

## MATB42: Assignment #10

1. Let  $\mathbf{F}$  be a vector field on  $\mathbb{R}^3$  given by  $\mathbf{F} = (F_1, F_2, F_3)$  where  $F_1$ ,  $F_2$ , and  $F_3$  are  $C^1$ -functions from  $\mathbb{R}^3 \rightarrow \mathbb{R}$

- (a) Let  $\eta$  be the 2-form given by

$$\eta = F_3 \, dx \, dy + F_1 \, dy \, dz + F_2 \, dz \, dx$$

Show that  $d\eta = (\operatorname{div} \mathbf{F}) \, dx \, dy \, dz$

(page 489, #6)

$$\eta = F_3 \, dx \, dy + F_1 \, dy \, dz + F_2 \, dz \, dx \quad = d(F_3 \, dx \, dy + F_1 \, dy \, dz + F_2 \, dz \, dx)$$