

Machine Learning Systems

Lecture 10: Machine Learning System Stack

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Machine Learning Systems Ecosystem

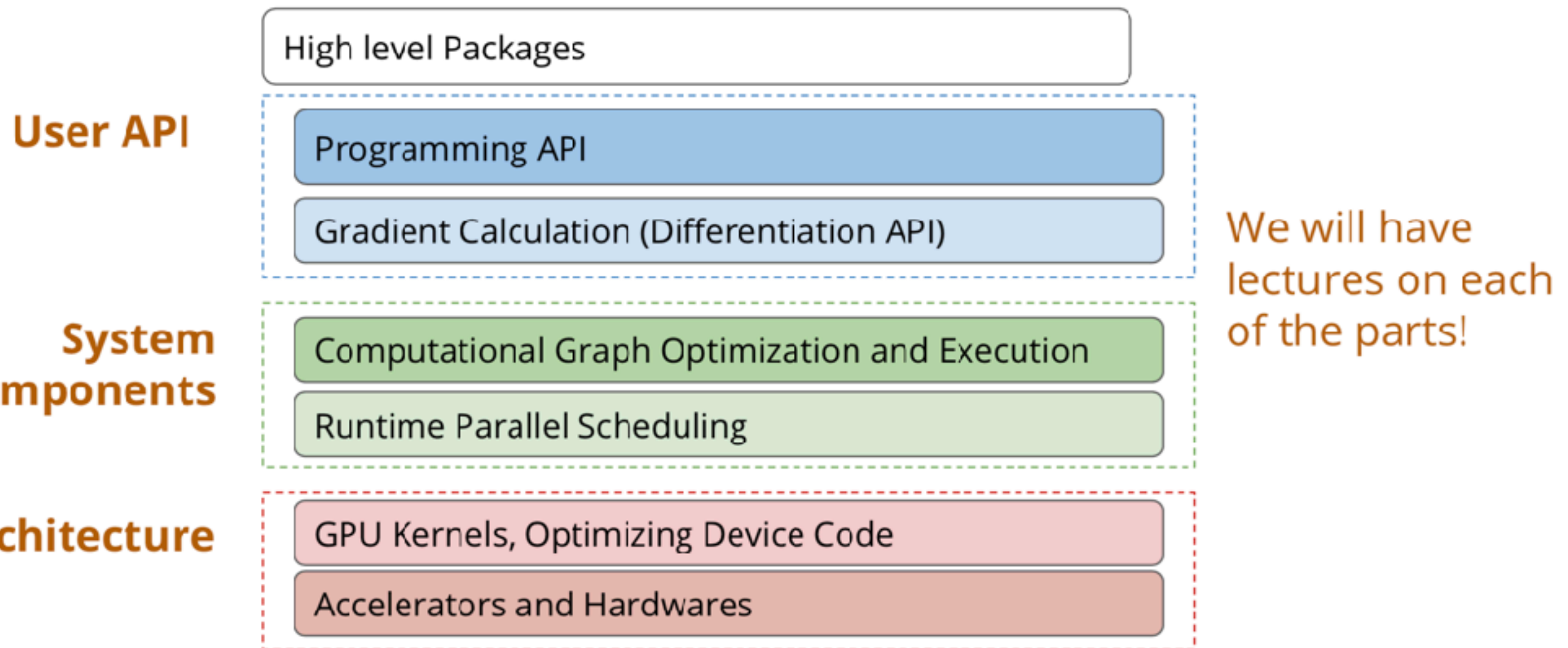


theano



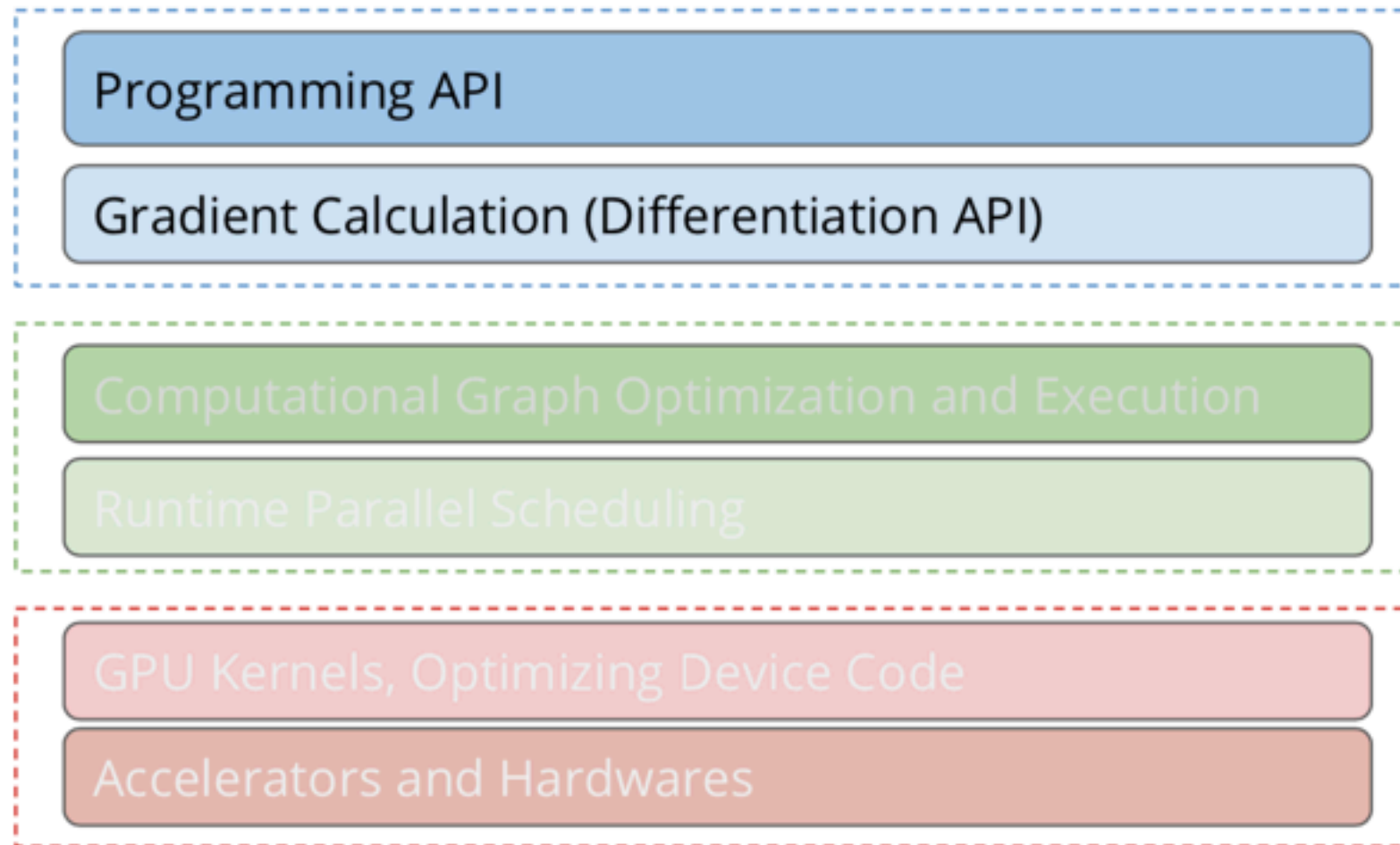
We won't focus on a specific one, but will discuss the common and useful elements of these systems

Typical Machine Learning System Stack



Typical Machine Learning System Stack

User API



Example: Logistic Regression

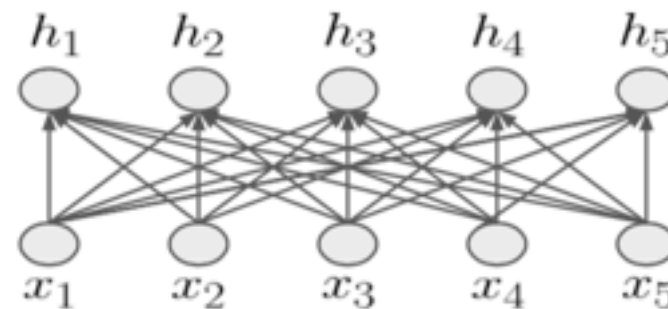
Data

$$x_i = \begin{bmatrix} \text{pixel}_1 \\ \text{pixel}_2 \\ \dots \\ \text{pixel}_m \end{bmatrix}$$



Fully Connected Layer

$$h_k = w_k^T x_i$$



Softmax

$$P(y_i = k | x_i) = \frac{\exp(h_k)}{\sum_{j=1}^{10} \exp(h_j)}$$

Logistic Regression in Numpy

```
import numpy as np
from tinyflow.datasets import get_mnist

def softmax(x):
    x = x - np.max(x, axis=1, keepdims=True)
    x = np.exp(x)
    x = x / np.sum(x, axis=1, keepdims=True)
    return x

# get the mnist dataset
mnist = get_mnist(flatten=True, onehot=True)
learning_rate = 0.5 / 100
W = np.zeros((784, 10))
for i in range(1000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    # forward
    y = softmax(np.dot(batch_xs, W))
    # backward
    y_grad = y - batch_ys
    W_grad = np.dot(batch_xs.T, y_grad)
    # update
    W = W - learning_rate * W_grad
```

