

A large, two-story, light-colored building with a red-tiled roof and a central tower, surrounded by green grass and trees under a clear blue sky.

# MAHARISHI UNIVERSITY of MANAGEMENT

*Engaging the Managing Intelligence of Nature*

## Computer Science Department

**CS390 Fundamental Programming  
Practices (FPP)  
Professor Paul Corazza**

# Lecture 9:

## Stacks and Queues

# Wholeness of the Lesson

Stacks and Queues are, essentially, a special kind of list with a highly restricted interface that permits rapid insertion and rapid access to elements, according to a "last in, first out" (Stacks) or "first in, first out" (Queues) scheme. These data structures express the Maharishi Vedic Science principle that creation emerges in the collapse of infinity to a point.

# The STACK ADT

- **Definition:** A STACK is an ordered collection of objects in which insertions and deletions can occur relative to just one designated position (called the *top of the stack*).
- **Example of a Stack in the Real World:**



a stack of dishes

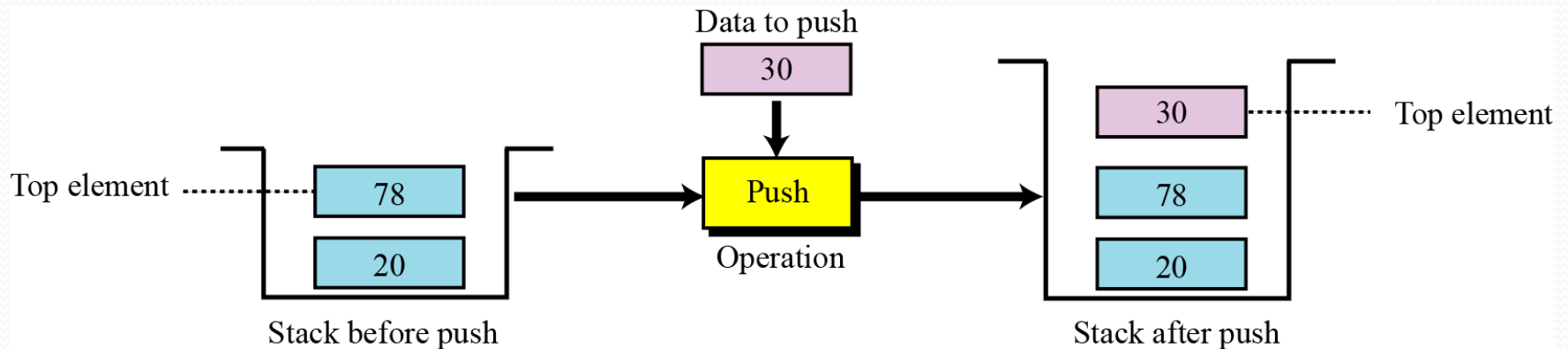
# The STACK ADT

- **Operations:**

pop	remove top of the stack and return this object
push	insert object as new top of stack
peek	view object at top of the stack without removing it

