

## Modifications to input files:

### CLASS:

#### Vertex.java:

Functions added:

// this method gives incident edge list for preflow push

```
public LinkedList getIncidentEdgeList()
{
    return this.incidentEdgeList;
}
```

// this method adds a new edge to incident edges list for a vertex.

```
public void addToIncidentEdgeList(Edge e) throws Exception
{
    boolean isAddSuccessful = this.incidentEdgeList.add(e);
    if(!isAddSuccessful)
    {
        throw new Exception("Error in adding an edge");
    }
}
```

#### Edge.java:

1. Removed a line code in *insertEdge* method

**Reason:** The below code line is removed as the inserting an edge adding the incident edges to both sides.

**Line removed:** w.incidentEdgeList.addLast(e);

**Method:** public Edge insertEdge(Vertex v, Vertex w, Object data, Object name)

**Old code:** public Edge insertEdge(Vertex v, Vertex w, Object data, Object name) {

```
    Edge e;
    e = new Edge(v, w, data, name);
    edgeList.addLast(e);
    v.incidentEdgeList.addLast(e);
    w.incidentEdgeList.addLast(e);
    return e;
}
```

**New code:** public Edge insertEdge(Vertex v, Vertex w, Object data, Object name) {

```
    Edge e;
    e = new Edge(v, w, data, name);
    edgeList.addLast(e);
    v.incidentEdgeList.addLast(e);
    // w.incidentEdgeList.addLast(e);
    return e;
}
```

## 2) Constructor :

**Line added :** this.getFirstEndpoint().getIncidentEdgeList().add(this);

**Old code :**

```
public Edge (Vertex v, Vertex w, Object data, Object name) {
    this.data = data;
    this.name = name;
    this.v1 = v;
```

```

        this.v2 = w;
    }

    New Code :
    public Edge (Vertex v, Vertex w, Object data, Object name) {
        this.data = data;
        this.name = name;
        this.v1 = v;
        this.v2 = w;
        this.getFirstEndpoint().getIncidentEdgeList().add(this);
    }

```

### Structure of the code:

**FordFulkerson.java** : This class computes the maximum flow in a network.

**Scaling FordFulkerson.java**: This class used to compute the max flow of a network. This implementation of algorithm exposes a method to calculate maximum flow of the input graph.

**VertexEdge.java** : This class contains the attributes vertex and Edge and the constructor which is used in FordFulkerson class.

**PreFlowPush.java** : This class computes the maximum flow in a network.

**tc543.java**: This class contains the main function of the project

### Name each routine and describe in 1-2 sentences what each routine does

#### Class : Ford Fulkerson:

**Method: bfs**-This method finds whether there is an augmented path in the graph. It uses Breadth First Search algorithm to find the path

**Method: edgeBetweenVertices** - This method returns an edge connecting the 2 vertices

**Method: fordFulkerson** - This method returns the maximum flow in the graph. It finds all the available augmented paths in the graph.

#### Class: VertexEdge

The class contains a constructor and getters.

#### Class : FordFulkersonScaling

**Method : bfsWithScaling**- Breadth First Search to find the path (s->t) with edge weights more than the min\_weight provided.

**Method : edgeBetweenVertices**- Gets edge connecting start vertex(v) to end vertex(w) and return Edge v->w if exists else null.

**Method: calculateScalingParam**- Calculates scaling parameter of the input Graph based on the edge weights and returns the scaling parameter value for the graph.

**Method : calculateMaxFlow** - This method takes in a graph as input and returns the max flow of the input graph using FordFulkerson Scaling algorithm. This method also measures the time taken in milliseconds to compute the max flow.

## Class : Preflow Push

**Method : PreFlowPush-** Constructor for loading the input graph in a Hash table.

**Method : initPreflowPush-** Initializes the heights and excess associated with vertices and Capacity and flow associated with edges. Gets a linked list of incident edges from GraphCode and forms residual graphs. This method is a void function and takes in the hash table(graph) as input.

**Method: computeMaxFlow-** This method does not take input and outputs the max flow using Preflow Push algorithm. This method measure the time taken in milliseconds while computing the max flow.

