Chapter 1 Functions and Limits

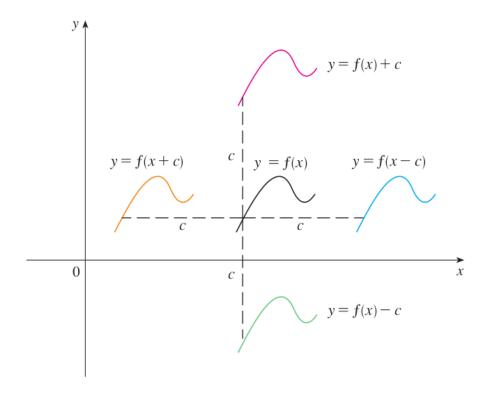
1.3 New Functions from Old Functions

Transformations of Functions.

Translation.

Vertical and Horizontal Shifts Suppose c > 0. To obtain the graph of

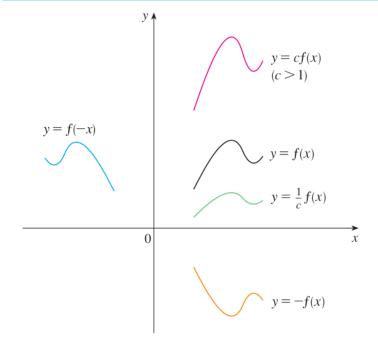
y = f(x) + c, shift the graph of y = f(x) a distance c units upward y = f(x) - c, shift the graph of y = f(x) a distance c units downward y = f(x - c), shift the graph of y = f(x) a distance c units to the right y = f(x + c), shift the graph of y = f(x) a distance c units to the left



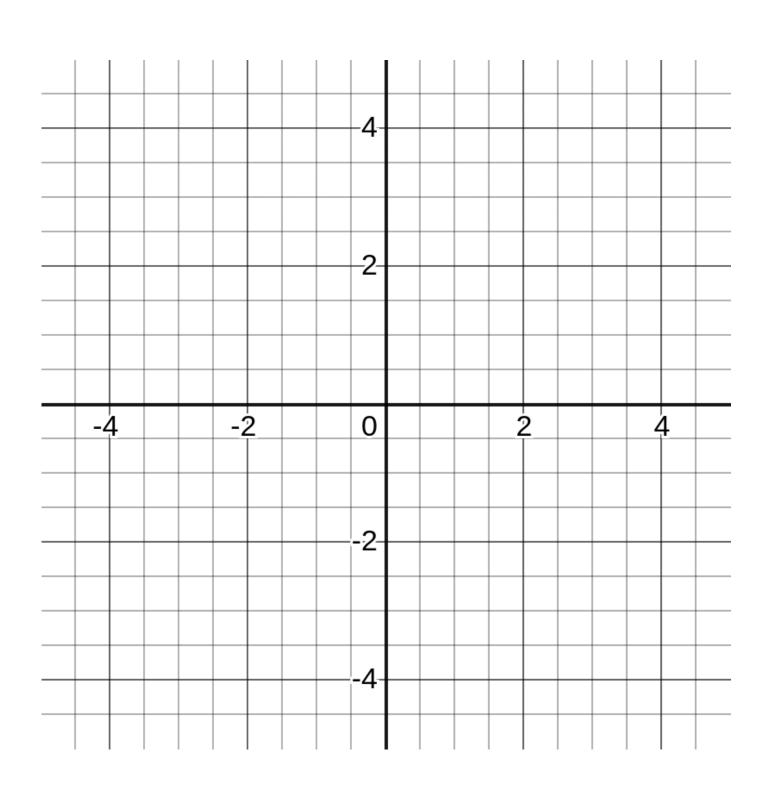
Stretching and reflecting.

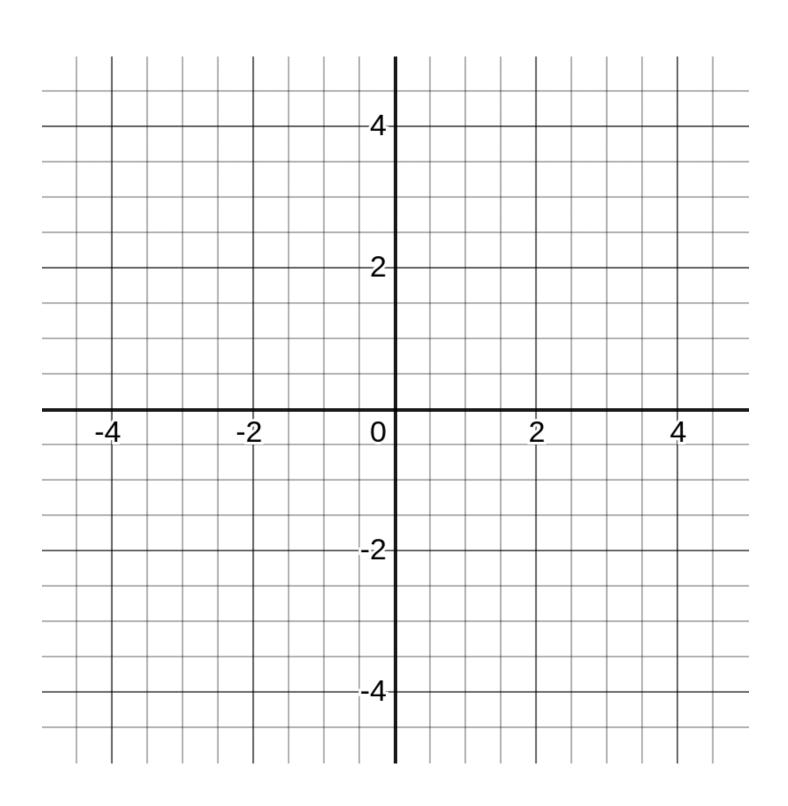
Vertical and Horizontal Stretching and Reflecting Suppose c>1. To obtain the graph of

