

Statistics Assignment 4

Problem statement 1:

Is gender independent of education level? A random sample of 395 people were surveyed & each person was asked to report the highest education level they obtained. The data that resulted from the survey is summarized in following tabel.

	High school	Bachelors	Masters	ph.d	Total
Female	60	54	46	41	201
Male	40	44	53	57	194
Total	100	98	99	98	395

Question: Are gender & education level dependent at 5% level of significance? In other words, given the data collected above is there a relationship between the gender of an individual & the level of education that they have obtained?

→ expected counts:

	High school	Bachelors	Masters	ph.d	Total
Female	50.886	49.868	50.377	49.868	201
Male	49.114	48.132	48.623	48.132	194
Total	100	98	99	98	395

$$\chi^2 = \frac{(60 - 50.886)^2}{50.886} + \frac{(45 - 48.132)^2}{48.132} + \frac{(51 - 48.132)^2}{48.132}$$

$$= 8.006$$

The critical value of χ^2 with 3 degree of freedom is 7.815. Since $8.006 > 7.815$ we reject null hypothesis & conclude that education level depends on gender at 5% level of significance.

problem statement 2.

Using the following data perform a oneway analysis of variance using $\alpha = 0.5$ write up the results in APA format.

[Group 1: 51, 45, 33, 45, 61]

[Group 2: 23, 43, 23, 43, 65]

[Group 3: 56, 76, 74, 81, 56]

	Group 1	Group 2	Group 3
51	23	56	
45	43	76	
33	23	74	
45	43	81	
61	65	56	
Mean	48.2	35.4	69.8

Group 1

	value	mean	deviations	sq. deviations
	51	48.2	2.8	7.84
	45	48.2	-3.2	10.24
	33	48.2	-15.2	231.04
	45	48.2	-3.2	10.24
	61	48.2	12.8	163.84
SS				612.8

Group 2

	value	mean	deviations	sq. deviations
	23	35.4	-12.4	153.76
	43	35.4	7.6	57.76
	23	35.4	-12.4	153.76
	43	35.4	7.6	57.76
	45	35.4	9.6	92.16
SS				515.2

Group 3

	value	mean	deviations	sq. deviations
	56	69.8	-13.8	190.44
	76	69.8	6.2	38.44
	74	69.8	4.2	17.64
	87	69.8	17.2	295.84
	56	69.8	-13.8	190.44
SS				732.8

$$\text{Mean square [Error or within group]} = 155.07$$

$$\text{degree of freedom [Error or within group]} = 12$$

$$\text{sum of squares [Within Group]} = 1800.8$$

Problem statement 3

calculate F Test for given 10, 20, 30, 40, 50 &
5, 10, 15, 20, 25 for 10, 20, 30, 40, 50

Ans \Rightarrow variance for 1st set

$$(N) = (10, 20, 30, 40, 50)$$

$$(N) = 5$$

$$\text{Mean} = (x_1 + x_2 + x_3 + \dots + x_n) / N$$

$$\text{Mean} = \frac{150}{5} = 30$$

$$SD = \sqrt{(1/(N-1)) * ((x_1 - x_m)^2 + (x_2 - x_m)^2 + \dots)}$$

$$= \sqrt{(1/(5-1))((10-30)^2 + (20-30)^2 + (30-30)^2 + (40-30)^2 + (50-30)^2)}$$

$$= \sqrt{(1/4)((-20)^2 + (-10)^2 + (0)^2 + (10)^2 + (20)^2)}$$

$$= \sqrt{(1/4)(400 + 100 + 0 + 100 + 400)}$$

$$= \sqrt{250}$$

$$= 15.8114$$

$$\text{Variance} = SD^2$$

$$\text{Variance} = 15.8114^2$$

$$\text{Variance} = 250$$

Variance of second set

for 5, 10, 15, 20, 25

$$(N) = (5, 10, 15, 20, 25)$$

$$(N) = 5$$

$$\text{Mean} = (x_1 + x_2 + x_3 + \dots + x_N) / N$$

$$\frac{75}{5} = 15$$

$$SD = \sqrt{\frac{1}{(N-1)} [(x_1 - \bar{x}_m)^2 + (x_2 - \bar{x}_m)^2 + \dots + (x_N - \bar{x}_m)^2]}$$

$$= \sqrt{\frac{1}{(5-1)} [(5-15)^2 + (10-15)^2 + (15-15)^2 + (20-15)^2 + (25-15)^2]}$$

$$= \sqrt{\frac{1}{4} [(-10)^2 + (-5)^2 + (0)^2 + (5)^2 + (10)^2]}$$

$$= \sqrt{\frac{1}{4} [100 + 25 + 0 + 25 + 100]}$$

$$= \sqrt{62.5}$$

$$= 7.9057$$

$$\text{Variance} = SD^2$$

$$= (7.9057)^2$$

$$= 62.5$$

F-Test

$$F\text{-Test} = (\text{Variance } 1^{\text{st}}) / (\text{Variance } 2^{\text{nd}})$$

$$= 250 / 62.5$$

$$= 4$$