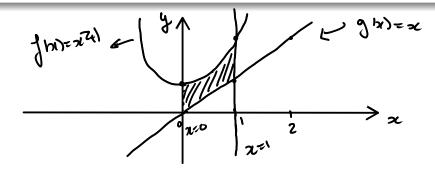


Compute the region bounded from above by the curve $f(x) = x^2 + 1$, bounded from below by the curve g(x) = x, and bounded on the sides by x = 0 and x = 1.





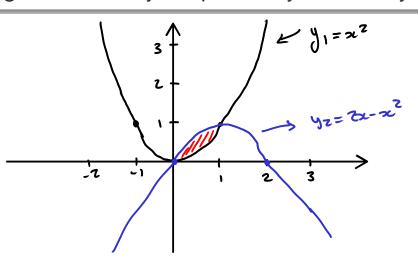
$$A = \int_0^1 \frac{f(x) - g(x)}{f(x) - g(x)} dx = \int_0^1 \frac{x^2 + 1 - x}{x^2 + 1 - x} dx$$

$$= \frac{x^3}{3} + x - \frac{x^2}{2} \Big|_0^1$$

$$= \frac{5}{6} u^2$$

Find the area of the region enclosed by the parabola $y = x^2$ and $y = 2x - x^2$.

$$y_2 = 2x - x^2$$
 $= (2 - x) x$
 $= 0$
 $1 \neq x = 2 \neq x = 0$



2) Find the intersections between y, d yz

Area het aveen
$$y, dy_2$$

$$A = \int_0^1 y_2 - y, dx = \int_0^1 2\pi - x^2 - x^2 dx$$

$$= \int_0^1 2\pi - 2x^2 dx$$

$$= \left(\frac{z^2 - \frac{z}{3}x^3}{3}\right)_0^1$$

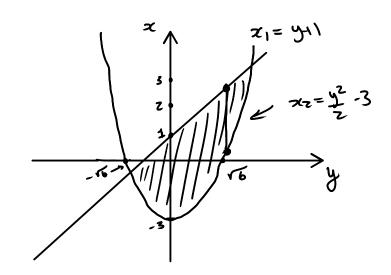
 $=\frac{1}{3}unt^2$

y= + \ Z = + 6

Find the area enclosed by the line y = x - 1 and the parabola $y^2 = 2x + 6$.



$$x_i = \frac{y^2}{a} - 3$$



(2) Intersections

$$\alpha_2 = \alpha_1$$

$$\frac{1}{4} - 3 = 4 + 1$$

$$x_2 = x_1$$
 if $y^2 - 3 = y + 1$ if $y = 4$ $y = -2$.

$$\frac{Area}{A} = \int_{-2}^{4} 2(1-2)(2) dy = \int_{-2}^{4} (4)(1-2)(2) dy$$

$$= \int_{-2}^{4} y+1 - (y^2 - 3) dy$$

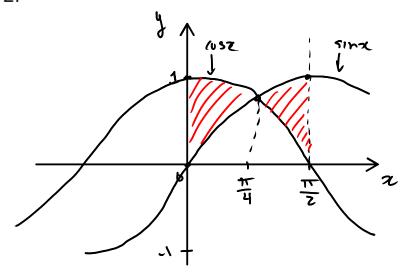
$$= \int_{-2}^{4} y - y^{2} + 4 dy$$

$$= \frac{y^{2}}{z} - \frac{y^{3}}{6} + 4y \Big|_{-2}^{4}$$

Find the area of the region bounded by the curve $y = \sin x$ and $y = \cos x$ from $\underline{x} = 0$ and $\underline{x} = \pi/2$.

(1) Grophs.

りっこらいつと



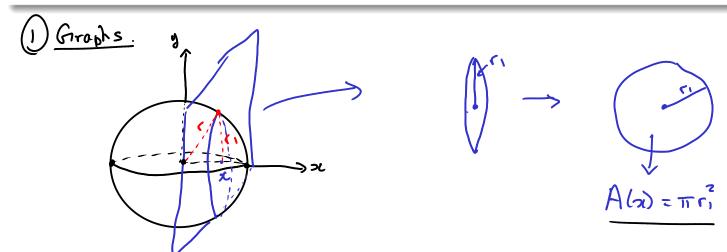
Nitia that cosx 2 pinx on [0,1/4]

Z) Intersection.

