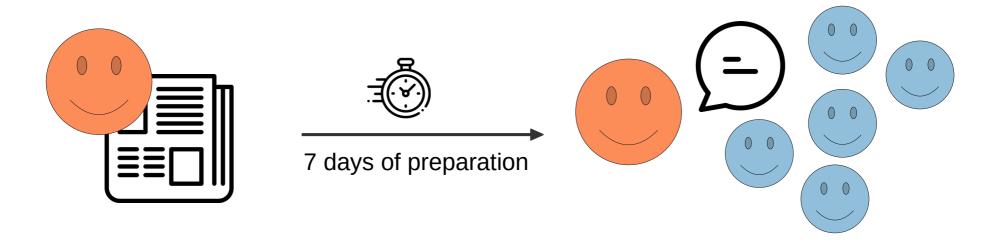
# Population genomics



camille.roux@univ-lille.fr

#### Evaluation on the module:

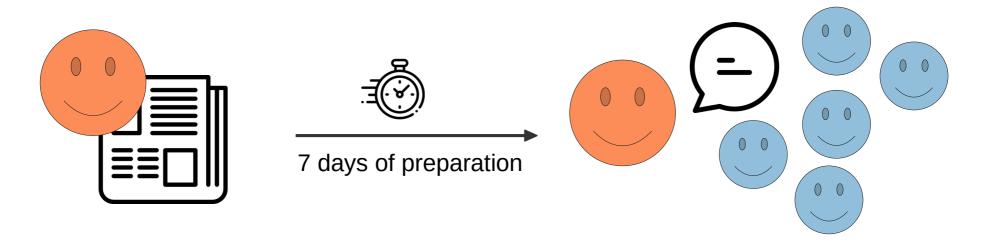
Each student will present an article at the beginning of each session



The aim of this student: make the message of the article clear to the audience.

#### Evaluation on the module:

Each student will present an article at the beginning of each session



The aim of this student: make the message of the article clear to the audience.

20 minutes of presentation ...

... followed by questions



#### Evaluation on the module:

Each student will present an article at the beginning of each session

#### Clarity:

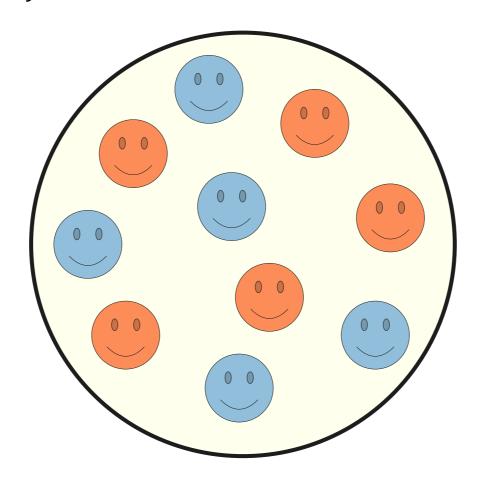
- · Making clear the **context** (why o this study?): 4 points
- · What is the **scientific question** ? 2 points
- · In concrete terms, what **do the authors do to answer** the question? 4 points
- · What are the **results** ? 4 points
- Interpretation of the results: 4 points
- Take home message from the paper : 2 points

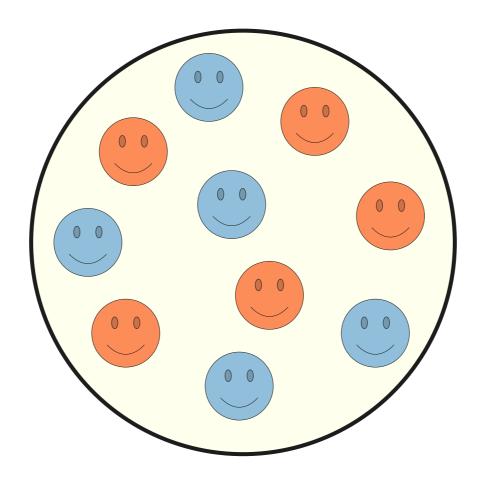
# Population genomics



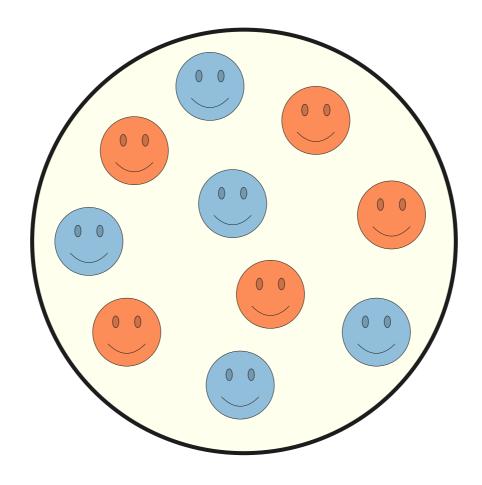
camille.roux@univ-lille.fr

Today: an introduction to pop. geno.



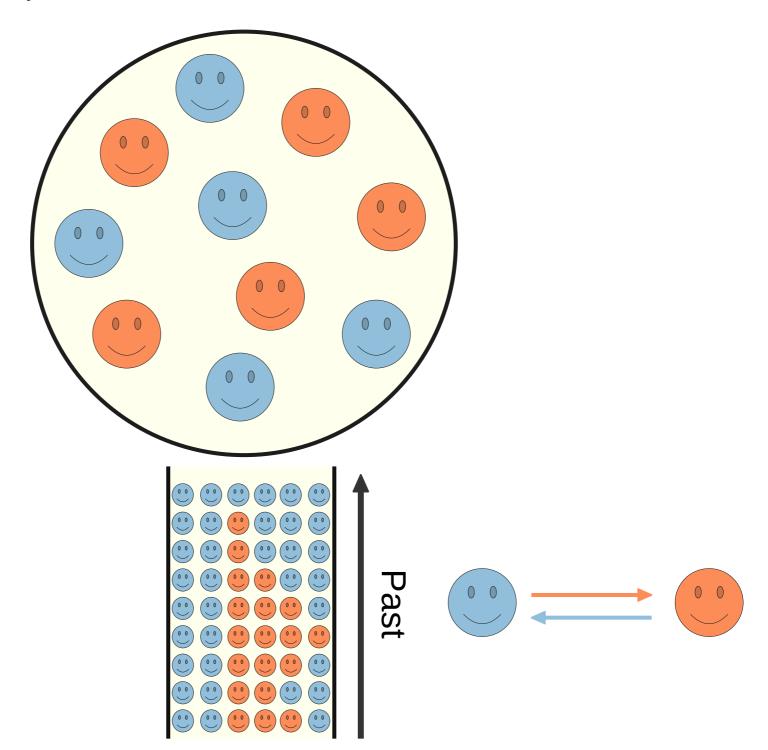


How to quantify diversity?

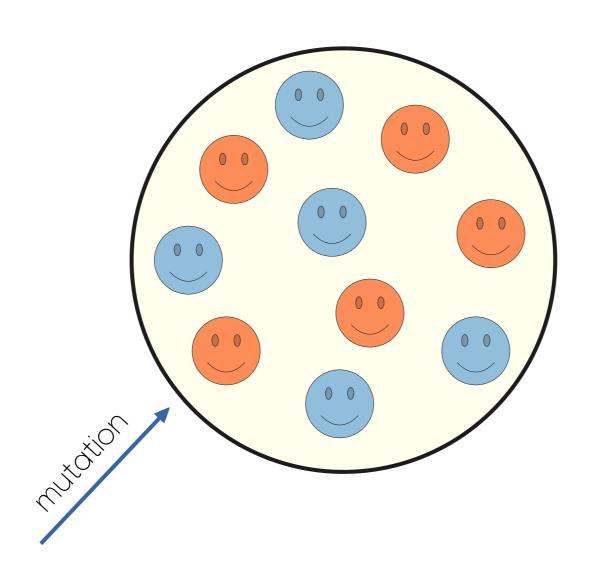


How to quantify diversity?

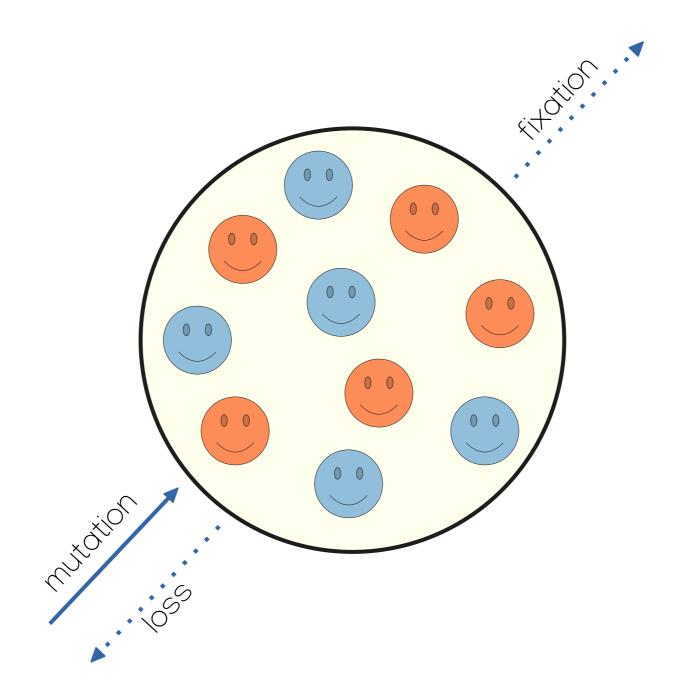
How to interpret this diversity?



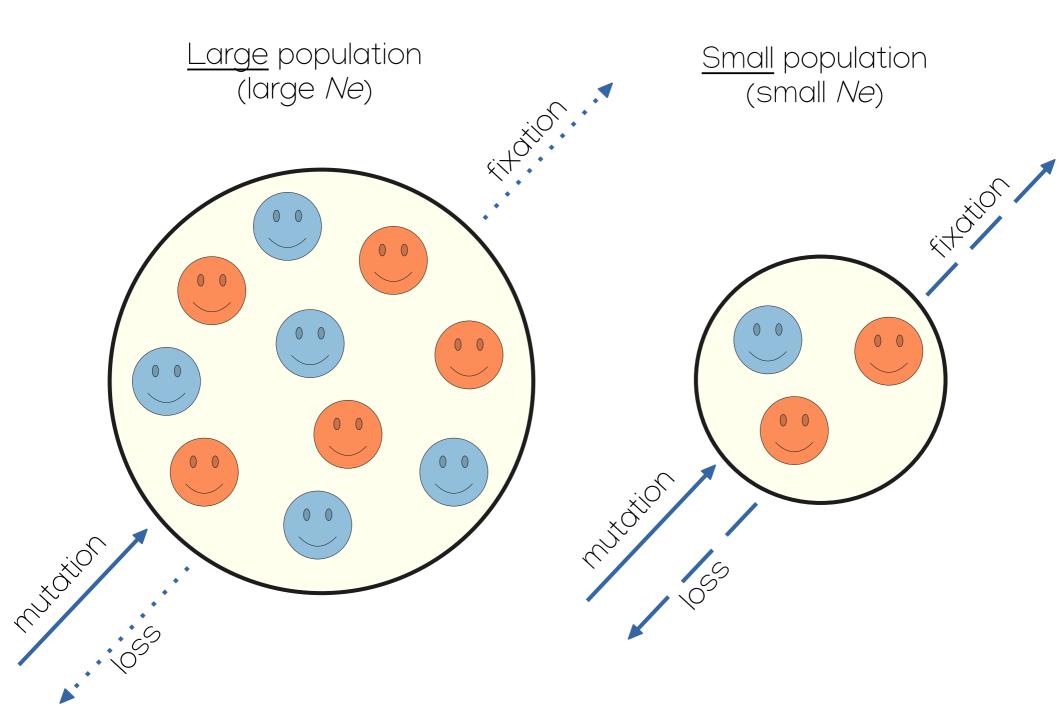
The product  $Ne.\mu$ : important determinant of genetic diversity



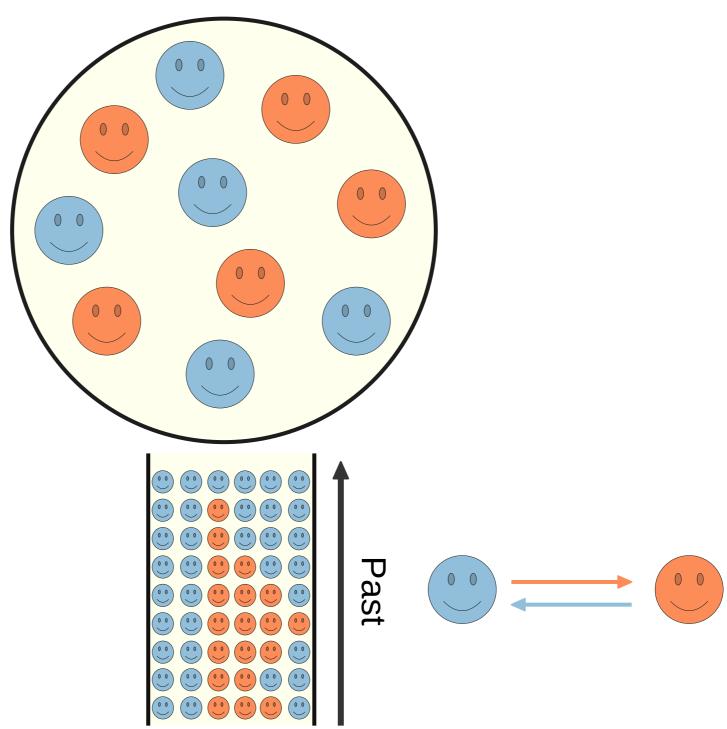
The product  $Ne.\mu$ : important determinant of genetic diversity