Forward computation:
Compute probability of each class y given input

- Matrix multiplication
 - `np.dot(batch_xs, W)`
- Softmax transform the result
 - `softmax(np.dot(batch_xs, W))`

Logistic Regression in Numpy

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```

Weight Update via SGD

$$w \leftarrow w - \eta \nabla_w L(w)$$

Logistic Regression in TinyFlow (TensorFlow like API)

```
import tinyflow as tf
from tinyflow.datasets import get_mnist
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W = tf.Variable(tf.zeros([784, 10]))
y = tf.nn.softmax(tf.matmul(x, W))
# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
# Update rule
learning_rate = 0.5
W_grad = tf.gradients(cross_entropy, [W])[0]
train_step = tf.assign(W, W - learning_rate * W_grad)
# Training Loop
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```

Forward Computation **Declaration**



Logistic Regression in TinyFlow

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```

Loss function **Declaration**

$$P(\text{label} = k) = y_k$$
$$L(y) = \sum_{k=1}^{10} I(\text{label} = k) \log(y_i)$$

Logistic Regression in TinyFlow

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```

Automatic Differentiation: Details
in next lecture!

Logistic Regression in TinyFlow

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```

← SGD update rule

Logistic Regression in TinyFlow

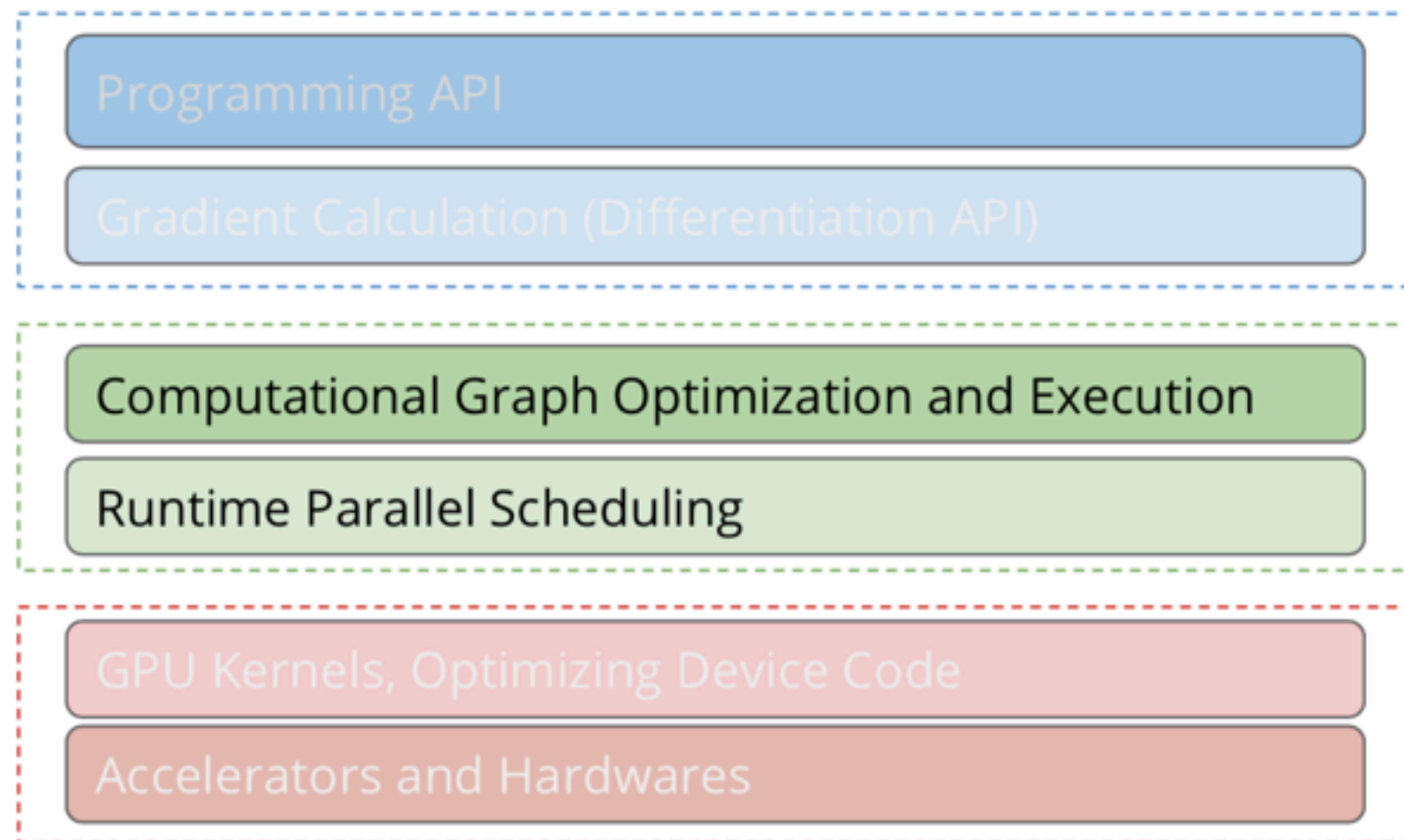
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```

Real execution happens here!



Typical Deep Learning System Stack

System Components



The Declarative Language: Computation Graph

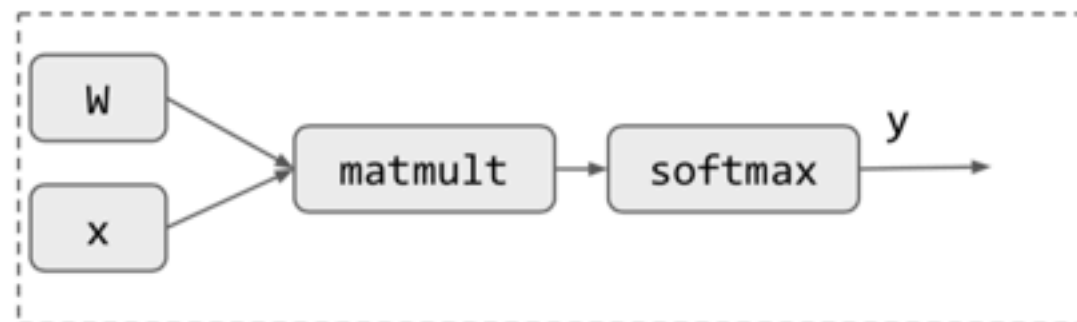
- Nodes represents the computation (operation)
- Edge represents the data dependency between operations

Computational Graph for $a * b + 3$



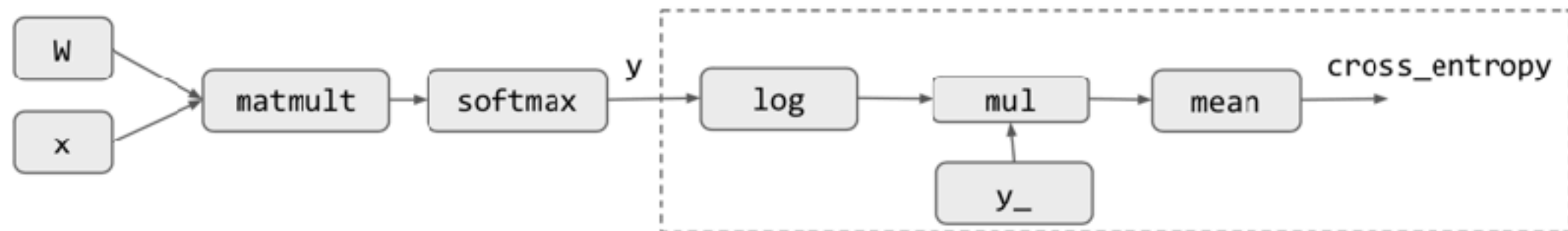
Computational Graph Construction by Step