 $\frac{1 \text{ nerselvin.}}{\cos 2} = \sin 2 \quad \text{if} \quad 1 = +\cos 2 \quad \text{if} \quad x = \sqrt{\frac{11}{4}} + k\pi$ $\sqrt{1 + \cos 2} = \cos 2 \quad \text{for } \cos 2 = \frac{\pi}{4}$ $\sqrt{1 + \cos 2} = \cos 2 \quad \text{for } \cos 2 = \frac{\pi}{4}$ $\sqrt{1 + \cos 2} = \cos 2 \quad \text{for } \cos 2 = \frac{\pi}{4}$

3) Tot Area $A = \int_{6}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi - \sin \pi| |\cos \pi| = \int_{0}^{\pi/2} |\cos \pi| = \int_{0}^{\pi$

Show that the volume of a sphere of radius r is $V = \frac{4}{3}\pi r^3$.



$$r_{1}^{2} + 2c^{2} = r^{2} \implies r_{1}^{2} = r^{2} - 2c^{2}$$

$$\implies r_{1} = \sqrt{r^{2} - 2c^{2}}$$

$$\implies r_{1} = \sqrt{r^{2} - 2c^{2}}$$

$$\implies r_{1} = \sqrt{r^{2} - 2c^{2}}$$

$$\implies r_{2} = \pi \left(r^{2} - 2c^{2}\right)$$

Find the Volume
$$-r \le x \le r$$

$$V = \int_{-r}^{r} \frac{A(x)}{a_{r}u} dx = \int_{-r}^{r} \frac{T(r^{2} - x^{2})}{r^{2}u} dx$$

$$= \frac{1}{r} \left(r^{2}x - \frac{x^{3}}{3} \right) \left[\frac{1}{r^{2}} \right]$$

$$= \pi \left(r^{2} \pi - \frac{\pi^{3}}{3} \right) \left[r^{2} \pi - \frac{\pi^{3}}{3} - \left(-r^{3} + \frac{r^{3}}{3} \right) \right]$$

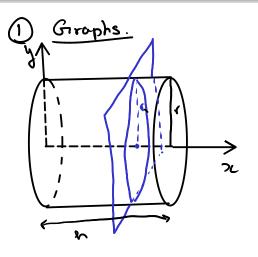
$$= \pi \left(2r^{3} - \frac{3r^{3}}{3} \right)$$

$$= \pi \left(r^{3} - \frac{7^{3}}{3} \right) = 2\pi \left(\frac{2r^{3}}{3} \right)$$

$$= 2\pi \left(r^{3} - \frac{7^{3}}{3} \right) = 2\pi \left(\frac{2r^{3}}{3} \right)$$

$$= 2\pi \left(r^{3} - \frac{7^{3}}{3} \right) = 2\pi \left(\frac{2r^{3}}{3} \right)$$

Find the volume of a cylinder of radius r and height h.



The place is a circle with the same roding as the base of the cylinder.

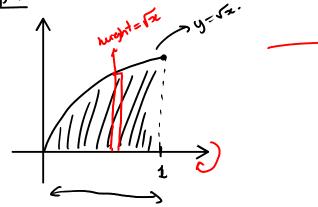
(2) Find A(x)
$$\Gamma_1 = \Gamma - A(x) = \pi - C^2$$

(3) Yolume
$$V = \int_0^h A(x) dx = \int_0^h \pi r^2 dx = \pi r^2 x \Big|_0^h$$

$$= \pi r^2 h$$

Find the volume of the object obtained by rotating the function $f(x) = \sqrt{x}$ $(0 \le x \le 1)$ around the x-axis.

1) Grophs.



A(si) = TT T

(2) Find A(2)

So,
$$A(x) = \pi r^2 = \pi (\sqrt{x})^2 = \pi x$$

Find Volume. $V = \int_{0}^{1} A(si) dsi = \int_{0}^{1} \pi x dx = \pi \frac{z^{2}}{z} = \frac{\pi}{z} units^{2}$

Find the volume of the object obtained by rotating the region enclosed by the curves $y=x^3$, y=8, and x=0 about the y-axis.

Find the volume of the object obtained by rotating the region enclosed by the curves y=x and $y=x^2$ about the line y=2.