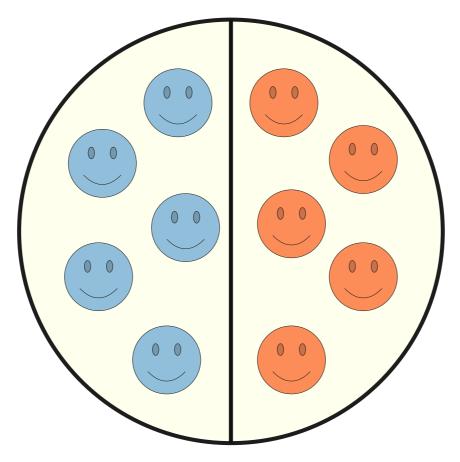


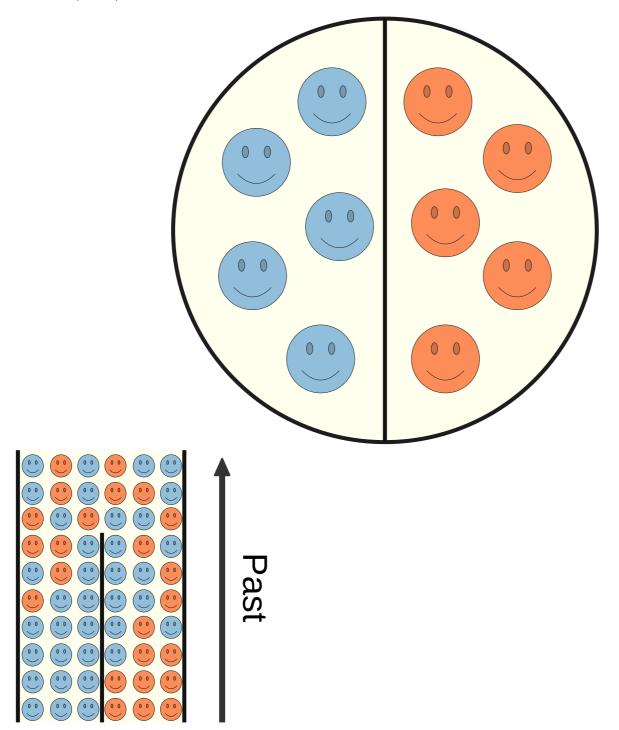
The product  $Ne.\mu$ : important determinant of genetic diversity

