

CSCI - B 551: Assignment #1

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Problem 1

Solution to Question 1 will be in the folder *problem1*
Abstraction

Problem 2

15 puzzle Problem Abstraction:

- **Initial State:** A random/user input state with 15 tiles on the board, each occupying exactly one place on the board. No duplicates are allowed. The board may often times be unsolvable.
- **Goal State:** Tiles arranged in the correct order from 1 to 15 and the blank space at the end after the 15th tile, wherein one tile exactly occupies one place.

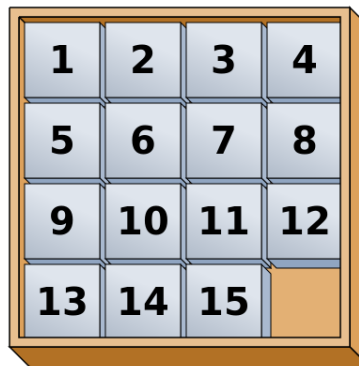


Figure 1: A Solved Board

- **Valid State:** Any state generated by the successor() is valid, where each tiles occupies exactly one place.
- **Successor Functions:** Through each state there are 4 possible states, wherein the tile can slide D, U, R, L into the empty place. Technically only 3 would be good to use depending upon the previous state, otherwise you would be replicating the parent state by moving back in the same position. Eg: If your parent is L, then moving in the Right direction would lead you back to the same state, hence we can eliminate that.
- **Cost Functions:** Cost Function is the cost of travelling from one state to another which is 1 for each movement. Also we use a heuristic to estimate the length of the goal which helps us get to the solution quicker than the brute force way.

Implementation Details: Try to make your solver as fast as possible. Which heuristic functions did you try, and which works best?

- We tried three different heuristics:
 - **Hamming Distance:** This heuristic calculates the number of misplaced tiles. In other words, all it does is that it checks whether if a tile is in its location, if not adds 1 to the cost. This is **not** a particularly good estimate of how far are we from the solution. The idea of a heuristic is to estimate the distance from the goal which in turn allows us to select a good probable path. Even though this is admissible since it does not overestimate the cost, it duly underestimates it most of the times.
 - **Permutation Inversion:** This heuristic particularly checks for inversion, which means it checks how many pairs are out of order. This is often times **not admissible** and hence can be discarded, since heuristic functions do not allow us to overestimate the distance to the goal.

- **Manhattan Distance:** This heuristic calculates the steps for each tile to reach its correct position when no other tiles is on the table. This is the **best of the three**, since it does not over estimate but also gives us a fair amount of idea as to how far are we from the solution.
- We implemented A search algorithm to find the optimal path to the solution, code would be present in the *problem2* folder.
- Tests carried for professors input, we obtain a path of 24 steps (LLUURULULDRDRDRRULDRUUUL) within about 2 seconds (0:00:02.189130) on our local machines. There are various test cases we tried, some take a while and some happen quickly, it fairly depends upon the complexity of the input.

Problem 3

The Marriage Problem Abstraction:

- **Monte Carlo Descent**

- **State Space:** Represented by an M-element vector, where the index of each element corresponds to a certain guest, and each element has a non-negative integer as its value corresponding to the index of the table where the guest are seated. M is the total number of the guests.
- **Initial State:** No guests have been seated in any table, represented by an m-element vector where each element is set to 0, which means that the corresponding guest has not been seated in any table yet.
- **Goal State:** Every guest has been seated in a table and the number of the tables is as least as possible, represented by an m-element vector where no elements are 0 and the maximum element is as least as possible.
- **Cost Function:** It equals to the number of the tables.
- **Successor function:** Assign a table to a guest who has not been seated yet, given the condition that
 1. This new state is never visited before
 2. After assigning, the number of guests in the assigned table will not exceed a given number N, and
 3. Guests in that table do not know each other before. item It is represented by assigning a positive integer P to an element which is currently 0, and making sure that after assigning
 - * The new state is not in our visited state records.
 - * The number of P in the vector will not exceed N.
 - * Guests with the index that has an element of P do not know each other.
- **Edge Weights:** It will equal 0 or 1. If after assigning, there will be one more table, then edge weight equals to 1. Otherwise, if the number of tables do not change, the edge weight equals to 0.
- **Heuristic Function:** It equals to the number of the tables,. Since we directly take the cost function as the heuristic function, it must be admissible.

$$h(s) = \text{number of tables}$$

- **A Search**

References

1. [15 Puzzle solved image](#)
2. [Something Linky](#)
3. [Something Linky](#)