# The STACK ADT

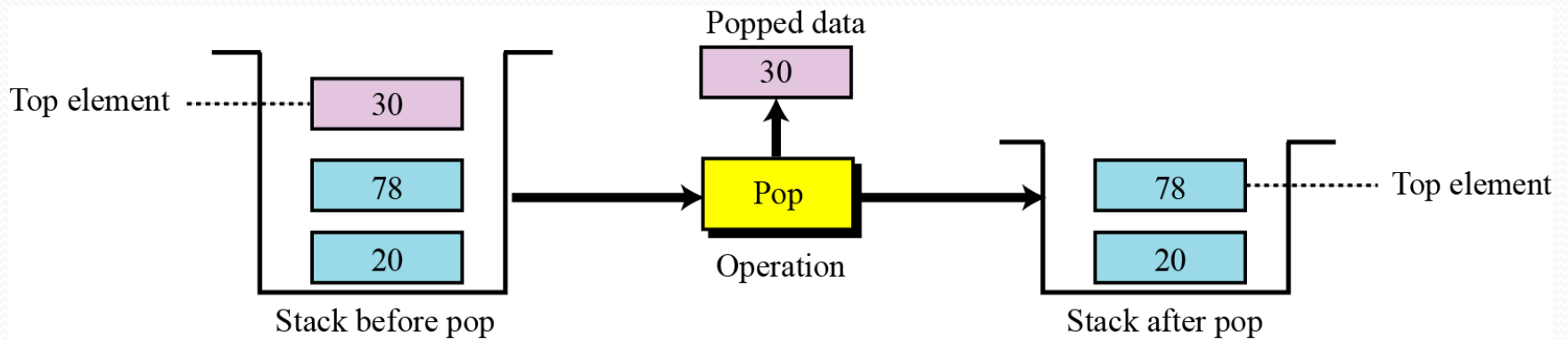
- **push operation:**





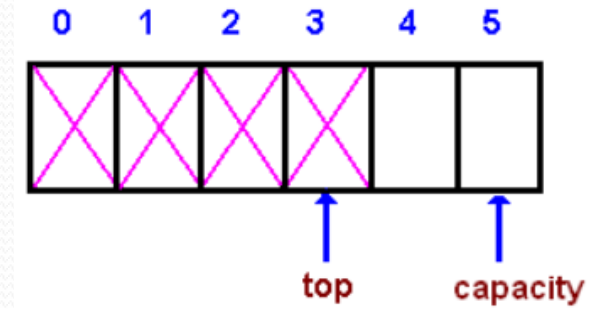
# The STACK ADT

- **pop operation:**



# Implementation of STACK Using an Array

- **Usual strategy:** Designate the rightmost array element to be the top of the stack.
- **Detail:** To avoid traversing the array in search of the current top of the Stack, maintain a pointer to the rightmost element (the "top").
- **Advantage:**
  - Avoids the usual cost of copying array elements that is required in insertion and deletion of arbitrary array elements
- **Disadvantage:**
  - If usage requires many more pushes than pops, the underlying array will have to be resized often, and this is costly.
- **Best Practice:** If resizing might become necessary, choose a different implementation



```
public class ArrayStack {
    /* Assumption: the stack will never become full */
    private static final int LEN = 500;
    private int top = -1;
    private int nextOpen = 0;
    private Integer[] arr = new Integer[LEN];

    public void push(Integer x) {
        if(x == null) return;
        arr[nextOpen] = x;
        top++;
        nextOpen++;
    }

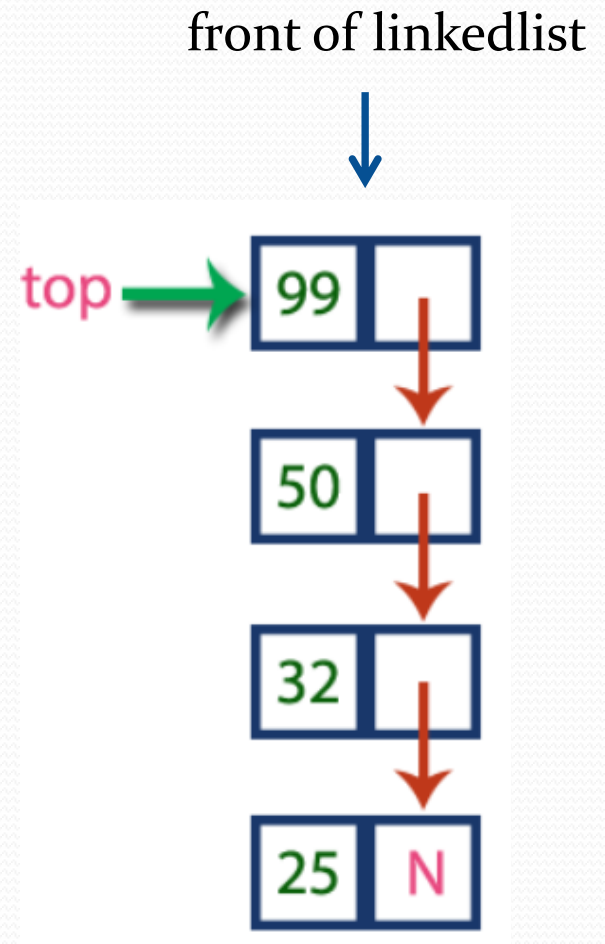
    public Integer peek() {
        //returns null if stack is empty
        return (top == -1) ? null : arr[top];
    }

    public Integer pop() {
        Integer ret = peek();
        if(ret != null) {
            arr[top] = null;
            top--;
            nextOpen--;
        }
        return ret;
    }
}
```



# Implementation of STACK Using a LinkedList

- The usual `addFirst` operation in a Java `LinkedList` adds the new element to the front of the list. Therefore, an object `S` can be pushed onto a Java `LinkedList` linked with the call `linked.addFirst(S)`
- The `peek` operation is equivalent to *find0th* (in a Java `LinkedList`, it is the call `get(0)`).
- The `pop` operation is equivalent to `remove(0)` (which returns the element removed).
- *Note:* This `LinkedList` implementation is essentially the same as the Node-based implementation, but hides the underlying Node operations behind the `LinkedList` API (see next slide)



# Exercise 9.1: Implementing a Stack with a Node

Implement the stack operations in NodeStack (see the startup code in InClassExercises project).

```
public class Node {
    String data;
    Node next;

    @Override
    public String toString() {
        if(data == null) return "";
        StringBuilder sb = new StringBuilder(data + " ");
        sb = toString(sb, next);
        return sb.toString();
    }
    private StringBuilder toString(StringBuilder sb, Node n) {
        if(n == null) return sb;
        sb.append(n.data + " ");
        return toString(sb, n.next);
    }
}
```

```
public class NodeStack {
    private Node top;

    public void push(String s) {
        //implement
    }
    public String peek() {
        return null;
    }
    public String pop() {
        return null;
    }
}
```

