CONFIDENTIAL: DO NOT RETURN TO STUDENT. SHRED TO DISPOSE.

Dear Professor Pierre-Olivier Parise,

Thank you for working with KOKUA to provide me with appropriate disability-related exam accommodations.

I am acknowledging that I understand the conditions stated below and will take the MATH 311 exam in accordance with these conditions.

NO book allowed, NO notes allowed, Calculator allowed - Scientific calculator (non-graphing)

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Jones, Lillie (Lillie)	Date		
KOKUA Proctor Notes:			
The MATH 211 even was administered on E/10/2024 from	9.16	10.07	
The MATH 311 exam was administered on 5/10/2024 from		to 10 0 1	

Return Method: Via email to parisepo@hawaii.edu.

University of Hawai'i



Last name:	Joves				
Loss name.	-				
First name:	Lille				

Question:	1	2	3	4	Total
Points:	15	15	15	5	50
Score:					

Instructions:

- Write your complete name on your copy.
- Answer all 4 questions below.
- Write your answers directly on the questionnaire.
- Show ALL your work to have full credit.
- Draw a square around your final answer.
- Return your copy when you're done or at the end of the 50min period.
- No electronic devices allowed during the exam.
- Scientific calculator allowed only (no graphical calculators).
- Turn off your cellphone(s) during the exam.
- Lecture notes and the textbook are not allowed during the exam.

Your Signature:

May the Force be with you! Pierre ____QUESTION 1

(15 pts)

Let $T: \mathbb{R}^3 \to \mathbb{R}^3$ be defined by T(x, y, z) = (2y, z, z).

- (a) (5 Pts) Show that T is a linear transformation.
- (b) (5 Pts) Find the kernel of T and its dimension.
- (c) (5 Pts) Using the Dimension Theorem, deduce the rank of T.

$$T\left(\begin{array}{c} x_1 \\ x_2 \\ x_3 \end{array}\right) + \left(\begin{array}{c} x_1 \\ y_2 \\ y_3 \end{array}\right) = T$$

$$7(x_{1}y_{1}z) = (2y_{1}z_{1}z_{2}) = 0$$

$$9(2y)+b(3)+c(2)=0$$

0) ItRAMIKT = 3 -1 Ramicī=2

$$x(0) = 0$$
 $x_{0} = 0$ x_{0

tim=1

Let $V = \mathbb{R}^3$. Let B be the standard basis $\{(1,0,0),(0,1,0),(0,0,1)\}$ and let the set $D = \{(1,2,0),(0,-1,2),(0,2,0)\}$ be another basis of \mathbb{R}^3 .

- (a) (10 Pts) Knowing that
 - (1,0,0) = a(1,2,0) + b(0,-1,2) + c(0,2,0), where a = 1, b = 0, c = -1;
 - (0,1,0) = a(1,2,0) + b(0,-1,2) + c(0,2,0), where a = 0, b = 0, c = 1/2;
 - (0,0,1) = a(1,2,0) + b(0,-1,2) + c(0,2,0), where a = 0, b = 1/2, c = 1/4;

Find the change matrix $P_{D\leftarrow B}$. Justify carefully your answer.

(b) (5 Pts) Let T(x, y, z) = (2y, z, z). Find the matrix representation of T on the basis B, that is $M_B(T)$.

$$\begin{array}{l} (c_{p}(\vec{b}_{1})) = \begin{bmatrix} \vec{0} \\ \vec{0} \end{bmatrix} & (110)(\vec{0}) = 1(112)(\vec{0}) + 0(0)(112) + -1(0)(10) \\ & = (112)(\vec{0}) + (0, -2, 0) \\ & = (112)(\vec{0}) + (0, -2, 0) \\ & = (112)(\vec{0}) \\ & = (112)(\vec{0}) \\ & = (112)(\vec{0}) + (0, -2, 0) \\ & = (0, 10)(\vec{0}) \\ & = (0, 10)(\vec{0})$$

$$(a) \quad (a) \quad (b) \quad (b)$$

QUESTION 3

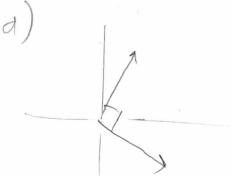
Let $U = \text{span}\{(-1, 0, 3), (0, -3, 2)\}.$

- (a) (3 Pts) Are (-1,0,3) and (0,-3,2) orthogonal?
- (b) (5 Pts) What is the dimension of U. Justify carefully your answer.
- (c) (5 Pts) Using the Gram-Schmidt process, transform the set of vectors $\{(-1,0,3),(0,-3,2)\}$ in a set of orthogonal vectors F.
- (d) (2 Pts) Illustrate visually the Gram-Schmidt orthogonalization process for two vectors in \mathbb{R}^2 .

c)
$$V_2 = (01.-3,2) - \frac{(-1,0,3)(0,-3,2)}{(-1)^2+(-)+(3)^2} \cdot (-1,0,3)$$

$$= (0, -3, 2) - (\frac{3}{5}) \cdot (-1, 0, 3)$$

$$= \left(\frac{3}{5}, -3, \frac{1}{5}\right)$$



Assume that $T: V \to \mathbb{R}^2$ is a linear transformation where V is a vector space and \mathbb{R} is the vector space of real numbers. Let $\{\mathbf{v_1}, \mathbf{v_2}, \mathbf{v_3}\}$ be a basis of V.

- (a) (1 Pt) If $T(\mathbf{v_1}) = (2, 2)$, $T(\mathbf{v_2}) = (1, 2)$ and $T(\mathbf{v_3}) = (2, 1)$, show that $-3\mathbf{v_1} + 2\mathbf{v_2} + 2\mathbf{v_3} \in \ker T$. Explain carefully your answer.
- (b) (4 Pts) If $T(\mathbf{v_1})$, $T(\mathbf{v_2})$ and $T(\mathbf{v_3})$ are defined as in part (a), find the nullity of T. Explain carefully your answer.

7) $T(v_1+v_2+v_3) = T(v_1) + T(v_2) + T(v_3)$ T(=(2,2) + ((1,2)) + (2,1)

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