

# Assignment-5

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**Abstract**—In this work, we estimate the area of triangle with vector representation.

Download all latex-tikz codes from

[https://github.com/poojah15/EE5609\\_AI20MTECH14003/tree/master/Assignment\\_5](https://github.com/poojah15/EE5609_AI20MTECH14003/tree/master/Assignment_5)

## 1 PROBLEM STATEMENT

Prove that the triangles on the same base (or equal bases) and between the same parallels are equal in area.

## 2 SOLUTION

Let ABC and ABD are the given triangles with the same base **AB** and between the same parallel lines **AB** and **CD**.

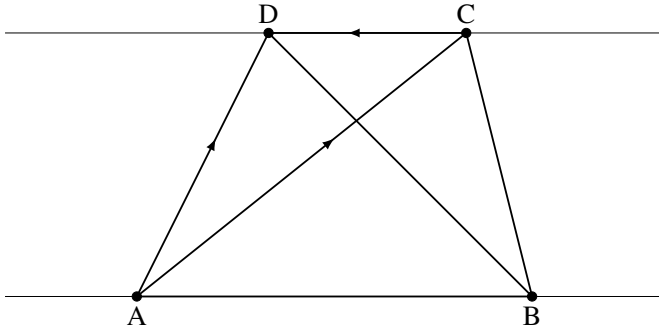


Fig. 1: Triangles on same base

The area of  $\triangle ABC$  is given by

$$Area(\triangle ABC) = \frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times (\mathbf{A} - \mathbf{C})\| \quad (2.0.1)$$

Since  $\mathbf{CD} \parallel \mathbf{AB}$ ,

$$\mathbf{C} - \mathbf{D} = k(\mathbf{A} - \mathbf{B}) \quad (2.0.2)$$

Hence, the area of  $\triangle ABD$  is given by

$$\frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times (\mathbf{A} - \mathbf{D})\| \quad (2.0.3)$$

$$= \frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times \{(\mathbf{A} - \mathbf{C}) + (\mathbf{C} - \mathbf{D})\}\| \quad (2.0.4)$$

$$= \frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times \{(\mathbf{A} - \mathbf{C}) + k(\mathbf{A} - \mathbf{B})\}\| \quad (2.0.5)$$

$$= \frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times (\mathbf{A} - \mathbf{C}) + k(\mathbf{A} - \mathbf{B}) \times (\mathbf{A} - \mathbf{B})\| \quad (2.0.6)$$

$$= \frac{1}{2} \|(\mathbf{A} - \mathbf{B}) \times (\mathbf{A} - \mathbf{C})\| [\because \mathbf{A} \times \mathbf{A} = 0] \quad (2.0.7)$$

From (2.0.1) and (2.0.7), we can infer that the area of two triangles are one and the same. Hence, it is proved that the triangles on the same base and between the same parallels are equal in area.