MATH-241 Calculus	Ι
Homework 6	

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QUESTION 1

When do we use the chain rule?

- A. When we don't feel like using the quotient rule.
- B. When we don't feel like using the definition of the derivative.
- C. When we have the composition of two functions  $h = f \circ g$ , defined by h(x) = f(g(x)), where q is differentiable at x and f is differentiable at q(x).
- D. When we have  $h(x) = \frac{f(g(x))}{g(x)^2}$  and f and g are both differentiable functions.

QUESTION 2

 $_{-}$  (1 pts)

Suppose we have the function h(x) = f(g(x)). What is h'(x) equivalent to?

A. 
$$\frac{f'(g(x))}{(g(x)')^2}$$

C. 
$$g'(f(x))f'(x)$$

B. 
$$f'(g(x))g'(x)$$

D. 
$$f(g(x)')f'(x)$$

 $h(x) = \frac{1}{\sqrt{x^3 - x + 1}}$ . What is h'(x)?

(1 pts)

$$n(x) \equiv \frac{1}{\sqrt{x^3 - x + 1}}$$
. What is  $n(x)$ 

A. 
$$-\frac{3x^2-1}{2(x^3-x+1)^{-3/2}}$$

C. 
$$-\frac{3x^2-1}{2(x^3-x+1)^{3/2}}$$

B. 
$$\frac{2(x^3 - x + 1)^{3/2}}{3x^2 - 1}$$

D. 
$$\frac{2(x^3 - x + 1)^{-3/2}}{3x^2 - 1}$$

 $_{-}$  Question 4

(1 pts)

$$h(x) = \sin^{n-1}(x), \text{ find } h'(x).$$

A. 
$$(n-1)\sin^n(x)\cos(x)$$

C. 
$$-(n-1)\cos^n(x)\sin(x)$$

B. 
$$(n-1)\sin(x)$$

D. 
$$(n-1)\sin^{n-2}(x)\cos(x)$$

QUESTION 5

Determine if the functions below are implicit or explicit functions. (Write your answers as A-Explicit, etc.)

A. 
$$\cos(\frac{x}{y}) = x + y$$

C. 
$$y = x^3 + 2$$

B. 
$$y = x \sin(x)$$

D. 
$$x^2 + 4y^2 = 4$$

 $_{---}$  Question 6

(1 pts)

 $\sqrt{x} + \sqrt{y} = 1$ . Find y'.

$$A. \ y' = \frac{1}{2\sqrt{x}}$$

C. 
$$y' = 2\sqrt{y} - \frac{\sqrt{yx}}{x}$$

B. 
$$y' = -\frac{\sqrt{y}}{\sqrt{x}}$$

D. 
$$y' = \frac{1}{2\sqrt{x}} + y$$

\_\_\_\_\_Question 7

(1 pts)

 $2y^2 + x^3 = 2$ . Find y'.

A. 
$$y' = -\frac{3x^2}{4y}$$

C. 
$$y' = \frac{3y^2}{4y}$$

B. 
$$y' = 2 - \frac{3x^2}{4y}$$

D. 
$$y' = 4y^2 + 3x^2$$

QUESTION 8

\_\_\_\_\_ (1 pts)

What is the average rate of change of y with respect to x?

A. 
$$\frac{dy}{dx} = \lim_{\Delta x \to 0} \frac{\Delta y}{\Delta x}$$

C. 
$$\Delta y = f(x_2) - f(x_1)$$

$$B. \frac{f(x_1) - f(x_2)}{y}$$

D. 
$$\frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

QUESTION 9

(1 pts)

What is the instantaneous rate of change of y with respect to x?

A. 
$$\frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

C. 
$$\frac{dy}{dx} = \lim_{\Delta x \to 0} \frac{\Delta y}{\Delta x}$$

B. 
$$\Delta x = x_2 - x_1$$

D. 
$$\Delta y = f(x_2) - f(x_1)$$

Question 10

(1 pts)

The position of a particle is given by the equation  $s = f(t) = t^2 + 3t - 1$ , where t is measured in seconds and s in meters. What is the velocity at t = 1?

B. 
$$2t + 3$$

D. 
$$6 \text{ m/s}$$