## Output :

### Fixed Degree Graphs

#### Fixed Graph 1: Number of Vertices Vs Average Runtime

| No. of vertices | No.of outgoing edges | min capacity | max capacity | Input.txt | Max Flow | Runtime in(ms)Ford Fulkerson | Runtime(ms)-Scaling Ford Fulkerson | Runtime in(ms) PrePush |
|-----------------|----------------------|--------------|--------------|-----------|----------|------------------------------|------------------------------------|------------------------|
| 20              | 10                   | 1            | 20           | f20       | 101      | 15                           | 3                                  | 20                     |
| 40              | 10                   | 1            | 20           | f40       | 110      | 28                           | 10                                 | 14                     |
| 60              | 10                   | 1            | 20           | f60       | 117      | 24                           | 12                                 | 17                     |
| 80              | 10                   | 1            | 20           | f80       | 109      | 32                           | 12                                 | 127                    |
| 100             | 10                   | 1            | 20           | f100      | 99       | 25                           | 19                                 | 215                    |

#### Fixed Degree Graph 2: Number of outgoing edges Vs Average Runtime

| No. of vertices | No.of outgoing edges | min capacity | max capacity | Input.txt | Max Flow | Runtime in(ms)Ford Fulkerson | Runtime(ms)-Scaling Ford Fulkerson | Runtime in(ms) PrePush |
|-----------------|----------------------|--------------|--------------|-----------|----------|------------------------------|------------------------------------|------------------------|
| 120             | 20                   | 1            | 220          | fe_20     | 3455     | 168                          | 105                                | 195                    |
| 120             | 40                   | 1            | 220          | fe_40     | 3902     | 213                          | 138                                | 1399                   |
| 120             | 60                   | 1            | 220          | fe_60     | 6834     | 311                          | 212                                | 2590                   |
| 120             | 80                   | 1            | 220          | fe_80     | 8553     | 381                          | 345                                | 4578                   |
| 120             | 100                  | 1            | 220          | fe_100    | 9988     | 563                          | 443                                | 6495                   |

### Fixed Degree Graph 3 : Maximum Capacity Vs Average Runtime

| No. of vertices | No.of outgoing edges | min capacity | max capacity | Input.txt | Max Flow | Runtime in(ms)Ford Fulkerson | Runtime(ms)-Scaling Ford Fulkerson | Runtime in(ms) PrePush |
|-----------------|----------------------|--------------|--------------|-----------|----------|------------------------------|------------------------------------|------------------------|
| 120             | 10                   | 1            | 200          | fc_100    | 678      | 56                           | 20                                 | 46                     |
| 120             | 10                   | 1            | 400          |           | 1991     | 44                           | 27                                 | 427                    |
| 120             | 10                   | 1            | 600          |           | 2695     | 37                           | 27                                 | 28                     |
| 120             | 10                   | 1            | 800          |           | 4111     | 59                           | 26                                 | 363                    |
| 120             | 10                   | 1            | 1000         |           | 4741     | 41                           | 25                                 | 384                    |

### Random graphs:

#### Random Graph 1 : Number of Vertices Vs Average Runtime

| Number of vertices | Dense value | min capacity | max capacity | Input.txt | Max Flow | Ford Fulkerson | Scaling Ford Fulkerson | Preflow |
|--------------------|-------------|--------------|--------------|-----------|----------|----------------|------------------------|---------|
| 20                 | 80          | 1            | 20           | r20       | 151      | 17             | 7                      | 29      |
| 40                 | 80          | 1            | 20           | r40       | 290      | 52             | 40                     | 232     |
| 60                 | 80          | 1            | 20           | r60       | 423      | 81             | 58                     | 677     |
| 80                 | 80          | 1            | 20           | r80       | 551      | 150            | 85                     | 1706    |
| 100                | 80          | 1            | 20           | r100      | 777      | 199            | 207                    | 1182    |
| 120                | 80          | 1            | 20           | r120      | 1016     | 187            | 216                    | 2519    |

