PS5841

Data Science in Finance & Insurance

Poisson Regression

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Poisson Distribution

•
$$Y_i \sim Po(\mu_i), i = 1, ... N$$

$$f(y_i) = \frac{\mu_i^{y_i} e^{-\mu_i}}{y!}, y = 0,1,2, ...$$

$$l(\mu; y) = \sum_{i=1}^{N} [y_i \log(\mu_i) - \mu_i - \log y_i!]$$

Poisson Regression

$$E(Y_i) = \mu_i = n_i \theta_i$$
$$\log(\mu_i) = \log(n_i) + \mathbf{x}_i^T \boldsymbol{\beta}$$

Goodness of Fit (1)

Pearson chi-squared statistic

$$X^{2} = \sum_{i=1}^{n} \frac{(o_{i} - e_{i})^{2}}{e_{i}} \sim \chi^{2}(N - p)$$

Pearson residuals

$$r_i = \frac{o_i - e_i}{\sqrt{e_i}}$$

$$\sum_{i=1}^{N} r_i^2 = X^2$$

Goodness of Fit (2)

• Pseudo R^2

pseudo
$$R^2 = \frac{l(\widehat{\boldsymbol{\beta}}_{min}) - l(\widehat{\boldsymbol{\beta}})}{l(\widehat{\boldsymbol{\beta}}_{min})}$$

That was