y=cf(x), stretch the graph of y=f(x) vertically by a factor of c y=(1/c)f(x), shrink the graph of y=f(x) vertically by a factor of c y=f(cx), shrink the graph of y=f(x) horizontally by a factor of c y=f(x/c), stretch the graph of y=f(x) horizontally by a factor of c y=-f(x), reflect the graph of y=f(x) about the x-axis y=f(-x), reflect the graph of y=f(x) about the y-axis



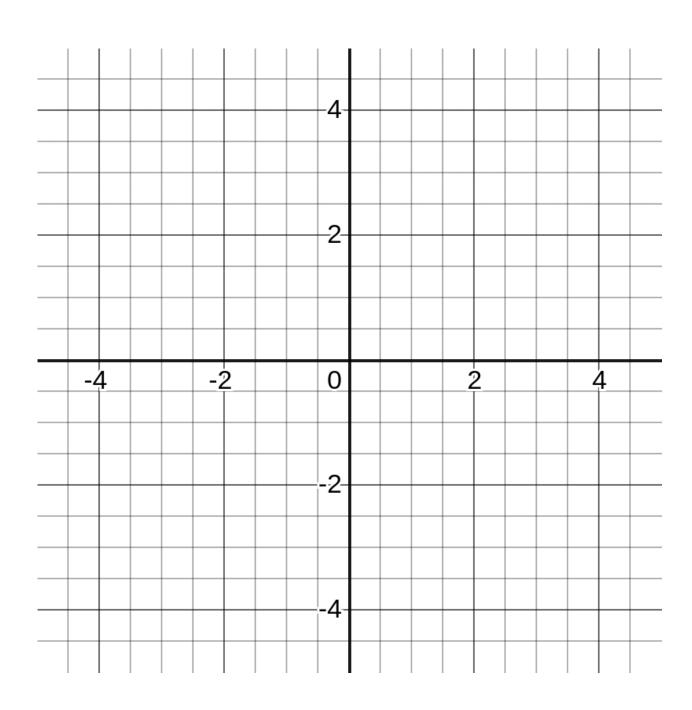
EXAMPLE 1 Given the graph of $y = \sqrt{x}$, use transformations to graph $y = \sqrt{x} - 2$, $y = \sqrt{x - 2}$, $y = -\sqrt{x}$, $y = 2\sqrt{x}$, and $y = \sqrt{-x}$.

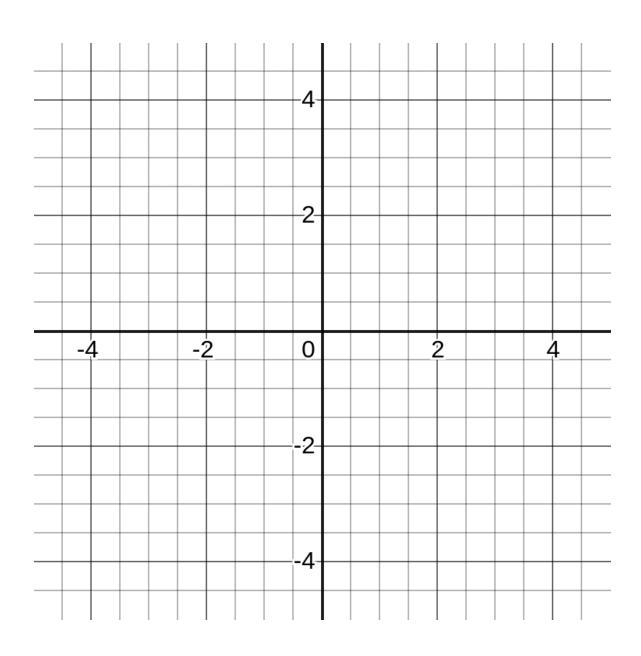




(a)
$$y = \sin 2x$$

(b)
$$y = 1 - \sin x$$





Combinaisons of Functions.	
Adding.	Substracting.
Domain:	Domain:
Multiplying.	Dividing.
	Domain:
Domain:	
Example. Find the domain of the function $f(x) = \sqrt{x} + \sqrt{2-x} \ .$	Example Find the domain of the function $f(x) = \frac{x^2}{x-1}$.
Composite of two functions (Composition).	
Definition Given two functions f and g , the composite function $f \circ g$ (also called the composition of f and g) is defined by	

 $(f \circ g)(x) = f(g(x))$

Domain:

EXAMPLE 6 If $f(x) = x^2$ and g(x) = x - 3, find the composite functions $f \circ g$ and $g \circ f$.

EXAMPLE 7 If $f(x) = \sqrt{x}$ and $g(x) = \sqrt{2-x}$, find each of the following functions and their domains.

- (a) $f \circ g$
- (b) $g \circ f$ (c) $f \circ f$ (d) $g \circ g$