```
x = tf.placeholder(tf.float32, [None, 784])  
W = tf.Variable(tf.zeros([784, 10]))  
y = tf.nn.softmax(tf.matmul(x, W))
```



Computational Graph Construction by Step

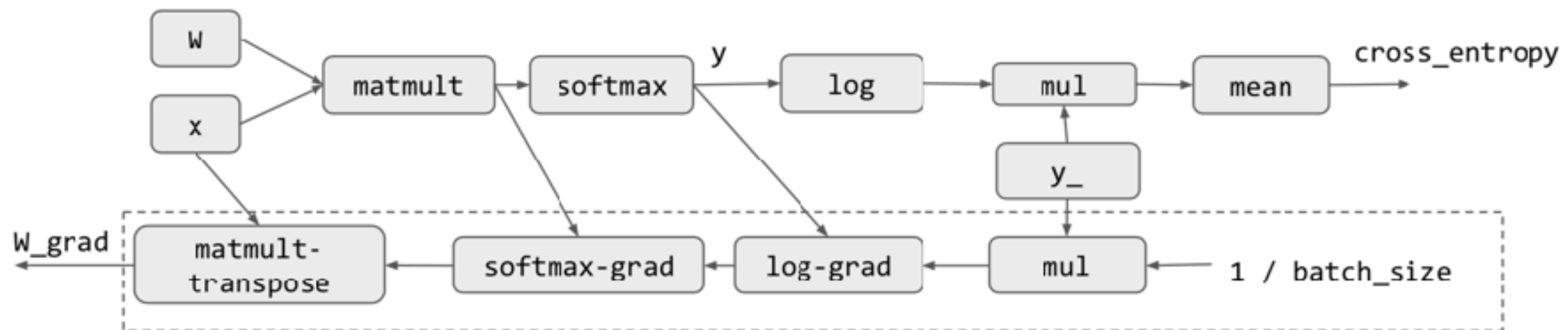
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Computational Graph Construction by Step

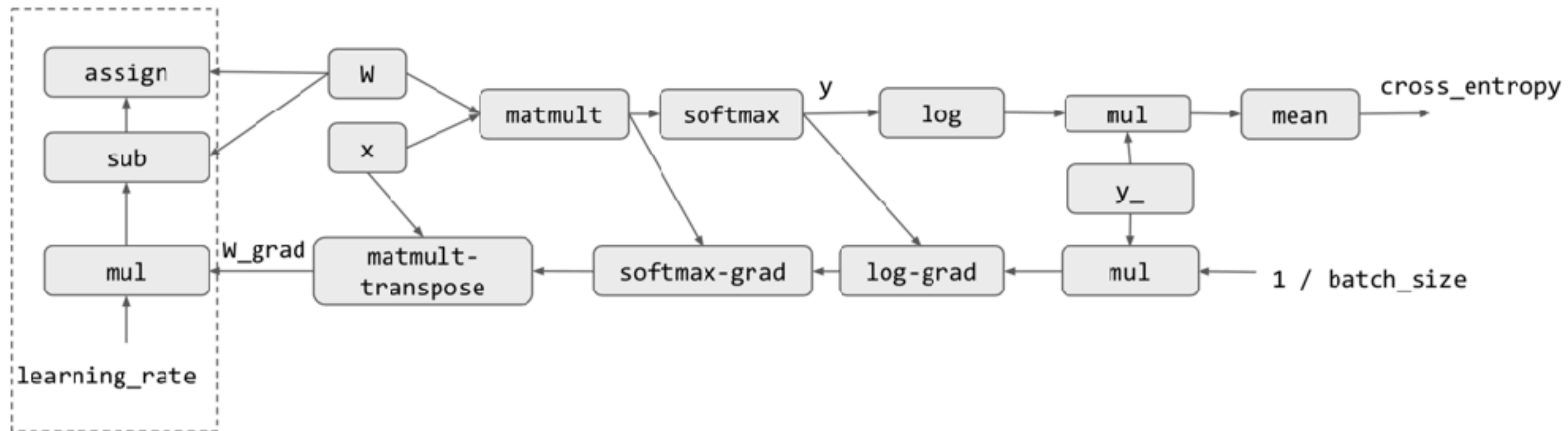
```
W_grad = tf.gradients(cross_entropy, [W])[0]
```

Automatic Differentiation,
detail in next lecture!



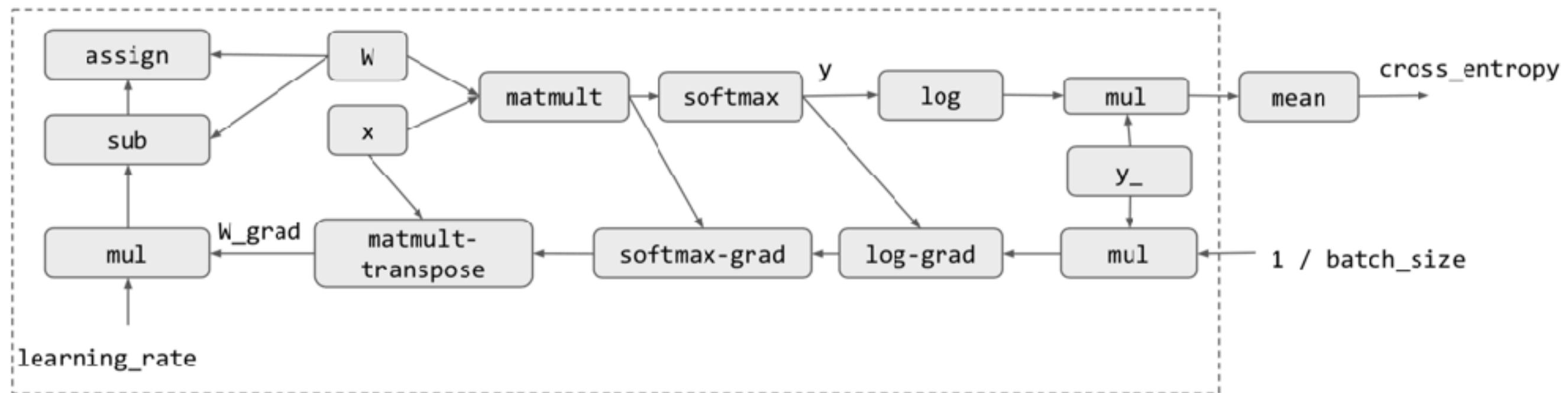
Computational Graph Construction by Step

