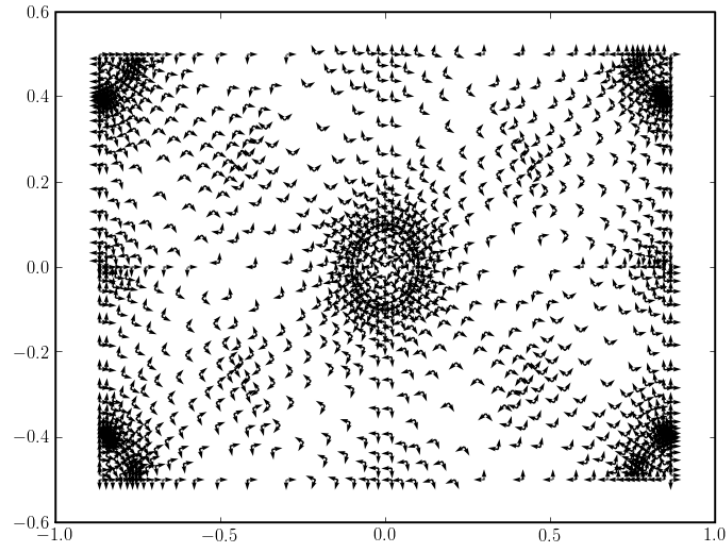


1 Micro-problem Coefficients

- anisotropic permeability K_{ij} :



1.1 Matrix

- D_{ijkl} : $\begin{bmatrix} 2.3 & 1.7 & 0. \\ & 1.7 & 2.3 & 0. \\ & & 0. & 0. & 0.3 \end{bmatrix}$
- μ : $[3.8]$
- μ^{-1} : $[0.26315789]$
- α_{ij} : $[0.132 \ 0.132 \ 0.092]$
- K_{ij} : $\begin{bmatrix} 0.01 & 0. \\ & 0. & 0.001 \end{bmatrix}$
 $\begin{bmatrix} 0.00101438 & -0.00035942 \\ & -0.00035942 & 0.00998562 \end{bmatrix}$
 $\dots, \begin{bmatrix} 0.00521131 & -0.00449073 \\ & -0.00449073 & 0.00578869 \end{bmatrix}$
 $\begin{bmatrix} 0.00265013 & -0.00348257 \\ & -0.00348257 & 0.00834987 \end{bmatrix}$

1.2 Channels

- D_{ijkl} : $\begin{bmatrix} 0.23 & 0.17 & 0. \\ & 0.17 & 0.23 & 0. \\ & & 0. & 0. & 0.03 \end{bmatrix}$
- μ : $[100.]$
- μ^{-1} : $[0.01]$
- α_{ij} : $[1. \ 1. \ 0.]$
- K_{ij} : $\begin{bmatrix} 1. & 0. \\ & 0. & 1. \end{bmatrix}$

2 Homogenized Coefficients

2.1 Steady coefficients

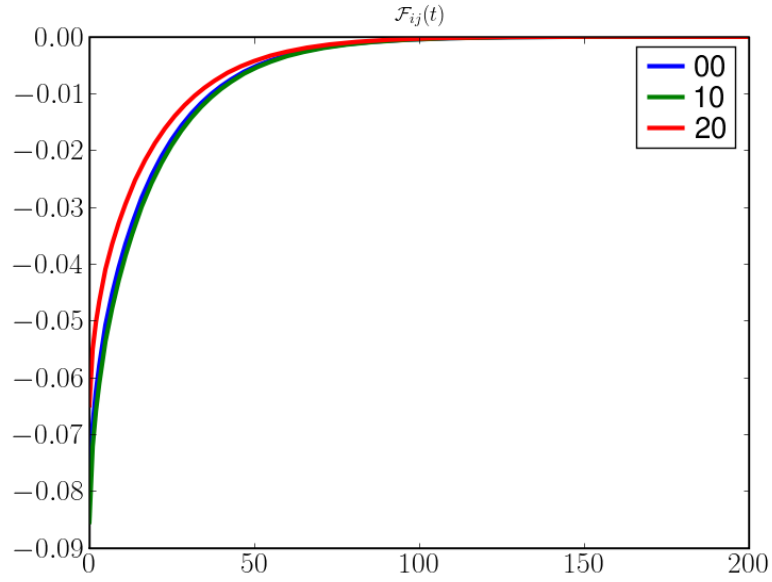
- E_{ijkl} : $[[[1.87440989e+00 \ 1.30524837e+00 \ -4.35442578e-05] [1.30524837e+00 \ 1.87431828e+00 \ -6.43057823e-06] [-4.35442578e-05 \ -6.43057823e-06 \ 2.84664158e-01]]$
- C_{ij} : $[[[1.34964528e-01 \ 1.43188517e-06] [1.43188517e-06 \ 1.34881785e-01]]$
- \mathcal{B}_{ij} : $[[1.132376 \ 1.13241074 \ 0.07930384]$
- \mathcal{M} : $[[0.45529815]$
- volume fractions: 'Yc': $\text{array}(0.14722441652250456)$, 'Ym': $\text{array}(0.85277558347749483)$
- volumeYm: 1.47700731058
- volumeYc: 0.254992689417
- volumeY: 1.732