# Exercise 9.1 - Solution

```
public class Node {
    String data;
    Node next;

    @Override
    public String toString() {
        if(data == null) return "";
        StringBuilder sb = new StringBuilder(data + " ");
        sb = toString(sb, next);
        return sb.toString();
    }
    private StringBuilder toString(StringBuilder sb, Node n) {
        if(n == null) return sb;
        sb.append(n.data + " ");
        return toString(sb, n.next);
    }
}
```

```
public class NodeStack {
    private Node top;
    public void push(String s) {
        Node newTop = new Node();
        newTop.data = s;
        newTop.next = top;
        top = newTop;
    }
    public String peek() {
        if(top != null) {
            return top.data;
        }
        else {
            return null;
        }
    }
    public String pop() {
        if(top != null) {
            String s = peek();
            top = top.next;
            return s;
        }
        else {
            return null;
        }
    }
}
```

# Java's Implementation of Stack

- The Java distribution comes with a `Stack` class, which is a subclass of `Vector`.
- `Vector` is an array-based implementation of `List`. Therefore, for implementations that require many more pushes than pops, a stack based on a `LinkedList` or on `Nodes` would be preferable. (NOTE: As discussed in MPP, a `Stack` is not truly a subclass of either `Vector` or `LinkedList` since it should not support all the operations of these classes. Better to use composition instead of inheritance.)
- Lab: Implement your own class `MyStringStack` that uses `MyStringLinkedList`.

# Application of Stacks: Symbol Balancing

- A Stack can be used to check whether all occurrences of symbol pairs (for symbol pairs like (), [], {}) are properly matched and occur in the correct order.
- This type of check is part of what the Java compiler does when it scans Java code.
- Simple Example:
  - {a, b, f(c)} – balanced
  - {a, b, f(c)) – not balanced

## Another Example:

```
class MyClass {  
    String[] strings;  
    MyClass() {  
        strings = new String[3];  
    }  
}
```

Removing non-bracketing characters produces:

{ [] () { [] } }

This string of symbols is "balanced".

# Symbol Balancing (cont)

- Here are some valid and some invalid strings of brackets (with all text removed)

VALID INPUTS	INVALID INPUTS
{ }	{ ( }
( { [ ] } )	( [ ( ( ) ] )
{ [ ] ( ) }	{ } [ ] )

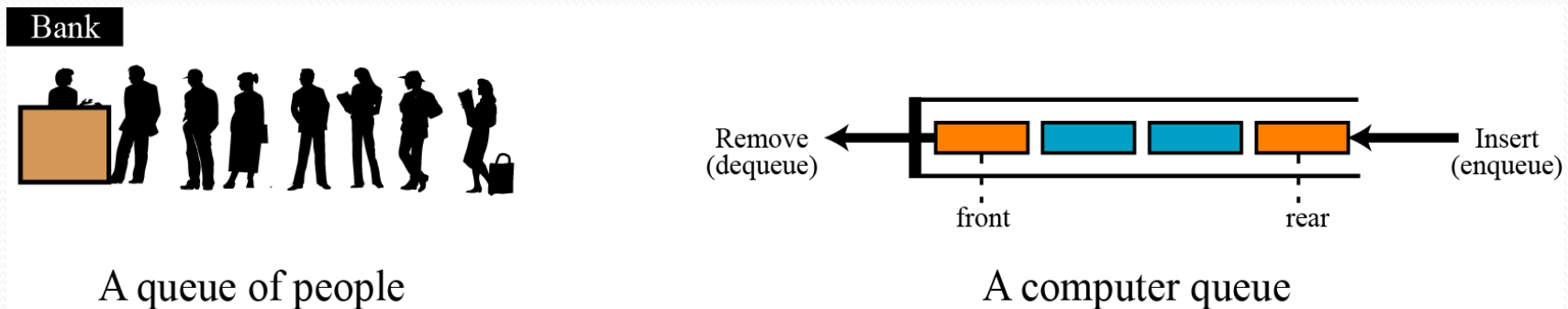


# Symbol Balancing Algorithm

- The following procedure can be used:
  - Begin with an empty Stack
  - Scan the text (will ignore all non-bracketing symbols)
  - When an open symbol (like '(' or '[' ) is read, push it
  - When a closed symbol (like ')' or ']' ) is read, pop the Stack –
    - i. if the stack is empty (so it can't be popped) return false.
    - ii. if the popped symbol doesn't match the symbol just read, return false.
  - After scanning is complete, if the Stack is not empty, return false.
- See `Symbol Balancer Demo.pdf`

# The QUEUE ADT

- **Definition.** Like a STACK, a QUEUE is a specialized LIST in which insertions may occur only at a designated position (the *back* or *rear*) and deletions may occur only at a designated position (the *front*).



