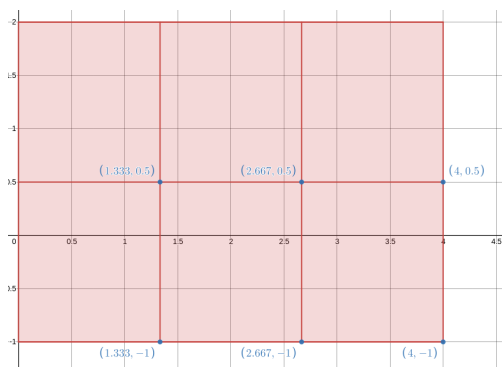


**Problem 2**

According to my lecture notes:

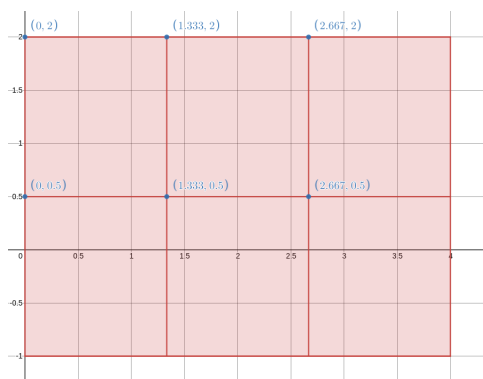
- (a) We split the rectangle in 6 smaller rectangles as depicted in the following figure (here  $m = 3$  and  $n = 2$ ):



We use  $x_1 = 4/3$ ,  $x_2 = 8/3$ ,  $x_3 = 4$ ,  $y_1 = -1$  and  $y_2 = 0.5$ . We then get

$$\iint_R (1 - xy^2) dA \approx \sum_{i=1}^3 \sum_{j=1}^2 (1 - x_i y_j^2) A(R_{ij}) = -8.$$

- (b) We split the rectangle in 6 smaller rectangles as depicted in the following figure (here  $m = 3$  and  $n = 2$ ):



We use  $x_1 = 0$ ,  $x_2 = 4/3$ , and  $x_3 = 8/3$ ,  $y_1 = 0.5$  and  $y_2 = 2$ . We then get

$$\iint_R (1 - xy^2) dA \approx \sum_{i=1}^3 \sum_{j=1}^2 (1 - x_i y_j^2) A(R_{ij}) = -22.$$

**Problem 18**

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We first compute the inside integral:

$$\int_0^{\pi/2} (\sin x + \sin y) dy = (y \sin x - \cos y) \Big|_0^{\pi/2} = (\pi/2) \sin x + 1.$$

Then we can compute the outer integral:

$$\int_0^{\pi/6} (\pi/2) \sin x + 1 dx = [-(\pi/2) \cos x + x] \Big|_0^{\pi/6} = (8 - 3\sqrt{3})\pi/12 \approx 0.734045.$$

**Problem 32**

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The integral is over a rectangle, so we use an iterated integral. We have

$$\iint_R \frac{x}{1+xy} dA = \int_0^1 \int_0^1 \frac{x}{1+xy} dy dx.$$

We put  $u = 1 + xy$ , so that  $du = x dy$ . This implies that

$$\int_0^1 \frac{x}{1+xy} dy = \int_1^{1+x} \frac{1}{u} du = \ln(1+x).$$

Then, we can evaluate the outer integral:

$$\int_0^1 \ln(1+x) dx = 2(\ln(2) - 1).$$

**Problem 36**

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The function  $z = 2 - x^2 - y^2$  is a paraboloid that is going downward and that is 2 units above the XY-plane. We are also integrating on the square  $R = [0, 1] \times [0, 1]$ . So the solid should look like this:

