

Example Quarto Site for R

Paul Villanueva

8/13/2021

Contents

1	Introduction	4
1.1	Installing Quarto	4
1.2	About this site	4
2	A qmd with R and Python	6
3	Let's make a table	7
4	Example images	8
5	Code and chunk options	10
5.1	Math stuff	13
5.2	Adding references	14
5.3	Cross-references	15
6	Bibliography	16
7	A qmd with only Python	17
7.1	Adding days per month from date range to a dataframe	17
7.1.1	Helper functions	18
7.2	Interactive Widgets	18
7.3	IPyLeaflet	19
7.4	Plotly	19
7.5	Learning more	19
8	A Jupyter Notebook	20
9	DNA String Manipulation	22
10	Sample Analysis	25
10.0.1	Data	25
10.1	Removing amoAs	26
10.2	Ordination	29
10.3	Arrows!	32
10.4	Statistics	34
10.4.1	Which factors have an impact on overall community composition? . . .	34

10.4.2	How do the treatment factors affect the “abundance” of genes on an individual level?	35
10.5	Biodiversity	37
10.6	Reading in the best BLAST hit info:	38
10.7	Creating a phyloseq object	39
10.8	Richness analysis	39
10.9	Statistical tests	42
10.9.1	Significance test of fertilization level on richness.	42
10.9.2	Significance test of fertilization level on richness	42
10.10	Making nice plots for stat differences	42
10.11	Beta diversity	44
10.12	Composition	47
10.13	Statistics on a best BLAST hit level	50

1 Introduction

This is an example Quarto project made for the Reproducible Research with R workshop at the R/Medicine conference on 8/25/2021.

1.1 Installing Quarto

In order to work with Quarto from your own computer, you'll need to install the Quarto CLI and a daily build of RStudio.

- You can download the latest version of the Quarto CLI from the [Quarto github](#). Select the appropriate version for your OS and run the installer.
- You can download a daily build of RStudio [here](#). The daily build has support for Quarto documents that isn't in the official release yet.

From here, you'll be able to render Quarto documents in RStudio just like you've been doing today.

For full installation instructions, see [the Quarto docs](#).

1.2 About this site

This is a Quarto book project. You're able to download the entire site as a single document by clicking the download button in the upper right hand corner.

A Quarto project is a collection of documents (`qmd`, `md`, `Rmd`, and `ipynb` files) that are unified by a `_quarto.yml` file. This `_quarto.yml` file contains, among other things (from the docs):

- A way to render all or some of the files in a directory with a single command (e.g. `quarto render myproject`).
- A way to share YAML configuration across multiple documents.
- The ability to redirect output artifacts to another directory.
- The ability to freeze rendered output (i.e. don't re-execute documents unless they have changed).

You can see the `_quarto.yml` for this site [here](#).

To learn more about Quarto projects, see the [Projects section](#) of the docs.

2 A qmd with R and Python

This is an example Quarto document. Note the `qmd` extension - this tells Quarto that this is a Markdown files that contains computations.

Since Quarto based on Markdown, we can **bold** and *italicize* text. We can also make headers.

3 Let's make a table

Meal	Food
Breakfast	Coffee
Lunch	Leftovers
Dinner	Spam Musubi

4 Example images

Quarto supports an easy to use syntax for arranging figures on a page. For example, this code:

```
:::{layout="[[1], [1, 1]]"}
! [Breakfast: Coffee] (images/vic.jpg "Breakfast: Vietnamese iced coffee")

! [Lunch: Leftovers] (images/leftovers.jpg "Leftovers fried rice? Fried rice leftovers? Leftovers")

! [Dinner: Spam musubi] (images/spam_musubi.jpg "Oh mama we eating good tonight") {width="400"}
:::
```

... will render as:

Read the [Custom Layouts](#) section in the Quarto docs for more info.



Figure 4.1: Breakfast: Coffee



Figure 4.2: Lunch: Leftovers



Figure 4.3: Dinner: Spam musubi

5 Code and chunk options

Quarto is based on **R**Markdown, so you can do all the R stuff you're used to as well.

```
library(tidyverse)

standard_curves <- readxl::read_xlsx('data/std_curve.xlsx', sheet = "everything") %>%
  janitor::clean_names() %>%
  filter(amo_a < 40)

lm_eqn = function(df){
  m = lm(log_qty ~ ct, df);
  data.frame(
    a = format(as.numeric(coef(m)[1]), digits = 2),
    b = format(as.numeric(coef(m)[2]), digits = 2),
    r2 = format(summary(m)$r.squared, digits = 3)
  )
}

st_splits <- standard_curves %>%
  group_by(amo_a, run) %>%
  group_split()

eqs <- st_splits %>%
  lapply(., lm_eqn) %>%
  bind_rows()

labels <- lapply(st_splits, slice_head, n = 1) %>%
  bind_rows() %>%
  select(amo_a, run) %>%
  bind_cols(eqs) %>%
  mutate(amo_a = paste0("amoA_AOB_p", amo_a)) %>%
  mutate(eq_label = paste0("y = ", a, " - ", abs(as.numeric(b)), "x<br>r^2 = ", r2))

standard_curves %>%
  mutate(amo_a = paste0("amoA_AOB_p", amo_a)) %>%
```

```

ggplot(aes(log_qty, ct)) +
  geom_point() +
  facet_grid(run ~ amoa, scales = "free") +
  theme(
    panel.border = element_rect(color = "black", size = 1, fill = NA),
    panel.grid.minor.x = element_blank(),
    panel.grid.minor.y = element_blank(),
    panel.grid.major.x = element_line(color = "gray", size = 0.5, linetype = "dashed"),
    panel.grid.major.y = element_line(color = "gray", size = 0.5, linetype = "dashed"),
    panel.spacing = unit(0.5, "lines"),
    panel.background = element_blank(),
    strip.background = element_rect(color = "black", size = 1, fill = NA),
  ) +
  labs(
    x = "Log(gene copies per reaction)",
    y = "Ct"
  ) +
  scale_x_continuous(limits = c(0, 7), breaks = seq(0, 7, 1), expand = c(0, 0)) +
  scale_y_continuous(limits = c(0, 25)) +
  geom_smooth(aes(group=1), method="lm", se=FALSE) +
  ggtext::geom_richtext(data = labels, aes(x = 3, y = 5, label = eq_label),
    size = 4, fontface = "bold", inherit.aes = FALSE)

```

We can also throw some Python in here:

```

xs = [x for x in range(10)]

print(*(f'{x} squared is {x ^ 2}.' for x in xs), sep='\n')

```

```

0 squared is 2.
1 squared is 3.
2 squared is 0.
3 squared is 1.
4 squared is 6.
5 squared is 7.
6 squared is 4.
7 squared is 5.
8 squared is 10.
9 squared is 11.

```

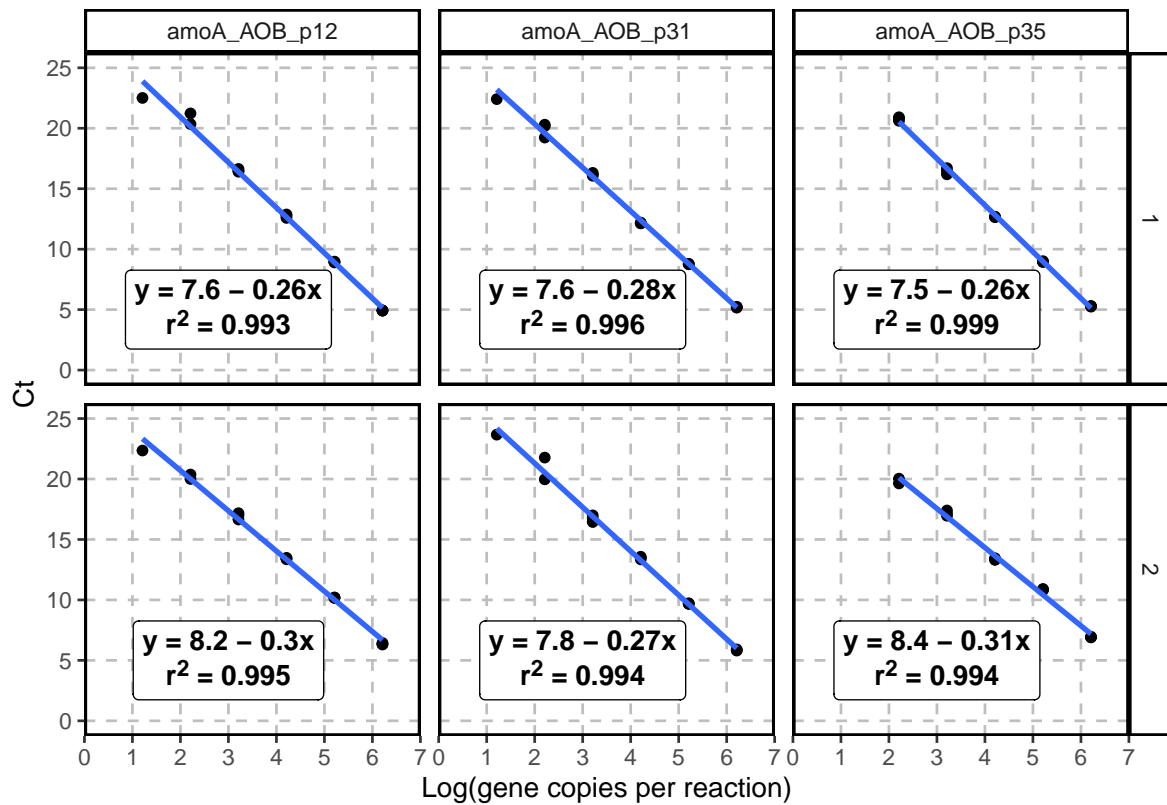


Figure 5.1: Standard curves for the LAMPS crop priming experiment

```
import matplotlib.pyplot as plt
import numpy as np

Z = np.random.rand(6, 10)
x = [x + 0.5 for x in xs]
y = np.arange(4.5, 11, 1)

fig, ax = plt.subplots();
ax.pcolormesh(x, y, Z)
```

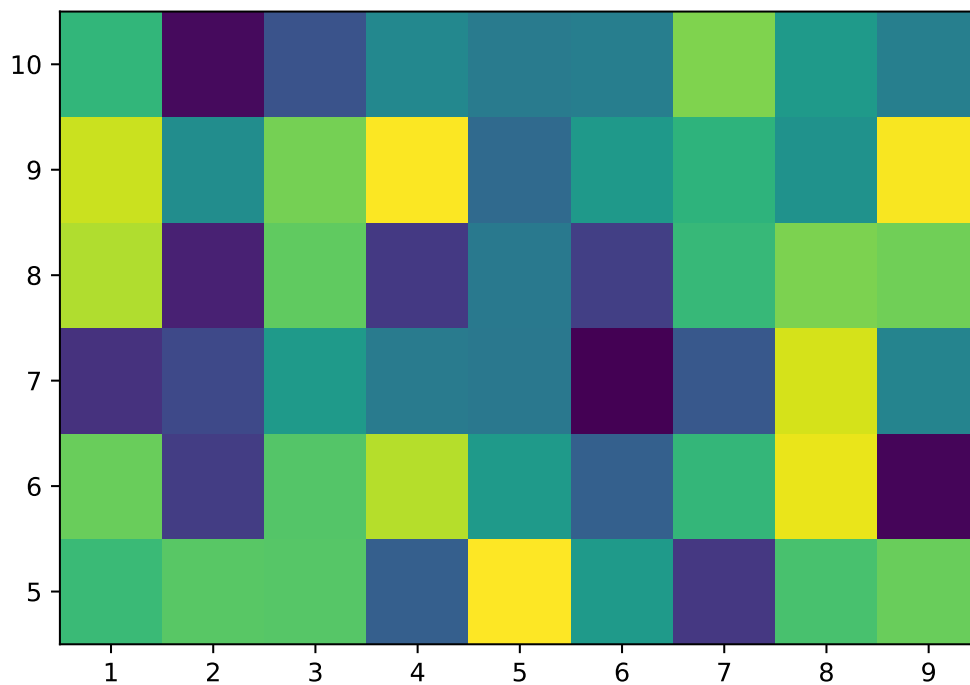


Figure 5.2: A good ol' heatmap.