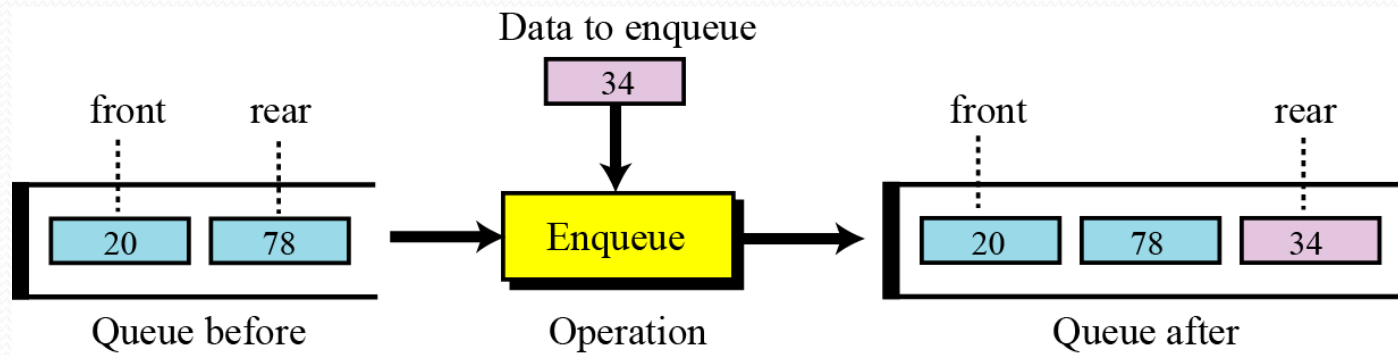
# The QUEUE ADT

- **Operations:**

dequeue	remove and return the element at the front
enqueue	insert object at the back
peek	view object at front of queue without removing it