2.2 Time-dependent coefficients at $t = 0+$

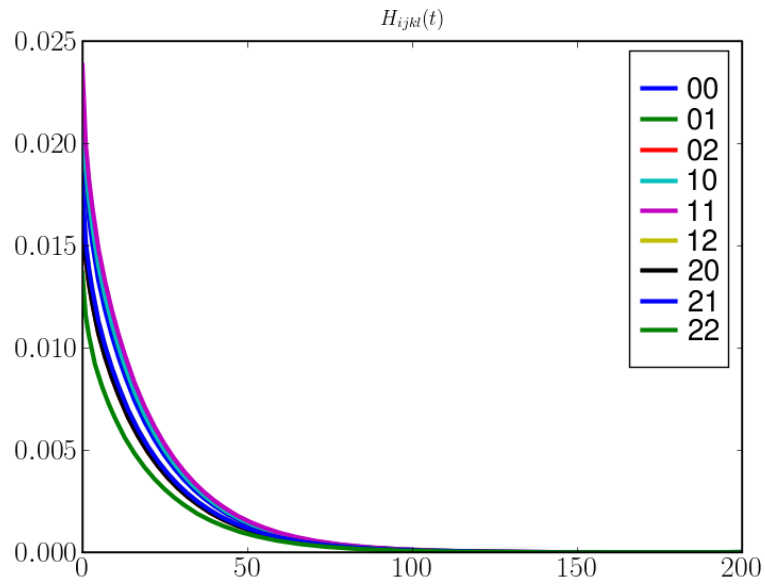
- $\mathcal{F}_{ij}(0+)$: $[-0.07244143 \ -0.07245437 \ -0.06301977]$
- $H_{ijkl}(0+)$: $[[[0.0185935 \ 0.01851298 \ 0.01605949] [0.01851298 \ 0.01851896 \ 0.01605837] [0.01605949 \ 0.01605837 \ 0.01398949]]$
- $\mathcal{G}(0+)$: $[[1.4329674]$

