

## Lab Experiment – 7

### GEA [Gene Expression Algorithm]

Lab - 7  
GEA

Gene expression Algorithm: 6 Main Phases.

- Initialisation
- Fitness Assignment.
- Selection
- Cross over
- Gene expression
- Termination

Steps: Fitness ( $x$ ) =  $x^2$

1) select encoding Technique: 0 - 31  
Use chromosome of fixed length with terminals (variables, constants and functions (+, -, \*, /)).

2) Initial Population:

S.NO	Initial chromosome	phenotype	Value	Fitness	P
1.	$x^2$	$x^2$	12	144	0.1297
2.	$+xx$	$2x$	25	625	0.541
3.	$x$	$x$	5	25	0.0216
4.	$-x$	$x-2$	19	361	0.8125

$\sum P(x) = 1155$   
Avg =  $288.75$

Actual cost	Exp. cost
1	0.5
2	2.1
0	0.08
1	1.25

### 3) Selection of Mating Pool.

S.No	selected chromosome	crossover point	offspring	Phenotype
1	*xx	2	*x+	$x^*(x+...)$
2	+xx	1	+xx	2x
3	+xx	3	+x-	$x+(x+...)$
4	-x2	1	+x2	$x+2$

$\alpha$  values Fitness

13	169
24	576
27	729
17	289

### 4) Crossover:

Perform crossover randomly chosen gene positions (not raw bits)

Max fitness after crossover = 729.

### 5) Mutation:

S.No	offspring before mutation	Mutation Applied	Offspring after mutation	Phenotype
1	*x+	+ $\rightarrow$ -	+x-	$x^*(x+...)$
2	+xx	None	+xx	2x
3	+x-	- $\rightarrow$ *	+x*	$x+(x+...)$
4	+x2	None	+x2	$x+2$

$\alpha$  value Fitness  $f(x)$

29	841
24	576
27	729
20	400

by Gene expression and evaluation:

Decode each genotype  $\rightarrow$  phenotype.

$$\sum f(x) = 841 + 576 + 729 + 400 = 2546$$

$$\text{Avg} = 636.5$$

$$\text{Max} = 841$$

1) Iterate until convergence:

Repeat step 3-6 until fitness improvement is negligible or generation limit has reached.

Pseudocode / Algorithm:

- \* Start
- \* Define Fitness function.
- \* Define parameters
- \* Select mating pool.
- \* Mutation after mating.
- \* Gene expression and evaluation.
- \* Iterate.
- \* Output best value.

Output:

Genes: [29.53, 29.82, 29.84, 28.57, 15.09,  
21.83, 23.43, 30.81, 22.51, 26.22].

$$x : 26.37$$

$$f(x) : 695.45$$

Output:

```
· Enter 4 chromosomes (each of 5 bits, e.g., '10101'):  
Chromosome 1: 01101  
Chromosome 2: 11000  
Chromosome 3: 11011  
Chromosome 4: 10001  
Generation 1: Best Fitness = 729, Best x = 27  
Generation 2: Best Fitness = 729, Best x = 27  
Generation 3: Best Fitness = 729, Best x = 27  
Generation 4: Best Fitness = 729, Best x = 27  
Generation 5: Best Fitness = 729, Best x = 27  
Generation 6: Best Fitness = 729, Best x = 27  
Generation 7: Best Fitness = 729, Best x = 27  
Generation 8: Best Fitness = 729, Best x = 27  
Generation 9: Best Fitness = 729, Best x = 27  
Generation 10: Best Fitness = 729, Best x = 27  
Generation 11: Best Fitness = 729, Best x = 27  
Generation 12: Best Fitness = 729, Best x = 27  
Generation 13: Best Fitness = 729, Best x = 27  
Generation 14: Best Fitness = 729, Best x = 27  
Generation 15: Best Fitness = 729, Best x = 27  
Generation 16: Best Fitness = 729, Best x = 27  
Generation 17: Best Fitness = 729, Best x = 27  
Generation 18: Best Fitness = 729, Best x = 27  
Generation 19: Best Fitness = 729, Best x = 27  
Generation 20: Best Fitness = 729, Best x = 27  
...  
Best solution found:  
Chromosome: 11011  
x = 27  
f(x) = 729
```

Code:

```
import random  
  
# Define the function to maximize  
def fitness_function(x):  
    return x ** 2  
  
# Convert binary string to integer  
def decode(chromosome):  
    return int(chromosome, 2)  
  
# Evaluate fitness for the entire population  
def evaluate_population(population):  
    return [fitness_function(decode(individual)) for individual in population]  
  
# Selection: Roulette Wheel
```

```

def select(population, fitnesses):
    total_fitness = sum(fitnesses)
    if total_fitness == 0:
        return random.choice(population)
    pick = random.uniform(0, total_fitness)
    current = 0
    for individual, fitness in zip(population, fitnesses):
        current += fitness
        if current > pick:
            return individual

```

# Crossover: Single-point crossover

```

def crossover(parent1, parent2):
    if random.random() < CROSSOVER_RATE:
        point = random.randint(1, CHROMOSOME_LENGTH - 1)
        return (parent1[:point] + parent2[point:], parent2[:point] + parent1[point:])
    return parent1, parent2

```

# Mutation: Flip random bit

```

def mutate(chromosome):
    new_chromosome = ''
    for bit in chromosome:
        if random.random() < MUTATION_RATE:
            new_chromosome += '0' if bit == '1' else '1'
        else:
            new_chromosome += bit
    return new_chromosome

```

# Get user input for initial population

```
def get_initial_population(size, length):
```

```
    population = []
```

```
    print(f"Enter {size} chromosomes (each of {length} bits, e.g., '10101'):")
```

```
    while len(population) < size:
```

```
        chrom = input(f"Chromosome {len(population)+1}: ").strip()
```

```
        if len(chrom) == length and all(bit in '01' for bit in chrom):
```

```
            population.append(chrom)
```

```
        else:
```

```
            print(f"Invalid input. Please enter a {length}-bit binary string.")
```

```
    return population
```

# Run the Genetic Algorithm

```
def genetic_algorithm():
```

```
    population = get_initial_population(POPULATION_SIZE, CHROMOSOME_LENGTH)
```

```
    best_solution = None
```

```
    best_fitness = float('-inf')
```

```
    for generation in range(GENERATIONS):
```

```
        fitnesses = evaluate_population(population)
```

```
        # Update best solution
```

```
        for i, individual in enumerate(population):
```

```
            if fitnesses[i] > best_fitness:
```

```
                best_fitness = fitnesses[i]
```

```
                best_solution = individual
```

```
        print(f"Generation {generation + 1}: Best Fitness = {best_fitness}, Best x =  
{decode(best_solution)}")
```

```
        new_population = []
```

```
        while len(new_population) < POPULATION_SIZE:
```

```
parent1 = select(population, fitnesses)
parent2 = select(population, fitnesses)
offspring1, offspring2 = crossover(parent1, parent2)
offspring1 = mutate(offspring1)
offspring2 = mutate(offspring2)
new_population.extend([offspring1, offspring2])
population = new_population[:POPULATION_SIZE]
print("\nBest solution found:")
print(f"Chromosome: {best_solution}")
print(f"x = {decode(best_solution)}")
print(f"f(x) = {fitness_function(decode(best_solution))}")

# Parameters
POPULATION_SIZE = 4
CHROMOSOME_LENGTH = 5
MUTATION_RATE = 0.01
CROSSOVER_RATE = 0.8
GENERATIONS = 20

# Run it
if __name__ == "__main__":
    genetic_algorithm()
```