5.1 Math stuff

We can also write math stuff! For example, here is a definition:

Definition 5.1 (Continuity). The function $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$ is *continuous at a point* $x \in \mathbb{R}^n$ if for all $\varepsilon > 0$ there exists $\delta > 0$ such that if $|x - x_0| < \delta$, then $|f(x) - f(x_0)| < \varepsilon$. If this is true for all such x in the domain of f , we say that f is a *continuous function*.

5.1.0.1 Example

Define $f : \mathbb{R} \rightarrow \mathbb{R}$ by:

$$f(x) = \begin{cases} 1, & x \in \mathbb{Q}, \\ 0, & x \notin \mathbb{Q} \end{cases}$$

Prove that f is not a continuous function.

Proof. Let $\varepsilon = \frac{1}{2}$ and choose any $x \in \mathbb{Q}$. For any $\delta > 0$, we can find some $c \notin \mathbb{Q}$ such that $|x - c| < \delta$ since the irrationals are dense in \mathbb{R} . But then $|f(x) - f(c)| = |1 - 0| = 1 > \frac{1}{2}$, showing that f is not continuous at x . ■

5.2 Adding references

We can also add references. For instance, the following definition of k -partially colored comes from this paper: (Blair et al. 2020)

Definition 5.2 (k -partially colored). Let D be a diagram of a link L with n crossings. We call D *k -partially colored* if we have specified a subset A of the strands of D and a function $f : \rightarrow \{1, 2, \dots, k\}$. We refer to this partial coloring by the tuple (A, f) . Given k -partial colorings (A_1, f_1) and (A_2, f_2) of D , we say (A_2, f_2) is the result of a coloring move on (A_1, f_1) if

1. $A_1 \subset A_2$ and $A_2 \setminus A_1 = \{s_j\}$ for some strand s_j in D ;
2. $f_2|_{A_1} = f_1$;
3. s_j is adjacent to s_i at some crossing $c \in v(D)$, and $s_i \in A_1$;
4. the over-strand s_k at c is an element of A_1 ;
5. $f_1(s_i) = f_2(s_j)$.

5.3 Cross-references

Along the way, we've been giving each of the items above labels. The Visual Editor knows about these labels and we can call them up for cross referencing. For example:

- We were pretty happy about the standard curves in fig. [5.1](#)
- I love heatmaps like fig. [5.2](#)
- def. [5.2](#) is trivially true for the unknot.

6 Bibliography

7 A qmd with only Python

This is a pure Python qmd document. Since there are no R code chunks, it is executed via the Jupyter kernel. Because it's written in a qmd file, all of the Rmarkdown/knitr functionality you're used to can be used here. Here is some example code below.

7.1 Adding days per month from date range to a dataframe

Suppose you have a dataset with a column of start dates and column of end dates. For example:

```
import pandas as pd
import calendar

date_df = pd.DataFrame({
    "START_TM": ['2/15/2010', '2/15/2010', '3/16/2010'],
    "END_TM": ['4/18/2010', '2/18/2010', '5/20/2010']
})
date_df["START_TM"] = date_df["START_TM"].astype('datetime64')
date_df["END_TM"] = date_df["END_TM"].astype('datetime64')
date_df
```

	START_TM	END_TM
0	2010-02-15	2010-04-18
1	2010-02-15	2010-02-18
2	2010-03-16	2010-05-20

Our goal is to count the number of days in each month this range of dates falls over.

We start by adding columns for each month:

```
months = {calendar.month_name[i]:[0 for _ in range(date_df.shape[0])] for i in range(1, 13)}
for m in months:
    date_df[m] = [0 for _ in range(date_df.shape[0])]
date_df
```

	START_TM	END_TM	January	February	March	April	May	June	July	August	September
0	2010-02-15	2010-04-18	0	0	0	0	0	0	0	0	
1	2010-02-15	2010-02-18	0	0	0	0	0	0	0	0	
2	2010-03-16	2010-05-20	0	0	0	0	0	0	0	0	

7.1.1 Helper functions

```
def insert_days_per_month(outer_row):
    dpm = days_per_month(outer_row)
    for index, inner_row in dpm.iterrows():
        outer_row[inner_row['Month']] = inner_row['NumDays']
    return(outer_row)

def days_per_month(row):
    s = pd.Series(index = pd.date_range(row[0], row[1]))[1: ]
    days_in_month = s.resample('MS').size().to_period('m').\
        rename_axis('Month').reset_index(name = 'NumDays')
    days_in_month['Month'] = days_in_month['Month'].apply(
        lambda x: calendar.month_name[x.month])
    return(days_in_month)
```

We can get the desired result with apply:

```
date_df = date_df.apply(lambda x: insert_days_per_month(x), axis = 1)
date_df
```

	START_TM	END_TM	January	February	March	April	May	June	July	August	September
0	2010-02-15	2010-04-18	0	13	31	18	0	0	0	0	
1	2010-02-15	2010-02-18	0	3	0	0	0	0	0	0	
2	2010-03-16	2010-05-20	0	0	15	30	20	0	0	0	

7.2 Interactive Widgets

Quarto has support for interactive documents. Supported formats include:

- JavaScript: Observable JS
- R: Shiny
- Python: Jupyter Widgets are all supported, such as IPyLeaflet and Plotly

Here are some examples:

7.3 IPyLeaflet

```
from ipyleaflet import Map, Marker

good_eats = {
    "Cham Soot Gol": (33.772819, -117.9694484),
    "The Boiling Crab": (33.6996179, -117.8905689),
    "Tan Hoang Huong": (33.7446965, -117.9629173)
}

cham_soot_gol = Map(center=good_eats["Cham Soot Gol"], scroll_wheel_zoom=True)
for place in good_eats:
    cham_soot_gol.add_layer(Marker(location=good_eats[place], title=place))
cham_soot_gol
```

```
Map(center=[33.772819, -117.9694484], controls=(ZoomControl(options=['position', 'zoom_in_te
```

7.4 Plotly

```
import plotly.express as px
df = px.data.iris()
fig = px.scatter(df, x="sepal_width", y="sepal_length",
                 color="species",
                 marginal_y="violin", marginal_x="box",
                 trendline="ols", template="simple_white")
fig.show()
```

Unable to display output for mime type(s): text/html

Unable to display output for mime type(s): text/html

7.5 Learning more

To learn more about using interactive documents with Quarto, see the [Interactive Docs section](#) of the Quarto documentation.

8 A Jupyter Notebook

The editing experience with Jupyter Notebook is very similar to the RStudio editing experience: when we make changes and save them, the preview window opened by `quarto preview` (if your document is not in a project) and `quarto serve` (if it is a project) will update.

Note that Quarto rendered this entire website with a single command. Quarto took `Rmd`, `qmd`, and `ipynb` files, converted them into a website with the same styling, as well as converting the website to a `docx` and `pdf` version.

```
for x in range(10):  
    print(f'{x} squared is {x ^ 2}.')
```

```
0 squared is 2.  
1 squared is 3.  
2 squared is 0.  
3 squared is 1.  
4 squared is 6.  
5 squared is 7.  
6 squared is 4.  
7 squared is 5.  
8 squared is 10.  
9 squared is 11.
```

What's different about using Quarto to render Jupyter notebooks is that we can use Knitr code chunk options in the code cells. For example, we can use the `label` and `fig.cap` code chunk options in to add a caption and a label to the figure in the cell below. By putting this code...

```
#| fig-cap: "A straight line projected into polar coordinates. "  
#| label: fig-polar
```

...at the top of the next cell...

```

import numpy as np
import matplotlib.pyplot as plt

r = np.arange(0, 2, 0.01)
theta = 2 * np.pi * r
fig, ax = plt.subplots(subplot_kw={'projection': 'polar'})
ax.plot(theta, r)
ax.set_rticks([0.5, 1, 1.5, 2])

ax.grid(True)
plt.show()

```

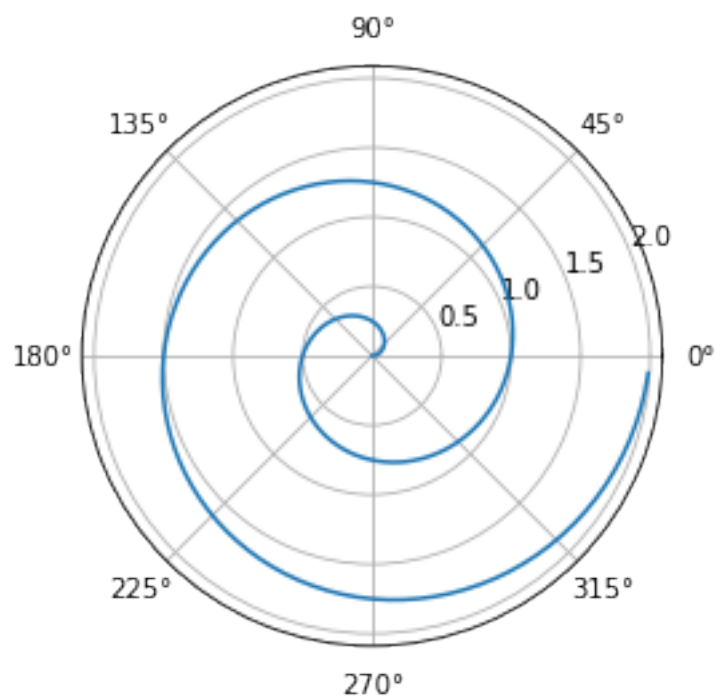


Figure 8.1: A straight line projected into polar coordinates.

... we can cross reference these items just like we did in `qmd` and `Rmd` files:

See fig. [8.1](#) for an example of a projection of a straight line into polar coordinates.

9 DNA String Manipulation

Below are some functions to do some basic DNA string calculations. This is a lot of function definitions and code testing that most people probably don't care about, so we'll use the code-fold chunk option to hide the code and label the fold with `code-summary`:

```
#!/ code-fold: true
#!/ code-summary: "Function definitions and doctests"

import pandas as pd
def reverse_complement(nuc_sequence: str) -> str:
    """
    Returns the reverse complement of a nucleotide sequence.
    >>> reverse_complement('ACGT')
    'ACGT'
    >>> reverse_complement('ATCGTGCTGCTGTCGTCAAGAC')
    'GTCTTGACGACAGCAGCACGAT'
    >>> reverse_complement('TGCTAGCATCGAGTCGATCGATATATTTAGCATCAGCATT')
    'AATGCTGATGCTAAATATATCGATCGACTCGATGCTAGCA'
    """
    complements = {
        "A": "T",
        "C": "G",
        "G": "C",
        "T": "A"
    }
    rev_seq = "".join([complements[s] for s in nuc_sequence.upper()[::-1]])
    return rev_seq

def gc_content(nuc_sequence: str) -> float:
    """
    Calculates the GC content of a nucleotide sequence.
    >>> gc_content('ACGT')
    0.5
    """
    gc_tally = 0
```

```

    for nuc in nuc_sequence.lower():
        if nuc == 'g' or nuc == 'c':
            gc_tally += 1
    return gc_tally / len(nuc_sequence)

def random_dna_string(seq_length: int = 10) -> str:
    """
    Generates a random DNA string seq_length bp long
    >>> len(random_dna_string())
    10
    >>> len(random_dna_string(20))
    20
    """
    from random import choice

    dna_string = ""
    for _ in range(seq_length):
        dna_string += choice("ACGT")
    return dna_string

def make_strings_df(num_strings: int = 10, str_length: int = 10) -> pd.DataFrame:
    """
    Generates a pandas dataframe with num_strings DNA sequences of length str_length with
    columns "Sequence", "GC Content", "Reverse Complement"
    >>> df = make_strings_df(100, 37)
    >>> df.shape
    (100, 3)
    >>> len(df['Sequence'][0])
    37
    """
    dna_strings_list = [random_dna_string(str_length) for _ in range(num_strings)]
    strings_df = pd.DataFrame({
        "Sequence": dna_strings_list
    })
    strings_df['GC Content'] = strings_df['Sequence'].apply(gc_content)
    strings_df['Reverse Complement'] = strings_df['Sequence'].apply(reverse_complement)
    return strings_df

import doctest
doctest.testmod(verbose=0)

```

TestResults(failed=0, attempted=9)

Let's use the function and create a histogram of the GC contents for the simulated sequences.