2.3 Time-dependent coefficients

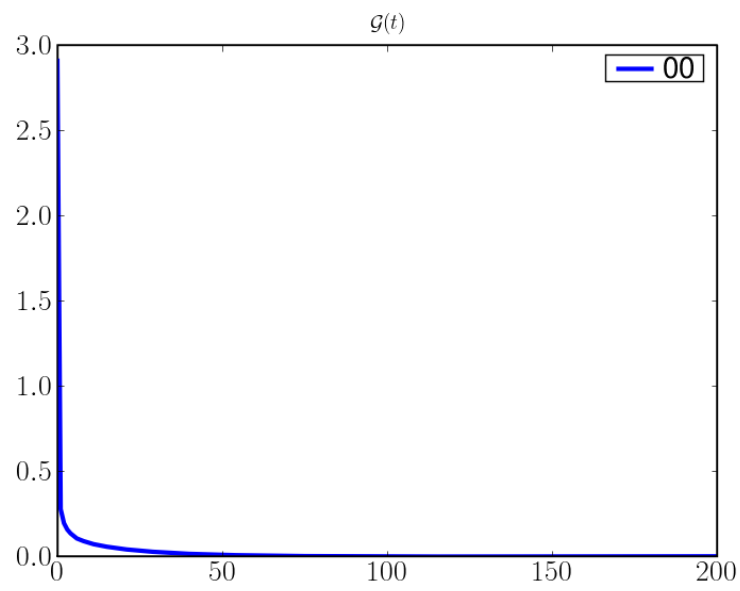
- $\mathcal{F}_{ij}(t)$



- $H_{ijkl}(t)$



- $\mathcal{G}(t)$

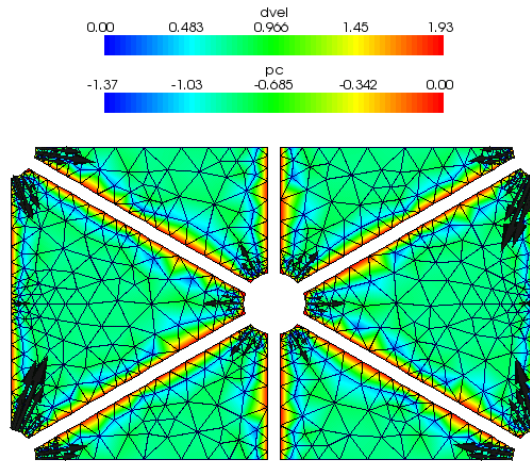


3 Correctors

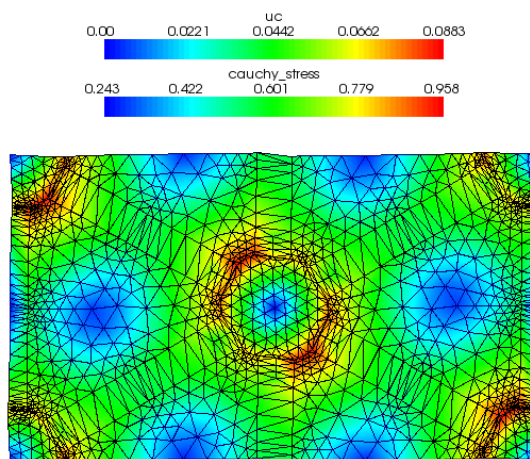
- pressure-like correctors: color = pressure, arrows = perfusion velocities (possibly scaled)
- displacements-like correctors: color = displacement, warped (possibly scaled), `cauchy_stress` colorbar only to see stress ranges

3.1 Steady-state pressure correctors

- pressure ... $\tilde{\pi}^P(0+)$, perfusion velocities
scaling: $1.55\text{e-}01\times$

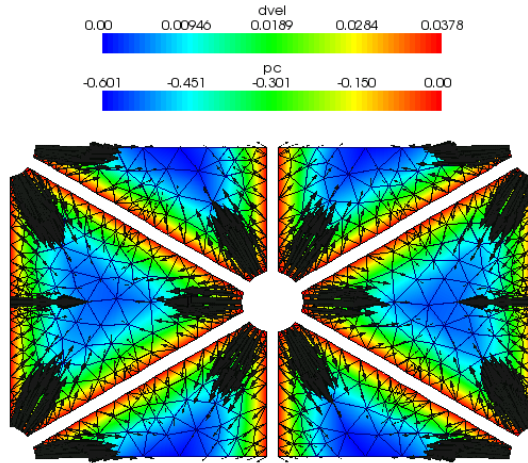


- displacements ... $\omega^{*,P}$
scaling: $1.00\text{e+}00\times$

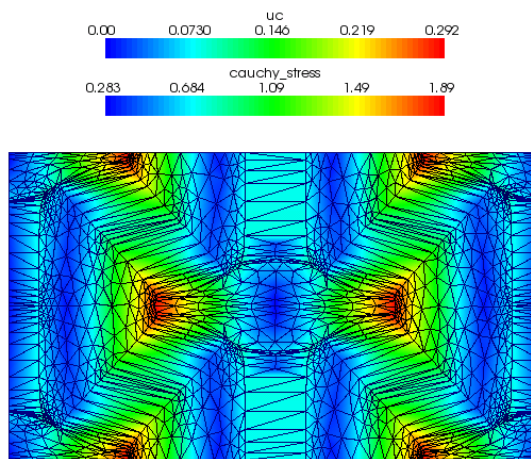


3.2 Steady-state RS correctors

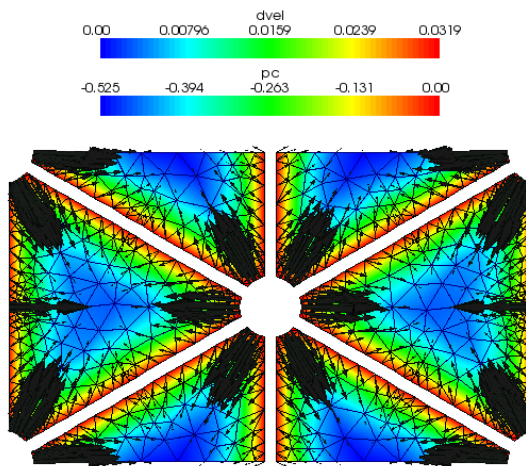
- pressure $\dots \bar{\pi}^{11}$, perfusion velocities
scaling: $7.93\text{e}+00\times$



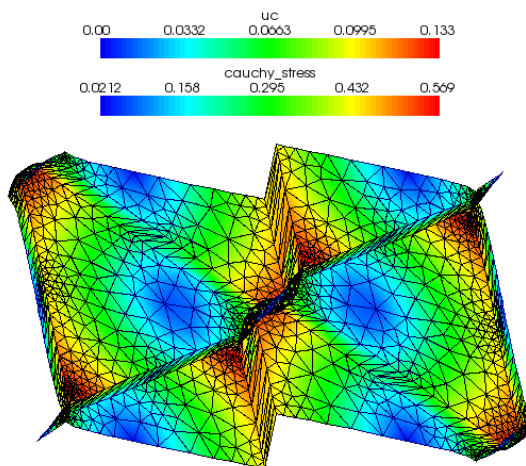
- displacements $\dots \bar{\omega}^{11}$
scaling: $1.00\text{e}+00\times$



