MATH-241 Calculus	Ι
Homework 13	

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QUESTION 1

(1 pts)

Express the limit, $\lim_{n\to\infty}\sum_{i=1}^n\frac{2}{n}(1+\frac{2i}{n})\sqrt{1+\frac{2i}{n}}$, as a definite integral.

A.
$$\int_1^3 x \sqrt{x} \, dx$$

C.
$$\int_1^3 (x\sqrt{x})^{\frac{2}{n}} dx$$

B.
$$\int_1^3 \sqrt{x} dx$$

D.
$$\int_1^n x \sqrt{x} \, dx$$

QUESTION 2

Suppose $\int_1^2 x^2 dx$. Using this information, what are absolute minimum and maximum of the integrand $f(x) = x^2$? (Write as an inequality).

A.
$$1 \le x \le 2$$

C.
$$1 \le x^2 \le 2$$

B.
$$1 \le x^2 \le 4$$

D.
$$1 < x < 4$$

Suppose you want to estimate $\int_1^4 f(x) dx$, with 3 rectangles. What are the midpoints of the subintervals?

A.
$$x_1 = 2, x_2 = 3, x_3 = 4$$

C.
$$x_1 = \frac{3}{2}, x_2 = \frac{5}{2}, x_3 = \frac{7}{2}$$

B.
$$x_1 = \frac{1}{2}, x_2 = \frac{3}{2}, x_3 = \frac{5}{2}$$

D.
$$x_1 = 1, x_2 = 2, x_3 = 3$$

QUESTION 4

(1 pts)

Which of the following defines a definite integral?

- A. An antiderivative that produces a function with an arbitrary constant C.
- B. The limit as f(x) goes to infinity.
- C. The derivative of the area function.
- D. An integral which is evaluated over a specific interval, and produces a constant value.

QUESTION 5

 $_{-}$ (1 pts)

The fundamental theorem of calculus (part 1) says: If f is continuous on [a, b], then the function g defined by $g(x) = \int_a^x f(t) dt$, $a \le x \le b$, is continuous on [a, b] and differentiable on (a,b), and g'(x)=f(x). What does this mean in words?

A. q'(x) exists on [a, x].

- C. The derivative of f(x) is equal to F(b) - F(a).
- B. The derivative of the area function is equal to the integrand.
- D. q(x) is only differentiable when f(t)exists on [a, b].

QUESTION 6

The fundamental theorem of calculus (part 2) says: If f(x) is continuous on [a, b], then $\int_a^b f(x) dx = F(b) - F(a)$, where F(x) is any antiderivative of f(x). What does this mean in words?

- A. If F(x) is the anti-derivative of f(x), then $\int_a^b f(x) dx$ is equal to F(x) evaluated at b, subtracted by F(x) evaluated at a.
- B. The derivative of f(x) is equal to F(b) F(a).
- C. The derivative of the area function is equal to the integrand.
- D. The derivative of f(x) is equal to F(x) evaluated at b, subtracted by the F(x)evaluated at a.

Suppose you have $\int_{-1}^{2} x^2 dx$ and F(x) + C is the antiderivative of f(x), where C = 0. Using the same notation as the Fundamental Theorem of Calculus, what is F(b) and F(a)?

A.
$$F(b) = F(-1) = \frac{-1}{3}$$

 $F(a) = F(2) = \frac{8}{3}$

C.
$$F(b) = F(2) = \frac{8}{3}$$

 $F(a) = F(-1) = \frac{-1}{3}$

B.
$$F(b) = F(2) = \frac{4}{3}$$

 $F(a) = F(-1) = \frac{-1}{3}$

D.
$$F(b) = F(2) = \frac{8}{3}$$

 $F(a) = F(-1) = \frac{1}{3}$

Which of the below is equivalent to $\int_1^2 x^3 + 2x + 3 dx$?

A.
$$\frac{39}{4}$$

C.
$$\left(\frac{2^4}{4} + 2^2 + 3(2)\right) - \left(\frac{1}{4} + 1 + 3\right)$$

B.
$$\frac{x^4}{4} + x^2 + 3x\Big|_{1}^{2}$$

D. A, B, and C.

QUESTION 9

 $_{-}$ (1 pts)

Evaluate $\int_2^2 \sqrt{x} \, dx$.

A. 0

C. Does not exist.

B.
$$\frac{2^{5/2}}{3}$$

D.
$$\frac{2^{5/2}-2}{3}$$

QUESTION 10

 $_{----}$ (1 pts)

Evaluate $\int_{-1}^{2} \frac{1}{x^3} dx$.

A. $\frac{3}{8}$

C. 0

B. Does not exist

D. $\frac{-3}{8}$