#### Random Graph 2 : Maximum Capacity Vs Average Runtime

| Different range of capacities |             |              |              |           |          |                |                        |         |
|-------------------------------|-------------|--------------|--------------|-----------|----------|----------------|------------------------|---------|
| Number of vertices            | Dense value | min capacity | max capacity | Input.txt | Max Flow | Ford Fulkerson | Scaling Ford Fulkerson | Preflow |
| 40                            | 80          | 1            | 100          | r101      | 1354     | 54             | 30                     | 90      |
| 40                            | 80          | 1            | 1000         | r102      | 12853    | 53             | 37                     | 235     |
| 40                            | 80          | 1            | 3000         | r106      | 37126    | 48             | 34                     | 245     |
| 40                            | 80          | 1            | 6000         | r107      | 68171    | 46             | 32                     | 271     |
| 40                            | 80          | 1            | 10000        | r103      | 144830   | 80             | 36                     | 296     |
| 40                            | 80          | 1            | 100000       | r104      | 1402127  | 46             | 43                     | 199     |
| 40                            | 80          | 1            | 1000000      | r105      | 13242013 | 58             | 33                     | 88      |

### Random Graph 3 : Density Vs Average Runtime

| the number of vertices in the graph | enter dense value | min - the lower bound on edge capacities | max - the upper bound on edge capacities | Input.txt | Max Flow | Running time-FF | Running time-FFS | Running time-Preflow |
|-------------------------------------|-------------------|--|--|-----------|----------|-----------------|------------------|----------------------|
| 100                                 | 30                | 10                                       | 100                                      | graph8    | 1422     | 95              | 67               | 88                   |
| 100                                 | 60                | 10                                       | 100                                      | graph9    | 3041     | 256             | 201              | 239                  |
| 100                                 | 90                | 10                                       | 100                                      | graph10   | 4401     | 369             | 348              | 862                  |
| 100                                 | 100               | 10                                       | 100                                      | graph11   | 5267     | 437             | 397              | 1353                 |

### Bipartite Graphs outputs-

**Table1- number of vertices vs run time and varying min and max capacity**

| nodes on source | nodes on sink | probability | min cap | max cap | input.txt | max flow FF/SFF/PPA | Runtime FF | Runtime SFF | Runtime PPA | total vertices |
|-----------------|---------------|-------------|---------|---------|-----------|---------------------|------------|-------------|-------------|----------------|
| 10              | 10            | 1           | 10      | 20      | result1   | 145                 | 31         | 0           | 47          | 20             |
| 20              | 10            | 1           | 20      | 30      | result2   | 232                 | 18         | 6           | 94          | 30             |
| 30              | 20            | 1           | 40      | 50      | result3   | 904                 | 92         | 31          | 486         | 50             |
| 70              | 30            | 1           | 50      | 60      | result4   | 1667                | 140        | 78          | 4011        | 100            |
| 100             | 100           | 1           | 100     | 120     | result5   | 10884               | 644        | 341         | 12107       | 200            |
| 100             | 150           | 1           | 5       | 50      | result6   | 2368                | 725        | 468         | 4698        | 400            |
| 200             | 200           | 1           | 5       | 50      | result7   | 5370                | 2528       | 2410        | 36730       | 400            |

**Table 2- Increasing and varying the maximum capacity vs runtime**

| Nodes on source side | Nodes on sink side | probability | min capacity | max capacity | Input.txt  | Max Flow | Runtime(ms)-Ford Fulkerson | Runtime(ms)-Scaling Ford Fulkerson | Runtime-Preflow |
|----------------------|--------------------|-------------|--------------|--------------|------------|----------|----------------------------|------------------------------------|-----------------|
| 10                   | 8                  | 1           | 2            | 50           | Bipartite1 | 194      | 16                         | 0                                  | 31              |
| 10                   | 8                  | 1           | 2            | 500          | Bipartite2 | 1774     | 0                          | 0                                  | 16              |
| 10                   | 8                  | 1           | 2            | 1000         | Bipartite3 | 3596     | 16                         | 16                                 | 31              |
| 10                   | 8                  | 1           | 2            | 10000        | bipartite4 | 3499     | 15                         | 0                                  | 16              |

**Table 3- varying the minimum capacity vs runtime**  
**Probability of 1**

| Nodes on source side | Nodes on sink side | probability | min capacity | max capacity | Input.txt  | Max Flow | Runtime(ms)-Ford Fulkerson | Runtime(ms)-Scaling Ford Fulkerson | Runtime-Preflow |
|----------------------|--------------------|-------------|--------------|--------------|------------|----------|----------------------------|------------------------------------|-----------------|
| 10                   | 8                  | 1           | 50           | 400          | bipartite5 | 2049     | 141                        | 0                                  | 62              |
| 10                   | 8                  | 1           | 100          | 400          | bipartite6 | 2131     | 31                         | 16                                 | 47              |
| 10                   | 8                  | 1           | 200          | 400          | bipartite7 | 2409     | 24                         | 16                                 | 19              |
| 10                   | 8                  | 1           | 300          | 400          | bipartite8 | 2640     | 0                          | 0                                  | 31              |