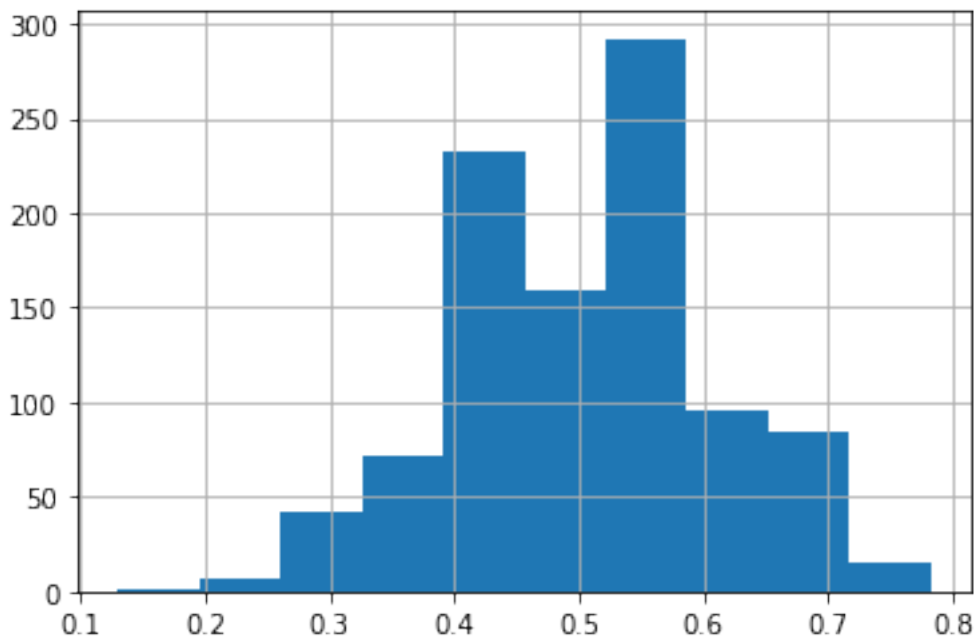
```
strings_df = make_strings_df(1000, 23)
print(f'strings_df has {strings_df.shape[0]} rows and {strings_df.shape[1]} columns.')
```

strings_df has 1000 rows and 3 columns.

```
strings_df.head(10)
```

	Sequence	GC Content	Reverse Complement
0	TAATAATGGGCTAAACTATGTTT	0.260870	AAACATAGTTTtagccattatta
1	GACCGTGACCCAAGGCAGATGGG	0.652174	CCCATCTGCCTTGGGTCACGGTC
2	TAGGGTTGTGCTTTACCTTACAT	0.391304	ATGTAAGGTAAAGCACAACCCTA
3	GCAAGGCCGGATACGCGTATAAT	0.521739	ATTATACGCGTATCCGGCCTTGC
4	ACCACTCCTCAAACGTTACTGAT	0.434783	ATCAGTAACGTTTGAGGAGTGGT
5	CCTCGTCAGTTGTCACTTCTATG	0.478261	CATAGAAGTGACAACTGACGAGG
6	ACAATGATCGCAGCCGAGGTATA	0.478261	TATACCTCGGCTGCGATCATTGT
7	GTTGGATATTCGCGAGCAGAGGA	0.521739	TCCTCTGCTGCGGAATATCCAAC
8	CGCTTAAAATCCCTGCATAGACC	0.478261	GGTCTATGCAGGGATTTTAAGCG
9	AGACCACTACTGGGTGGAGACGG	0.608696	CCGTCTCCACCCAGTAGTGGTCT

```
strings_df['GC Content'].hist();
```



10 Sample Analysis

This is some preliminary analysis I did for an experiment we're doing to quantify the effects of crop priming on nitrogen fixation rates. You can see the latest version of this analysis [at my research journal](#) and learn more about the experiment at [my website](#). Also note that you can view the source code of this page by click on the **Code** button to the right of the title of this page.

10.0.1 Data

```
data.priming <- read.csv("data/priming_amoA_deltaCt.csv", header = T) %>%
  rename(sample_id = X)

data.raw <- read.csv("data/priming_amoA_rawCt.csv", header = T) %>%
  rename(sample_id = X)

data.priming.long <- data.priming %>%
  pivot_longer(cols = starts_with("amoA"), names_to = "amoA", values_to = "deltaCT")

data.raw.long <- data.raw %>%
  pivot_longer(cols = starts_with("amoA"), names_to = "amoA", values_to = "CT")

data.priming.long$sample_id <- fct_reorder(data.priming.long$sample_id, parse_number(data.pr

df <- data.priming[, -1]
rownames(df) <- data.priming[, 1]

metadata <- df %>%
  select(fert_level:field_rep) %>%
  mutate(across(everything(), as.factor))

amoA_counts <- df %>%
  select(starts_with("amoA"))
```

`data.priming` contains the data for our experiment. There are rows for samples, columns for the delta CTs of the different amoAs, and some metadata.

```
data.priming[1:5, 1:5]
```

	sample_id	amoA.001	amoA.002	amoA.003	amoA.004
1	2b	10.119249	27.41268	8.764504	8.992937
2	35b	9.837943	27.51089	9.300077	10.445448
3	52f	26.345485	26.34548	26.345485	26.345485
4	34f	26.914432	26.91443	26.914432	26.914432
5	16f	8.337293	25.94591	8.371314	25.945907

`data.raw` contains the same columns but lists the raw CT values instead of the 16s-normalized ones.

```
data.raw[1:5, 1:5]
```

	sample_id	amoA.001	amoA.002	amoA.003	amoA.004
1	2b	22.70657	40	21.35182	21.58026
2	35b	22.32706	40	21.78919	22.93456
3	52f	40.00000	40	40.00000	40.00000
4	34f	40.00000	40	40.00000	40.00000
5	16f	22.39139	40	22.42541	40.00000

The `long` versions of these dataframes contains the same info but in long format to play nicely with `ggplot`.

10.1 Removing amoAs

We'll start by removing those amoAs from our data that are not present in over 30 samples across both treatments.

We'll first start by counting the non-detects for each amoA.

```
non_detect_counts <- data.raw.long %>%  
  group_by(fert_level, amoA) %>%  
  count(CT == 40) %>%  
  rename(non_detect = `CT == 40`) %>%  
  filter(non_detect == TRUE)
```

Finding the amoAs that are not detected in > 30 across both samples

```
removes <- non_detect_counts %>%
  pivot_wider(names_from = fert_level, values_from = n, names_prefix = "fert.") %>%
  filter(fert.0 > 30 & fert.336 > 30) %>%
  pivot_longer(cols = fert.0:fert.336, names_to = "fert_level", values_to = "n")
```

We'll now reduce `data.priming` by removing those amoAs that are largely non-detects. We'll also update the `long` version while we're at it

```
data.priming.reduced <- data.priming %>%
  select(-one_of(removes$amoA))

data.priming.reduced.long <- data.priming.reduced %>%
  select(-sample_id, field_rep) %>%
  pivot_longer(cols = contains("amoA"))
```

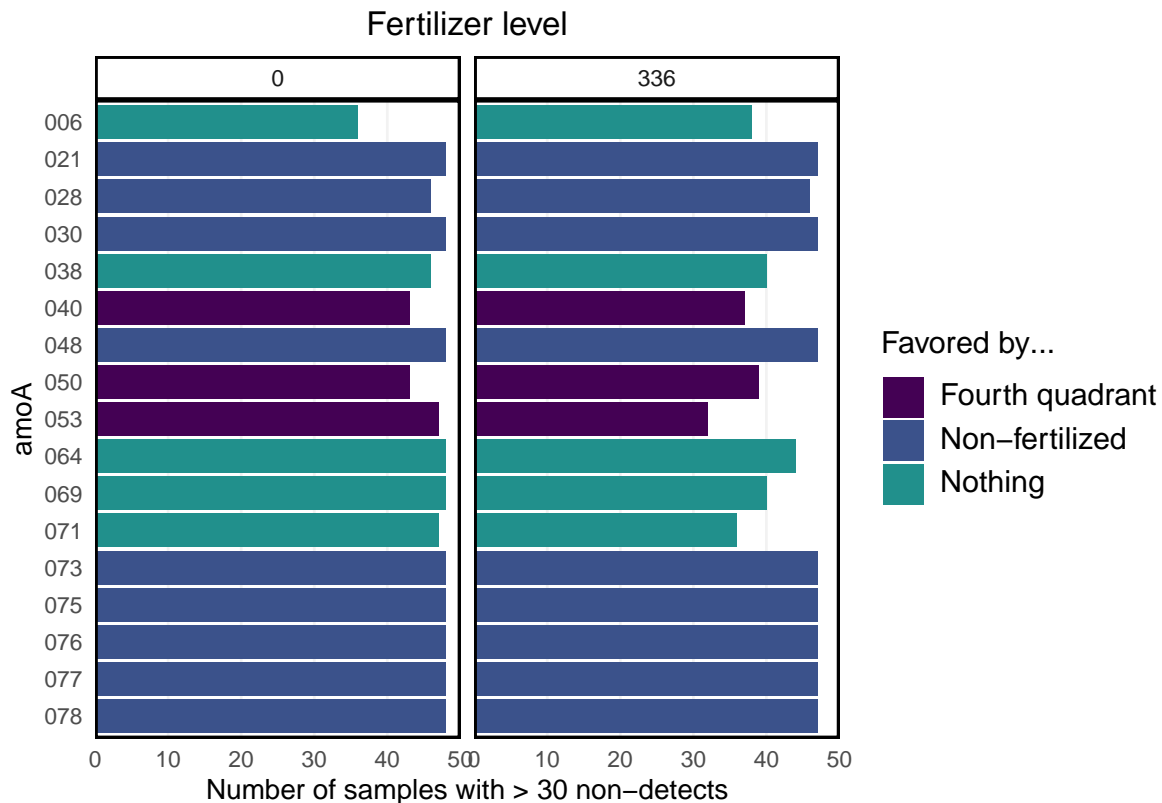
Here's a barchart of what we're removing:

```
removes %>%
  mutate(amoA = str_sub(amoA, -3)) %>%
  mutate(favored = case_when(
    amoA %in% c("006", "038", "064", "069", "071") ~ "Nothing",
    amoA %in% c("021", "028", "030", "048", "073", "075", "076", "077", "078") ~ "Non-fertil.",
    amoA %in% c("040", "050", "053") ~ "Fourth quadrant",
    TRUE ~ "First quadrant"
  )) %>%
  mutate(fert_level = str_sub(fert_level, start = 6)) %>%
  ggplot(aes(amoA, n, fill = favored)) +
  geom_col() +
  facet_wrap(~ fert_level) +
  theme(
    plot.title = element_text(hjust = 0.5),
    legend.text = element_markdown(size = 12),
    legend.title = element_markdown(size = 12, hjust = 0),
    strip.background = element_rect(size = 1, color = "black", fill = "NA"),
    panel.grid = element_line(color = "gray95"),
    panel.grid.major.y = element_blank(),
    panel.grid.minor.y = element_blank(),
    panel.grid.minor.x = element_blank(),
    panel.border = element_rect(color = "black", size = 1, fill = NA)
  ) +
```

```

scale_fill_viridis_d(begin = 0, end = 0.5) +
scale_y_continuous(limits = c(0, 50), expand = expansion(add = c(0, 0))) +
scale_x_discrete(limits = rev) +
coord_flip() +
labs(
  y = "Number of samples with > 30 non-detects",
  title = "Fertilizer level",
  fill = "Favored by..."
)

```



Note that most of the non-detects that we're removing are from the non-fertilized group.