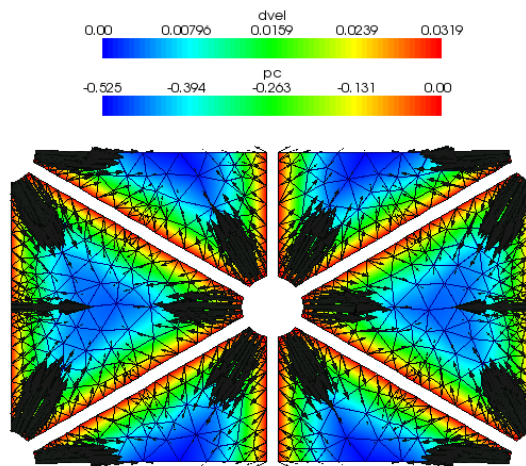
- pressure ... $\bar{\pi}^{12}$, perfusion velocities
scaling: $9.42\text{e}+00\times$



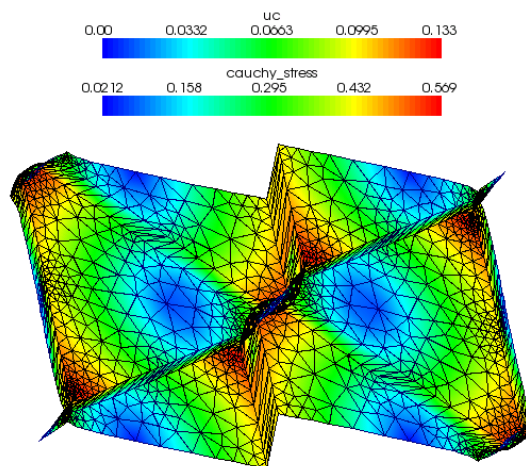
- displacements ... $\bar{\omega}^{12}$
scaling: $1.00\text{e}+00\times$



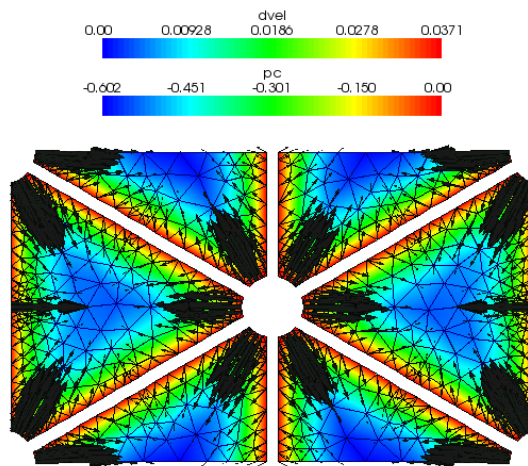
- pressure ... $\bar{\pi}^{21}$, perfusion velocities
scaling: $9.42\text{e}+00\times$



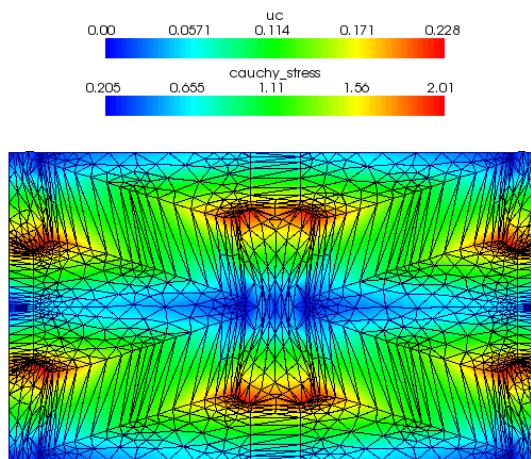
- displacements ... $\bar{\omega}^{21}$
scaling: $1.00\text{e}+00\times$



- pressure ... $\bar{\pi}^{22}$, perfusion velocities
scaling: $8.08\text{e}+00\times$