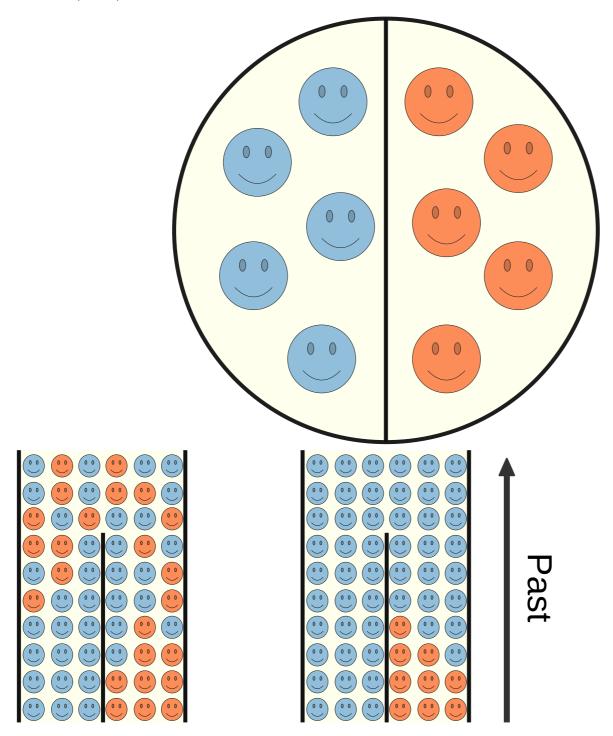


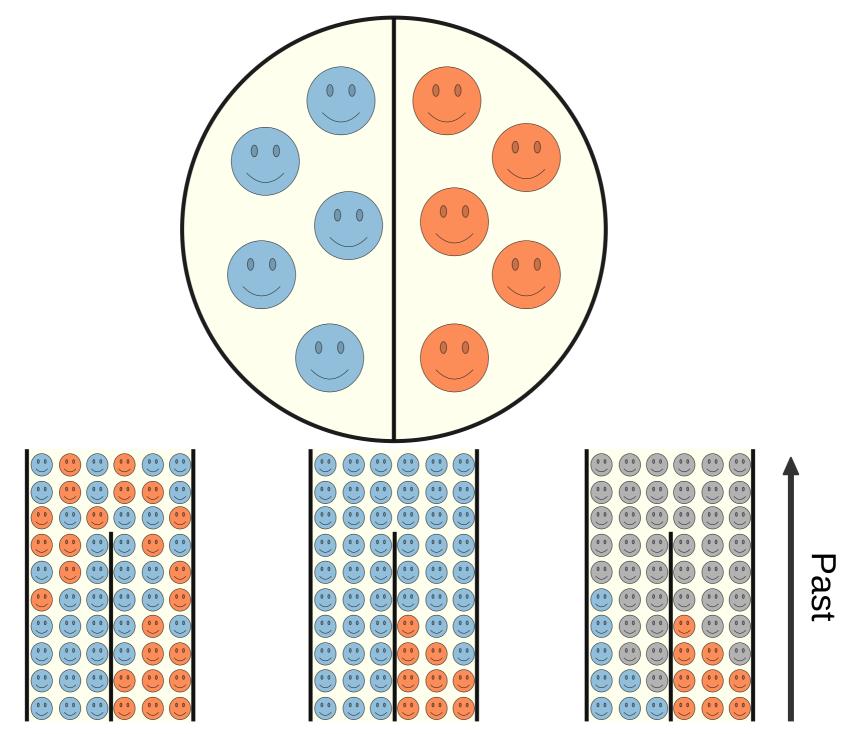
## Wright and Fisher model



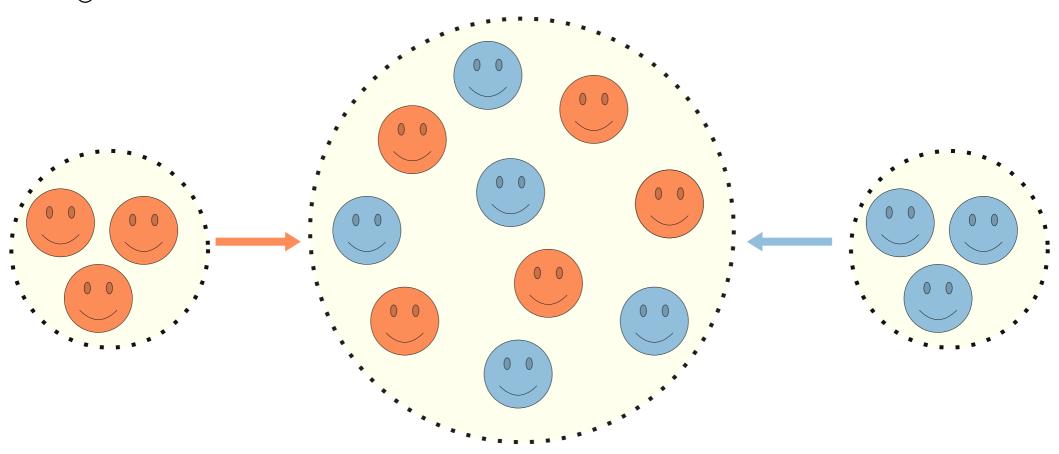




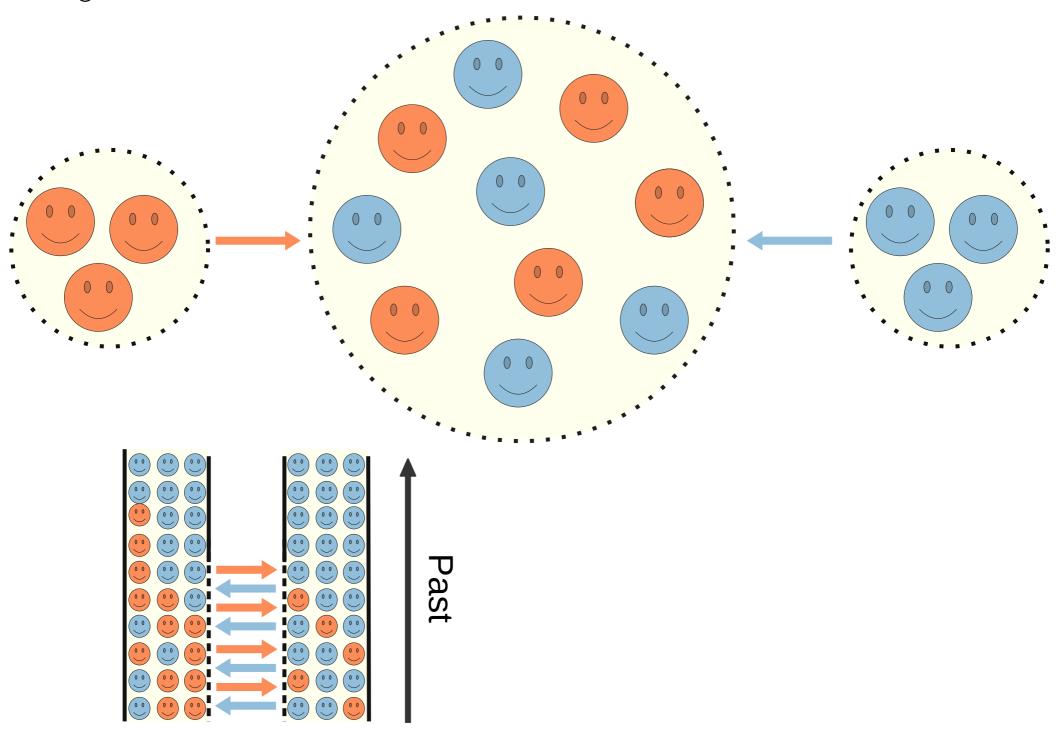




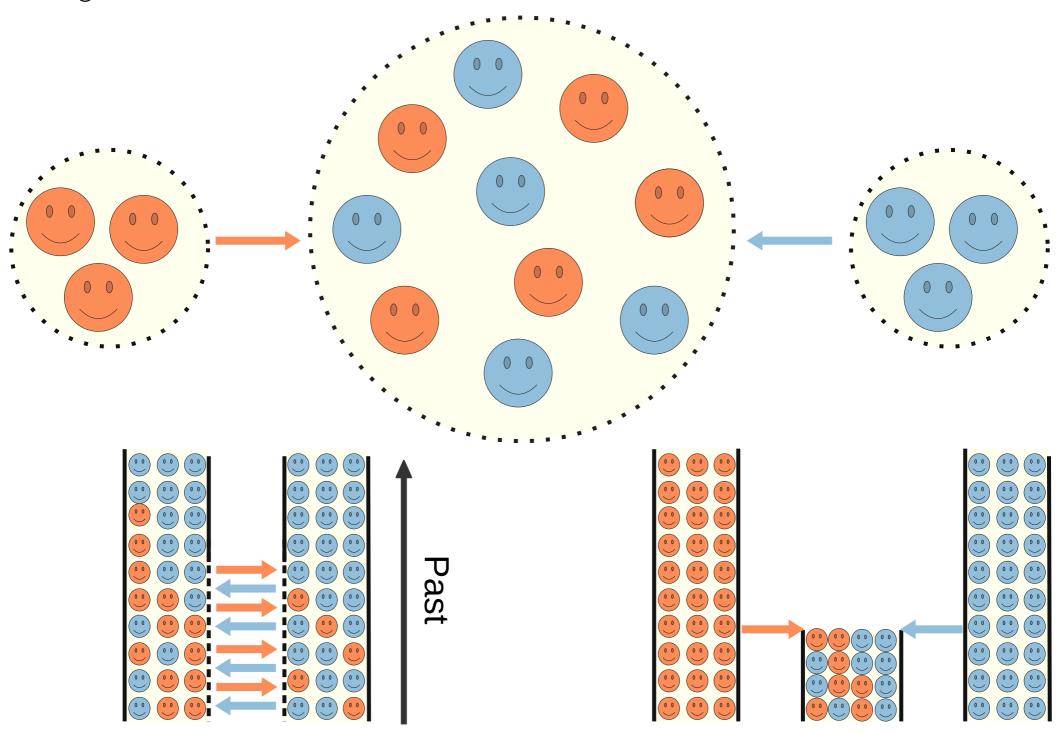
# Migration

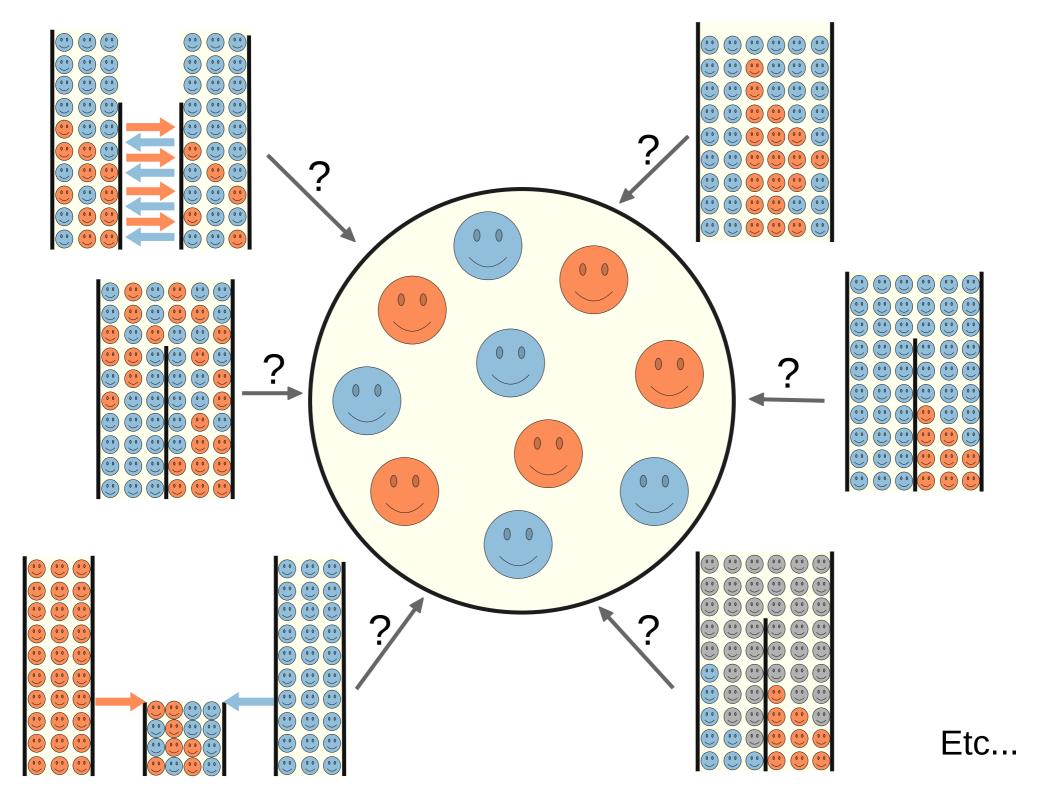


## Migration

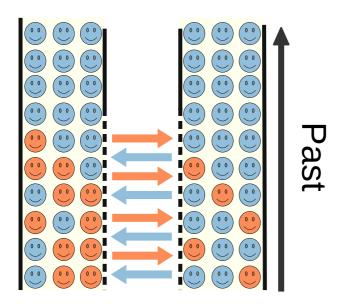


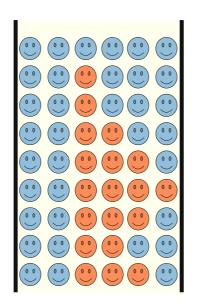
### Migration

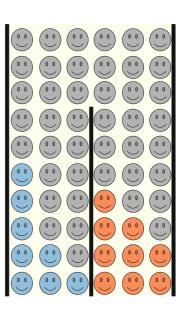




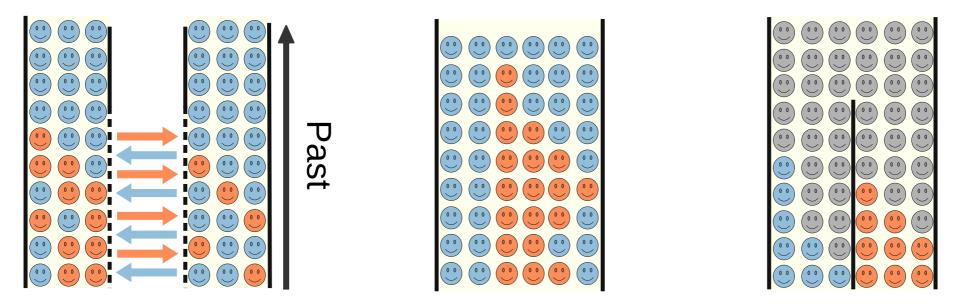
#### 1. How to compare alternative demographic scenarios?





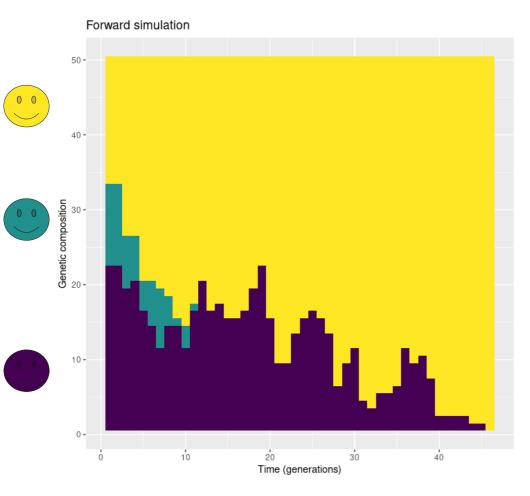


1. How to compare alternative demographic scenarios?



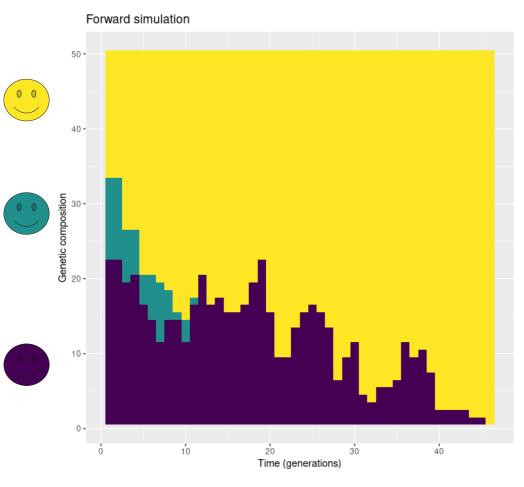
2. What evolutionary forces act on a given locus?

#### Genetic drift

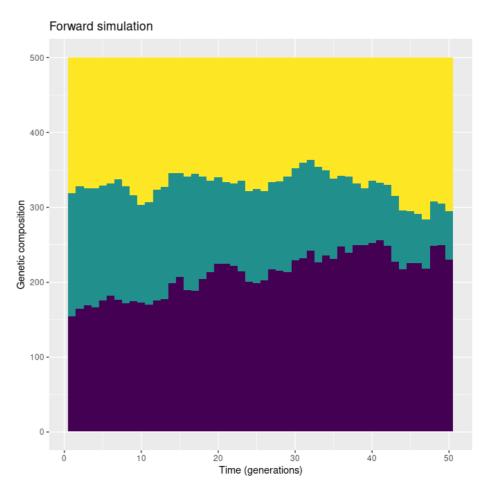


Ne = 50 (individuals)

#### Genetic drift

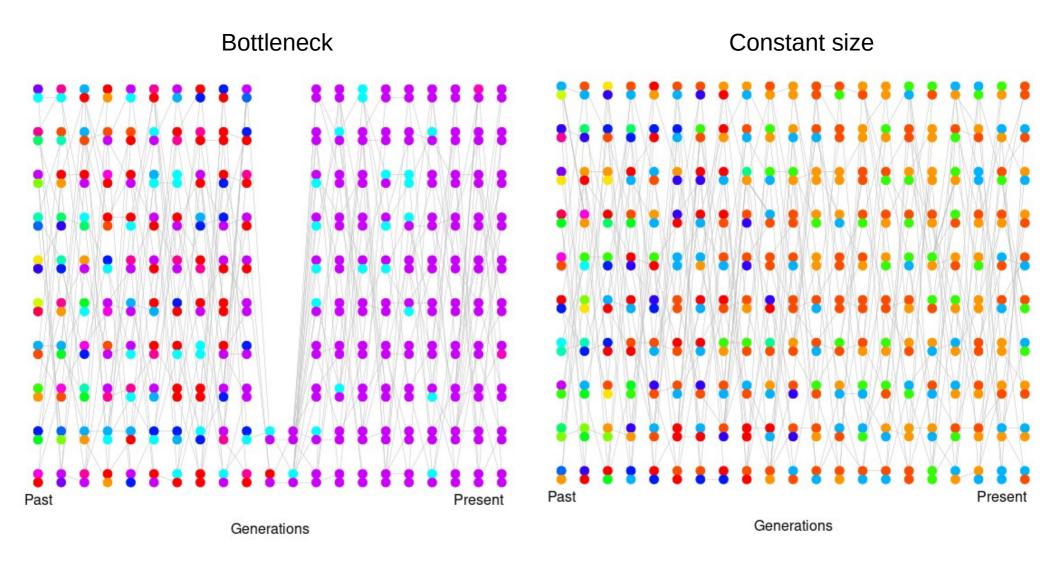


Ne = 50 (individuals)



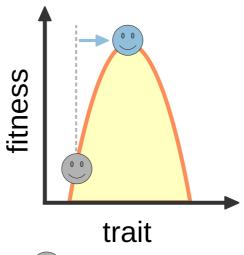
Ne = 500

#### Genetic drift



#### Natural selection

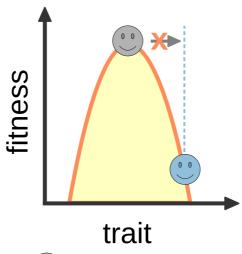
#### **Directional selection**



- Ancestral allele
- **Derived allele**

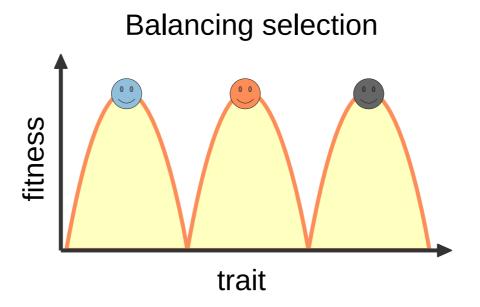
#### Natural selection

#### Purifying selection



- Ancestral allele
- **Derived allele**

#### Natural selection

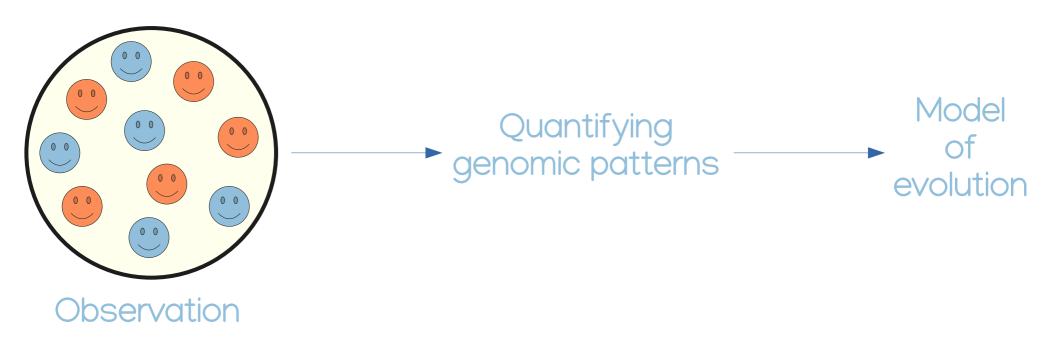


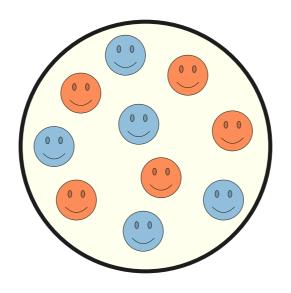
1. How to compare alternative demographic scenarios?

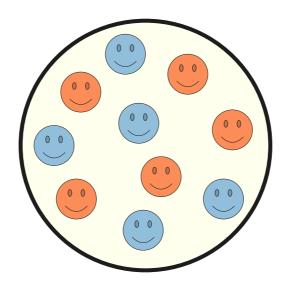
2. What evolutionary forces act at a given locus?

1. How to compare alternative demographic scenarios?

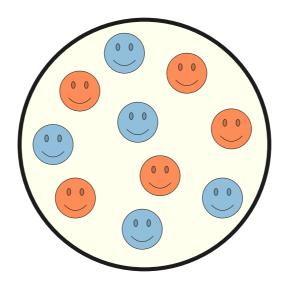
2. What evolutionary forces act at a given locus?