```
train_step = tf.assign(W, W - learning_rate * W_grad)
```



Execution only Touches the Needed Subgraph

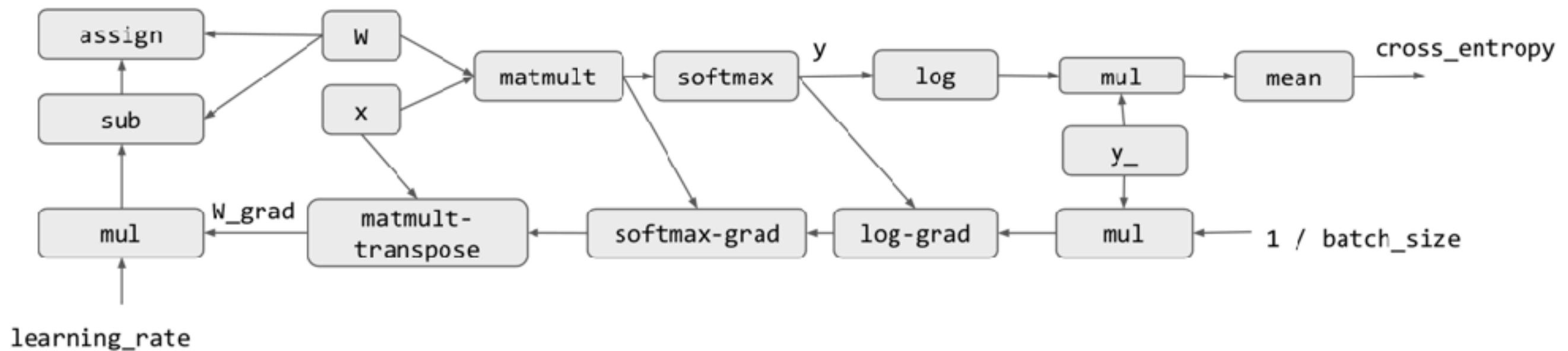
```
sess.run(train_step, feed_dict={x: batch_xs, y_:batch_ys})
```



Discussion:

Computational Graph

- What is the benefit of computational graph?
- How can we deploy the model to mobile devices?



Discussion:

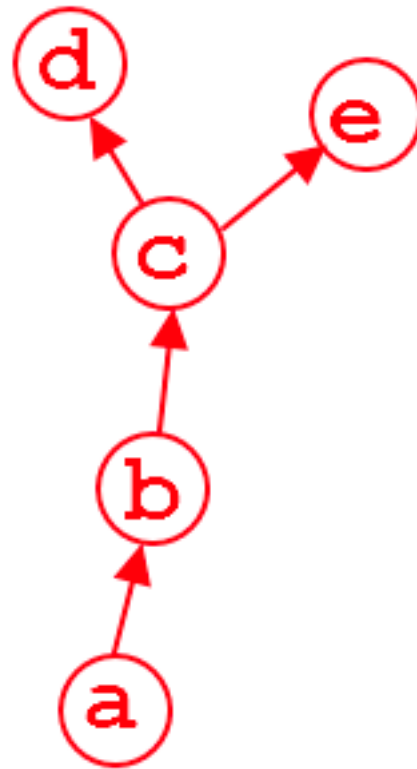
Numpy vs TF Program

What is the benefit/drawback of the TF model vs Numpy Model

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from tinyflow.datasets import get_mnist
def softmax(x):
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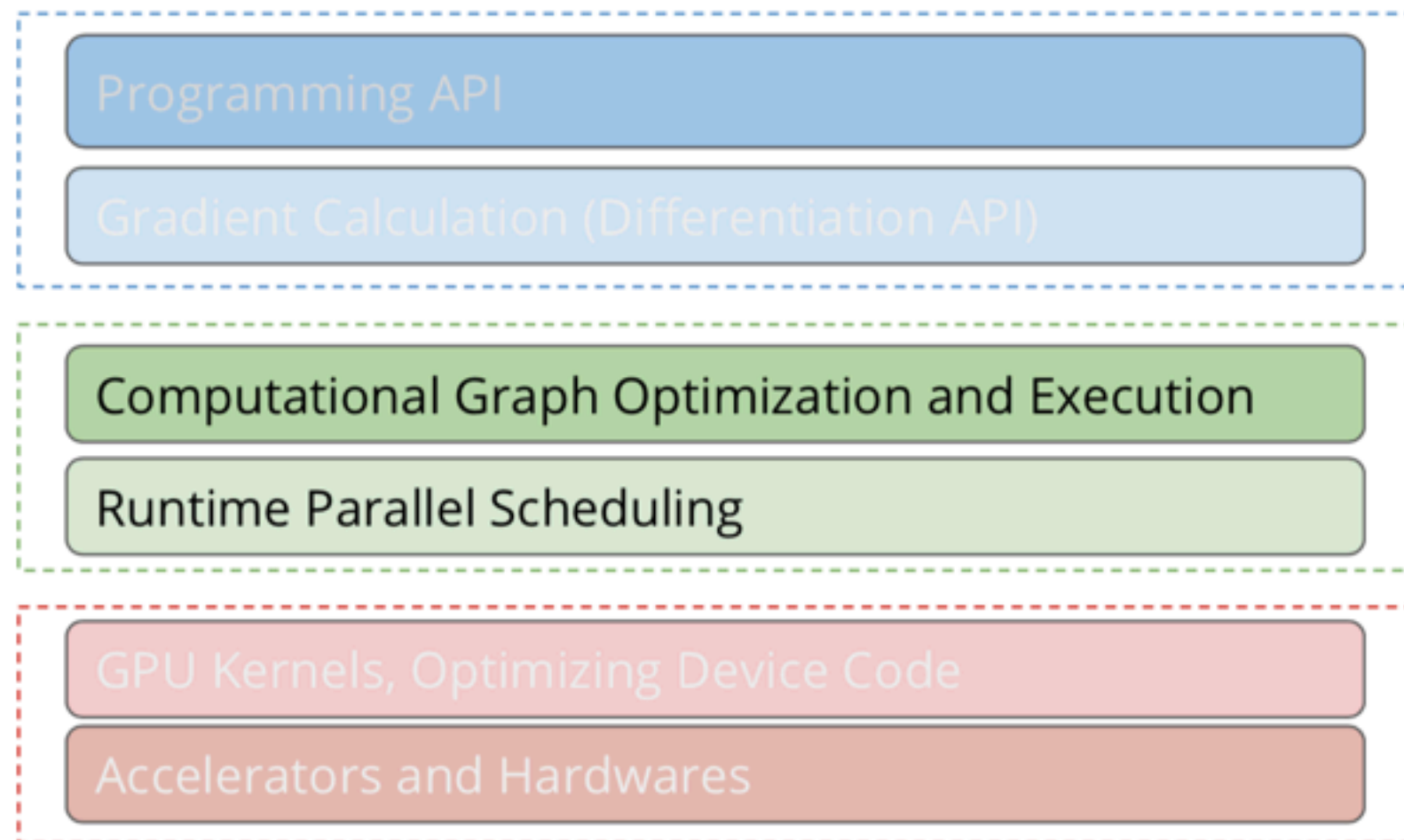
Computational graphs in other frameworks: PyTorch



