



$$T_0 = 20^\circ\text{C}$$

Initial value of T_1, T_2, T_3 in tank

$$T_1 = 50^\circ\text{C}, \quad T_2 = 50^\circ\text{C}, \quad T_3 = 50^\circ\text{C}$$

given,

$$UA = 10 \text{ kJ/min}^\circ\text{C}$$

$$C_p = 2 \text{ kJ/kg}^\circ\text{C}$$

$$W = 100 \text{ kg/min}$$

$$T_s = 250^\circ\text{C}$$

Mass present inside the tank is constant

$$M_1 = M_2 = M_3 = M$$

from Energy Balance,

$$\frac{d}{dt} (MC_p T_1) = WC_p (T_0 - T_1) + UA (T_s - T_1)$$

$$\frac{d}{dt} (MC_p T_2) = WC_p (T_1 - T_2) + UA (T_s - T_2)$$

$$\frac{d}{dt} (MC_p T_3) = WC_p (T_2 - T_3) + UA (T_s - T_3)$$

(a) The dynamic Model Equations are :-

$$\frac{dT_1}{dt} = \frac{W}{M} (T_0 - T_1) + \frac{UA}{M C_p} (T_s - T_1) \quad \text{--- (1)}$$

$$\frac{dT_2}{dt} = \frac{W}{M} (T_1 - T_2) + \frac{UA}{M C_p} (T_s - T_2) \quad \text{--- (2)}$$

$$\frac{dT_3}{dt} = \frac{W}{M} (T_2 - T_3) + \frac{UA}{M C_p} (T_s - T_3) \quad \text{--- (3)}$$

(b) At steady state $\frac{d}{dt} \rightarrow 0$

$$\frac{dT_1}{dt} = \frac{dT_2}{dt} = \frac{dT_3}{dt} = 0$$

$$f_1: W C_p (T_0 - T_1) + UA (T_s - T_1) = 0$$

$$f_2: W C_p (T_1 - T_2) + UA (T_s - T_2) = 0$$

$$f_3: W C_p (T_2 - T_3) + UA (T_s - T_3) = 0$$

solving the above eqns using solve in MATLAB.