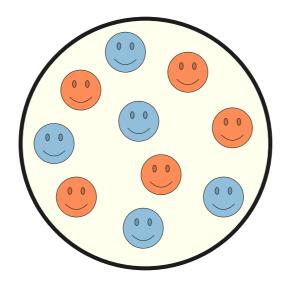
1. Sampling individuals from natural population(s)



1. Sampling individuals from natural population(s)



2. Sequencing them



1. Sampling individuals from natural population(s)



2. Sequencing them

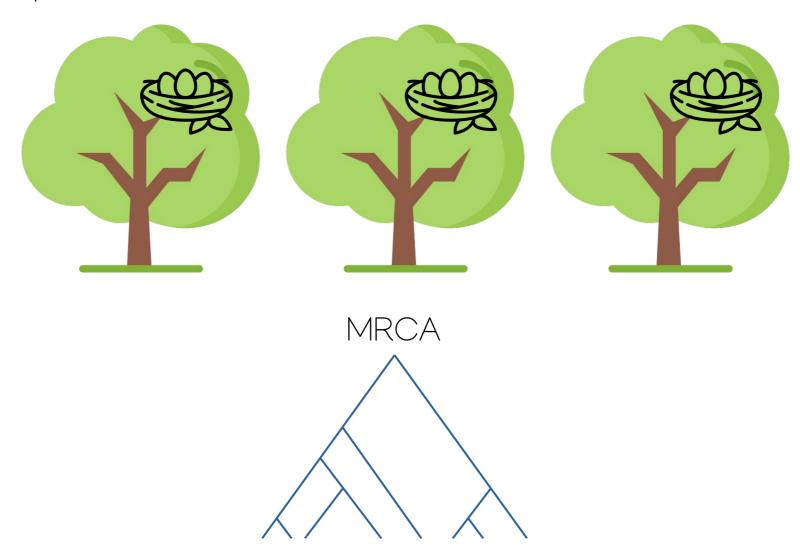


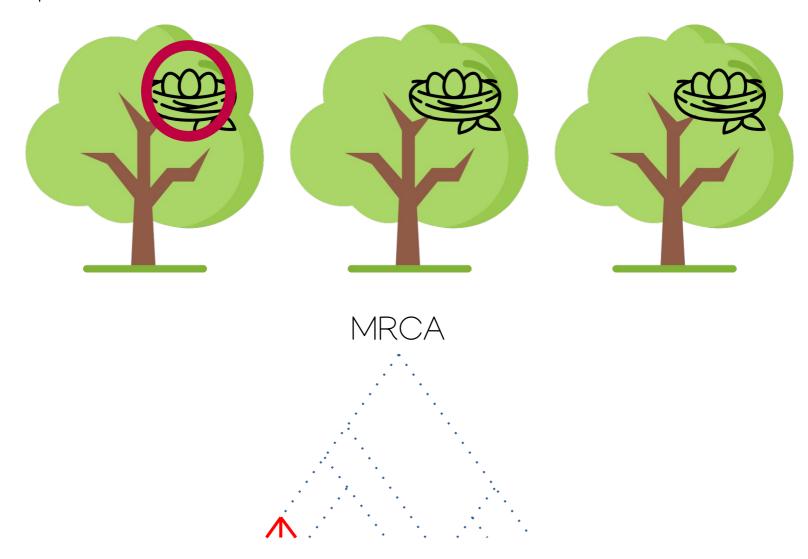
3. Analyse the sequences

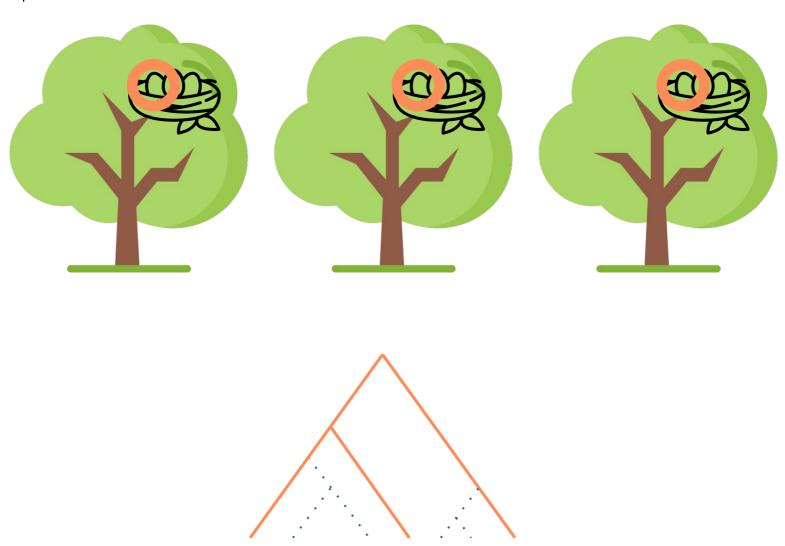
1. Sampling individuals from natural population(s)

Samples must be a set of unrelated individuals

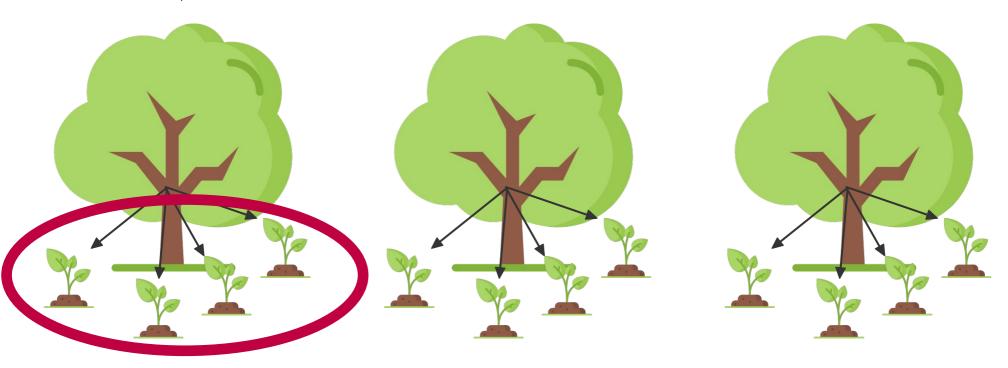














Samples must be a set of unrelated individuals

Generally: use between 10 and 50 individual chromosomes (5 to 25 diploid individuals)

Samples must be a set of unrelated individuals

Generally: use between 10 and 50 individual chromosomes (5 to 25 diploid individuals)

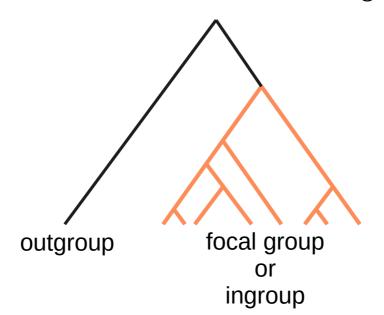
Inference requires a set of seuqnces sampled from a single population population = group of randomly mating individuals

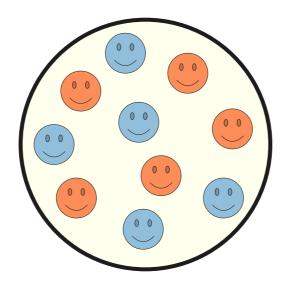
Samples must be a set of unrelated individuals

Generally: use between 10 and 50 individual chromosomes (5 to 25 diploid individuals)

Inference requires a set of seuqnces sampled from a single population population = group of randomly mating individuals

For some methods: a sequenced outgroup is required



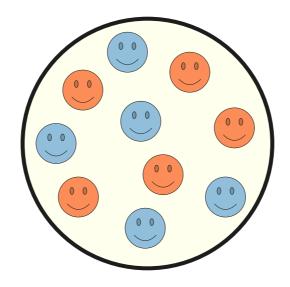


How can we measure that ?!?

1. Sampling individuals from natural population(s)



2. Sequencing them



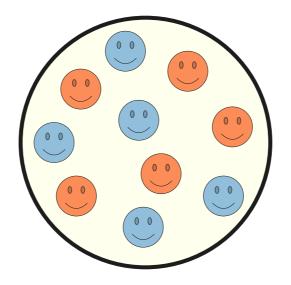
How can we measure that ?!?

1. Sampling individuals from natural population(s)



2. Sequencing them

How?



How can we measure that ?!?

1. Sampling individuals from natural population(s)

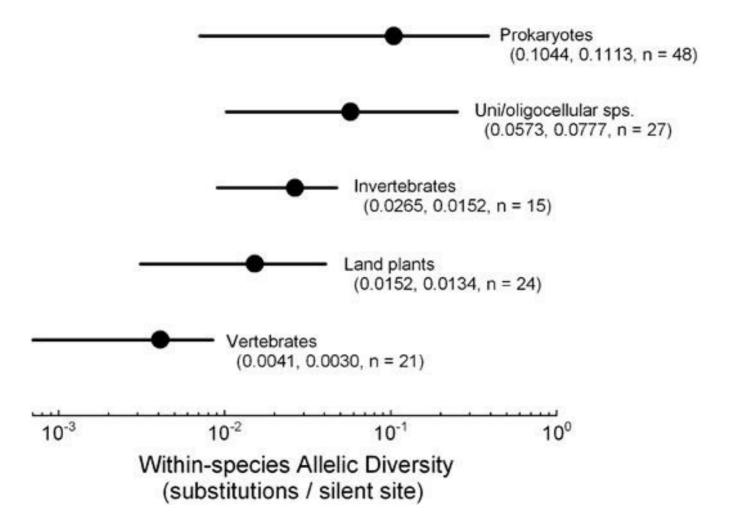


2. Sequencing them

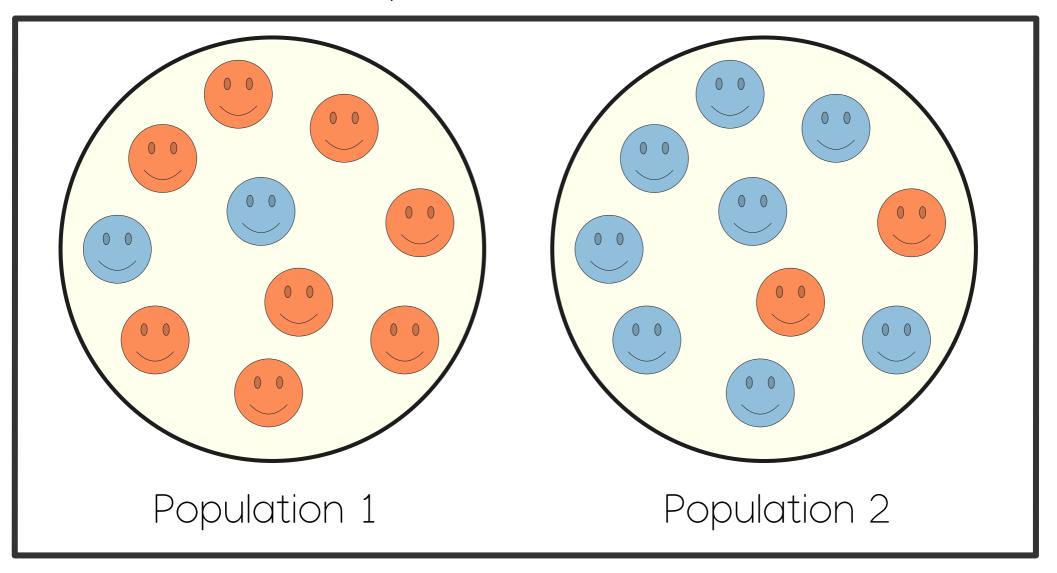


3. Analyse the sequences

### With missing data?

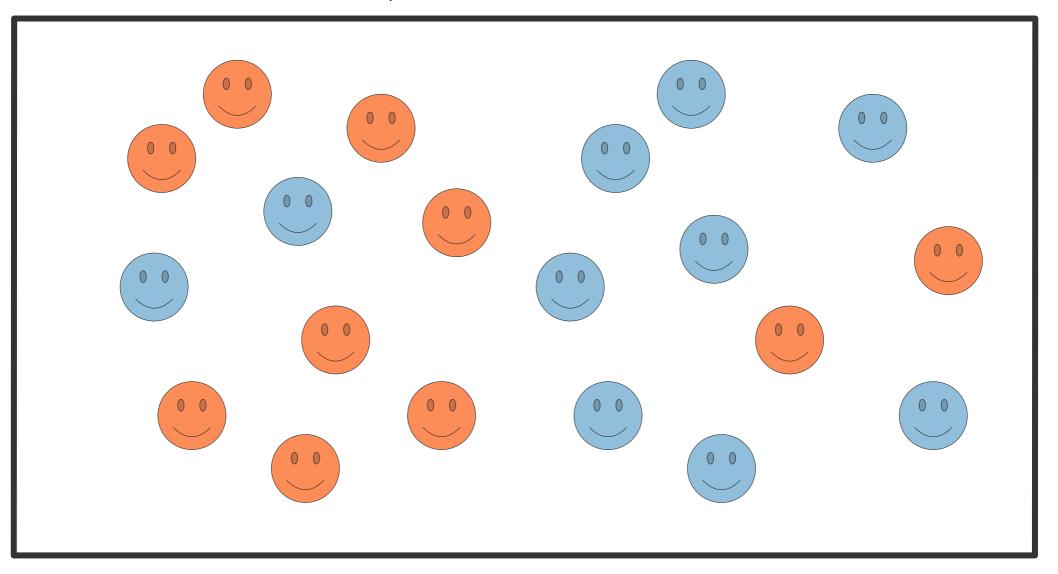


### Population structure

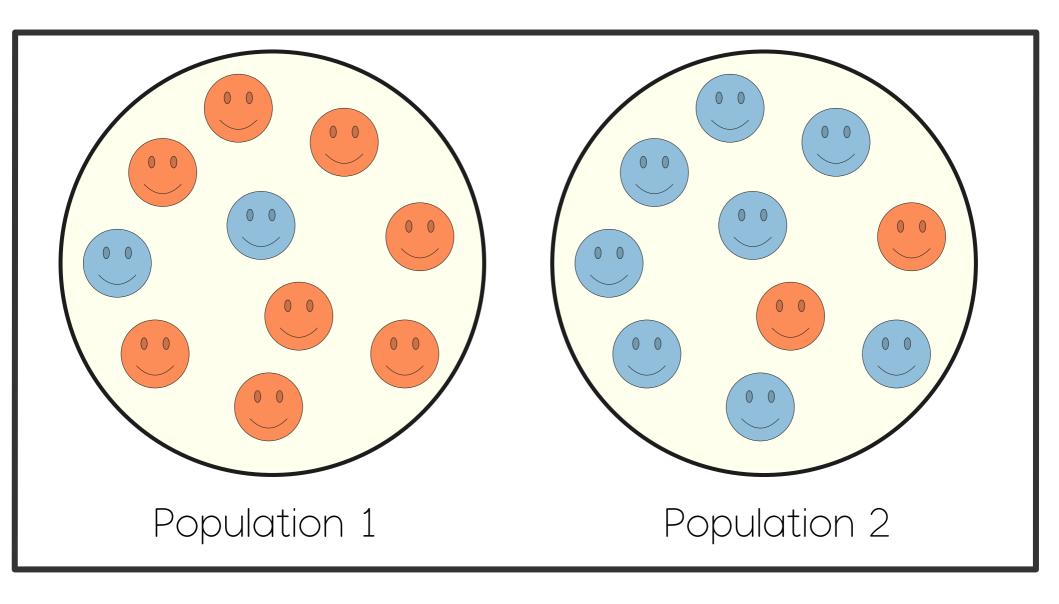


How do we measure differences among populations?
How do we define populations in practice?