Next, we'll convert the CT values to presence/absence for use in later analysis.

```

amoA_presence_absence <- data.raw %>%
  select(sample_id, starts_with("amoA")) %>%
  mutate(across(starts_with("amoA"), ~ ifelse(.x == 40, 0, 1)))

```

10.2 Ordination

Calculating the NMDS (positioning the sites):

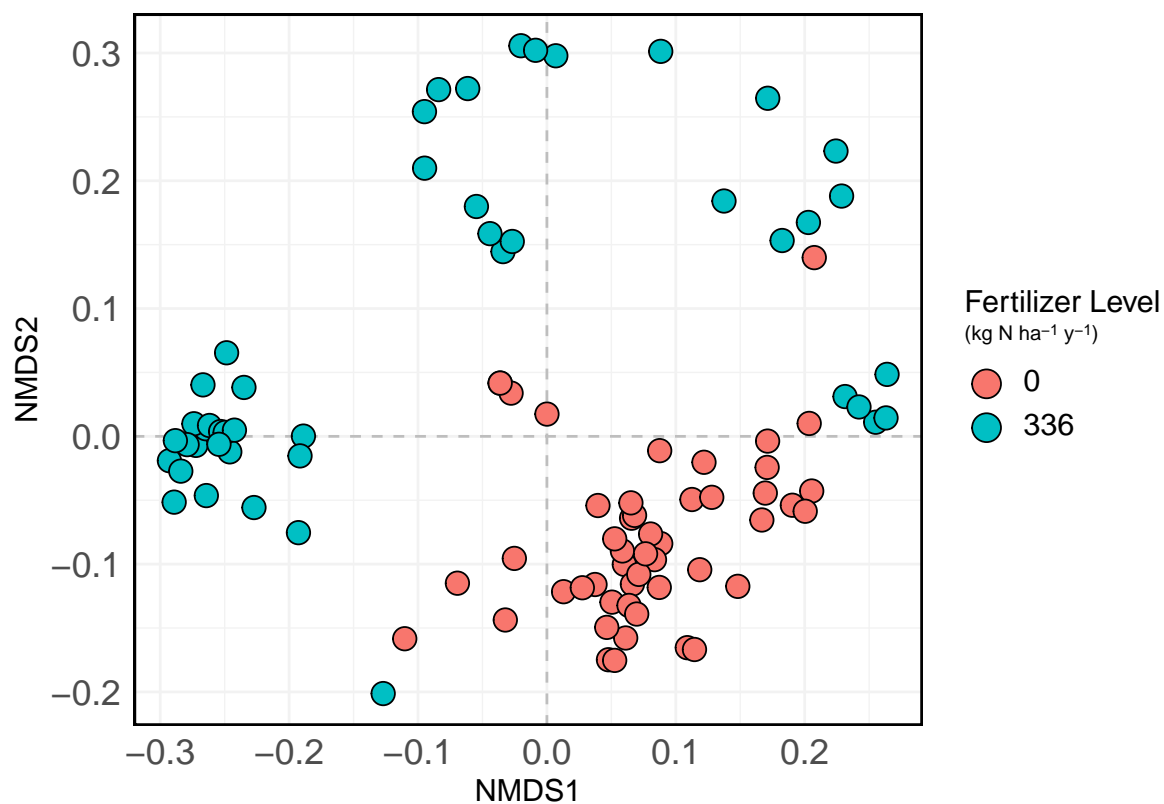
```
mds.priming = metaMDS(data.priming.reduced %>% select(contains("amoa")), distance = "bray", 100)

site.scores <- as.data.frame(scores(mds.priming, display = "sites")) %>%
  mutate(sample_id = data.priming.reduced$sample_id,
         Crop = data.priming.reduced$crop,
         Fert_Level = as.factor(data.priming.reduced$fert_level),
         Day = as.factor(data.priming.reduced$doe),
         Substrate_Addition = as.factor(data.priming.reduced$addition))
```

This is enough to plot a basic NMDS:

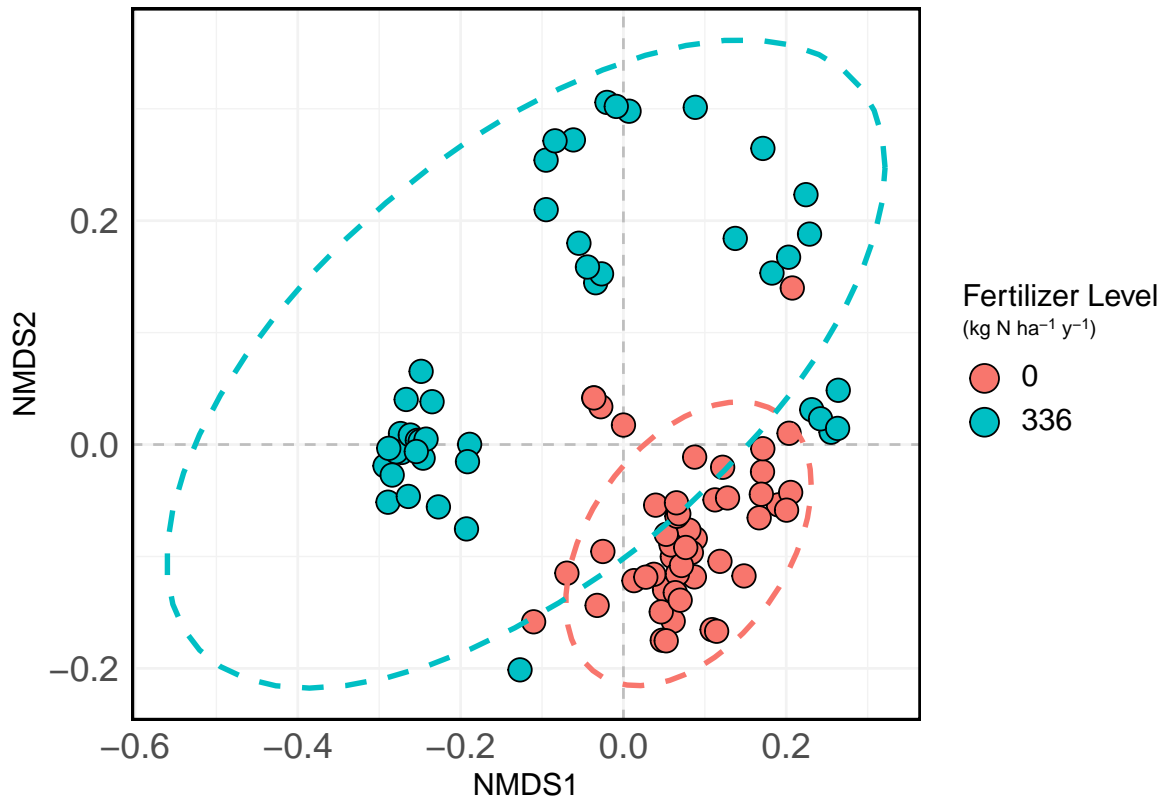
```
nmds.plot <- site.scores %>%
  ggplot(aes(NMDS1, NMDS2, fill = Fert_Level)) +
  geom_hline(yintercept = 0.0,
            colour = "grey",
            lty = 2) +
  geom_vline(xintercept = 0.0,
            colour = "grey",
            lty = 2) +
  geom_point(size = 4, shape = 21) +
  theme(
    plot.title = element_text(hjust = 0.5),
    legend.text = element_markdown(size = 12),
    legend.title = element_markdown(size = 12, hjust = 0),
    axis.text.x = element_text(size = 14),
    axis.text.y = element_text(size = 14),
    axis.title.x = element_text(size = 12),
    axis.title.y = element_text(size = 12),
    panel.grid = element_line(color = "gray95"),
    panel.border = element_rect(color = "black", size = 1, fill = NA)
  ) +
  scale_fill_discrete(name = "Fertilizer Level<br>
    <span style = 'font-size:8pt;'>
    (kg N ha<sup>-1</sup> y<sup>-1</sup>)</span>" +
    </span>") +
  guides(
    fill = guide_legend(override.aes = list(shape = 21, size = 5))
  )
```

```
nmds.plot
```



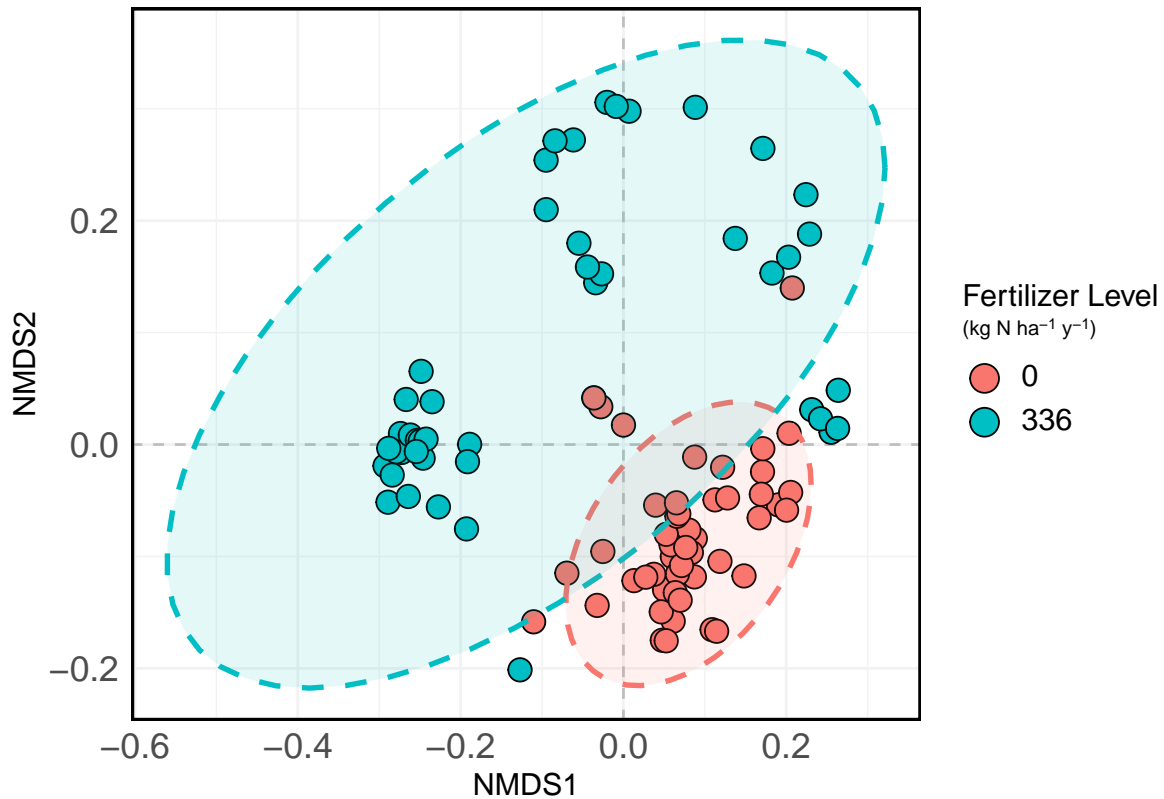
We can also add ellipses to the plot indicate confidence intervals if you're interested in that:

```
nmds.plot +  
  stat_ellipse(aes(color = Fert_Level), size = 1, linetype = "dashed", show.legend = FALSE)
```