```
import torch
from torch.autograd import Variable
a = Variable(torch.rand(1, 4), requires_grad=True)
b = a**2
c = b*2
d = c.mean()
e = c.sum()
```

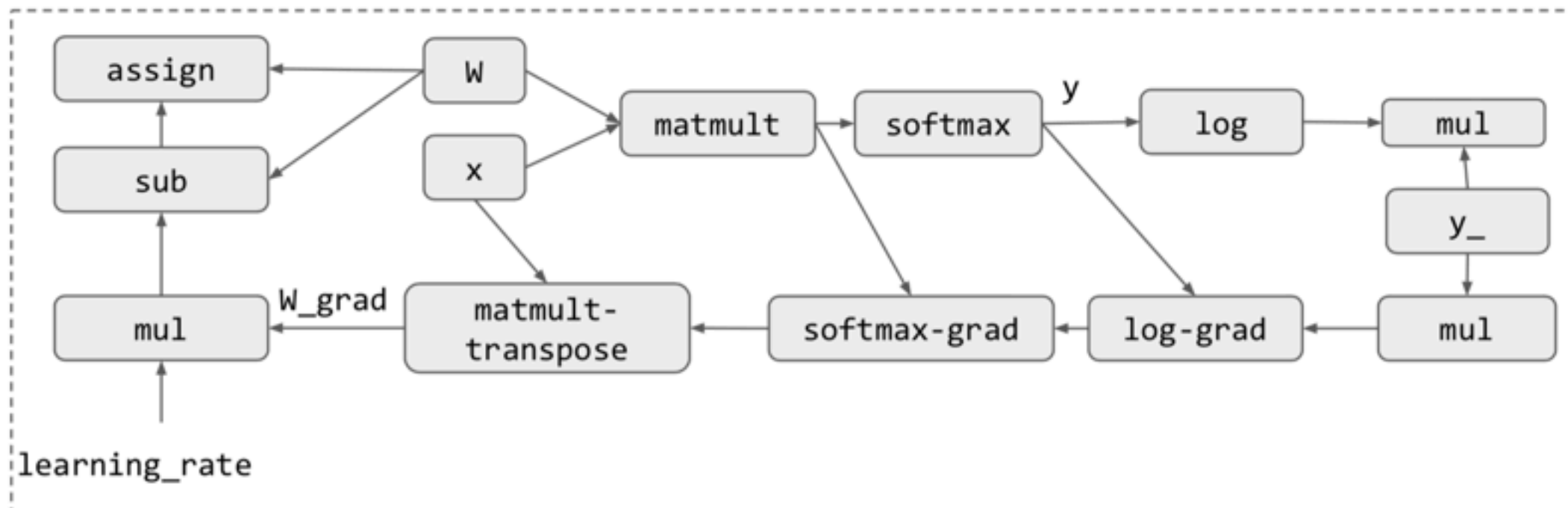
Typical Deep Learning System Stack

System Components



Computation Graph Optimization

- E.g. Deadcode elimination
- Memory planning and optimization
- What other possible optimization can we do given a computational graph?

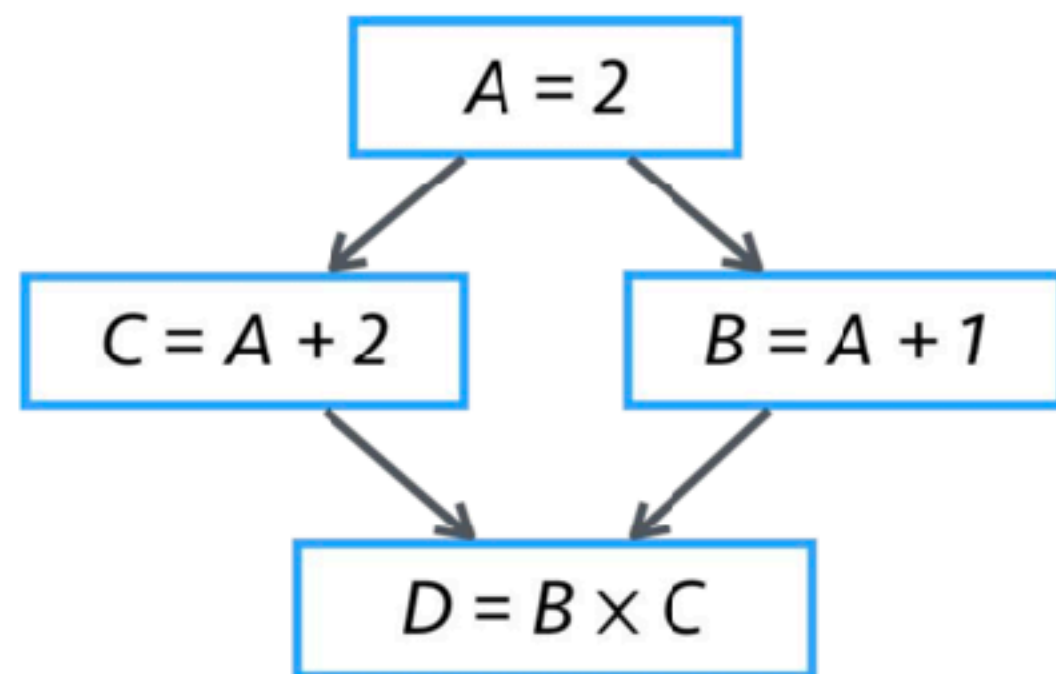


Parallel Scheduling

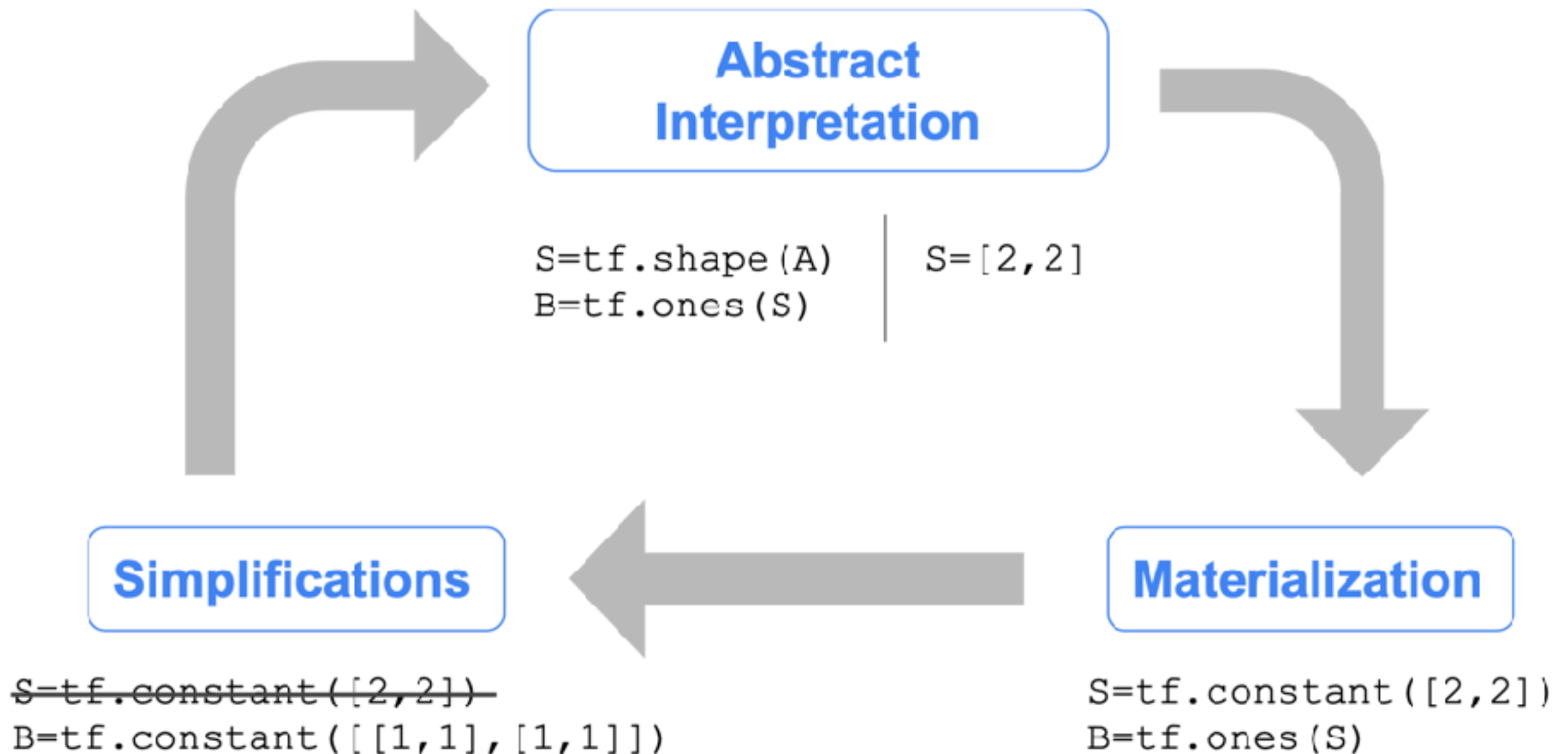
- Code need to run parallel on multiple devices and worker threads