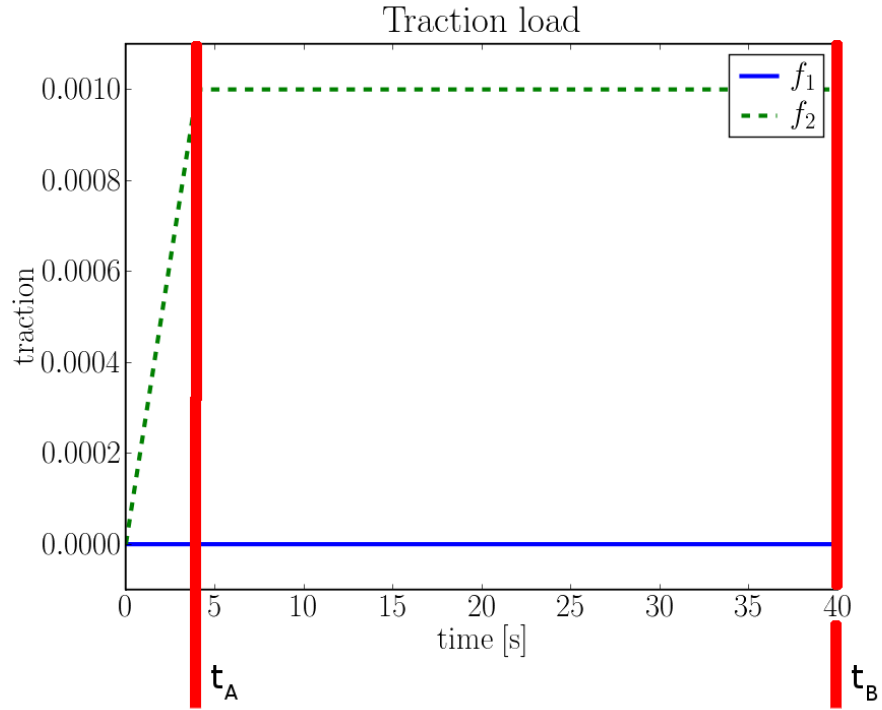


- displacements ... $\bar{\omega}^{22}$
scaling: $1.00\text{e}+00\times$



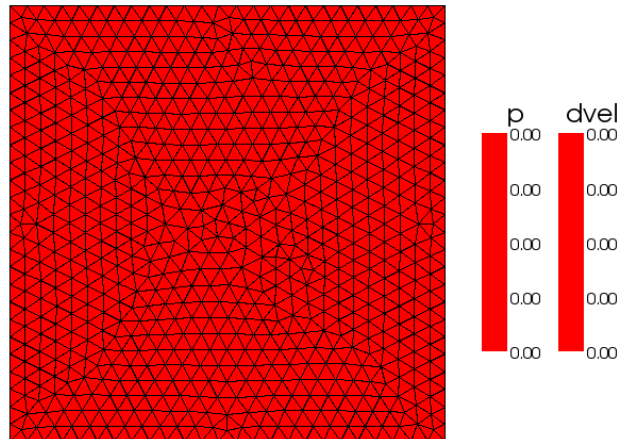
4 Macroscopic Solution

The structure is fixed on its left side and loaded by traction in y direction on the right side boundary:

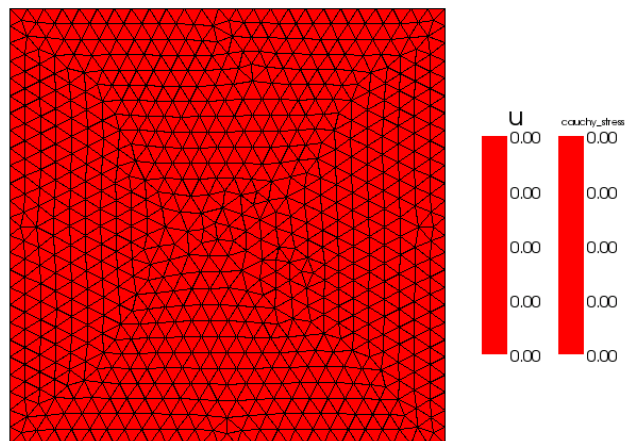


4.1 Bones macro-problem

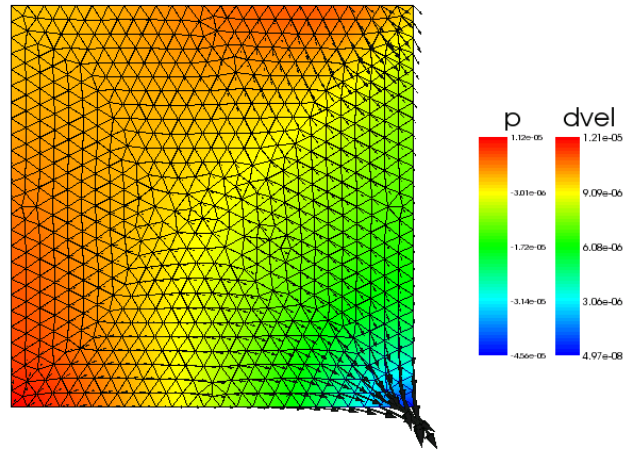
- step 0: pressure $\dots p$, perfusion velocities
scaling: $\text{inf}\times$



