

LAB 09 :

Perform Knapsack problem using Dynamic programming technique using $n=4$ objects with associated weights and profits .

Display the table values and the objects selected in the knapsack to get maximum profit.

CODE:

```
#include <stdio.h>

#define MAX_OBJECTS 100

// Function to calculate maximum of two integers
int max(int a, int b) {
    return (a > b) ? a : b;
}

// Function to solve 0/1 Knapsack problem using Dynamic Programming
void knapsack(int n, int W, int weights[], int profits[]) {
    int i, w;
    int K[MAX_OBJECTS + 1][W + 1]; // DP table to store results

    // Build DP table K[][] in bottom-up manner
    for (i = 0; i <= n; i++) {
        for (w = 0; w <= W; w++) {
            if (i == 0 || w == 0)
                K[i][w] = 0;
            else if (weights[i - 1] <= w)
                K[i][w] = max(profits[i - 1] + K[i - 1][w - weights[i - 1]], K[i - 1][w]);
            else
                K[i][w] = K[i - 1][w];
        }
    }

    // Print DP table
    printf("DP Table:\n");
    for (i = 0; i <= n; i++) {
        for (w = 0; w <= W; w++) {
            printf("%d\t", K[i][w]);
        }
        printf("\n");
    }

    // Maximum profit will be at K[n][W]
    int maxProfit = K[n][W];
}
```

```

printf("Maximum profit: %d\n", maxProfit);

// To find the selected items
printf("Objects selected in the knapsack:\n");
int res = maxProfit;
w = W;
for (i = n; i > 0 && res > 0; i--) {
    if (res == K[i - 1][w])
        continue;
    else {
        printf("Object %d (weight = %d, profit = %d)\n", i, weights[i - 1], profits[i - 1]);
        // Move to the previous item considering its weight
        res -= profits[i - 1];
        w -= weights[i - 1];
    }
}
}

int main() {
    int n, W;
    int weights[MAX_OBJECTS], profits[MAX_OBJECTS];
    int i;

    // Input number of objects
    printf("Enter number of objects (max %d): ", MAX_OBJECTS);
    scanf("%d", &n);

    if (n <= 0 || n > MAX_OBJECTS) {
        printf("Invalid number of objects\n");
        return 1;
    }

    // Input weights of objects
    printf("Enter the weights of the objects:\n");
    for (i = 0; i < n; i++) {
        scanf("%d", &weights[i]);
    }

    // Input profits of objects
    printf("Enter the profits of the objects:\n");
    for (i = 0; i < n; i++) {
        scanf("%d", &profits[i]);
    }

    // Input knapsack capacity
    printf("Enter the capacity of the knapsack: ");

```

```

scanf("%d", &W);

if (W <= 0) {
    printf("Invalid knapsack capacity\n");
    return 1;
}

knapsack(n, W, weights, profits);

return 0;
}

```

OUTPUT:

```

Enter number of objects (max 100): 4
Enter the weights of the objects:
2 1 3 2
Enter the profits of the objects:
12 10 20 15
Enter the capacity of the knapsack: 5
DP Table:
0      0      0      0      0      0
0      0      12     12     12     12
0      10     12     22     22     22
0      10     12     22     30     32
0      10     15     25     30     37
Maximum profit: 37
Objects selected in the knapsack:
Object 4 (weight = 2, profit = 15)
Object 2 (weight = 1, profit = 10)
Object 1 (weight = 2, profit = 12)

Process returned 0 (0x0)   execution time : 21.922 s
Press any key to continue.
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```

2. Pfa of the Prims algorithm pseudo code please try to convert this into C program and find the MST of a Given graph with cost adjacency matrix as input.

```

#include <stdio.h>
#include <limits.h>

#define MAX_VERTICES 100
#define INF INT_MAX // Infinity

// Function to find vertex with minimum distance value from the set of vertices not yet
// included in MST
int minKey(int n, int d[], int s[]) {
    int min = INF, min_index;

    for (int v = 0; v < n; v++) {
        if (s[v] == 0 && d[v] < min) {
            min = d[v];
            min_index = v;
        }
    }

    return min_index;
}

// Function to print MST using parent array and calculate total cost
int printMST(int n, int p[], int cost[MAX_VERTICES][MAX_VERTICES]) {
    int total_cost = 0;
    printf("Edge  Weight\n");
    for (int i = 1; i < n; i++) {
        printf("%d - %d  %d \n", p[i], i, cost[i][p[i]]);
        total_cost += cost[i][p[i]];
    }
    return total_cost;
}

// Function to implement Prim's MST algorithm
void primMST(int n, int cost[MAX_VERTICES][MAX_VERTICES]) {
    int p[MAX_VERTICES]; // Array to store constructed MST
    int d[MAX_VERTICES]; // Key values used to pick minimum weight edge in cut
    int s[MAX_VERTICES]; // To represent set of vertices included in MST

    // Initialize all keys as INFINITE
    for (int i = 0; i < n; i++) {
        d[i] = INF;
        s[i] = 0;
    }
}

```

```

// Start with the first vertex as source
d[0] = 0;    // Make key 0 so that this vertex is picked as first vertex
p[0] = -1;   // First node is always root of MST

// The MST will have n vertices
for (int count = 0; count < n - 1; count++) {
    // Pick the minimum key vertex from the set of vertices not yet included in MST
    int u = minKey(n, d, s);

    // Add the picked vertex to the MST set
    s[u] = 1;

    // Update key value and parent index of the adjacent vertices of the picked vertex.
    // Consider only those vertices which are not yet included in MST
    for (int v = 0; v < n; v++) {
        // Update the key only if cost[u][v] is smaller than d[v]
        if (cost[u][v] && s[v] == 0 && cost[u][v] < d[v]) {
            p[v] = u;
            d[v] = cost[u][v];
        }
    }
}

// Print the constructed MST and calculate total cost
int total_cost = printMST(n, p, cost);
printf("Total cost of Minimum Spanning Tree (MST): %d\n", total_cost);
}

int main() {
    int n;
    int cost[MAX_VERTICES][MAX_VERTICES];

    // Input number of vertices
    printf("Enter number of vertices (max %d): ", MAX_VERTICES);
    scanf("%d", &n);

    // Input the cost adjacency matrix
    printf("Enter the cost adjacency matrix (use %d for infinity):\n", INF);
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            scanf("%d", &cost[i][j]);
            if (cost[i][j] == 0 && i != j) { // Diagonal elements remain zero
                cost[i][j] = INF; // Replace zero with infinity
            }
        }
    }
}

```

```
// Apply Prim's algorithm to find Minimum Spanning Tree
printf("Minimum Spanning Tree (MST) using Prim's algorithm:\n");
primMST(n, cost);

return 0;
}
```

OUTPUT:

```
Enter number of vertices (max 100): 4
Enter the cost adjacency matrix (use 2147483647 for infinity):
0 2 6 8
2 0 3 5
6 3 0 2147483647
8 5 2147483647 0
Minimum Spanning Tree (MST) using Prim's algorithm:
Edge   Weight
0 - 1   2
1 - 2   3
1 - 3   5
Total cost of Minimum Spanning Tree (MST): 10

Process returned 0 (0x0)   execution time : 94.923 s
Press any key to continue.
```