- Detect and schedule parallelizable patterns
- Detail lecture on later

MXNet Example

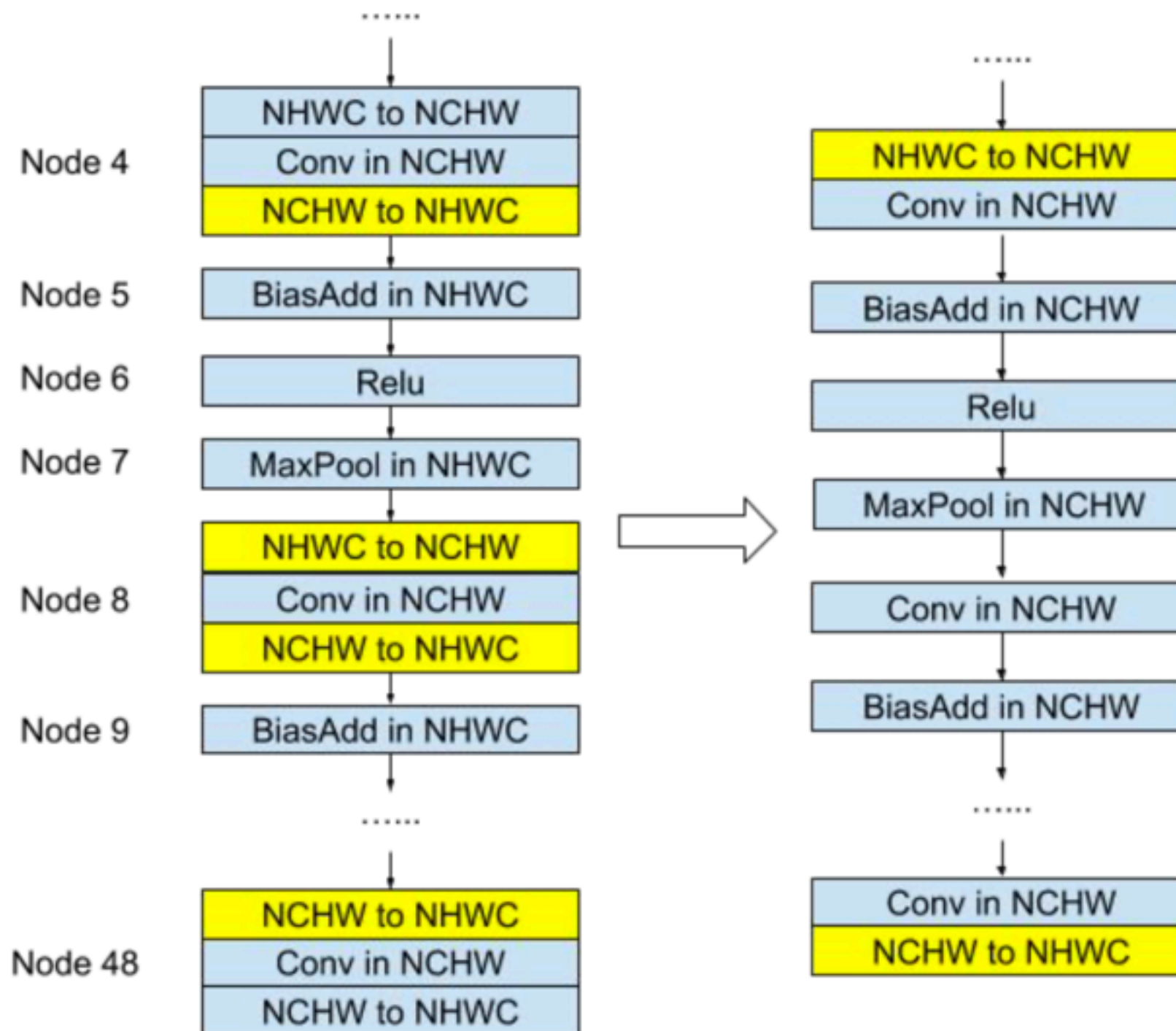
```
>>> import mxnet as mx
>>> A = mx.nd.ones((2,2)) * 2
>>> C = A + 2
>>> B = A + 1
>>> D = B * C
```



Graph Simplifications

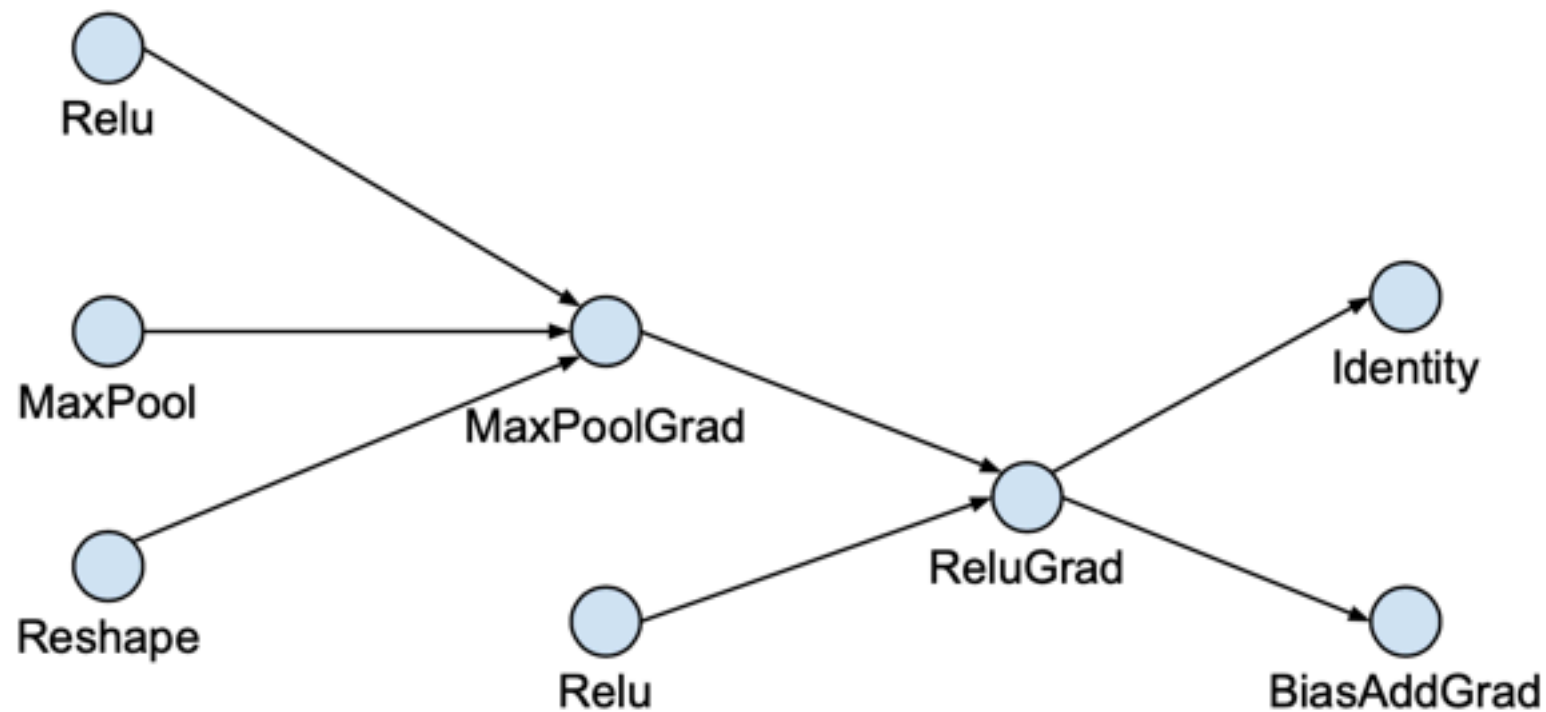


Layout Optimization



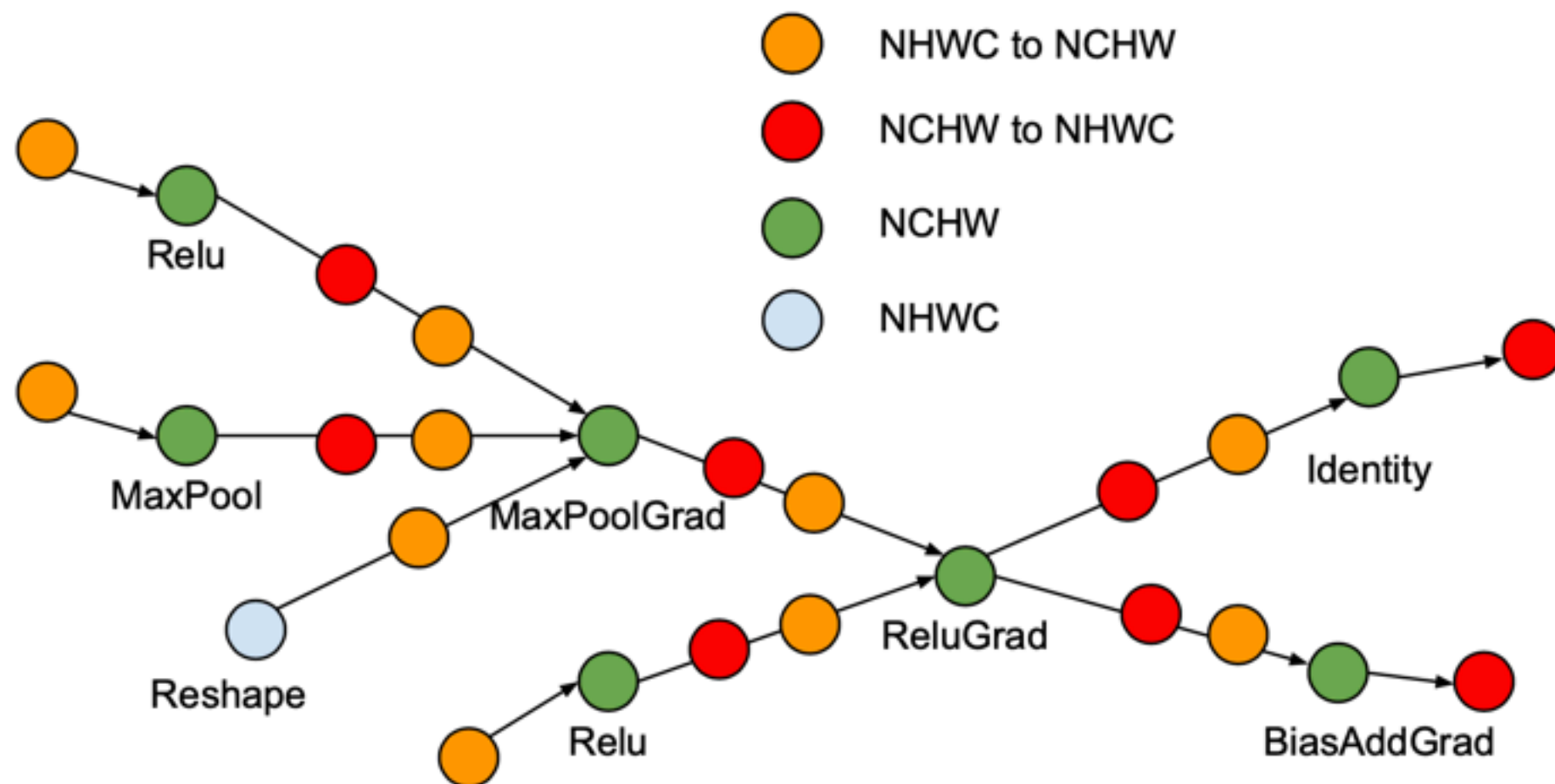
Layout Optimization

Example: Original graph with all ops in NHWC format



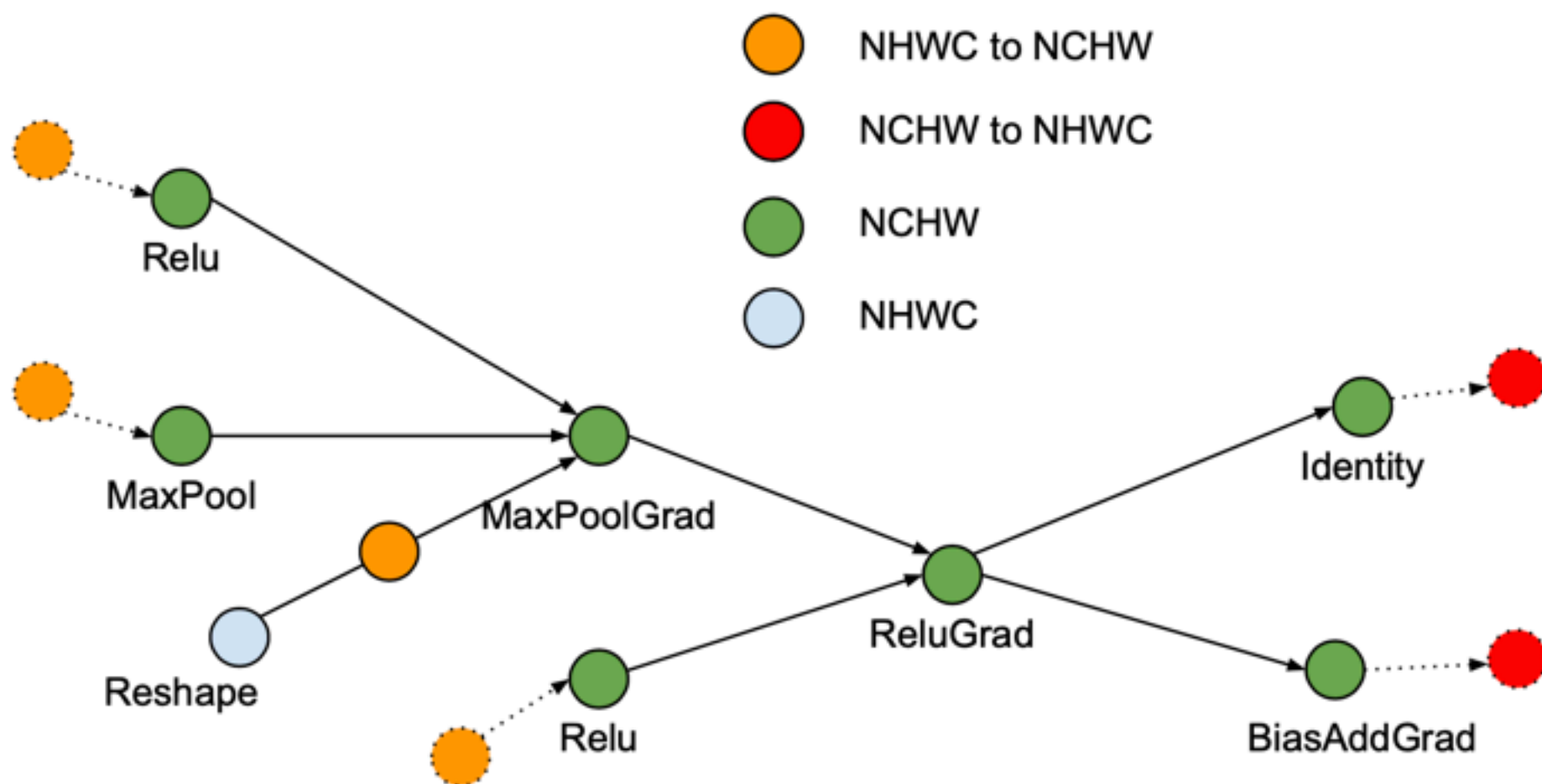
Layout Optimization

Phase 1: Expand by inserting conversion pairs

