

Asymptotic Notation and Analysis

4/4 questions correct

Excellent!

Retake

Next (/learn/data-structures-optimizing-performance/lecture/YBL2r/core-introduction-to-benchmarking)



1.

Consider the function $f(n) = 3 \log_2(n) + 4n \log_2(n) + n$. What is the tightest big O class for $f(n)$?

- ☐ $O(\log(n))$
- ☐ $O(n \log(n))$

Well done!

Since $\log_2(n)$ and n each grow more slowly than $n \log_2(n)$, the term $4n \log_2(n)$ dominates both the term $3 \log_2(n)$ and the term n . In asymptotic notation, keep only the dominant term and then drop the constants. Dropping the constants from $4n \log_2(n)$ gives $O(n \log(n))$.

- ☐ $O(n)$



2.

What is the big-O class of the number of operations executed when running the method below, where n is the size of `arr`? Remember, when we're talking about Big-O analysis, we only care what happens when n is very large, so don't worry that this method might have problems on small array sizes.

```
int sumTheMiddle(int[] arr) {
    int range = 100;
    int start = arr.length/2 - range/2;
    int sum = 0;
    for (int i=start; i< start+range; i++)
    {
        sum += arr[i];
    }
    return sum;
}
```

- ☐ $O(2^n)$
- ☐ $O(n^2)$
- ☐ $O(n)$
- ☐ $O(1)$

Well done!

Good! We are starting at a constant less than the middle of the array, and going to a constant more.



3.

What is the big-O class of the number of operations executed when running the method below, where n is the size of `arr`? Remember, when we're talking about Big-O analysis, we only care what happens when n is very large, so don't worry that this method might have problems on small array sizes. [[Notice that the only difference between this method and the one from the previous question is the initialization of the variable "range".]]

```
int sumTheMiddle(int[] arr) {
    int range = arr.length/100;
    int start = arr.length/2 - range/2;
    int sum = 0;
    for (int i=start; i< start+range; i++)
    {
        sum += arr[i];
    }
    return sum;
}
```

- ☐ $O(2^n)$

☐ $O(n^2)$

☐ $O(n)$

Well done!

Good! Now range is no longer a constant, so the size of the interval traversed by the for loop now depends on the length of the array.

☐ $O(1)$

 4.

If a piece of code runs in linear time, $O(n)$, what impact will doubling the input size have on the number of operations required to run?

☐ The number of operations will be roughly the same.

☐ The number of operations will roughly double.

Well done!

☐ The number of operation will grow, but you cannot say anything about by how much.