**Table4- minimum capacity vs runtime**  
**Probability of 0.2**

| Nodes on source side | Nodes on sink side | probability | min capacity | max capacity | Input.txt   | Max Flow | Runtime(ms)-Ford Fulkerson | Runtime(ms)-Scaling Ford Fulkerson | Runtime-Preflow |
|----------------------|--------------------|-------------|--------------|--------------|-------------|----------|----------------------------|------------------------------------|-----------------|
| 10                   | 8                  | 0.2         | 50           | 400          | bipartite9  | 1679     | 46                         | 27                                 | 172             |
| 10                   | 8                  | 0.2         | 100          | 400          | bipartite10 | 944      | 0                          | 3                                  | 16              |
| 10                   | 8                  | 0.2         | 200          | 400          | bipartite11 | 2281     | 15                         | 0                                  | 0               |
| 10                   | 8                  | 0.2         | 300          | 400          | bipartite12 | 1927     | 8                          | 0                                  | 5               |

## Mesh Graph - Outputs

**Table1 : Overall table with all the dimensions, runtimes of all the algorithms and Maxflow.**

| Input graphs | Dimensions | Capacity | Ford Fulkerson | Preflow Push | Scaling FF | Maxflow |
|--------------|------------|----------|----------------|--------------|------------|---------|
| mesh1.txt    | 40*20      | 30       | 370            | 1290         | 315        | 393     |
| mesh2.txt    | 40*20      | 20       | 356            | 2503         | 107        | 276     |
| mesh3.txt    | 40*20      | 40       | 368            | 1649         | 114        | 498     |
| mesh4.txt    | 40*20      | 50       | 426            | 1154         | 104        | 614     |
| mesh5.txt    | 40 * 10    | 50       | 216            | 392          | 195        | 656     |
| mesh6.txt    | 40 * 30    | 50       | 697            | 1226         | 134        | 671     |
| mesh7.txt    | 10*20      | 50       | 88             | 239          | 38         | 153     |
| mesh8.txt    | 50 * 20    | 50       | 586            | 2633         | 119        | 762     |
| mesh9.txt    | 100*100    | 60       | 17947          | 43283        | 2376       | 1948    |
| mesh10.txt   | 100*100    | 20       | 5073           | 140915       | 2238       | 662     |
| mesh11.txt   | 250*150    | 100      | 432868         | 35043085     | 27271      | 8070    |

**Table 2 : Capacity Varied keeping Dimensions constant**

| Input Graphs | Dimensions | Capacity | Runtime: ff | Runtime: ppf | Runtime: scaling ff |
|--------------|------------|----------|-------------|--------------|---------------------|
| mesh1.txt    | 40*20      | 20       | 356         | 2503         | 107                 |
| mesh2.txt    | 40*20      | 30       | 370         | 1290         | 315                 |
| mesh3.txt    | 40*20      | 40       | 368         | 1649         | 114                 |
| mesh4.txt    | 40*20      | 50       | 426         | 1154         | 104                 |

**Table 3 : Column dimension varied keeping Capacity and Row dimension constant**

| Input Graphs | Column dimn | Capacity | Runtime: ff | Runtime: ppf | Runtime: Scaling ff |
|--------------|-------------|----------|-------------|--------------|---------------------|
| mesh5.txt    | 40 * 10     | 50       | 216         | 392          | 195                 |
| mesh4.txt    | 40*20       | 50       | 426         | 1154         | 104                 |
| mesh6.txt    | 40 * 30     | 50       | 697         | 1226         | 134                 |

**Table 4 : Row Dimension varied keeping Capacity and Column dimension constant.**

| Input Graphs | Row dimn | Capacity | Runtime: ff | Runtime: ppf | Runtime: Scaling ff |
|--------------|----------|----------|-------------|--------------|---------------------|
| mesh7.txt    | 10*20    | 50       | 88          | 239          | 38                  |
| mesh4.txt    | 40*20    | 50       | 426         | 1154         | 104                 |
| mesh8.txt    | 50 * 20  | 50       | 586         | 2633         | 119                 |