MATH-241 Calculus	I
Homework 4	

Created by Rukiyah Walker Spring 2023

QUESTION 1

(1 pts)

We use the Intermediate Value Theorem to:

- A. To show that a function is continuous.
- B. To show that for a continuous function f(x), a solution to f(x) = 0 exists.
- C. To show that a function is discontinuous.
- D. To show that  $\lim_{x\to a} f(x)$  does not exist.

QUESTION 2

(1 pts)

What do we need to check in order to use the Intermediate Value Theorem?

- A. Our function f(x) is continuous on the closed interval [a, b].
- B.  $f(a) \neq f(b)$ .
- C.  $f(a) \leq N \leq f(b)$ , where N is some number.
- D. All of the above.

QUESTION 3

(1 pts)

The derivative of a function f is:

A. 
$$f'(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}$$

- B. The value a, when f(a) = 0.
- C. When the limit of a function does not exist.
- D. The value at which a function is discontinuous.

\_ Question 4

(1 pts)

What is one interpretation of the average rate of change?

A. Instantaneous velocity.

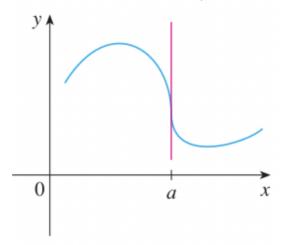
B. 
$$f'(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}$$

- C. The average change in position with respect to time.
- D. The derivative of a function f.

What is the instantaneous rate of change?	(1 pts)
A. The derivative of a function $f$ .	
B. Acceleration.	
C. The point at which a function is discontinuous.	
D. When a function $f(x) = 0$ .	
QUESTION 6	(1 pts)
The derivative of a function $f$ is equal to 0 when:	,
A. The graph of the function crosses the $x$ -axis.	
B. When the slope of the tangent line is 0.	
C. At the point $x = 0$ .	
D. The derivative does not exist.	
What does $\frac{dy}{dx} _{x=a} = f'(a)$ mean?	(1 pts)
A. The average rate of change is equal to $f'(a)$ .	
B. The derivative of y divided by the derivative of x is equal to $f'(a)$ .	
C. $f(x) = f'(a)$ when $x = a$ .	
D. The derivative of a function $f$ at the point $x = a$ is equal to $f'(a)$ .	
QUESTION 8	(1 pts)
Suppose we have a function $f$ that represents the position of a particle. The act the particle can be represented by:	
A. The velocity.	
B. $f'(x)$ .	
C. The second derivative of the function.	
D. The instantaneous rate of change.	

QUESTION 9

(1 pts)



Is the function, represented by the graph above, differentiable? Why?

A. No, since the slope of the tangent line is equal to  $\pm \infty$ .

B. Yes, since 
$$\lim_{x\to a^-} f(x) = \lim_{x\to a^+} f(x)$$
.

C. Yes, since there is no jump discontinuity.

D. No, since 
$$\lim_{x\to a} f(x) = 0$$

(1 pts)

Suppose we have the function  $f(x) = x^3 - x^2$ .

Using the power and difference rules for derivatives, what is f'(x)?

A. 
$$3x^3 - 2x^2$$

B. 
$$3x^2 - 2x$$

C. 
$$3x - 2x$$

D. 
$$3x^4 - 2x^3$$