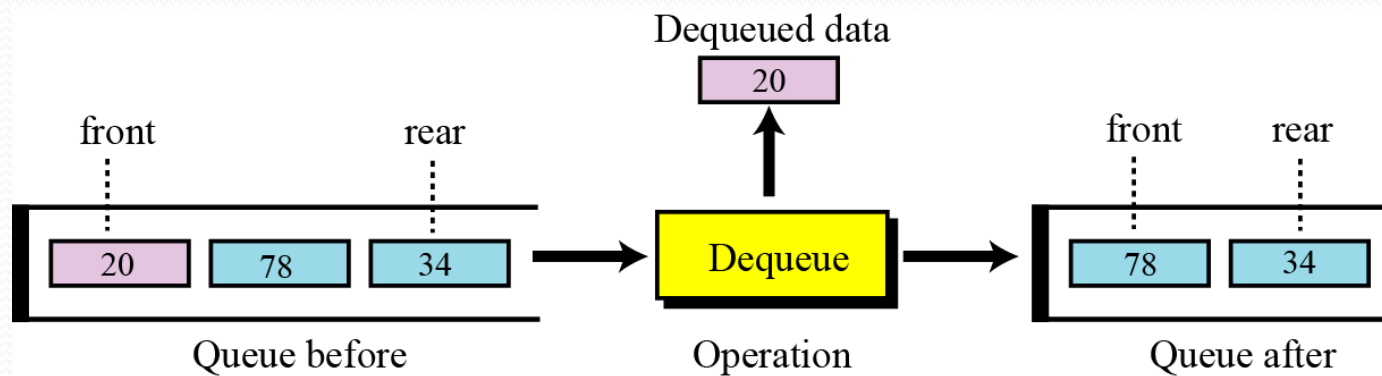
# The QUEUE ADT

- **enqueue operation:**

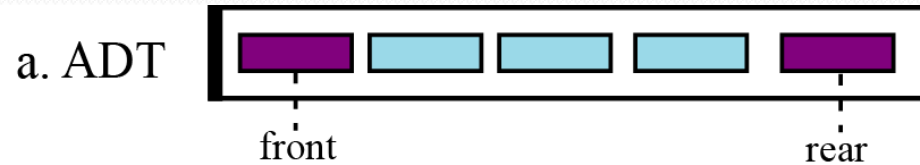


# The QUEUE ADT

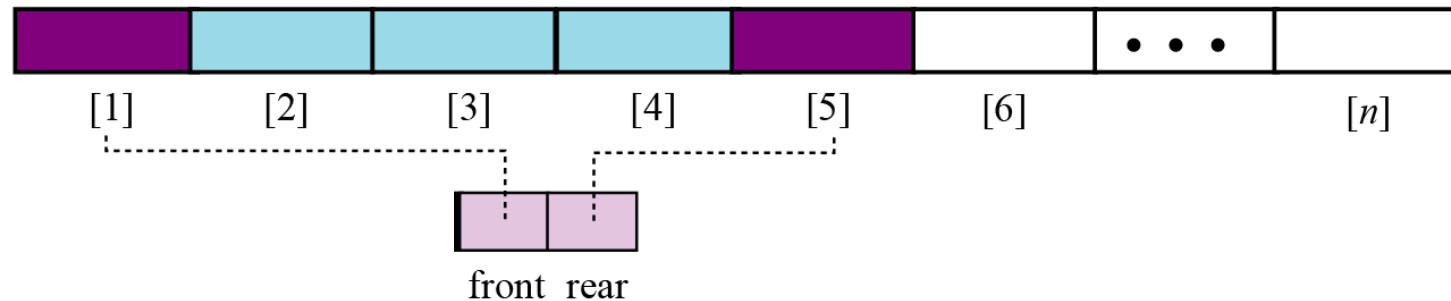
- **dequeue operation:**



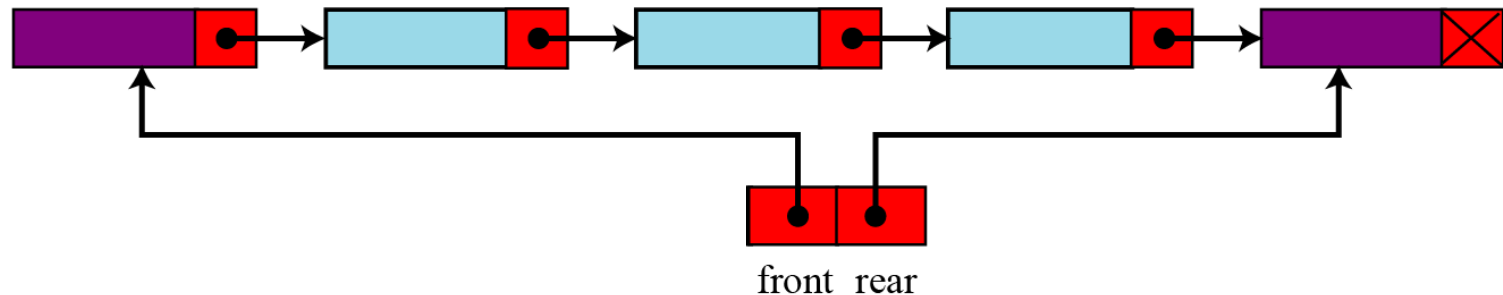
# Implementations of QUEUES



b. Array implementation



c. Linked list implementation





# Implementations of QUEUES

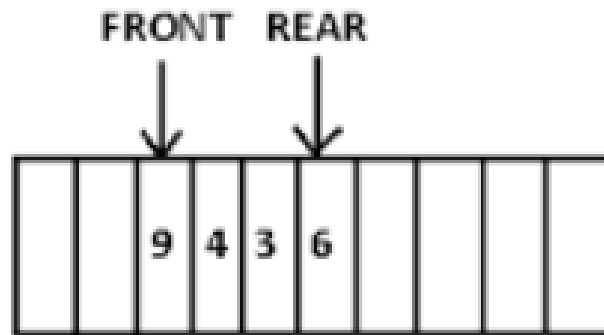
- **Using a Linked List**

- The enqueue operation is equivalent to adding each element to the end of a LinkedList.
- The dequeue operation is equivalent to removing the element at the front of a LinkedList.
- It is possible to implement a queue using Nodes, as we did with stack. See the labs.

