Don't get confused, π is a constant (it does not depend on x). So π^2 is a constant. Then f'(x) = 0.

Problem 4

Using the fact that the derivative of a sum is the sum of the derivatives and the power rule, we have

$$g'(x) = \frac{dg}{dx} = \frac{d}{dx} \left(\frac{7}{4}x^2\right) - 3\frac{d}{dx}(x) + \frac{d}{dx}(12)$$
$$= (7/4)2x - 3(1) + 0$$
$$= (7/2)x - 3.$$

Therefore, g'(x) = (7/2)x - 3.

Problem 18

Using the quotient rule, we obtain

$$y' = \frac{(\sqrt{x} + x)'x^2 - (\sqrt{x} + x)(x^2)'}{x^4}.$$

We have, from the power rule,

$$(\sqrt{x} + x)' = 1/2\sqrt{x} + 1$$
 and $(x^2)' = 2x$

and so replacing that in y', we obtain

$$y' = \frac{(1/2\sqrt{x}+1)x^2 - (\sqrt{x}+x)2x}{x^4} = \frac{x^{3/2}/2 + x^2 - 2x^{3/2} - 2x^2}{x^4} = \frac{-3x^{3/2}/2 - x^2}{x^4}.$$

Finally, we get $y' = -3x^{-5/2}/2 - x^{-2}$.

There is another approach. By letting $x \neq 0$, we can rewrite the expression as

$$y = x^{-3/2} + x^{-1}$$

and by the sum and quotient rules, we obtain

$$y' = -3x^{-5/2}/2 - x^{-2}.$$

Using the product rule, we have

$$B'(u) = (2u^2 - 4u - 1)\frac{d}{du}(u^3 + 1) + (u^3 + 1)\frac{d}{du}(2u^2 - 4u - 1).$$

Then, using the sum rule and the power rule for derivatives, we get

$$\frac{d}{du}(u^3+1) = 3u^2$$

and

$$\frac{d}{du}(2u^2 - 4u - 1) = 4u - 4.$$

Plugging in back in B'(u), we get

$$B'(u) = (2u^2 - 4u - 1)3u^2 + (u^3 + 1)(4u - 4) = 6u^4 - 12u^3 - 3u^2 + 4u^4 - 4u^3 + 4u - 4$$
$$= 10u^4 - 16u^3 - 3u^2 + 4u - 4.$$

Therefore, $B'(u) = 10u^4 - 16u^3 - 3u^2 + 4u - 4$.

Problem 30

Using the quotient rule, we get

$$h'(t) = \frac{(6t-1)\frac{d}{dt}(6t+1) - (6t+1)\frac{d}{dt}(6t-1)}{(6t-1)^2}$$
$$= \frac{(6t-1)6 - (6t+1)6}{(6t-1)^2}$$
$$= -\frac{36}{(6t-1)^2}.$$

Problem 54

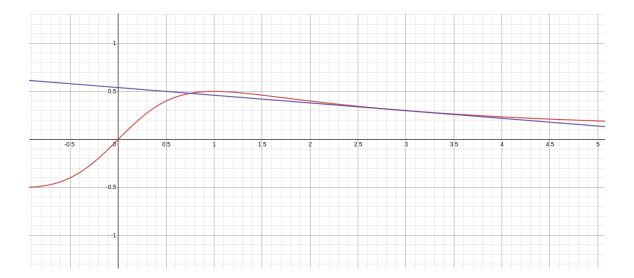
(a) We first find the derivative. We get

$$y' = \frac{1 + x^2 - 2x^2}{1 + x^2} = \frac{1 - x^2}{(1 + x^2)^2}.$$

The equation of the tangent line is given by the equation y - 0.3 = y'(3)(x - 3). So, pugging in the numbers, with y' = -8/100 = -2/25, we obtain

$$y - 0.3 = (-2/25)(x - 3) \Rightarrow y = (-0.08)x + 0.54.$$

(b) Using Desmos, we get the following picture.



The equation of the tangent line at (4, 0.4) is

$$y - 0.4 = f'(0.4)(x - 4).$$

We have $f(x) = \sqrt{x}/(x+1)$. Using the quotient rule, we get

$$f'(x) = \frac{\frac{x+1}{2\sqrt{x}} - \sqrt{x}}{(x+1)^2} = \frac{1-x}{2\sqrt{x}(x+1)^2}.$$

Therefore, we have f'(4) = -0.03. Plugging this into the equation of the tangent line and after simplifying, we get

$$y = 0.52 - 0.03x$$
.

Problem 66

Using the power rule for derivatives, we see that

$$S'(A) = (0.882)(0.842)A^{-0.158} = (0.742644)A^{-0.158}.$$

Using the formula for S'(A), we find that

$$S'(100) = (0.882)(0.842)(100)^{-0.158} \approx 0.35874 \text{ trees/m}^2$$

where m² means square meters.

Since the function f(x) = x is not zero at x = 2, we can use the quotient rule. We obtain

$$\frac{d}{dx}\left(\frac{h(x)}{x}\right) = \frac{h'(x)x - h(x)}{x^2}$$

and then, at x = 2, we get

$$\left. \frac{d}{dx} \left(\frac{h(x)}{x} \right) \right|_{x=2} = \frac{h'(2) \times 2 - h(2)}{4} = \frac{(-3) \times 2 - 4}{4} = -5/2.$$