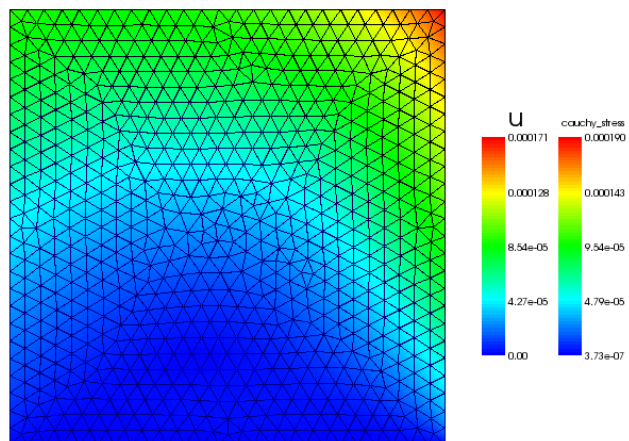
- step 0: displacements $\dots u$
scaling: $1.00\text{e}+01\times$



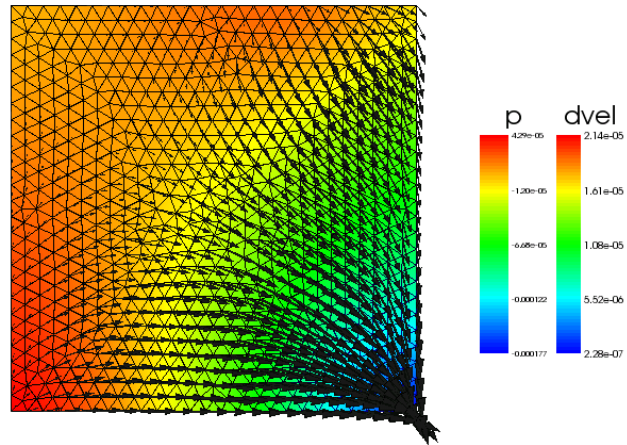
- step 1: pressure $\dots p$, perfusion velocities
scaling: $2.48\text{e}+04\times$



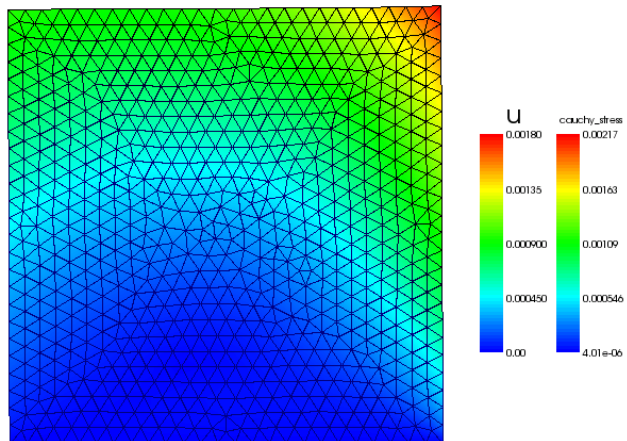
- step 1: displacements $\dots u$
scaling: $1.00\text{e}+01\times$



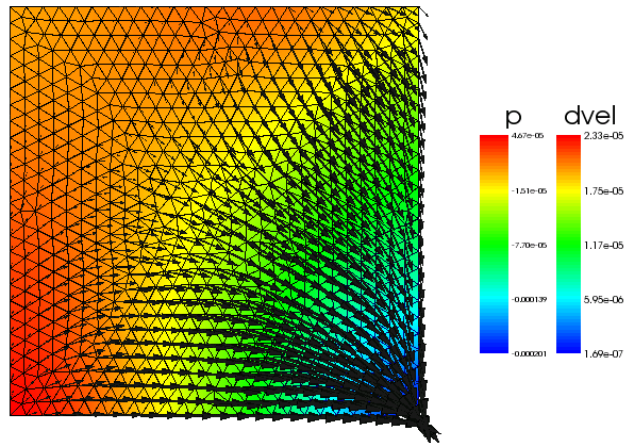
- step 10: pressure ... p , perfusion velocities
scaling: $1.40\text{e}+04\times$



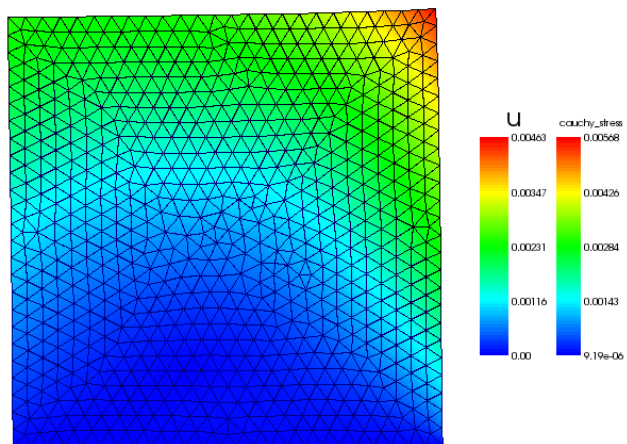
- step 10: displacements ... u
scaling: $1.00\text{e}+01\times$