# Implementations of QUEUES

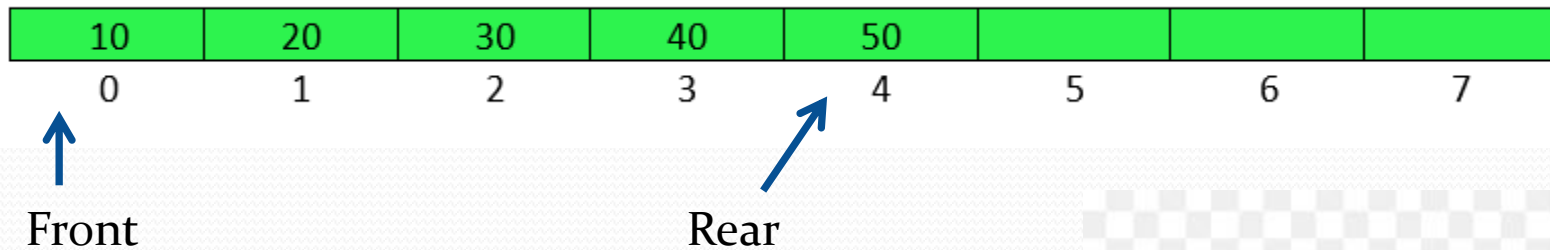
- **Using an Array**

- Need to maintain pointers to front and back elements

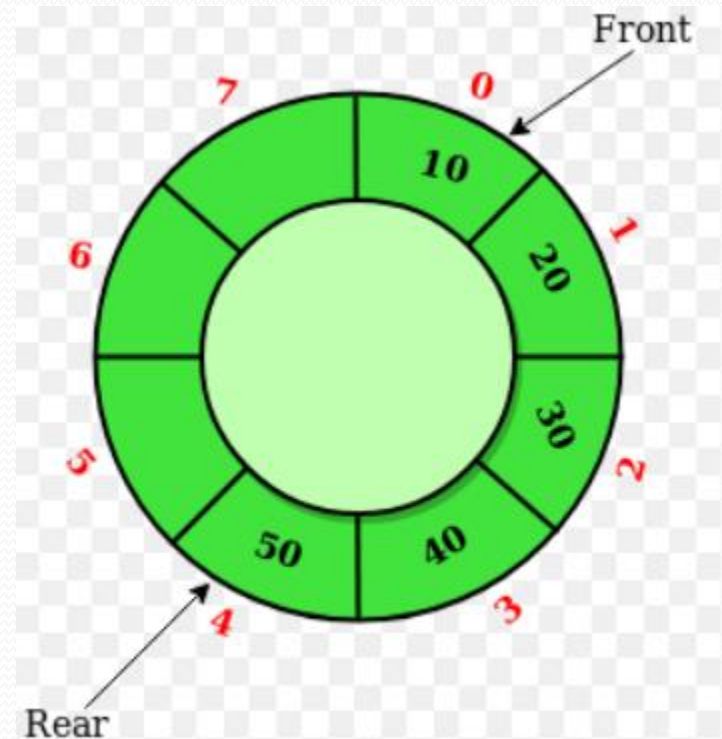


- Repeated enqueueing will fill the right half of the array prematurely—solution is a *circular queue*.

# Circular Queue



Linear queue as  
a circular queue



## Java's Implementation

In j2se5.0, an interface `Queue<E>` (implemented by `LinkedList<E>`) is provided, with these declared operations:

- `E peek()` – returns but does not remove the front of the queue
- `void add(E obj)` – same as `enqueue`
- `E remove()` – returns and removes the front of the queue (same as `dequeue`)

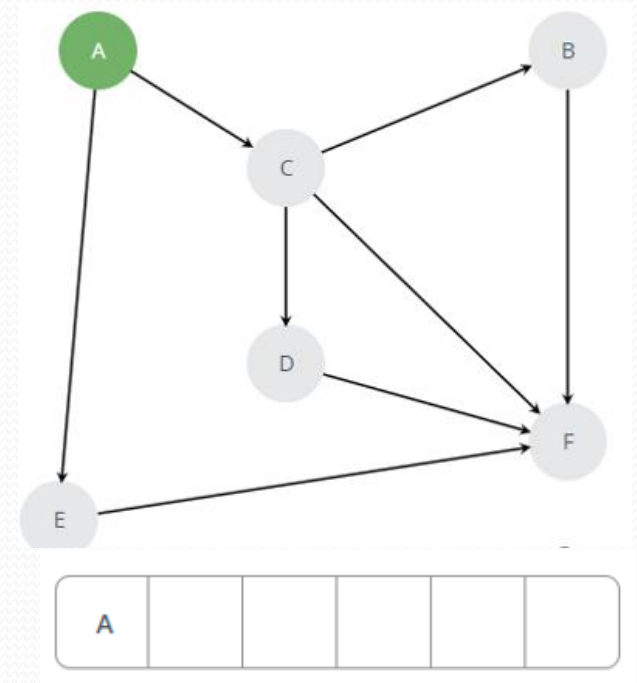
NOTE: Once again, a queue should not be considered a subclass of `LinkedList` since queues should not support all the operations of a list. A better design would use composition instead of inheritance (or instead of interface implementation).

# Application of Queues: Breadth First Search

Breadth First Search is a strategy for visiting every vertex in a graph.

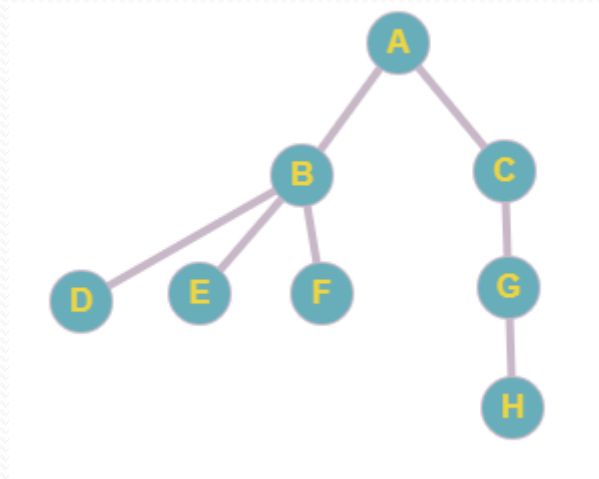
<https://www.hackerearth.com/practice/algorithms/graphs/breadth-first-search/visualize/>

*Idea.* Pick a starting vertex. Visit every adjacent vertex. Then take each of those vertices in turn and visit every one of its adjacent vertices. And so forth. Use a Queue to keep track of recently visited vertices.