And again with shading:

```
nmds.plot +
  stat_ellipse(aes(color = Fert_Level), size = 1, linetype = "dashed", show.legend = FALSE) +
  stat_ellipse(aes(fill = Fert_Level), size = 1, linetype = "dashed", show.legend = FALSE,
```



10.3 Arrows!

Let's calculate the loading factors of the individual amoas:

```
dune_dist <- vegdist(data.priming %>% select(starts_with('amoA'))))

amo_aanosim <- anosim(dune_dist, data.priming$fert_level)

mds.spp.fit <- envfit(mds.priming, data.priming.reduced %>% select(contains("amo_a")), permu

spp.scrs <- as.data.frame(scores(mds.spp.fit, display = "vectors"))
spp.scrs <- cbind(spp.scrs, Species = rownames(spp.scrs))
spp.scrs <- cbind(spp.scrs, pval = mds.spp.fit$vectors$pvals)

spp.scores <- as.data.frame(scores(mds.spp.fit, display = "vectors")) %>%
  mutate(Species = rownames(.),
         pval = mds.spp.fit$vectors$pvals)
```

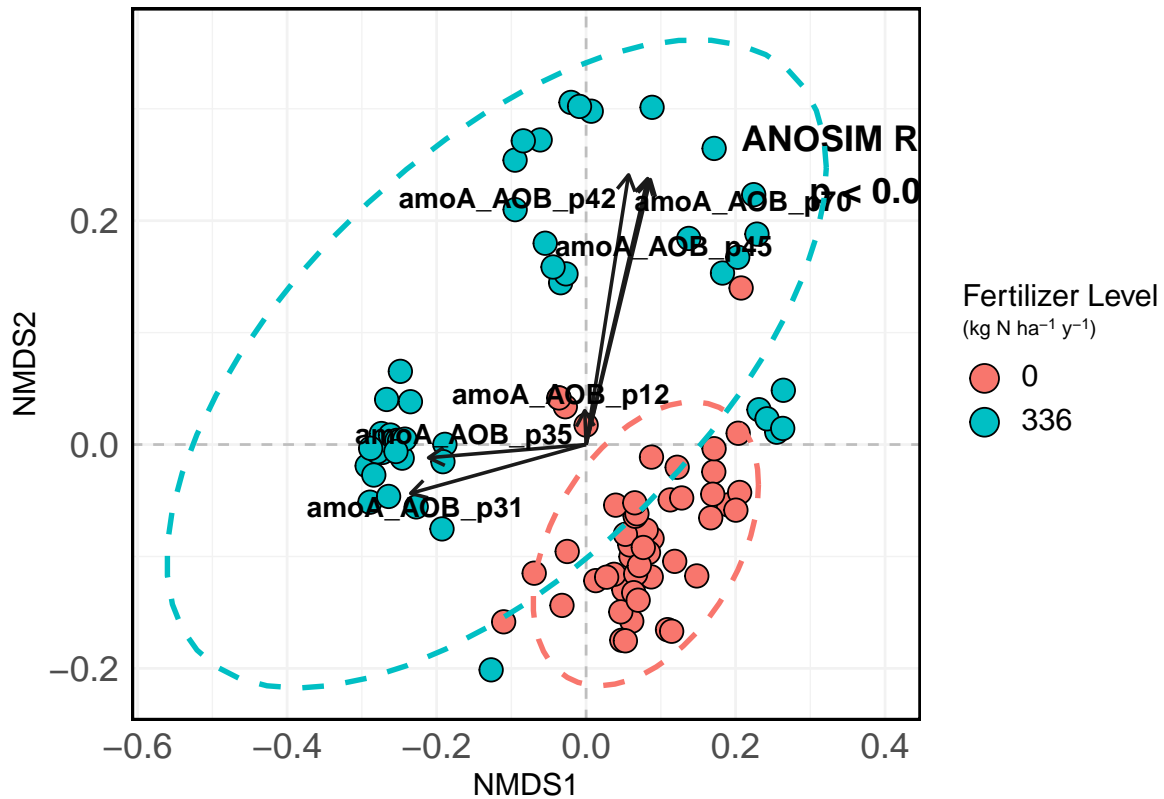

This is enough to plot arrows on the NMDS. We'll show the loadings of some amoAs of interest that we identified in a previous analysis.

```
special <- c("amoA.012", "amoA.031", "amoA.035", "amoA.042", "amoA.045", "amoA.070")

special_arrows <- spp.scores %>%
  rownames_to_column() %>%
  filter(rowname %in% special) %>%
  mutate(x = -0.25 * NMDS1,
         y = -0.25 * NMDS2,
         assay = str_sub(rowname, -2),
         assay = paste0("amoA_AOB_p", assay)
  )

nm.ds.plot +
  geom_segment(data = special_arrows,
             aes(x = 0, xend = -0.3 * NMDS1,
                y = 0, yend = -0.3 * NMDS2),
             size = 0.66,
             arrow = arrow(length = unit(0.25, "cm")),
             color = "grey10", lwd = 0.3,
             inherit.aes = FALSE) +
  ggrepel::geom_text_repel(
    data = special_arrows,
    aes(x * 1, y * 1, label = assay),
    fontface = "bold",
    size = 4,
    inherit.aes = FALSE,
    force = 1,
    nudge_x = -0.001
  ) +
  annotate(
    "text",
    label = paste0("ANOSIM R = ", round(amoA_anosim$statistic, 2),
                  "\np < 0.001"),
    x = 0.4,
    y = 0.25,
    size = 5,
    fontface = 2
  ) +
  stat_ellipse(aes(color = Fert_Level), size = 1, linetype = "dashed", show.legend = FALSE)
```

Warning: Duplicated aesthetics after name standardisation: size



10.4 Statistics

10.4.1 Which factors have an impact on overall community composition?

```
X <- data.priming.reduced %>%
  select(-c(contains("amoA")))
Y <- data.priming.reduced %>%
  select(c(contains("amoA")))

adonis(Y ~ X$fert_level + X$addition + X$crop + X$timepoint)
```

Call:

```
adonis(formula = Y ~ X$fert_level + X$addition + X$crop + X$timepoint)
```

Permutation: free

Number of permutations: 999

Terms added sequentially (first to last)

	Df	SumsOfSqs	MeanSqs	F.Model	R2	Pr(>F)
X\$fert_level	1	1.4426	1.44255	56.092	0.37093	0.001 ***
X\$addition	2	0.0327	0.01633	0.635	0.00840	0.697
X\$crop	1	0.0882	0.08823	3.431	0.02269	0.024 *
X\$timepoint	1	0.0367	0.03671	1.427	0.00944	0.197
Residuals	89	2.2889	0.02572		0.58855	
Total	94	3.8890			1.00000	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

This tells us that fertilization level is very significant and explains ~37% of the variation in our samples. Crop is also a significant factor on community composition, though it only explains 2.3% of the variation.

10.4.2 How do the treatment factors affect the “abundance” of genes on an individual level?

All the code below does is perform an ANOVA of the gene’s abundance against all the terms and all of their interactions.

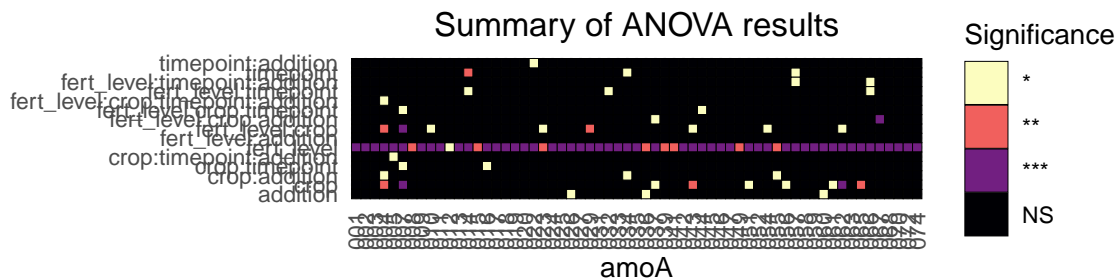
```
formulae <- lapply(colnames(data.priming.reduced) %>% select(starts_with("amoA"))), function(x) {  
  res <- lapply(formulae, function(x) broom::tidy(aov(x, data = data.priming.reduced)))  
  names(res) <- format(formulae)  
  names(res) <- str_sub(names(res), end = 8)  
  
  anova_results <- lapply(seq_along(res), function(i) res[[i]] %>% mutate(gene = names(res)[[i]]  
    bind_rows() %>%  
    filter(term != "Residuals") %>%  
    mutate(sig = case_when(  
      p.value < 0.05 & p.value > 0.01 ~ "*",  
      p.value < 0.01 & p.value > 0.001 ~ "**",  
      p.value < 0.001 ~ "***",  
      TRUE ~ "NS"  
    ))  
  })
```

Visualization:

```

anova_results %>%
  mutate(gene = str_sub(gene, -3)) %>%
  ggplot(aes(gene, term, fill = sig)) +
  geom_tile(color = "black") +
  coord_equal() +
  labs(y = "",
       x = "amoA",
       title = "Summary of ANOVA results",
       fill = "Significance ") +
  theme(
    plot.title = element_text(hjust = 0.5),
    axis.text.x = element_text(angle = 90, hjust = 0, vjust = 0.5)
  ) +
  scale_fill_viridis_d(option = "magma", direction = -1)

```

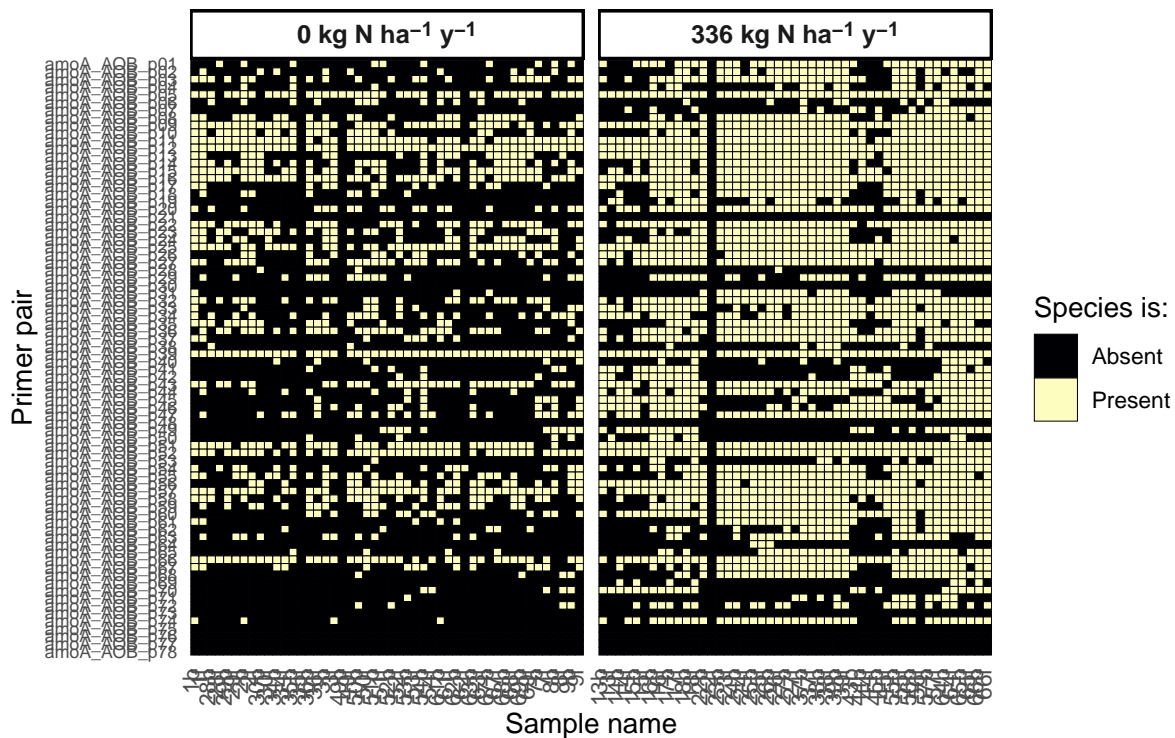


Overall, we see that, again, fertilization level has a significant impact on abundance levels of the individual genes, and it's not even really that close. There are other factors that might be worth investigating on a gene-by-gene basis, too, but that's for later.