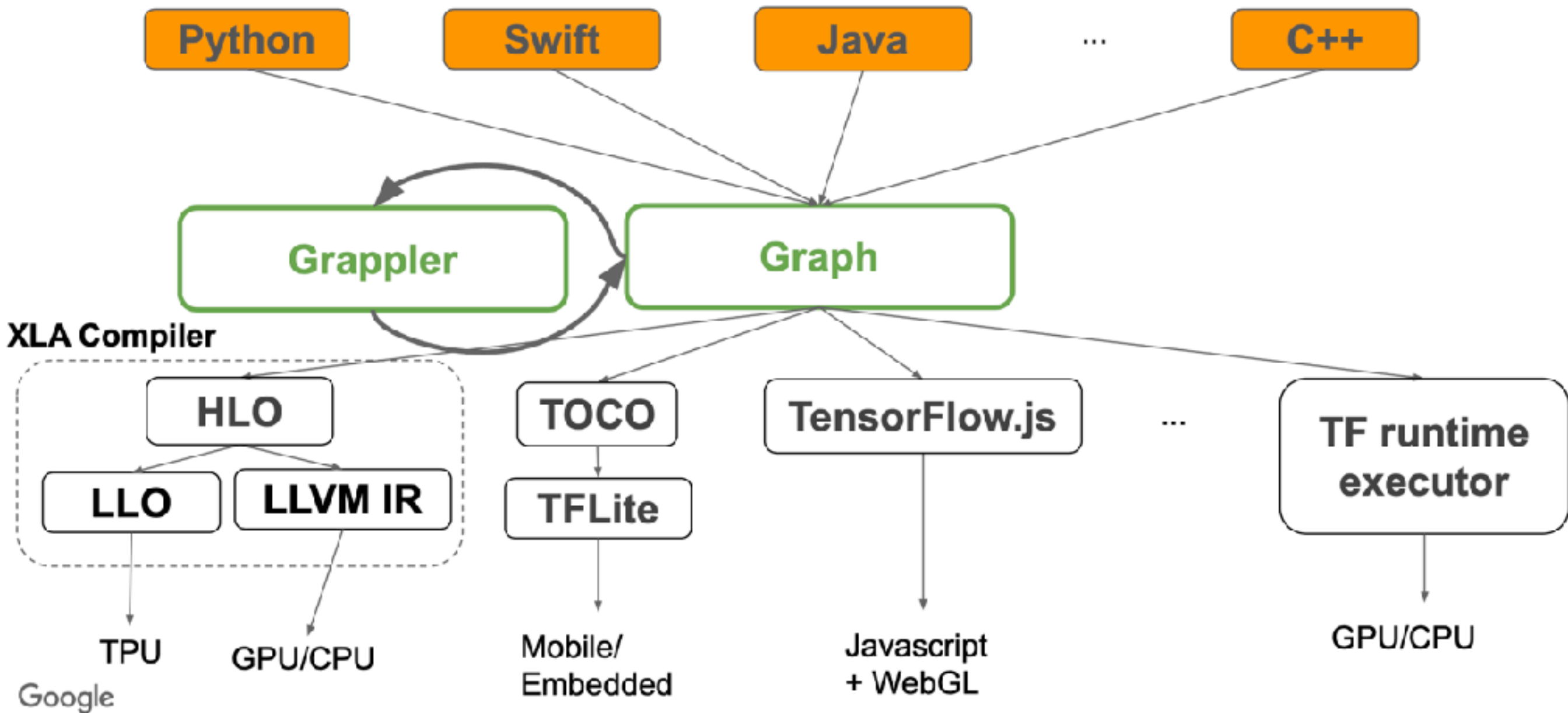


Layout Optimization

Phase 2: Collapse adjacent conversion pairs

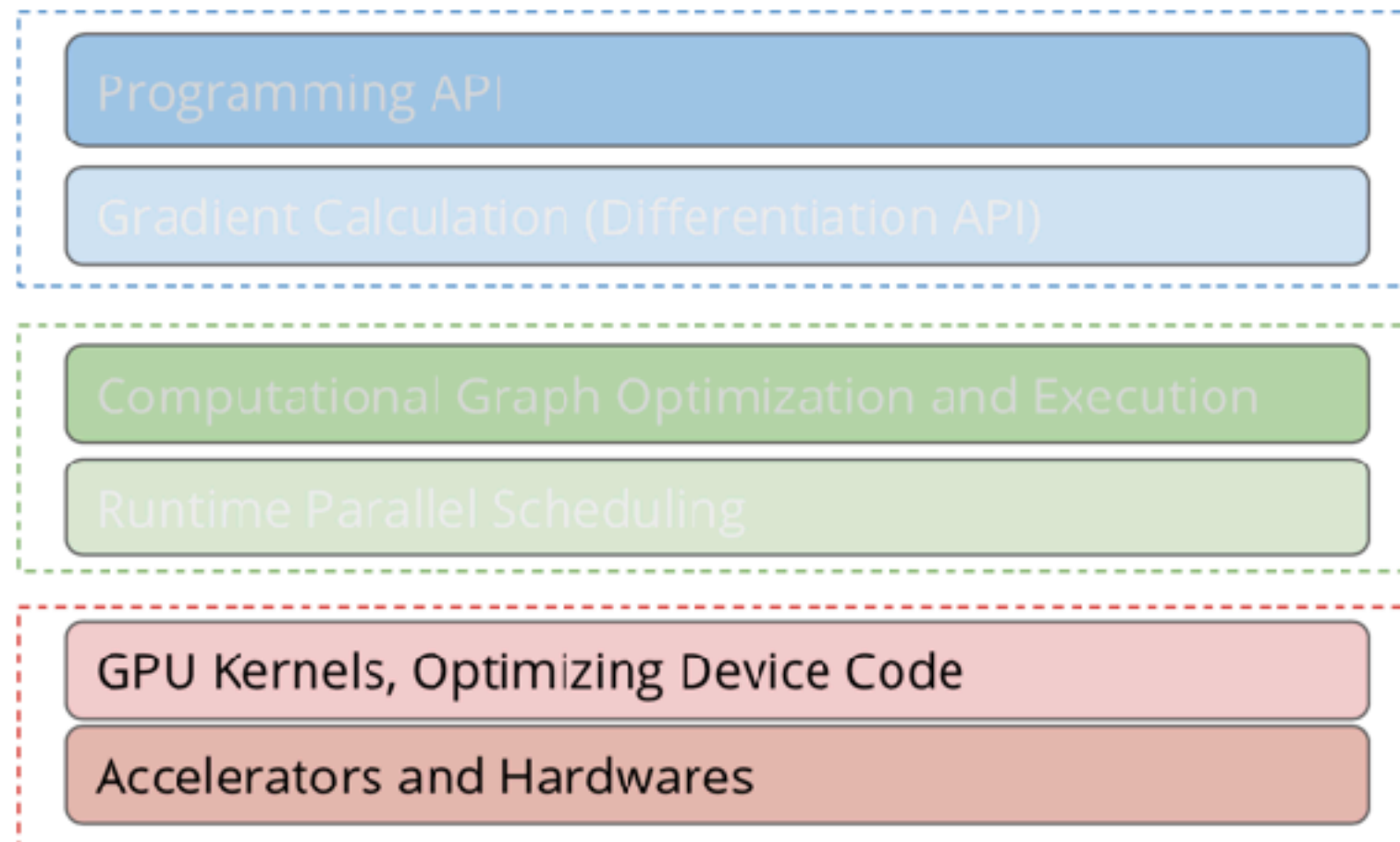


Computation Graph Optimization



Typical Deep Learning System Stack

Architecture



GPU Acceleration

- Most existing deep learning programs runs on GPUs
- Modern GPU have Teraflops of computing power



Typical Deep Learning System Stack

Not a comprehensive list of elements
The systems are still rapidly evolving :)

User API

Programming API

Gradient Calculation (Differentiation API)

System Components