## Exercise 9.2

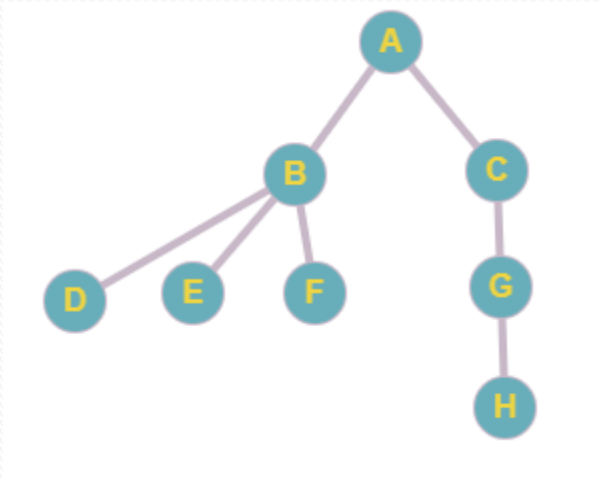
Without using a queue, write down the vertices in the order in which the BFS algorithm will visit them, starting from vertex A, and choosing adjacent vertices in alphabetical order





# Exercise 9.2 - Solution

Without using a queue, write down the vertices in the order in which the BFS algorithm will visit them, starting from vertex A, and choosing adjacent vertices in alphabetical order