10.5 Biodiversity

Let's start by visualizing the presence/absence table:

```
amoA_presence_absence %>%
  pivot_longer(cols = starts_with("amoA"), names_to = "amoA", values_to = "presence") %>%
  mutate(amoA = str_sub(amoA, -2),
         amoA = paste0("amoA_AOB_p", amoA),
         presence = as.factor(presence)) %>%
  left_join(metadata %>% rownames_to_column(var = "sample_id")) %>%
  mutate(strip_label = paste0(fert_level, " kg N ha<sup>-1</sup> y<sup>-1</sup>")) %>%
  ggplot(aes(sample_id, amoA, fill = presence)) +
  geom_tile(color = "black") +
  labs(
    x = "Sample name",
    y = "Primer pair",
    fill = "Species is:",
    title = "",
    subtitle = ""
  ) +
  scale_fill_viridis_d(labels = c("Absent", "Present"),
                       begin = 0, end = 1,
                       option = "magma") +
  theme(
    axis.text.x = element_text(angle = 90, hjust = 1, vjust = 0.25),
    axis.text.y = element_text(size = 7),
    plot.title = element_text(hjust = 0.5),
    plot.subtitle = element_text(hjust = 0.5),
    strip.text = element_markdown(size = 10, face = "bold"),
    strip.background = element_rect(size = 1, color = "black", fill = NA),
    plot.margin = unit(c(0, 0.1, 0.1, 0.1), "cm")
  ) +
  scale_y_discrete(limits = rev) +
  facet_grid(~ strip_label, scales = "free")
```



10.6 Reading in the best BLAST hit info:

```
amoA_organism_info <- readxl::read_xlsx("data/amoA_mfp_qpcr_org_accessions.xlsx", sheet = 5)
select(-c(contains(c("forward", "reverse", "notes"))))
```

Counts of best BLAST hits:

```
amoA_organism_info %>%
  count(best_blast_hits, sort = TRUE)
```

```
# A tibble: 25 x 2
  best_blast_hits      n
  <chr>            <int>
1 Nitrosolobus multififormis AmoA (amoA) gene    10
2 Nitrosospira sp. En13 AmoA                      9
```

3	Nitrosospira multiformis ATCC 25196	7
4	Nitrosospira sp. Wyke8 AmoA	7
5	Nitrosospira lacus strain APG3	6
6	Nitrosospira sp. Np39-19	6
7	Nitrosospira sp. Wyke2	4
8	Nitrosospira sp. NpAV	3
9	Nitrosomonas sp. JL21	2
10	Nitrosospira briensis	2
# ... with 15 more rows		

10.7 Creating a phyloseq object

```

amoA_tax_table <- amoA_organism_info %>%
  select(array_name, best_blast_hits) %>%
  column_to_rownames(var = "array_name") %>%
  tax_table()

rownames(amoA_tax_table) <- amoA_organism_info$array_name

```

```

ps <- phyloseq(
  otu_table(amoA_presence_absence %>% column_to_rownames(var = "sample_id"), taxa_are_rows =
  sample_data(metadata),
  amoA_tax_table
)

```

10.8 Richness analysis

How does observed richness and evenness change with treatment level? This is a modified diversity function that does a bunch of nice stuff that `phyloseq::estimate_richness` doesn't do.

```

estimate_richness_mod <- function(physeq, split=TRUE, measures=NULL){

  if( !split ){
    OTU <- taxa_sums(physeq)
  } else if( split ){
    OTU <- as(otu_table(physeq), "matrix")
  }
}

```

```

    if( taxa_are_rows(physeq) ){ OTU <- t(OTU) }
  }

  renamevec = c("Observed", "Chao1", "ACE", "Shannon", "Pielou", "Simpson", "InvSimpson", "S.
names(renamevec) <- c("S.obs", "S.chao1", "S.ACE", "shannon", "pielou", "simpson", "invsimp

if( is.null(measures) ){
  measures = as.character(renamevec)
}

if( any(measures %in% names(renamevec)) ){
  measures[measures %in% names(renamevec)] <- renamevec[names(renamevec) %in% measures]
}

if( !any(measures %in% renamevec) ){
  stop("None of the `measures` you provided are supported. Try default `NULL` instead.")
}

outlist = vector("list")

estimRmeas = c("Chao1", "Observed", "ACE")
if( any(estimRmeas %in% measures) ){
  outlist <- c(outlist, list(t(data.frame(estimateR(OTU)))))
}
if( "Shannon" %in% measures ){
  outlist <- c(outlist, list(shannon = diversity(OTU, index="shannon")))
}
if( "Pielou" %in% measures){
  #print("Starting Pielou")
  outlist <- c(outlist, list(pielou = diversity(OTU, index = "shannon")/log(estimateR(OTU)
}
if( "Simpson" %in% measures ){
  outlist <- c(outlist, list(simpson = diversity(OTU, index="simpson")))
}
if( "InvSimpson" %in% measures ){
  outlist <- c(outlist, list(invsimpson = diversity(OTU, index="invsimpson")))
}
if( "SimpsonE" %in% measures ){

```



```

    outlist <- c(outlist, list(simpsons = diversity(OTU, index="invsimpson")/estimateR(OTU)[
  ]
  if( "Fisher" %in% measures ){
    fisher = tryCatch(fisher.alpha(OTU, se=TRUE),
                      warning=function(w){
                        warning("phyloseq::estimate_richness: Warning in fisher.alpha(). See
                        suppressWarnings(fisher.alpha(OTU, se=TRUE)[, c("alpha", "se")])
                      }
    )
    if(!is.null(dim(fisher))){
      colnames(fisher)[1:2] <- c("Fisher", "se.fisher")
      outlist <- c(outlist, list(fisher))
    } else {
      outlist <- c(outlist, Fisher=list(fisher))
    }
  }
}
out = do.call("cbind", outlist)

namechange = intersect(colnames(out), names(renamevec))
colnames(out)[colnames(out) %in% namechange] <- renamevec[namechange]

colkeep = sapply(paste0("(se\\.\\.){0,}", measures), grep, colnames(out), ignore.case=TRUE)
out = out[, sort(unique(unlist(colkeep)))], drop=FALSE]

out <- as.data.frame(out)
return(out)
}

```

```

metrics <- c("Observed", "Shannon")
richness <- estimate_richness_mod(ps, measures = metrics) %>%
  rownames_to_column(var = "sample_id") %>%
  mutate(sample_id = str_sub(sample_id, start = 2))

richness <- left_join(sample_data(ps) %>% data.frame() %>% rownames_to_column(var = "sample_id") %>%
  pivot_longer(cols = Observed:Shannon, names_to = "Metric", values_to = "Value")

```

Joining, by = "sample_id"

10.9 Statistical tests

10.9.1 Significance test of fertilization level on richness.

```
(sig_rich_fert <- kruskal.test(Value ~ fert_level, data = richness %>% filter(Metric == "Obs"))
```

Kruskal-Wallis rank sum test

data: Value by fert_level

Kruskal-Wallis chi-squared = 54.212, df = 1, p-value = 1.8e-13

The p-value < 0.001 gives us strong statistical evidence that richness is significantly different between fertilization treatment groups.

10.9.2 Significance test of fertilization level on richness

```
(sig_even_fert <- kruskal.test(Value ~ fert_level, data = richness %>% filter(Metric == "Shan"))
```

Kruskal-Wallis rank sum test

data: Value by fert_level

Kruskal-Wallis chi-squared = 54.268, df = 1, p-value = 1.75e-13

The p-value < 0.001 gives us strong statistical evidence that Shannon diversity is significantly different between fertilization treatment groups.

10.10 Making nice plots for stat differences

Standard deviations, mean

```
summaries <- richness %>%  
  group_by(Metric, fert_level) %>%  
  summarize(mean_val = mean(Value),  
            sd_val = sd(Value),  
            n = n(),  
            .groups = "drop") %>%
```

```

mutate(se = abs((sd_val / sqrt(n)) * qt(0.025, n - 1) )) %>%
mutate(ymax = mean_val + se,
       ymin = mean_val - se)

this_annotation <- data.frame(
  Metric = c("Observed", "Shannon"),
  lab = c("***", "***"),
  x = 1.5,
  y = c(50 + 5 + 2, 4 + 0.5),
  lineheights = c(50 + 5, 4 + 0.25)
)

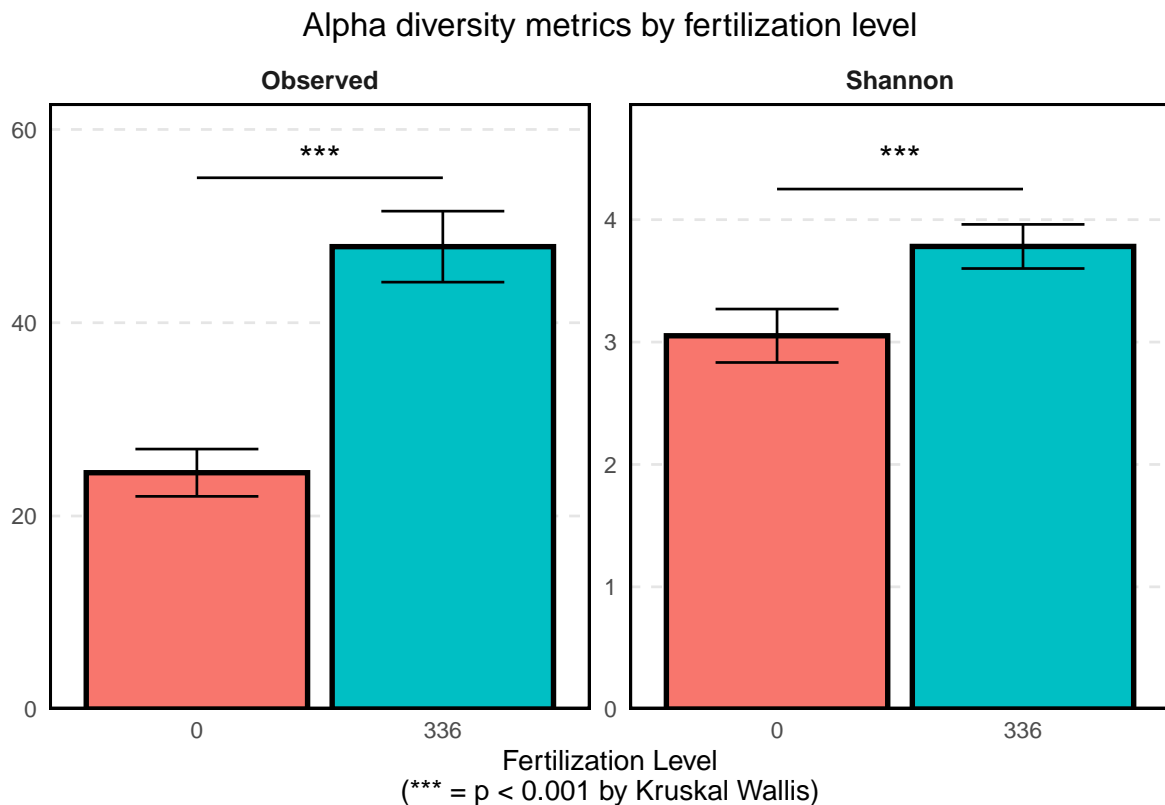
summaries %>%
  ggplot(aes(fert_level, mean_val, fill = fert_level)) +
  geom_col(color = "black", size = 1) +
  facet_wrap(~ Metric, scales = "free_y") +
  theme(
    legend.position = "none",
    strip.background = element_blank(),
    axis.title.y = element_blank(),
    strip.placement = "outside",
    plot.title = element_text(hjust = 0.5),
    strip.text.y = element_text(face = "bold", size = 10),
    strip.text = element_text(face = "bold", size = 10),
    panel.grid.major.x = element_blank(),
    panel.grid.minor.x = element_blank(),
    panel.grid.minor.y = element_blank(),
    panel.grid.major.y = element_line(color = "gray90", linetype = "dashed"),
    axis.ticks = element_blank(),
    panel.border = element_rect(color = "black", size = 1, fill = "NA")
  ) +
  scale_y_continuous(expand = expansion(mult = c(0, 0.1))) +
  geom_errorbar(aes(ymin = ymin, ymax = ymax, width = 0.5)) +
  geom_text(
    data = this_annotation,
    aes(x = x, y = y, label = lab),
    inherit.aes = FALSE,
    size = 5
  ) +
  geom_segment(data = this_annotation,
              aes(x = 1,
                  xend = 2,