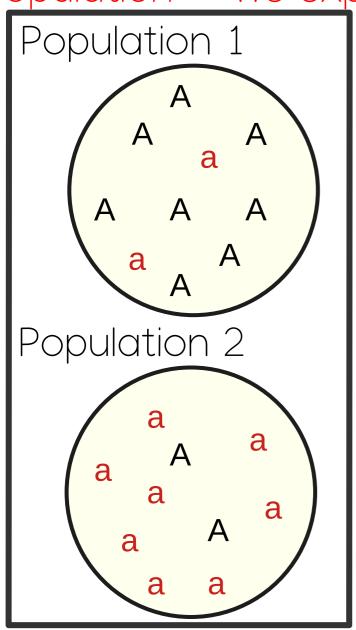
### Population structure



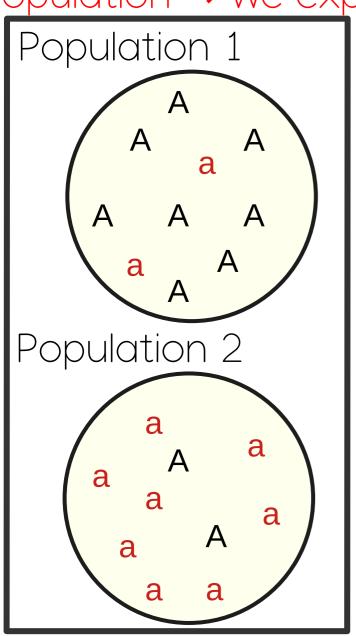
How do we measure differences among populations? How do we define populations in practice?



How differente are genotypic frequencies (assuming HW)?

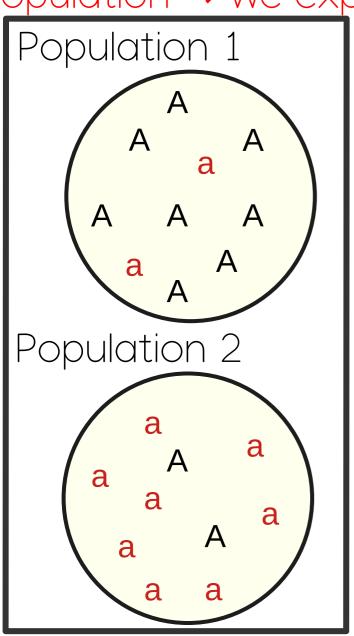


Total population



|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    |       |       |       |
| Pop. 2    |       |       |       |
| Tot. Pop. |       |       |       |

Total population

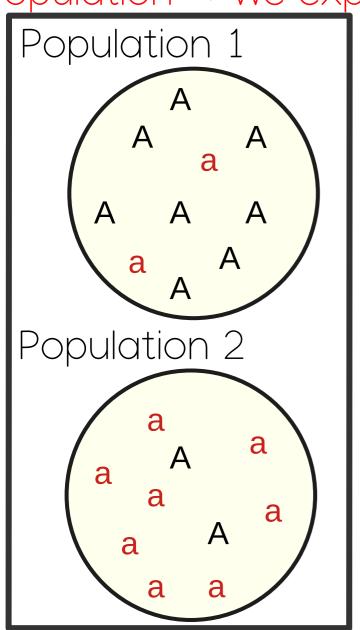


|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

Total population

### The Wahlund effect If pop.1 and pop.2 are part from the same panmictic

population → we expect similar genotypic frequencies



|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

50 % of individuals are expected to be heterozygous.

Total population

If pop.1 and pop.2 are part from the same panmictic population → we expect similar genotypic frequencies

Population 1 Population 2

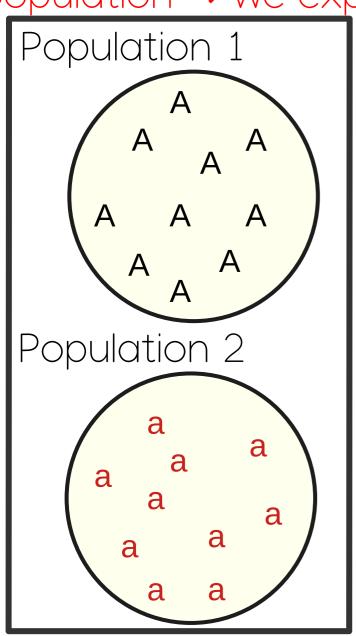
| <del></del> |                       | 1 1    |
|-------------|-----------------------|--------|
| Total       | non1                  | Intion |
| 1000        | $\rho \cup \rho \cup$ | 10011  |

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

50 % of individuals are expected to be heterozygous.

However, we observe 32 %.

 $mean(pop_1; pop_2) = f(Aa)_{Tot} - 0.18$ 

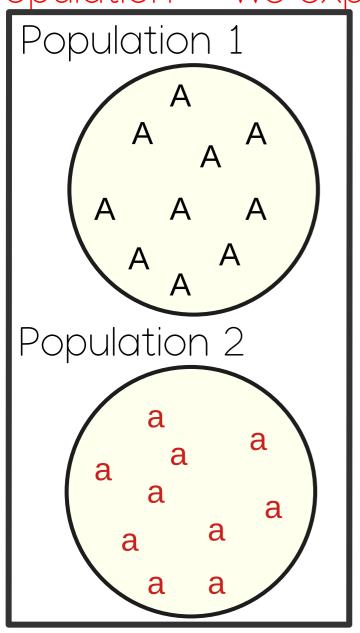


|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    |       |       |       |
| Pop. 2    |       |       |       |
| Tot. Pop. |       |       |       |

Total population

If pop.1 and pop.2 are part from the same panmictic

population → we expect similar genotypic frequencies



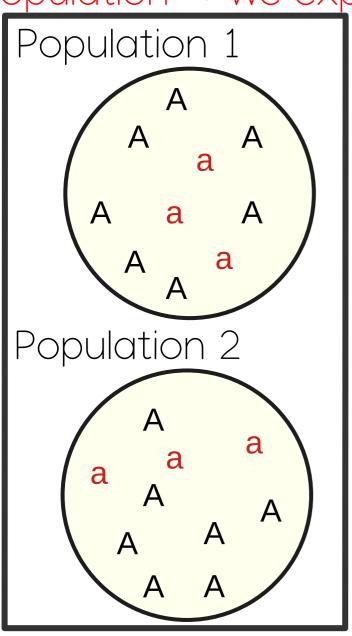
| <br>1 1    | 1          |     |
|------------|------------|-----|
| population | nonulation | 7   |
| POPUIGION  | POPUIGIC   | - 1 |

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 1     | 0     | 0     |
| Pop. 2    | 0     | 0     | 1     |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

50 % of individuals are expected to be heterozygous.

However, we observe 0%.

mean(pop<sub>1</sub>; pop<sub>2</sub>) =  $f(Aa)_{Tot}$  - 0.5

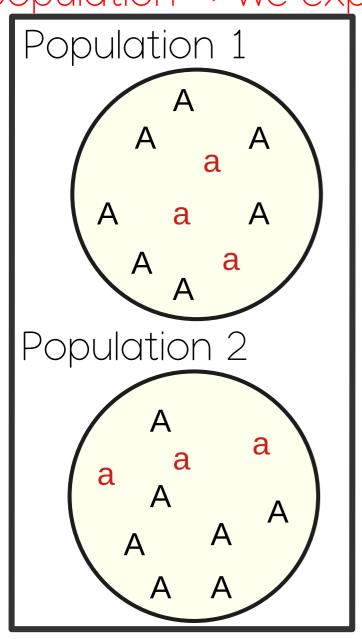


|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    |       |       |       |
| Pop. 2    |       |       |       |
| Tot. Pop. |       |       |       |

Total population

If pop.1 and pop.2 are part from the same panmictic

population → we expect similar genotypic frequencies



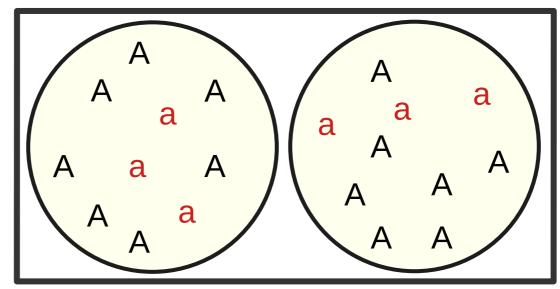
| <del></del> , ,   |                       |        |
|-------------------|-----------------------|--------|
| $1 \cap t \cap I$ | n                     | Intion |
| Total             | $\rho \cup \rho \cup$ | 10011  |

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.49  | 0.42  | 0.09  |
| Pop. 2    | 0.49  | 0.42  | 0.09  |
| Tot. Pop. | 0.49  | 0.42  | 0.09  |

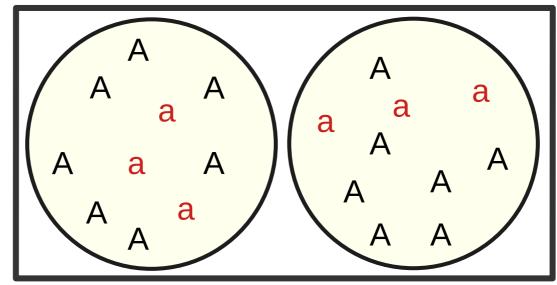
42% of individuals are expected to be heterozygous.

We effectively observe 42%.

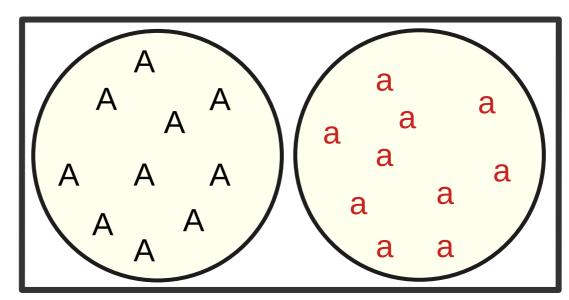
 $mean(pop_1; pop_2) = f(Aa)_{Tot} - 0$ 



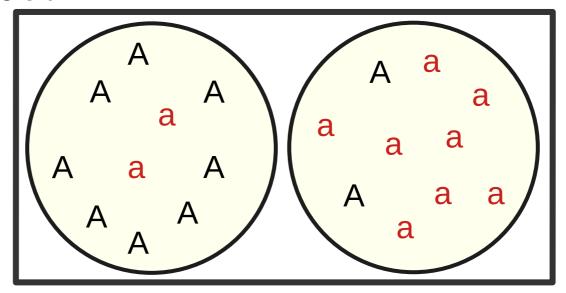
Populations with <u>similar</u> allele frequencies → show very <u>small</u> <u>deviations</u> from HWE.



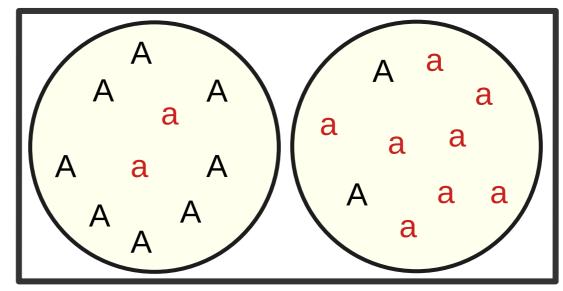
Populations with <u>similar</u> allele frequencies → show very <u>small</u> deviations from HWE.



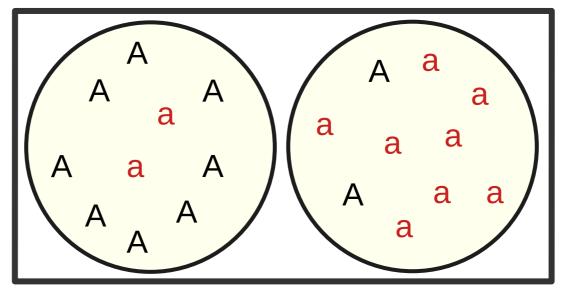
Populations with <u>different</u> allele frequencies → show <u>strong</u> deviations from HWE.



Useful measure of allele frequency differences among populations



Useful measure of allele frequency differences among populations  $\rightarrow$  variance in frequencies  $\sigma^2$ 



Useful measure of allele frequency differences among populations → variance in frequencies σ²

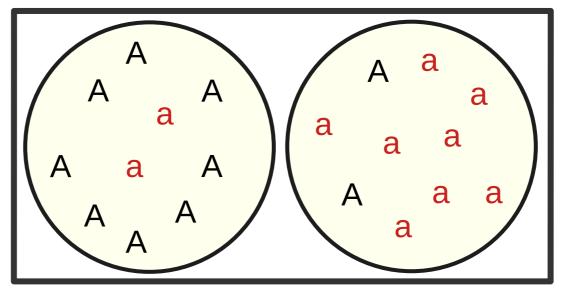
$$\frac{1}{n} \cdot \sum_{i=1}^{n} (p_i - \overline{p})^2$$

#### Where:

n is the number of populations

 $p_i$  is the frequency of allele A (or a) in population *i*.