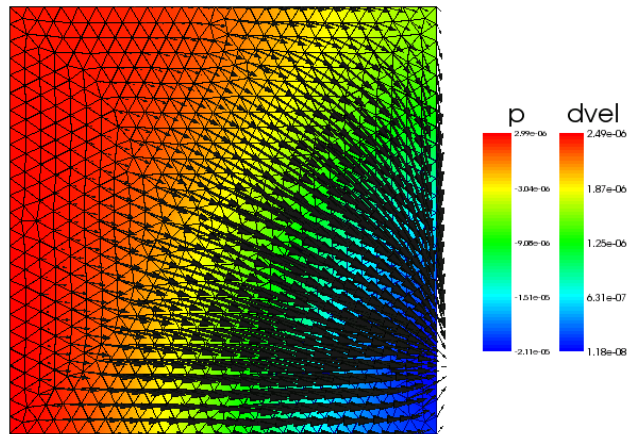
- step 25: pressure ... p , perfusion velocities
scaling: $1.29\text{e}+04\times$



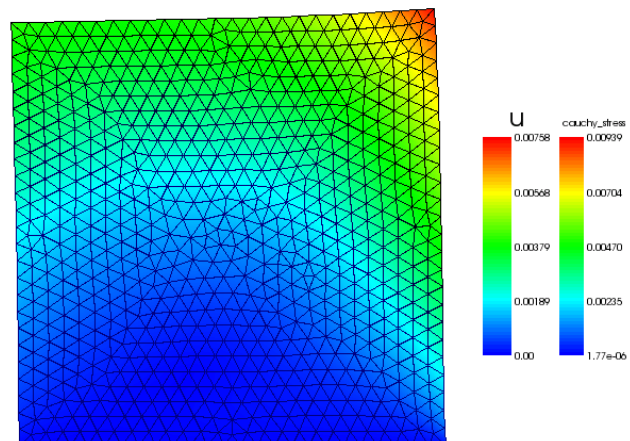
- step 25: displacements ... u
scaling: $1.00\text{e}+01\times$



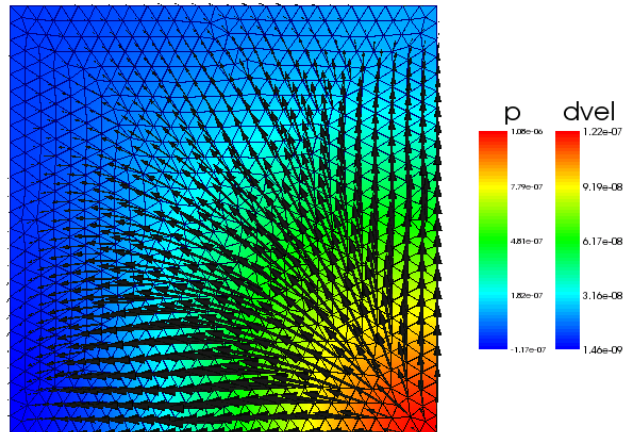
- step 50: pressure ... p , perfusion velocities
scaling: $1.21\text{e}+05\times$



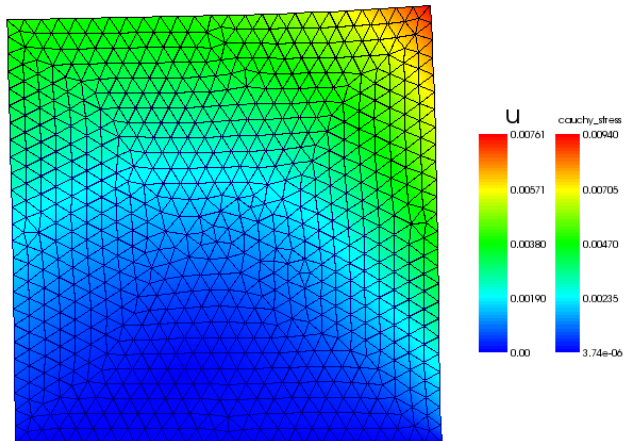
- step 50: displacements ... u
scaling: $1.00\text{e}+01\times$



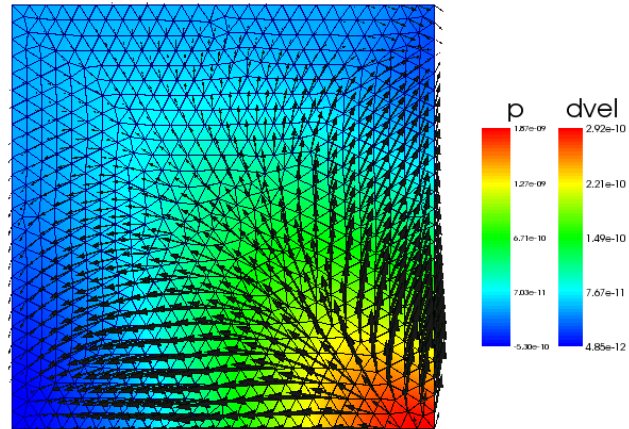
- step 100: pressure ... p , perfusion velocities
scaling: $2.46\text{e}+06\times$