```

```

        y = lineheights,
        yend = lineheights),
        inherit.aes = FALSE) +
labs(
  x = "Fertilization Level\n(***) = p < 0.001 by Kruskal Wallis)",
  title = "Alpha diversity metrics by fertilization level"
)

```



10.11 Beta diversity

We'll start beta diversity analysis off by doing an ADONIS/PERMANOVA to determine if treatment centroids/treatment variations are different between groups.

```

dis <- vegdist(otu_table(ps))
groups <- sample_data(ps)$fert_level

```

```
mod <- betadisper(dis, groups)
anova(mod)
```

Analysis of Variance Table

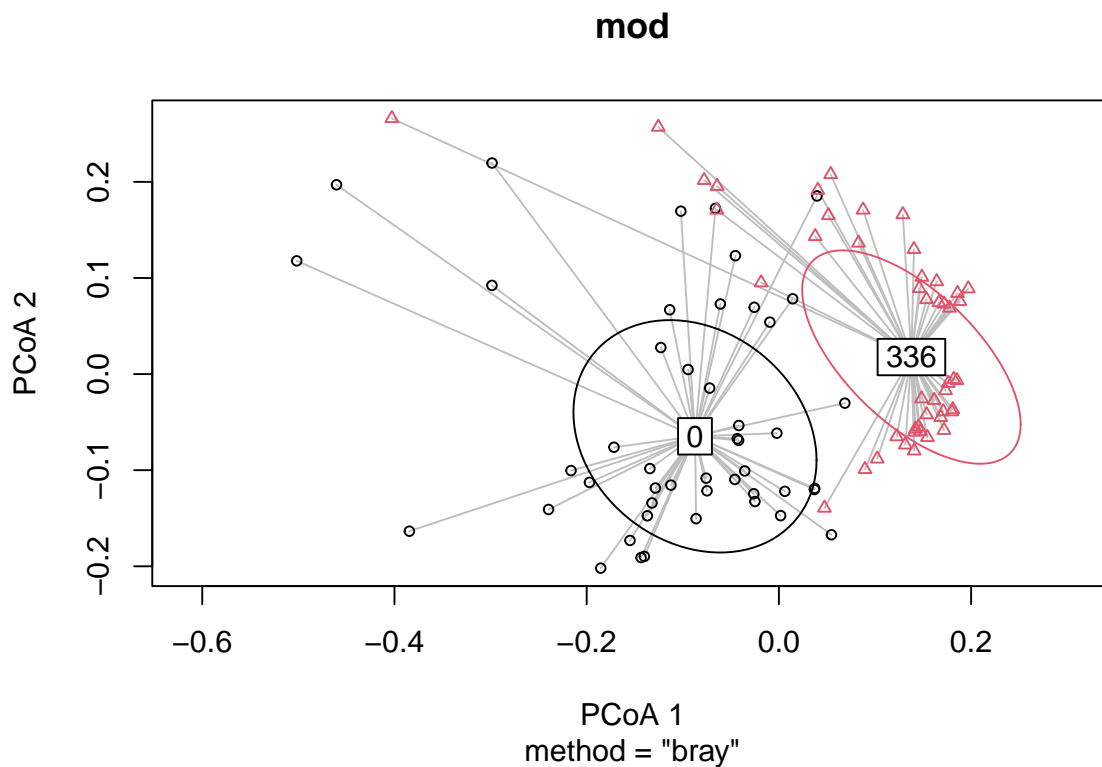
Response: Distances

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Groups	1	0.52595	0.52595	24.589	3.228e-06 ***
Residuals	92	1.96781	0.02139		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Since $p \lll 0.0001$, there is strong evidence that the overall community compositions are significantly different (treatment centroid, distance to centroid, community variation) between the two groups. We can visualize this with a 1 SD ellipse:

```
plot(mod, ellipse = TRUE, hull = FALSE)
```

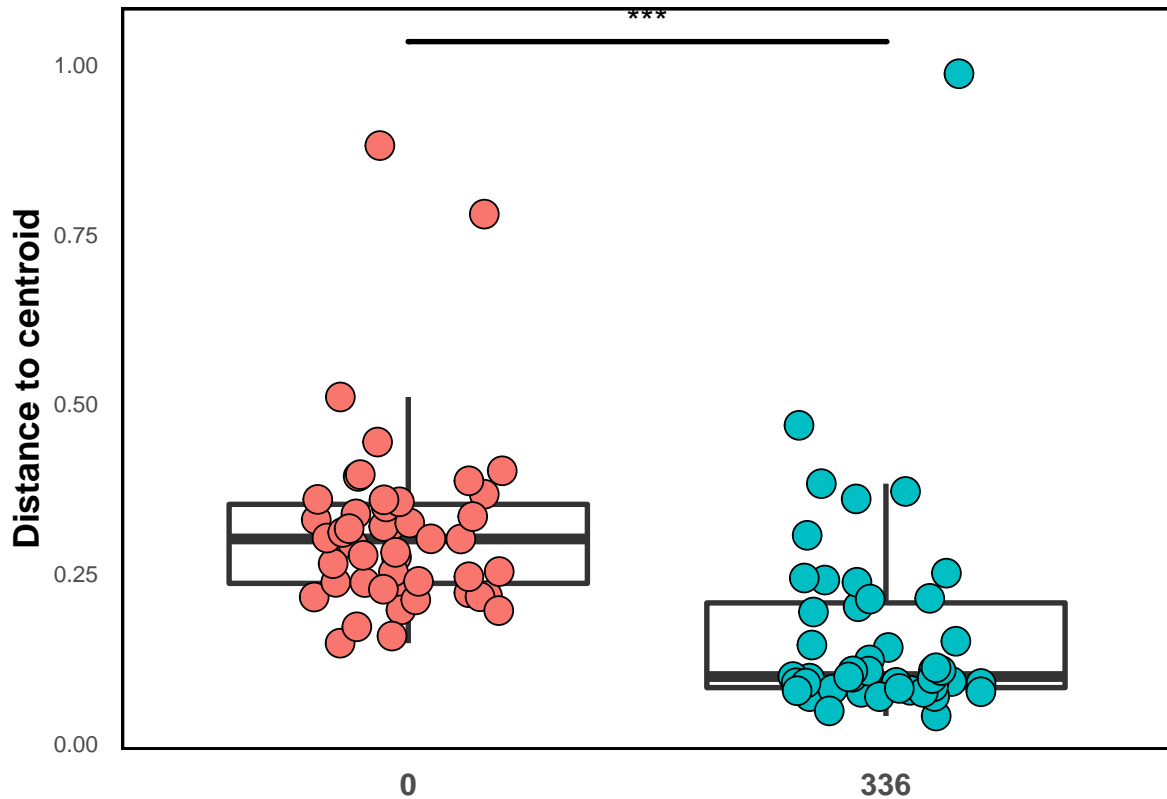


We see that there is clear separation between the two treatment centroids. Let's do some more analysis on the distance-to-centroids that we're seeing:

```
betadistances <- data.frame(
  time_frame = mod$group,
  distance = mod$distances
)

betadistances %>%
  ggplot(aes(time_frame, distance)) +
  geom_boxplot(size = 1, outlier.shape = NA) +
  geom_jitter(aes(fill = time_frame), size = 5, shape = 21, width = 0.2) +
  theme(
    legend.position = "none",
    panel.grid.minor.x = element_blank(),
    panel.grid.major.x = element_blank(),
    panel.grid.minor.y = element_blank(),
    panel.grid.major.y = element_blank(),
    plot.title = element_text(size = 17),
    plot.subtitle = element_text(size = 9),
    axis.ticks.length = unit(0.25, "cm"),
    axis.ticks.x = element_blank(),
    axis.text.x = element_text(face = "bold", angle = 0, size = 12),
    panel.border = element_rect(color = "black", size = 1, fill = NA),
    axis.title.x = element_blank(),
    axis.title.y = element_text(size = 14, face = "bold"),

  ) +
  labs(
    color = "",
    y = "Distance to centroid"
  ) +
  ggsignif::geom_signif(
    map_signif_level = TRUE,
    comparisons = list(c("0", "336")),
    test = "t.test",
    step_increase = 0.1,
    color = "black",
    size = 1,
    textsize = 5,
    tip_length = 0
  )
```



The significance bar is coming from the PERMANOVA test we did above. We see that there is actually less beta diversity (as measured by distance-to-centroid) in the fertilized group than in the non-fertilized group. We'll see another visualization backing this up in the next section:

10.12 Composition

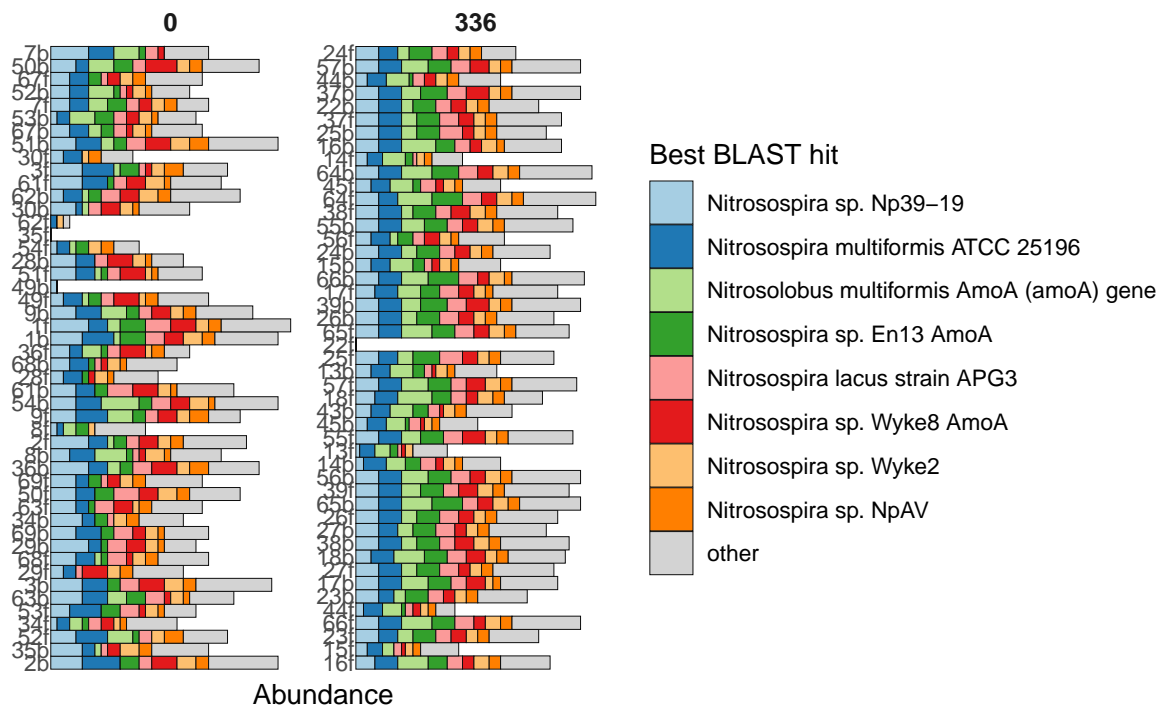
Let's visualize the composition of the communities, separated by fertilization. We'll start with raw counts - how many times was that best BLAST hit seen in that sample?

```
comp_barplot(ps, "ta1",
             facet_by = "fert_level",
             sample_order = "default",
             tax_transform_for_plot = "identity") +
coord_flip() +
labs(
  title = "Sample composition by fertilization level",
  subtitle = "(raw counts)"
```

```
) +
theme(
  axis.text.x = element_blank(),
  axis.text.y = element_text(margin = margin(r = -7)),
  plot.title = element_text(hjust = 0.5),
  plot.subtitle = element_text(hjust = 0.5, size = 10),
  strip.text = element_text(size = 10, face = "bold")
) +
guides(
  fill = guide_legend(title = "Best BLAST hit", reverse = TRUE)
)
```

Sample composition by fertilization level

(raw counts)



We see that overall the fertilized group appears to have more richness in it.

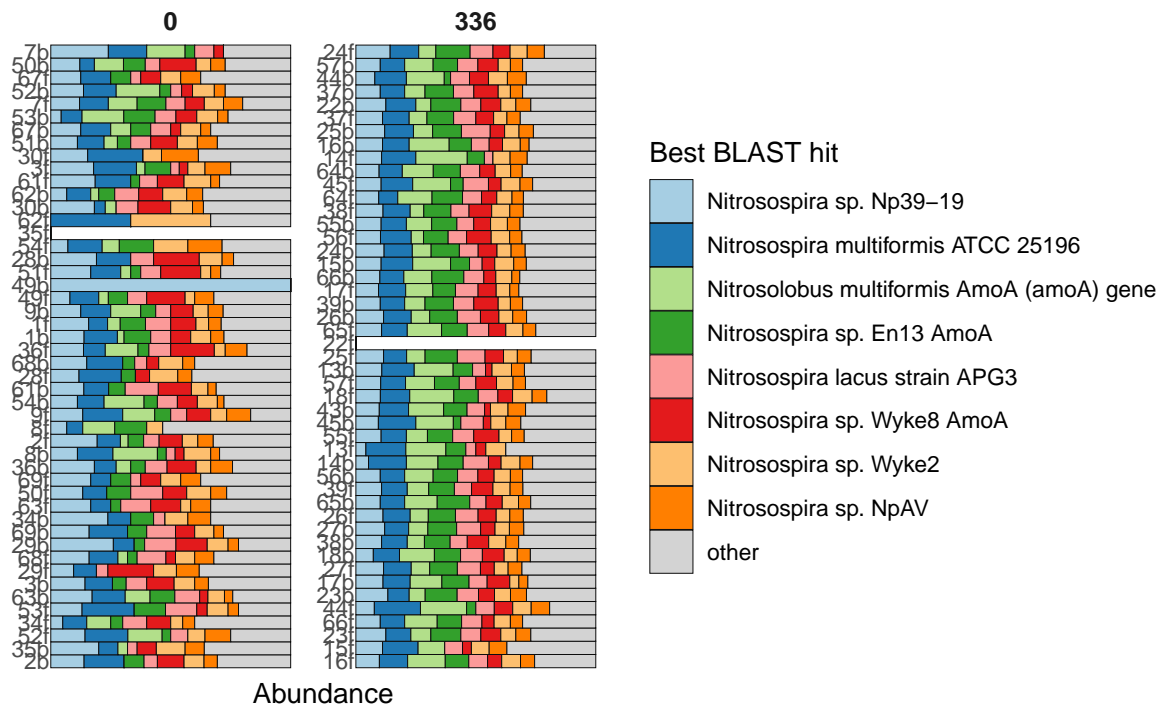
How about sample composition? IE, relative abundances?

```
comp_barplot(ps, "ta1",
  facet_by = "fert_level",
  sample_order = "default") +
```



```
coord_flip() +
labs(
  title = "Sample composition by fertilization level",
  subtitle = "(relative abundance)"
) +
theme(
  axis.text.x = element_blank(),
  axis.text.y = element_text(margin = margin(r = -7)),
  plot.title = element_text(hjust = 0.5),
  plot.subtitle = element_text(hjust = 0.5, size = 10),
  strip.text = element_text(size = 10, face = "bold")
) +
guides(
  fill = guide_legend(title = "Best BLAST hit", reverse = TRUE)
)
```

Sample composition by fertilization level
(relative abundance)



Two big things pop out:

- Species distribution is more even in the fertilized group. This makes sense given previous

results showing that Shannon entropy is higher and beta diversity is lower in the fertilized group. You can also see that the communities just look more like each other in the fertilized group, which manifests in shorter distance-to-centroids/lower community variation.

- There's more green in the fertilized group, suggesting that *Nitrosolobus multiformus* and *Nitrosospora* sp. En13 abundances are significantly affected by fertilization addition.

10.13 Statistics on a best BLAST hit level

The next chunk is just doing some data transformation stuff to count the number of times each organism was seen in each sample in preparation for the statistical analysis.

```
pa_count <- ps %>%
  otu_table() %>%
  data.frame %>%
  rownames_to_column(var = "sample_id") %>%
  pivot_longer(starts_with("amoA"))

org_table <- tax_table(ps) %>%
  data.frame %>%
  rownames_to_column(var = "name") %>%
  rename(bbh = ta1) %>%
  mutate(cleaned_names = janitor::make_clean_names(bbh))

bbh_sample_counts <- left_join(pa_count, org_table, by = "name") %>%
  group_by(sample_id, bbh) %>%
  summarize(value = sum(value)) %>%
  pivot_wider(names_from = "bbh", values_from = value)

bbh_level_counts <- left_join(bbh_sample_counts,
  sample_data(ps) %>%
  data.frame %>%
  rownames_to_column(var = 'sample_id') %>%
  right_join(bbh_sample_counts)
) %>%
  ungroup()
```

Here, we're preparing formulas to feed to a `lapply` function to perform a Kruskal-Wallis test on all of the organisms.

```

formulae <- lapply(colnames(bbh_sample_counts) %>% select(-sample_id) %>% janitor::clean_names)

formulae[[1]] <- NULL

res <- lapply(formulae, function(x) broom::tidy(aov(x, data = bbh_level_counts) %>% janitor::clean_names))
names(res) <- format(formulae)
names(res) <- lapply(names(res), function(x) str_split(x, "~")[[1]][1]) %>% unlist()

anova_results.counts <- lapply(seq_along(res), function(i) res[[i]] %>% mutate(gene = names(res)[i])
  bind_rows() %>%
  filter(term != "Residuals") %>%
  mutate(gene = str_trim(gene)))

```

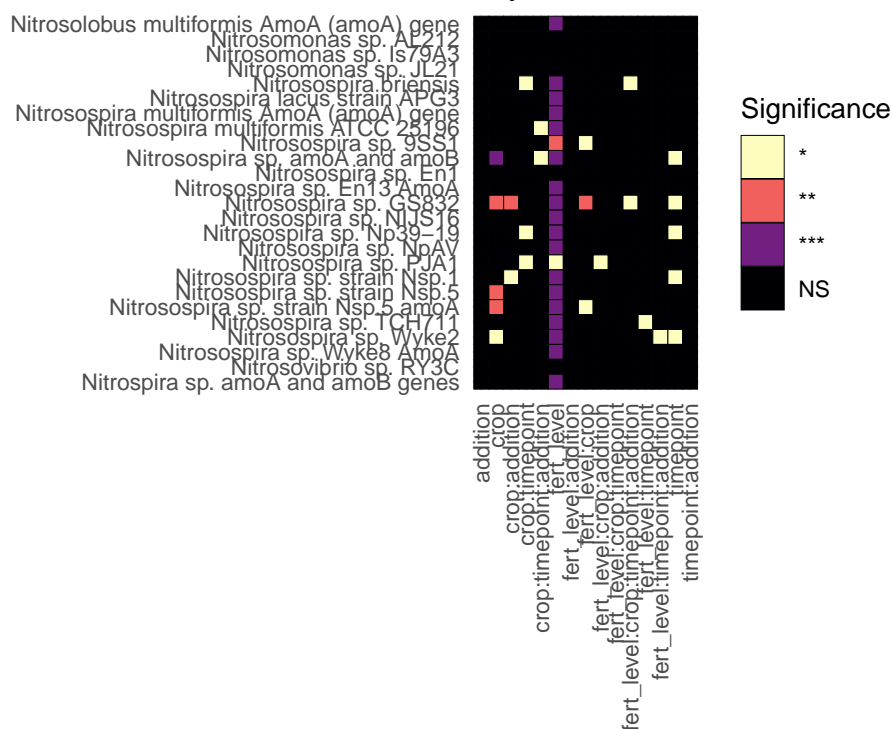
Visualizing the results again:

```

anova_results.counts %>%
  left_join(org_table, by = c("gene" = "cleaned_names")) %>%
  mutate(sig = case_when(
    p.value < 0.05 & p.value > 0.01 ~ "*",
    p.value < 0.01 & p.value > 0.001 ~ "**",
    p.value < 0.001 ~ "***",
    TRUE ~ "NS"
  )) %>%
  ggplot(aes(term, bbh, fill = sig)) +
  geom_tile(color = "black") +
  labs(y = "",
       x = "",
       title = "Summary of ANOVA results",
       fill = "Significance ") +
  theme(
    plot.title = element_text(hjust = 0.5),
    axis.text.x = element_text(angle = 90, hjust = 1, vjust = 0.5),
    axis.text.y = element_text()
  ) +
  scale_fill_viridis_d(option = "magma", direction = -1) +
  scale_y_discrete(limits = rev) +
  coord_equal()

```

Summary of ANOVA results



We see the same pattern at the organism level as when we did this at the gene level: fertilization level is by far the most significant factor affecting Presence/Absence of organisms.

Blair, R., A. Kjuchukova, R. Velazquez, and P. Villanueva. 2020. "Wirtinger Systems of Generators of Knot Groups." *Communications in Analysis and Geometry* 28 (2): 243–62. <https://doi.org/10.4310/cag.2020.v28.n2.a2>.