Computational Graph Optimization and Execution

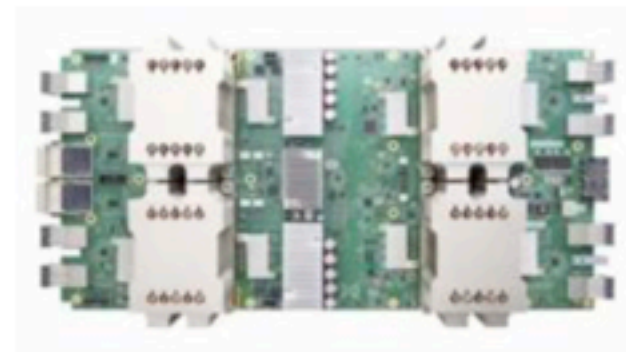
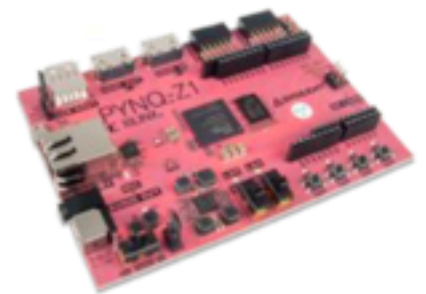
Runtime Parallel Scheduling

Architecture

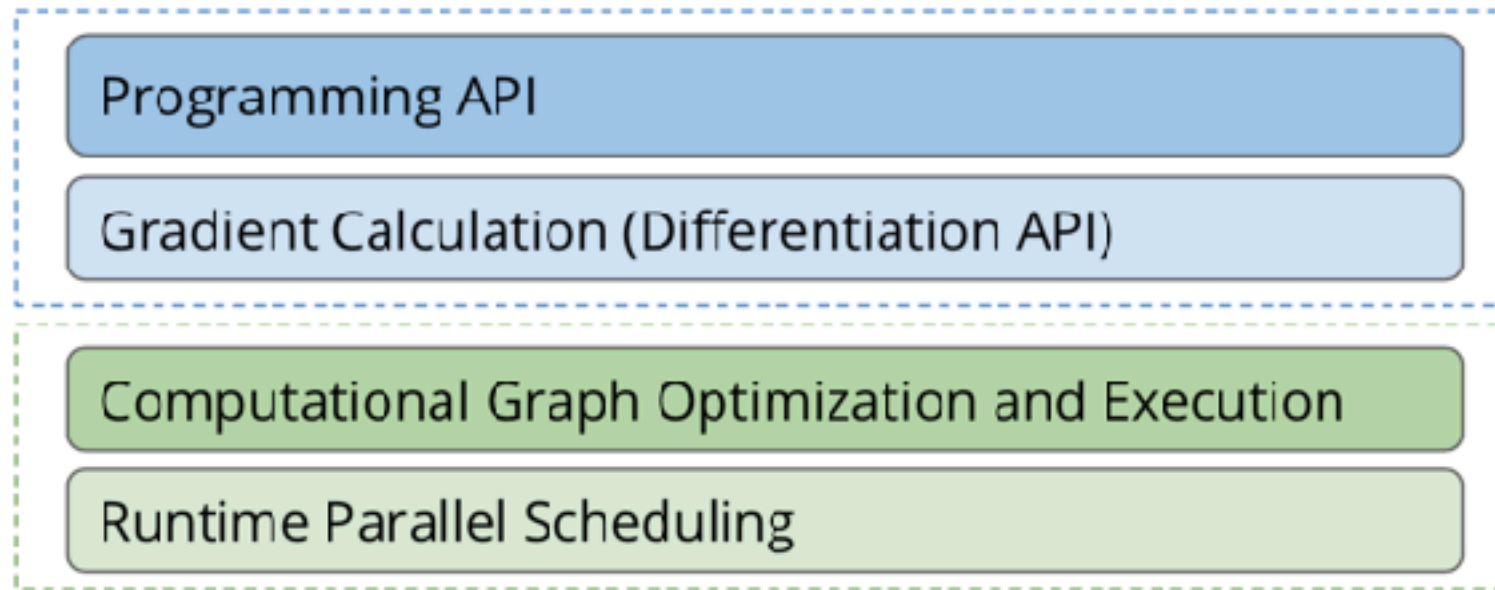
GPU Kernels, Optimizing Device Code

Accelerators and Hardwares

Supporting More Hardware backends



Each Hardware backend requires a software stack



CUDA Library

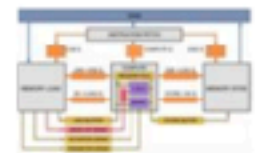
MKL Library

TPU Library

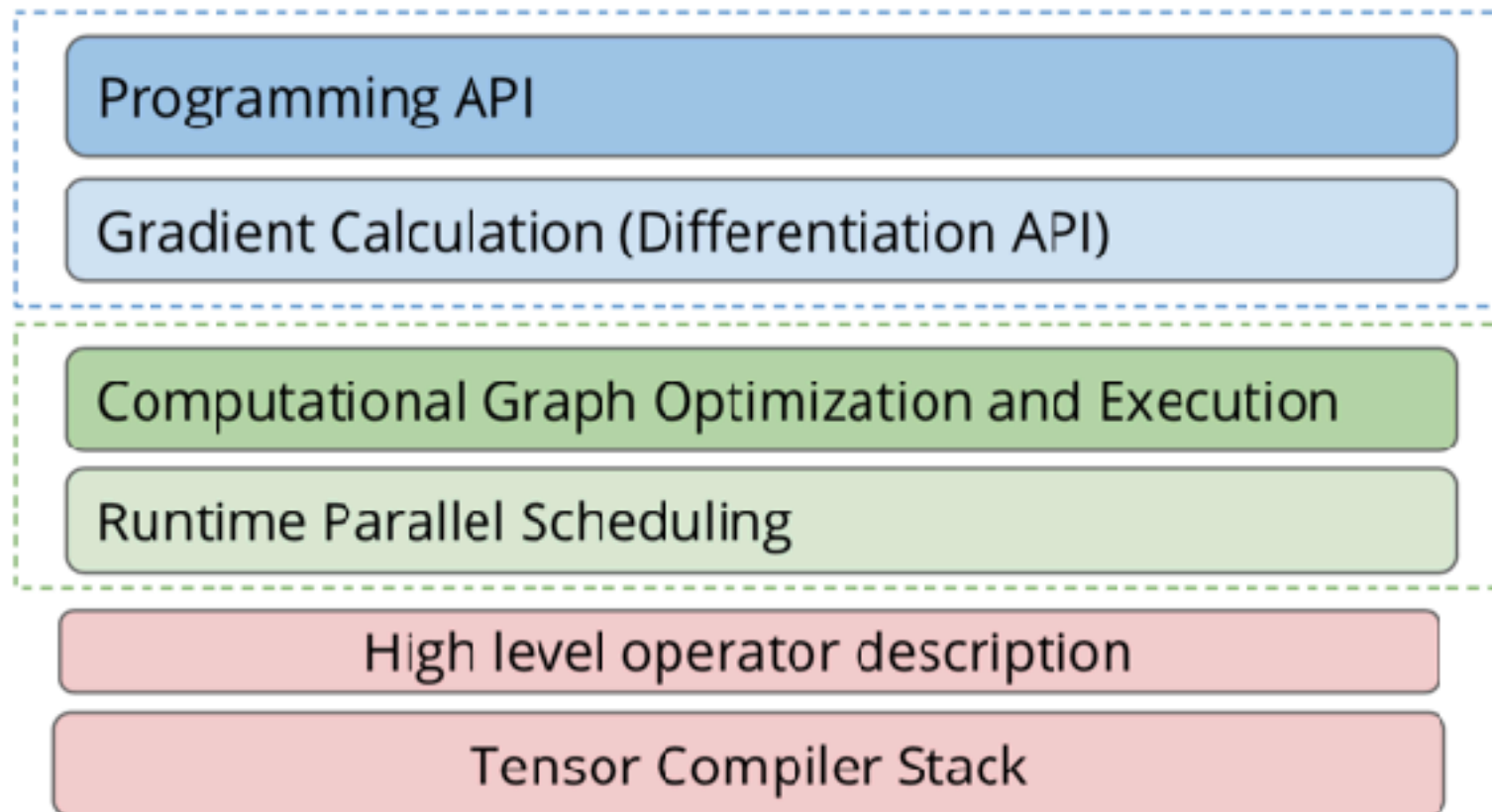
ARM Library

JS Library

Hardware



New Trend: Compiler based Approach



Hardware