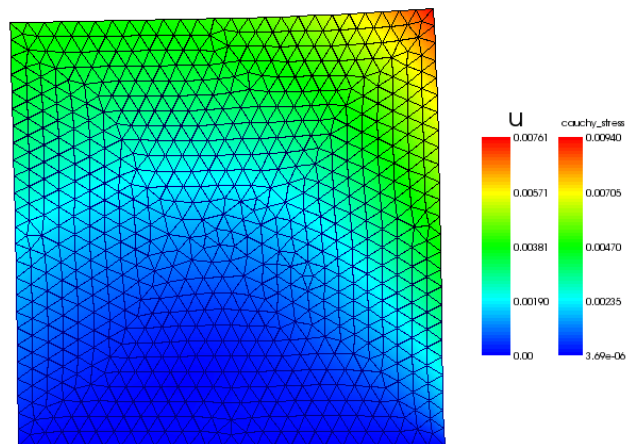
- step 100: displacements ... u
scaling: $1.00\text{e}+01\times$



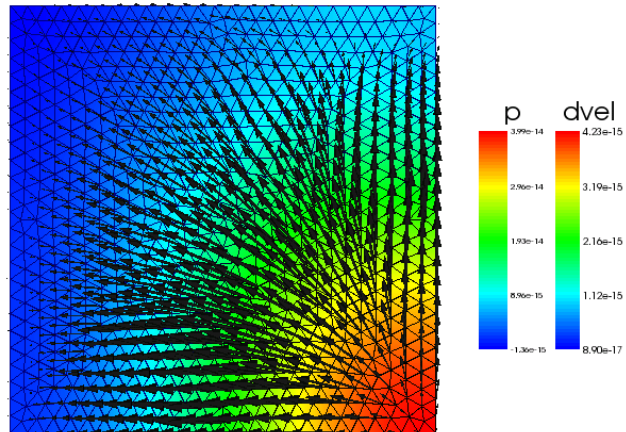
- step 200: pressure ... p , perfusion velocities
scaling: $1.03\text{e}+09\times$



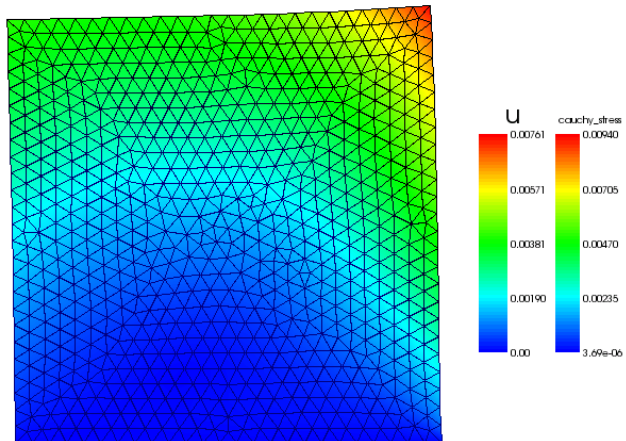
- step 200: displacements ... u
scaling: $1.00\text{e}+01\times$



- step 400: pressure ... p , perfusion velocities
scaling: $7.10\text{e}+13\times$

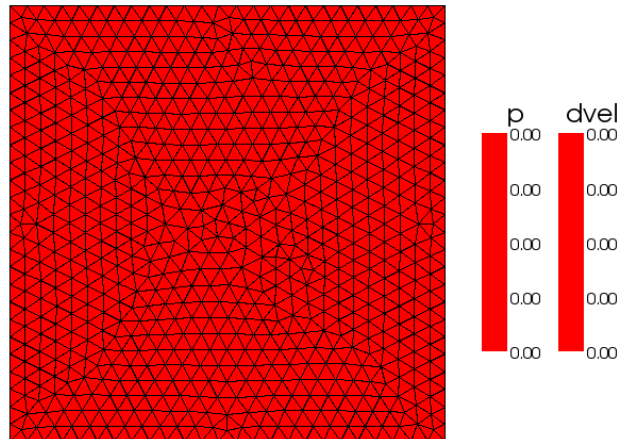


- step 400: displacements ... u
scaling: $1.00\text{e}+01\times$



4.2 Steady-state solution of bones macro-problem

- pressure ... p , perfusion velocities
scaling: $\text{inf}\times$



- displacements ... u
scaling: $1.00\text{e}+01\times$