 $\overline{p}$  is the frequency of allele A (or a) in the whole metapopulation.



Useful measure of allele frequency differences among populations → variance in frequencies σ²

$$\frac{1}{n} \cdot \sum_{i=1}^{n} (p_i - \overline{p})^2$$

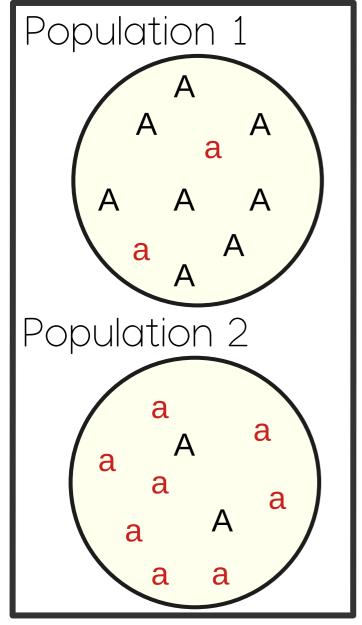
#### Where:

n is the number of populations

 $p_i$  is the frequency of allele A (or a) in population *i*.

 $\overline{p}$  is the frequency of allele A (or a) in the whole metapopulation.

$$\sigma^2 = (1/2) * [(0.8-0.5)^2 + (0.2-0.5)^2] = 0.09$$



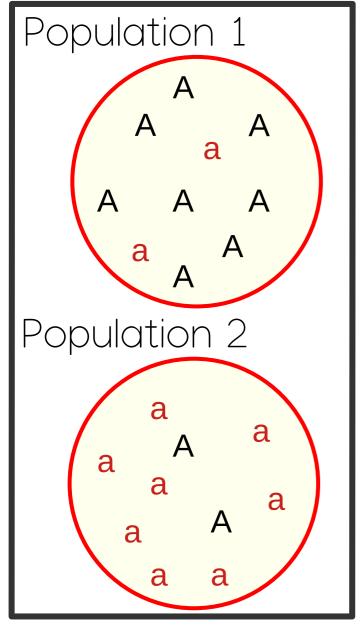
Total population

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

$$E[f(AA)] = \overline{p}^{2} + \sigma^{2}$$

$$E[f(Aa)] = 2\overline{pq} - 2\sigma^{2}$$

$$E[f(aa)] = \overline{q}^{2} + \sigma^{2}$$



Total population

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

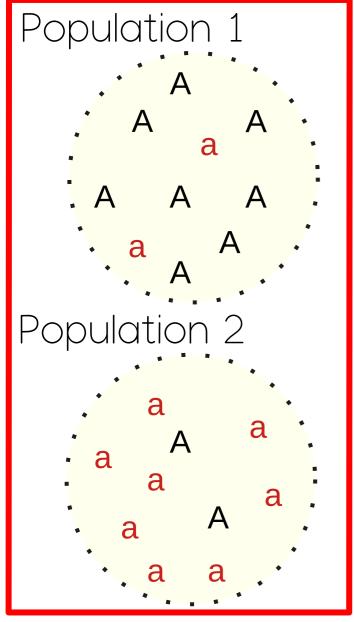
$$E[f(AA)] = \overline{p}^{2} + \sigma^{2}$$

$$E[f(Aa)] = 2\overline{pq} - 2\sigma^{2}$$

$$E[f(aa)] = \overline{q}^{2} + \sigma^{2}$$

Expected genotypic frequencies within populations

#### The Wahlund effect



Total population

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

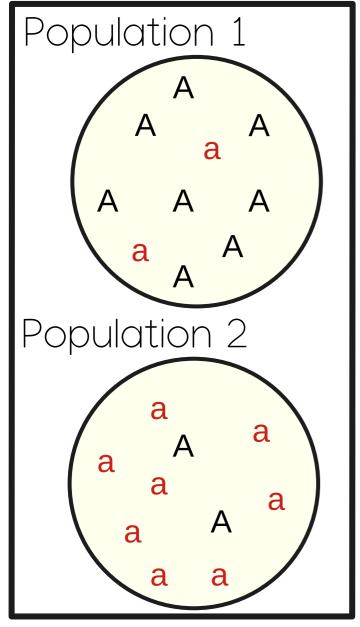
$$E[f(AA)] = \overline{p}^{2} + \sigma^{2}$$

$$E[f(Aa)] = 2\overline{pq} - 2\sigma^{2}$$

$$E[f(aa)] = \overline{q}^{2} + \sigma^{2}$$

Expected genotypic frequencies in total

#### The Wahlund effect



Total population

|           | f(AA) | f(Aa) | f(aa) |
|-----------|-------|-------|-------|
| Pop. 1    | 0.64  | 0.32  | 0.04  |
| Pop. 2    | 0.04  | 0.32  | 0.64  |
| Tot. Pop. | 0.25  | 0.5   | 0.25  |

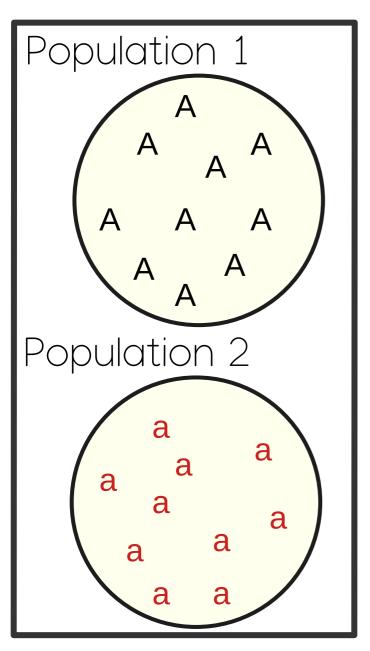
$$E[f(AA)] = \overline{p}^{2} + \sigma^{2}$$

$$E[f(Aa)] = 2\overline{pq} - 2\sigma^{2}$$

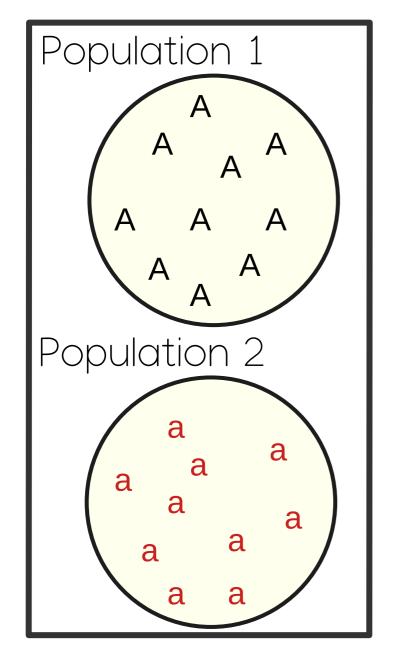
$$E[f(aa)] = \overline{q}^{2} + \sigma^{2}$$

Variance in allele frequencies

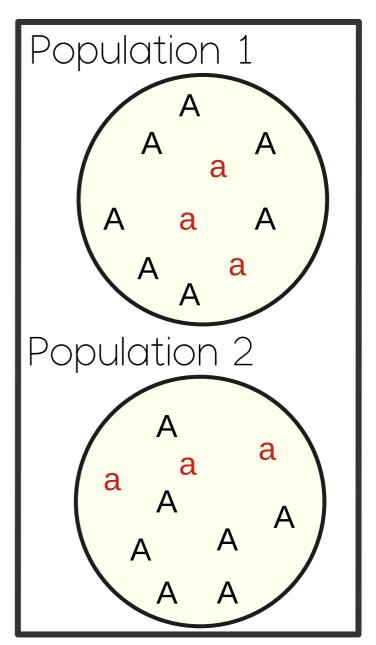
Variance in allelic frequencies ( $\sigma^2$ ) measures the genetic differentiation



Variance in allelic frequencies ( $\sigma^2$ ) measures the genetic differentiation

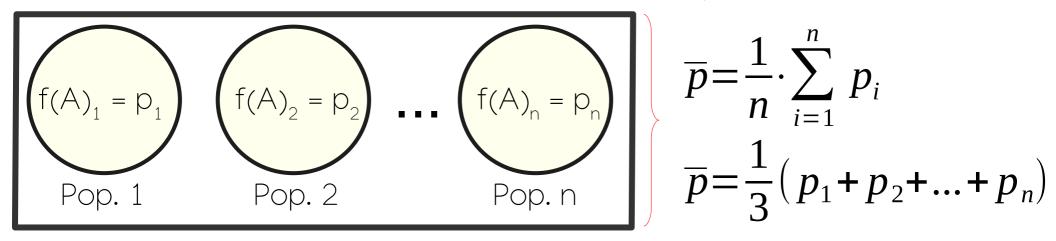




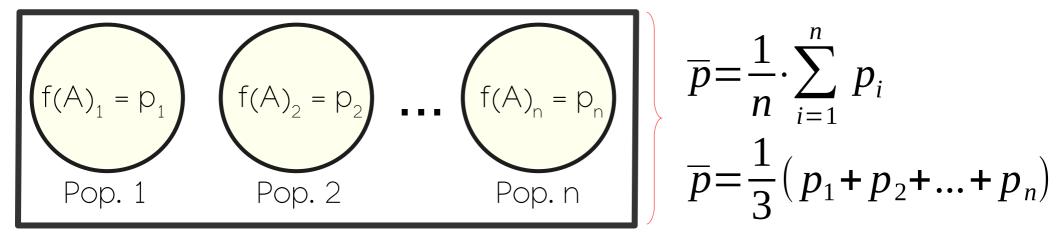


What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

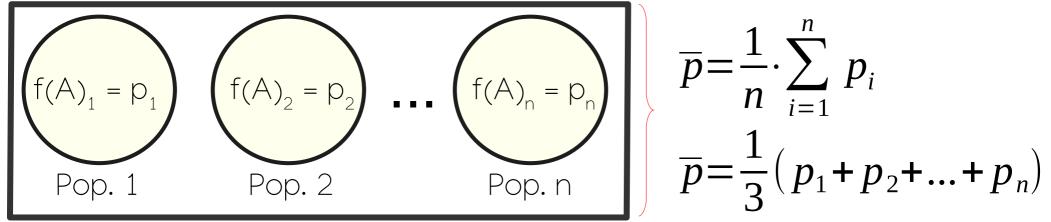


What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

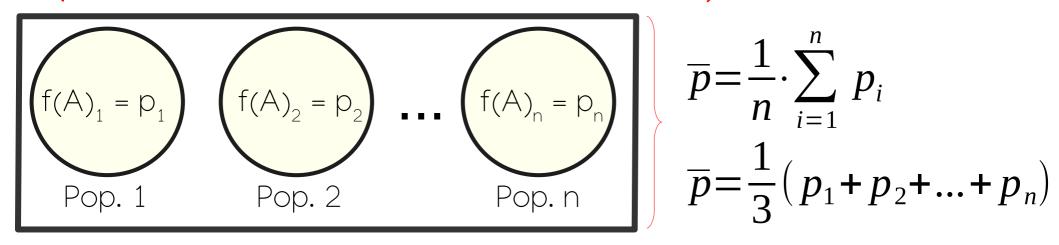


#### Lowest variance

What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )



What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

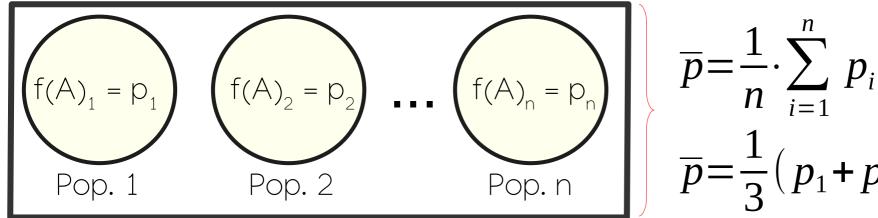


### Lowest variance $\rightarrow$ when $p_i = \overline{p}$

$$\begin{array}{c|c}
\hline
p_1 = \overline{p} \\
\hline
p_2 = \overline{p} \\
\hline
Pop. 1 \\
\hline
Pop. 2
\end{array}$$

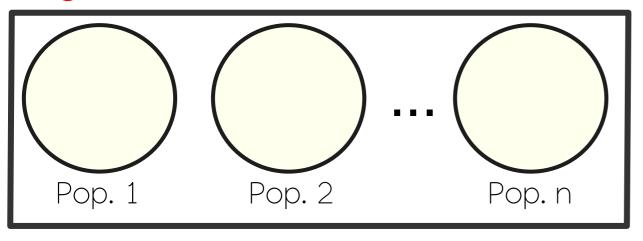
$$\begin{array}{c|c}
\sigma^2 = \frac{1}{n} \cdot \sum_{i=1}^{n} (p_i - \overline{p})^2 \\
\sigma^2 = \frac{1}{n} \cdot \sum_{i=1}^{n} (\overline{p} - \overline{p})^2 = 0
\end{array}$$

What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma$ )



Pop. 1 Pop. 2 Pop. n 
$$\overline{p} = \frac{1}{3}(p_1 + p_2 + ... + p_n)$$

### Highest variance



What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

Highest variance  $\rightarrow$  when p = 0 or 1

$$p_1 = 1$$
  $p_2 = 1$   $p_3 = 0$  Pop. 1 Pop. 2 Pop. n

Proportion  $\overline{p}$  with  $p_i=1$  and proportion  $\overline{q}$  with  $p_i=0$ 