A, B, C, D, E, F, G, H

# Breadth First Search Algorithm

**Algorithm:** Breadth First Search (BFS)

**Input:** A graph  $G = (V, E)$

**Output:**  $G$ , with all vertices marked as visited.

Initialize a queue  $Q$

Pick a starting vertex  $s$  and mark  $s$  as visited

$Q.add(s)$

while  $Q \neq \emptyset$  do

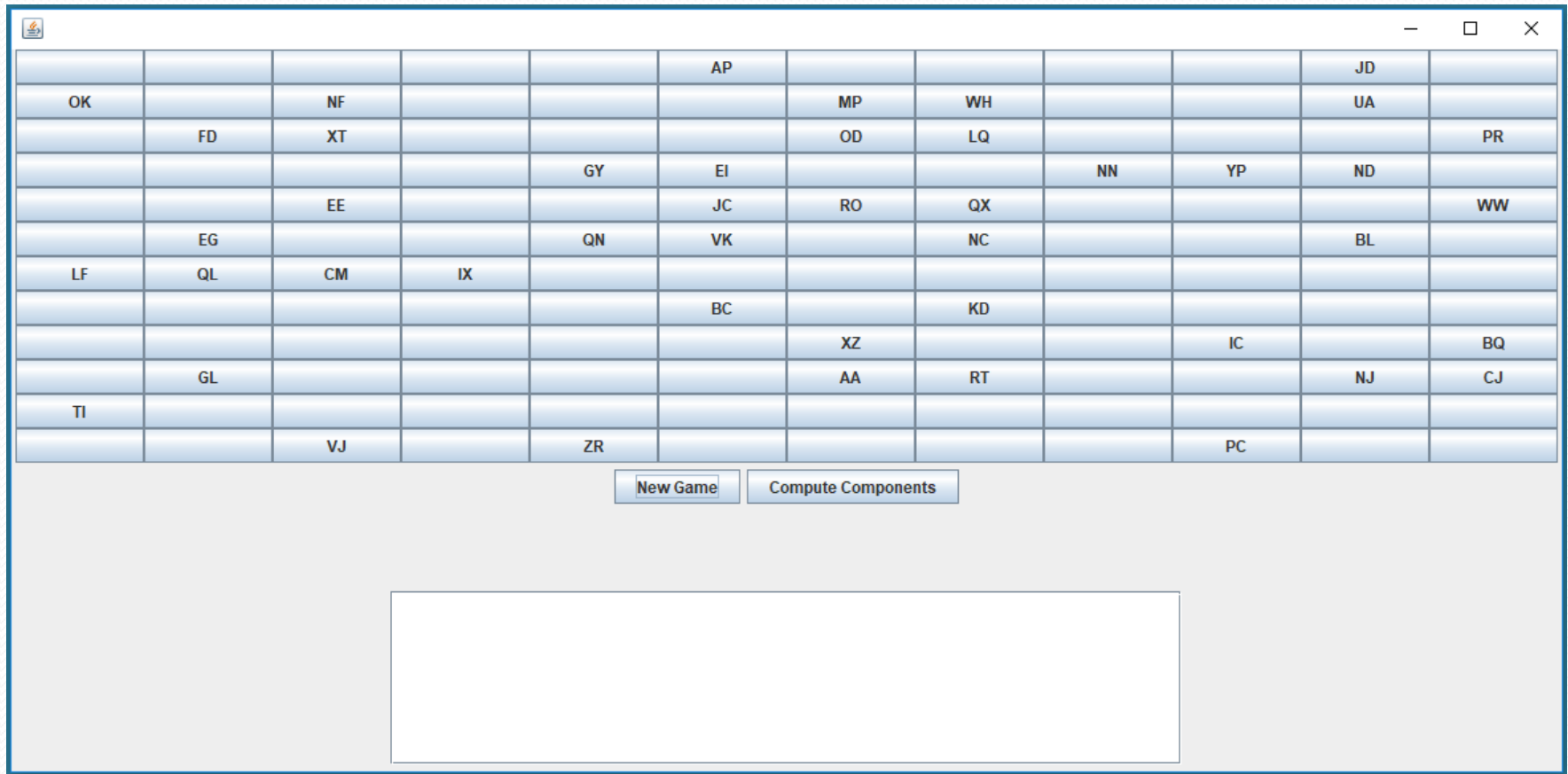
$v \leftarrow Q.dequeue()$

    for each unvisited  $w$  adjacent to  $v$  do

        mark  $w$  //adds  $w$  to  $X$ , the “pool” of marked vertices

$Q.add(w)$

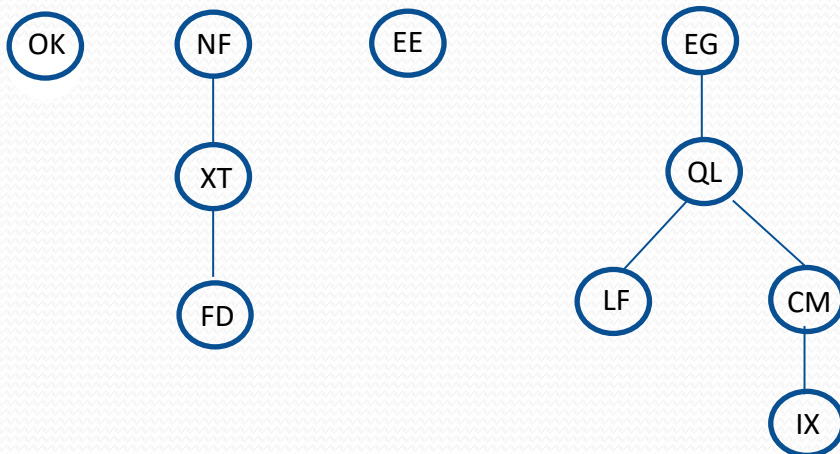
# The Queue Game



(see queueGame.jar)

# Solving the Queue game with BFS

OK		NF	
	FD	XT	
		EE	
	EG		
LF	QL	CM	IX



1. Represent the board with its occupied cells as a graph. An occupied cell is a vertex in the graph. Adjacent occupied cells will be treated as adjacent vertices.
2. Start with some occupied cell, viewed as a vertex, and perform BFS. When finished, the first component has been discovered.
3. Move to an unvisited occupied cell (viewed as a vertex again). Perform BFS. When finished, the second component has been discovered.
4. Continue till no unvisited vertices remain.

# Main Point

The Stack ADT is a special ADT that supports insertion of an element at “the top” and the removal of the top element, by way of operations *push* and *pop*, respectively. Similarly, the Queue ADT is a special ADT that supports insertion of an element at “the rear” (called *enqueueing*) and removal of an element from the “front” (called *dequeueing*). Both ADT’s, when implemented properly, are extremely efficient. Sun provides a Stack class and a Queue interface in its Collections API.

Stacks and Queues make use of the Maharishi Vedic Science principle that the dynamism of creation arises in the concentration of dynamic intelligence to a point value ("collapse of infinity to a point"); stacks and queues achieve their high level of efficiency by concentrating on a single point of input (top of stack or rear of queue) and a single point of output (top of stack or front of queue).

# Connecting the Parts of Knowledge With the Wholeness of Knowledge

*Collapse of infinity to a point embodied in Stacks and Queues*

1. Lists may be used as an all-purpose collection class. Nearly any need for storing collections of objects can be met by using some kind of list, though in some cases, other choices of data structures could improve performance. Lists have a more "unbounded" range of applicability.
  2. Stacks and Queues are extremely specialized data structures, designed to accomplish (primarily) two operations with optimum efficiency. These data structures have a restricted range of applicability that is like a "point".
- 
3. **Transcendental Consciousness:** Transcendental Consciousness is the unbounded value of awareness.
  4. **Wholeness moving within itself:** In Unity Consciousness, creation is seen as the interaction of unboundedness and point value: the unbounded collapses to its point value; point value expands to infinity; all within the wholeness of awareness.

