

Name of the members of the team: \_\_\_\_\_

Team name (if any): \_\_\_\_\_

|           |    |    |       |
|-----------|----|----|-------|
| Question: | 1  | 2  | Total |
| Points:   | 10 | 10 | 20    |
| Score:    |    |    |       |

**Instructions:** You must answer all the questions in teams of 3 and hand out one copy per team. You are allowed to use the lecture notes only. No other tools such as a cell-phone, a calculator, or a laptop. Only your pen and eraser. The space between the questions are there to write the final versions of your answers.

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QUESTION 1 (10 pts)

Let  $f : [0, 2] \rightarrow \mathbb{R}$  be the function defined by  $f(x) = x^3 + 2x - 1$  and let  $L = 0$ . Find the interval  $[a_3, b_3]$  constructed in the proof of the Intermediate Value Theorem. (Exceptionnally, you can use the calculator to do some of the calculations.)

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**QUESTION 2**

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**(10 pts)**

Let  $S, T \subseteq \mathbb{R}$  be two open sets. Show that  $S \cap T$  is an open set. [Hint to start: Try to illustrate the situation and what you want to prove with a picture.]