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QUESTION 1

(1 pts)

Suppose  $\lim_{x \rightarrow \infty} f(x) = \infty$  and  $\lim_{x \rightarrow \infty} g(x) = -\infty$ . What is  $\lim_{x \rightarrow \infty} f(x)g(x)$ ?

- A.  $\infty$
- B. 0
- C.  $-\infty$
- D. Does not exist.

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QUESTION 2

(1 pts)

What is  $\infty - \infty$ ?

- A.  $\infty$
- B. Does not exist.
- C. 0
- D.  $-\infty$

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QUESTION 3

(1 pts)

When is a function  $f$  an odd function?

- A. If  $f(-x) = -f(x)$ .
- B. If  $\lim_{x \rightarrow \infty} f(x) = -\infty$
- C. If  $f(-x) = f(x)$ .
- D. If  $\lim_{x \rightarrow \infty} f(x)$  does not exist.

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QUESTION 4

(1 pts)

Suppose  $f(x) = \frac{x}{x+1}$ . Find the vertical and horizontal asymptotes.

- A. Vertical asymptote at  $y = 1$   
Horizontal asymptote at  $x = -1$
- B. Vertical asymptote at  $x = 1$   
Horizontal asymptote at  $y = -1$
- C. Vertical asymptote at  $x = -1$   
Horizontal asymptote at  $y = 1$
- D. No vertical asymptote.  
Horizontal asymptote at  $y = -1$

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QUESTION 5

(1 pts)

$f(x) = \frac{x^2+4x}{x^2-16}$ . Find the vertical asymptote(s).

- A.  $x = 16$
- B.  $x = -4$  and  $x = 4$
- C. There are no vertical asymptotes.
- D.  $x = 4$

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QUESTION 6

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(1 pts)

Suppose we have a function  $f(x) = \frac{x^4}{12} + x$ , where  $f''(x) = x^2$ . What does  $f''(x)$  tell us about the curve of  $f(x)$ ?

- A.  $f''(x)$  will always be positive, so the graph of  $f(x)$  is concave upward.
- B.  $f''(x)$  will always be negative, so the graph of  $f(x)$  is concave upward.
- C.  $f''(x)$  will always be positive, so the graph of  $f(x)$  is concave downward.
- D.  $f''(x)$  will always be negative, so the graph of  $f(x)$  is concave downward.

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QUESTION 7

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(1 pts)

Suppose  $f'(x) < 0$  and  $f''(x) > 0$  for some function  $f(x)$ . What does this tell us about the graph of  $f(x)$ ?

- A.  $f(x)$  is decreasing and concave upward.
- B.  $f(x)$  is decreasing and concave upward.
- C. Since they are opposite signs we can not conclude anything about  $f(x)$ .
- D.  $f(x)$  is decreasing and concave downward.

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QUESTION 8

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(1 pts)

Give the function to optimize for the following problem:

Find the dimensions of a rectangle with perimeter 100m whose area is as large as possible.

- A.  $y = \frac{100-x}{2}$
- B.  $100 = 2x + 2y$
- C.  $A = x(50 - x)$
- D.  $A = xy$

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QUESTION 9

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(1 pts)

Give the function to optimize for the following problem:

The sum of two positive numbers is 16. What is the smallest possible value of their squares?

- A.  $16 = x + y$
- B.  $16 = x^2 + y^2$
- C.  $S = x^2 + y^2$
- D.  $S = x^2 + (16 - x)^2$

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QUESTION 10

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(1 pts)

Give the function to optimize for the following problem:

Find the dimensions of the rectangle of largest area that can be inscribed in a circle with radius  $r$  centered at the origin. (Both the circle and the rectangle are centered at the origin).

- A.  $A = xy$
- B.  $A = 4x\sqrt{r^2 - x^2}$
- C.  $A = \pi r^2$
- D.  $A = 4xy$