

Comp 411  
Principles of Programming Languages  
Lecture 13  
The Semantics of Recursive Let

Corky Cartwright  
February 8, 2023

# The Semantics of Recursive Binding

- Let's add the recursive binding construct **letrec** (akin to **let**) to LC where we restrict right-hand sides to  $\lambda$ -expressions (which is the only useful case for unary **letrec**).
- The Scheme code for the AST is:

```
(define-struct rec-let (lhs ; variable  
                      rhs ; a  $\lambda$ -expression  
                      body))
```

where **lhs** is the new local variable, **rhs** is the lambda-expression defining the value of the new variable, and **body** is an expression that can use the new local variable. The new variable **lhs** is visible in both **rhs** and **body** in both **rhs** and **body**. The code for it in the interpreter might look like:

```
((rec-let? M) (MEval (rec-let-body M)  
                    (extend env  
                          (rec-let-lhs M)  
                          (make-closure (rec-let-rhs M) <E>))))
```

- Problem: how should **<E>** expand into code? The environment should be the enclosing **(extend ...)** expression.

# How Can We Construct This Circular Environment?

Let's treat environments abstractly.

We need to build an environment **E** such that

```
E = (extend env
      (rec-let-lhs M)
      (make-closure (rec-let-rhs M) E)))
```

What is wrong with the following Scheme code?

```
(define E (extend env
                  (rec-let-lhs M)
                  (make-closure (rec-let-rhs M) E)))
```

Does the value of **E** satisfy the equation above?



# OO Representations for Environments

- If an environment is represented by an OO class or interface, it can include whatever methods are appropriate. Methods such as printing, equality testing (not an issue in our interpreters) and iteration (not currently an issue in our interpreters since mutation is forbidden) can easily be included. Moreover, deferred evaluation can be incorporated (if desired) in the interface. For example, a **Binding** interface might have both eager (call-by-value) and lazy (call-by-name) subclasses.
- On the other hand, poorly designed OO interfaces can be just as opaque as functions. Consider the standard command pattern interface which has only one method (command invocation).

# Question to Ponder

- Can we eliminate  $\lambda$  if we include the right functional constants (combinators) in our language?
- Haskell Curry preferred combinators to explicit  $\lambda$ -notation. The former are algebraic (can be interpreted as functions) while the latter is not. Schoenfinkel and (later) Curry independently discovered combinators before Church invented the  $\lambda$ -calculus.