

# MATH 302

## CHAPTER 1

### SECTION 1.1: APPLICATIONS LEADING TO DES

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| CONTENTS |
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|   |   |
|---|---|
| Little experiment                         | 2 |
| Newton's Law of Cooling                   | 3 |
| Second Version of Newton's Law of Cooling | 4 |

LITTLE EXPERIMENT

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**EXAMPLE 1.** Poor some hot water in a teapod and take its temperature with a thermometer. Take the temperature every 5 minutes. Record your data in a table and plot them in a Times VS Temperature graph.

TABLES

| Time | Temperature |
|------|-------------|
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| Time | Temperature |
|------|-------------|
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PLOTS

## NEWTON'S LAW OF COOLING

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**EXAMPLE 2.** Let  $T = T(t)$  be the temperature of a body at time  $t$  and let  $T_m$  be the temperature of its surrounding. Assuming that

- the rate of cooling of the body is directly proportional to the temperature difference of the surface area exposed
- the temperature of the surrounding does not change

deduce a model describing the evolution of the temperature  $T(t)$  of the body.

## SECOND VERSION OF NEWTON'S LAW OF COOLING

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Assuming that the medium (surrounding) remains at constant temperature seems reasonable if we're considering a cup of tea/coffee cooling in a room.

What if the body warms or cools its surrounding, resulting in changing drastically the surrounding temperature?

**EXAMPLE 3.** Let  $T = T(t)$  be the temperature of the body at time  $t$  and let  $T_m = T_m(t)$  be the temperature of its surrounding. Assuming that

- the rate of cooling of the body is directly proportional to the temperature difference of the surface area exposed
- the energy is preserved

deduce a model describing the evolution of the temperature  $T(t)$  of the body.