What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

$$\overline{p} = \frac{1}{n} \cdot \sum_{i=1}^{n} p_i$$
Pop. 1 Pop. 2 Pop. n 
$$\overline{p} = \frac{1}{3} (p_1 + p_2 + ... + p_n)$$

Highest variance  $\rightarrow$  when  $p_i = 0$  or 1

Proportion  $\overline{p}$  with  $p_i=1$  and proportion  $\overline{q}$  with  $p_i=0$ 

What are the limits of  $\sigma^2$ ? (the min. and max. values for  $\sigma^2$ )

Highest variance  $\rightarrow$  when  $p_i = 0$  or 1

Proportion  $\overline{p}$  with  $p_i=1$  and proportion  $\overline{q}$  with  $p_i=0$ 

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max)

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max) Depend on allele frequencies

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max)

Depend on allele frequencies

Makes comparisons between loci complicated

Locus 1 :  $\sigma^2 = 0.09$ 

Locus 2 :  $\sigma^2 = 0.12$ 

Differentiation at locus 2 appears higher than locus 1

Values for  $\sigma$  are lying from 0 (min) to  $\overline{pq}$  (max)

Depend on allèle frequencies

Makes comparisons between loci complicated

Locus 1 :  $\sigma^2 = 0.09$ 

If  $\overline{p} = 0.1$  Then  $\sigma^2$  in [0; 0.09]

Locus 2 :  $\sigma^2 = 0.12$ 

Differentiation at locus 2 appears higher than locus 1

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max)

Depend on allele frequencies

Makes comparisons between loci complicated

Locus 1 :  $\sigma^2 = 0.09$ 

If  $\overline{p} = 0.1$ 

Then  $\sigma^2$  in [0; 0.09]

Locus 2 :  $\sigma^2 = 0.12$ 

If  $\overline{p} = 0.5$ 

Then  $\sigma^2$  in [0; 0.25]

Differentiation at locus 2 appears higher than locus 1

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max)

Depend on allele frequencies

Makes comparisons between loci complicated

Locus 1 :  $\sigma^2 = 0.09$ 

If  $\overline{p} = 0.1$ 

Then  $\sigma^2$  in [0; 0.09]

Locus 2 :  $\sigma^2 = 0.12$ 

If  $\overline{p} = 0.5$ 

Then  $\sigma^2$  in [0; 0.25]

Differentiation at locus 2 appears higher than locus 1

We standardize  $\sigma$  by the maximum variance possible

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max)

Depend on allele frequencies

Makes comparisons between loci complicated

Locus 1 :  $\sigma^2 = 0.09$ 

Locus 2 :  $\sigma^2 = 0.12$ 

If  $\overline{p} = 0.1$ 

If  $\overline{p} = 0.5$ 

Then  $\sigma^2$  in [0; 0.09]

Then  $\sigma^2$  in [0; 0.25]

Differentiation at locus 2 appears higher than locus 1

We standardize  $\sigma^2$  by the maximum variance possible

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$

Values for  $\sigma^2$  are lying from 0 (min) to  $\overline{pq}$  (max)

Depend on allele frequencies

Makes comparisons between loci complicated

Locus 1 :  $\sigma^2 = 0.09$ 

If  $\overline{p} = 0.1$ 

Then  $\sigma^2$  in [0; 0.09]

Locus 2 :  $\sigma^2 = 0.12$ 

If  $\overline{p} = 0.5$ 

Then  $\sigma^2$  in [0; 0.25]

Differentiation at locus 2 appears higher than locus 1

We standardize  $\sigma$  by the maximum variance possible

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$

Locus  $1:F_{ST}=1$ 

Locus 2 :  $F_{ST} = 0.48$ 

Locus 1 actually more differentiated than 2

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$

$$\sigma^2 = F_{ST} \cdot \overline{p} \, \overline{q}$$

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$
$$\sigma^2 = F_{ST} \cdot \overline{p}\,\overline{q}$$

$$E[f(Aa)] = 2 \overline{p} \overline{q} - 2 \sigma^2$$

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$
$$\sigma^2 = F_{ST} \cdot \overline{p}\,\overline{q}$$

$$E[f(Aa)] = 2\overline{p}\overline{q} - 2\sigma^2$$

$$E[f(Aa)]=2\overline{p}\overline{q}-2F_{ST}.\overline{p}\overline{q}$$

$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$

$$\sigma^2 = F_{ST} \cdot \overline{p}\,\overline{q}$$

$$E[f(Aa)] = 2\,\overline{p}\,\overline{q} - 2\,\sigma^2$$

$$E[f(Aa)] = 2\,\overline{p}\,\overline{q} - 2\,F_{ST} \cdot \overline{p}\,\overline{q}$$

$$E[f(Aa)] = 2\,\overline{p}\,\overline{q}(1 - F_{ST})$$

$$1 - F_{ST} = \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

$$F_{ST} = \frac{\sigma^2}{\overline{p} \, \overline{q}}$$

$$\sigma^2 = F_{ST} \cdot \overline{p} \, \overline{q}$$

$$E[f(Aa)] = 2 \, \overline{p} \, \overline{q} - 2 \, \sigma^2$$

$$E[f(Aa)] = 2 \, \overline{p} \, \overline{q} - 2 \, F_{ST} \cdot \overline{p} \, \overline{q}$$

$$E[f(Aa)] = 2 \, \overline{p} \, \overline{q} (1 - F_{ST})$$

$$1 - F_{ST} = \frac{E[f(Aa)]}{2 \, \overline{p} \, \overline{q}}$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2 \, \overline{p} \, \overline{q}}$$



$$F_{ST} = \frac{\sigma^2}{\overline{p}\,\overline{q}}$$

$$\sigma^2 = F_{ST} \cdot \overline{p}\,\overline{q}$$

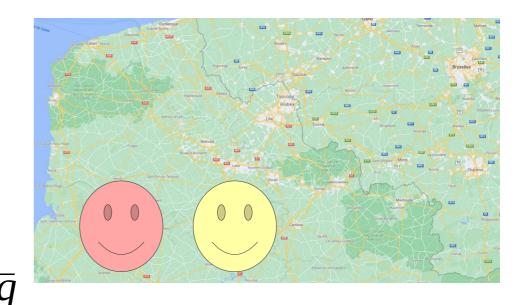
$$E[f(Aa)] = 2\,\overline{p}\,\overline{q} - 2\,\sigma^2$$

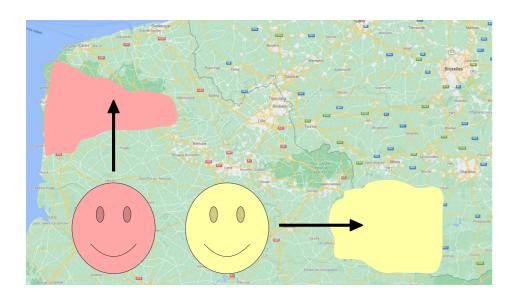
$$E[f(Aa)] = 2\,\overline{p}\,\overline{q} - 2F_{ST} \cdot \overline{p}\,\overline{q}$$

$$E[f(Aa)] = 2\,\overline{p}\,\overline{q}(1 - F_{ST})$$

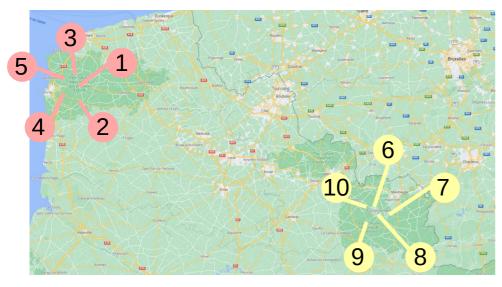
$$1 - F_{ST} = \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$





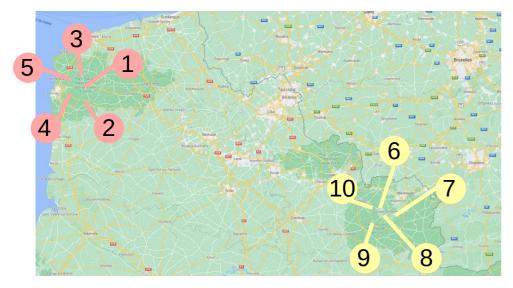
$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$



Sampling

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$



Sampling Sequencing

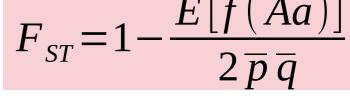
10 sequenced copies of one gene

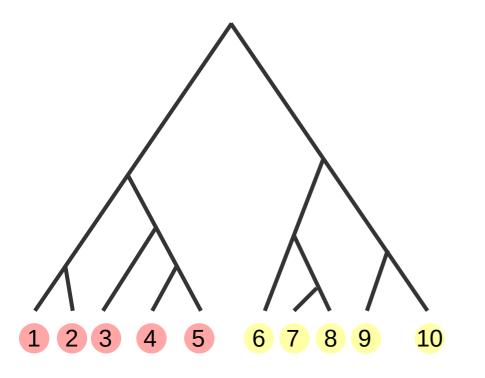
### length = L nucleotides

- 1
- 2
- 3
- 4 —
- 5
- 6
- 7
- 8 \_\_\_\_\_
- 9
- 10 \_\_\_\_\_

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree

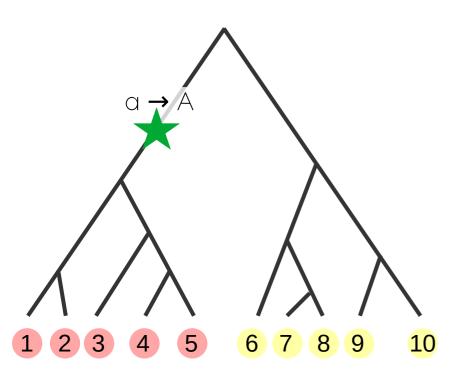




| 1 —  |  |
|------|--|
| 2 —  |  |
| 3 —  |  |
| 4 —  |  |
| 5    |  |
| 6 —  |  |
| 7 —  |  |
| 8 —  |  |
| 9    |  |
| 10 — |  |

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\overline{p}\overline{q}}$$

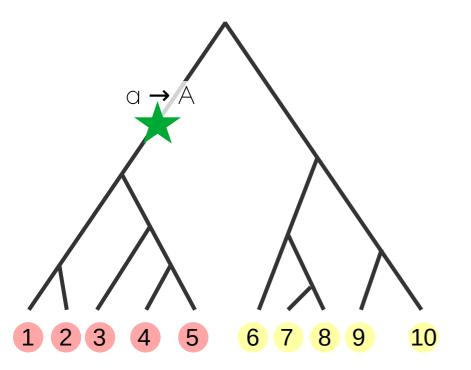
Real (unknown) coalescent tree



| 1  |  |
|----|--|
| 2  |  |
| 3  |  |
| 4  |  |
| 5  |  |
| 6  |  |
| 7  |  |
| 8  |  |
| 9  |  |
| 10 |  |

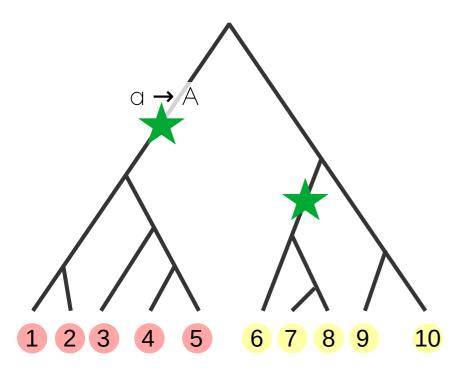
$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



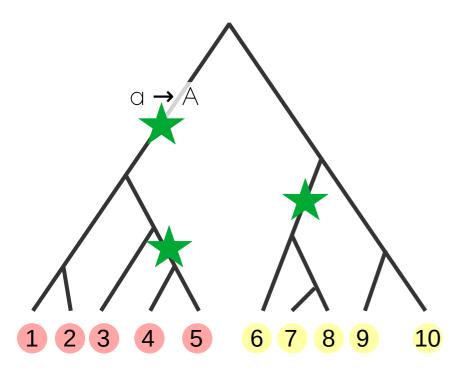
$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



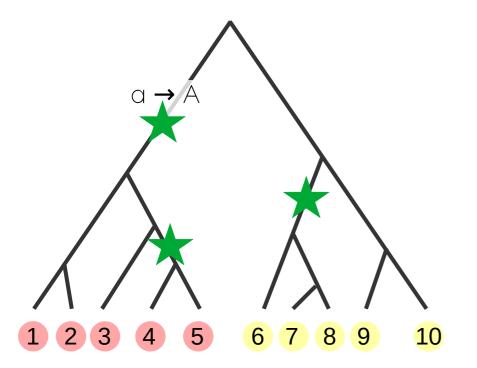
$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

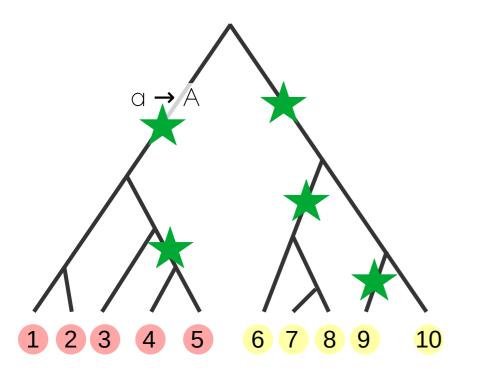
Real (unknown) coalescent tree



#### Sequenced dataset

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\overline{p}\overline{q}}$$

Real (unknown) coalescent tree



#### Sequenced dataset

8 \_ a \_\_\_ A \_\_\_ a \_\_\_ a \_\_\_ A \_\_

9 \_ a \_\_\_ a \_\_\_ A \_\_ A \_\_

**10** — a — a — a — a — A —

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\overline{p}\overline{q}}$$

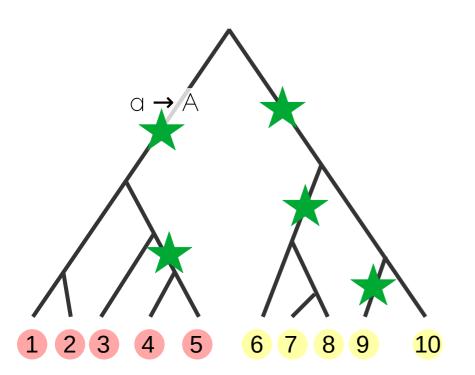
Real (unknown) coalescent tree

# 1 - A - 2 - A - 3 - A - 4 - A - 5 - A - 6 - a - 7 - a - 8 - a - 9 - a

Sequenced dataset

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree

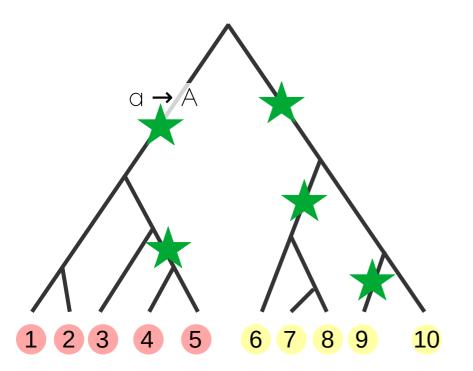


#### Sequenced dataset

$$E[f(Aa)] = \frac{1}{n} \sum_{i}^{n} f(Aa)_{i}$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



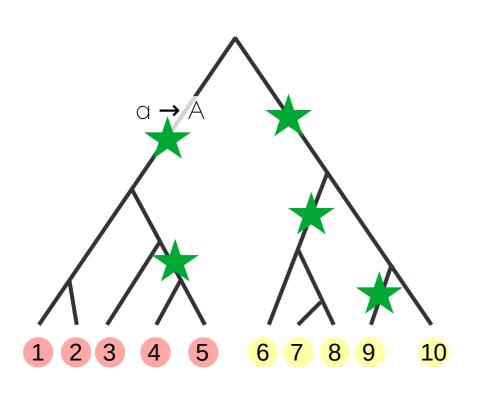
#### Sequenced dataset

$$E[f(Aa)] = \frac{1}{n} \sum_{i=1}^{n} f(Aa)_{i} = \frac{1}{2} (2 p_{1}q_{1} + 2 p_{2}q_{2})$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\overline{p}\overline{q}}$$

Real (unknown) coalescent tree

#### Sequenced dataset

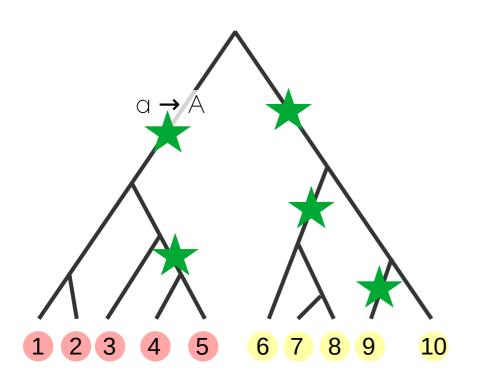


$$E[f(Aa)] = \frac{1}{n} \sum_{i=1}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow ? ? ?$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree

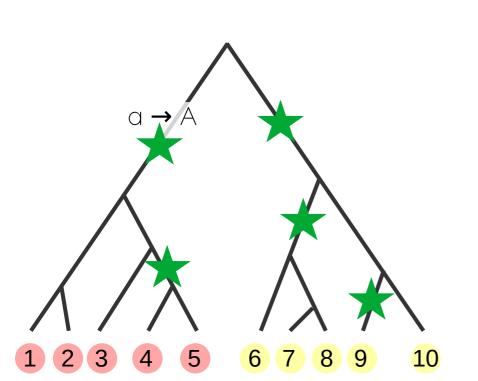
## Sequenced dataset



$$E[f(Aa)] = \frac{1}{n} \sum_{i=1}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow 0 \quad 0.24 \quad 0.24 \quad 0.16 \quad 0$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



Sequenced dataset

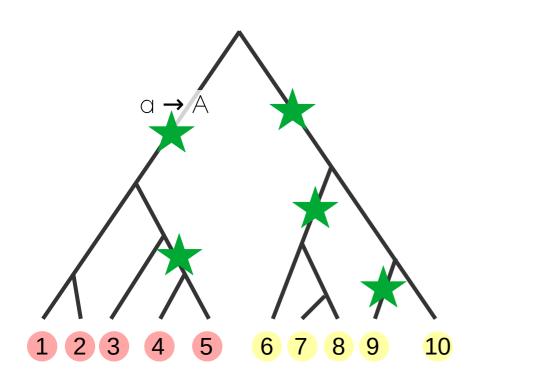
$$E[f(Aa)] = \frac{1}{n} \sum_{i}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow 0 \quad 0.24 \quad 0.24 \quad 0.16 \quad 0$$

$$2\overline{p}\overline{q} \longrightarrow 0$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree

# Sequenced dataset

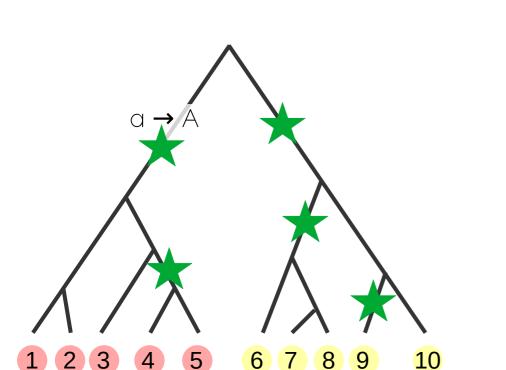


$$E[f(Aa)] = \frac{1}{n} \sum_{i}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow 0 \quad 0.24 \quad 0.24 \quad 0.16 \quad 0$$

$$2\overline{p}\overline{q} \longrightarrow 0.5 \quad 0.42 \quad 0.32 \quad 0.18 \quad 0.5$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\overline{p}\overline{q}}$$

Real (unknown) coalescent tree



#### Sequenced dataset

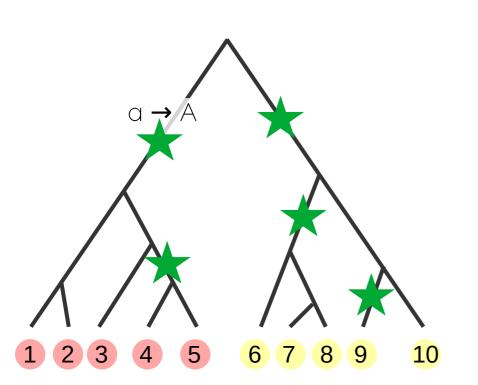
$$E[f(Aa)] = \frac{1}{n} \sum_{i}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow 0 \quad 0.24 \quad 0.24 \quad 0.16 \quad 0$$

$$2\overline{p} \overline{q} \longrightarrow 0.5 \quad 0.42 \quad 0.32 \quad 0.18 \quad 0.5$$

$$F_{ST} \longrightarrow$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



#### Sequenced dataset

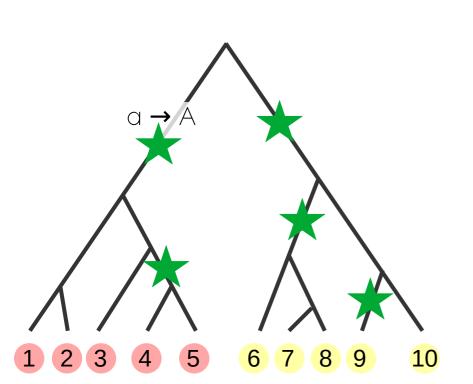
$$E[f(Aa)] = \frac{1}{n} \sum_{i}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow 0 \quad 0.24 \quad 0.24 \quad 0.16 \quad 0$$

$$2\overline{p} \overline{q} \longrightarrow 0.5 \quad 0.42 \quad 0.32 \quad 0.18 \quad 0.5$$

$$F_{ST} \longrightarrow 1 \quad 0.43 \quad 0.25 \quad 0.11 \quad 1$$

$$F_{ST} = 1 - \frac{E[f(Aa)]}{2\,\overline{p}\,\overline{q}}$$

Real (unknown) coalescent tree



#### Sequenced dataset

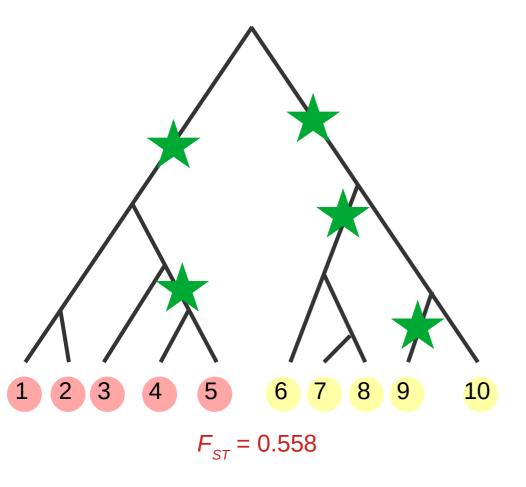
$$E[f(Aa)] = \frac{1}{n} \sum_{i}^{n} f(Aa)_{i} = \frac{1}{2} (2p_{1}q_{1} + 2p_{2}q_{2}) \longrightarrow 0 \quad 0.24 \quad 0.24 \quad 0.16 \quad 0$$

$$2\overline{p} \overline{q} \longrightarrow 0.5 \quad 0.42 \quad 0.32 \quad 0.18 \quad 0.5$$

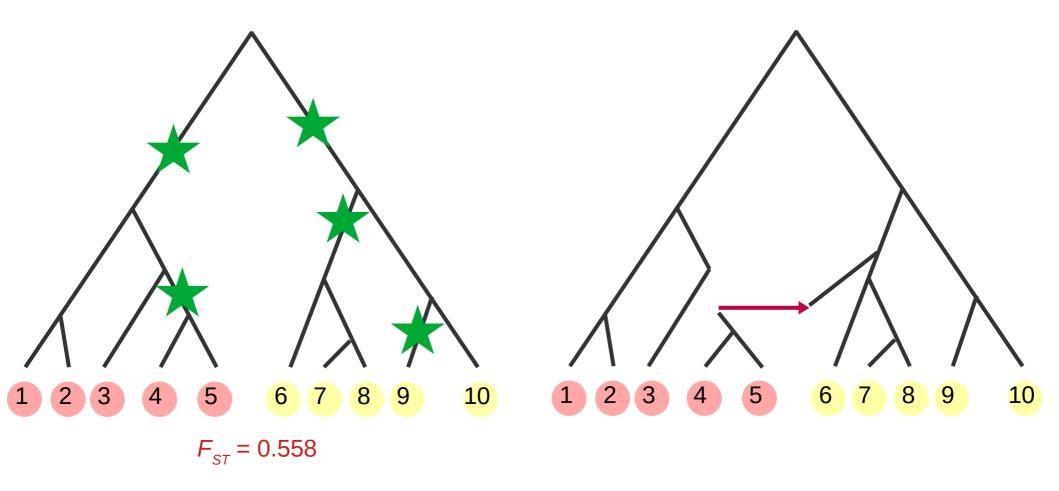
$$F_{ST} \longrightarrow 1 \quad 0.43 \quad 0.25 \quad 0.11 \quad 1$$

$$F_{ST} = 0.558$$

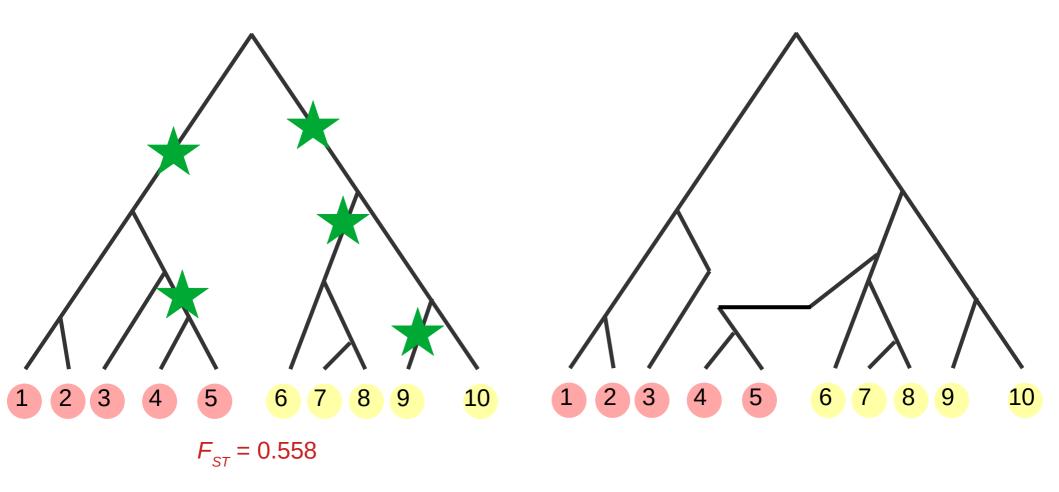
The effect of migration on  $F_{{\scriptscriptstyle ST}}$ 



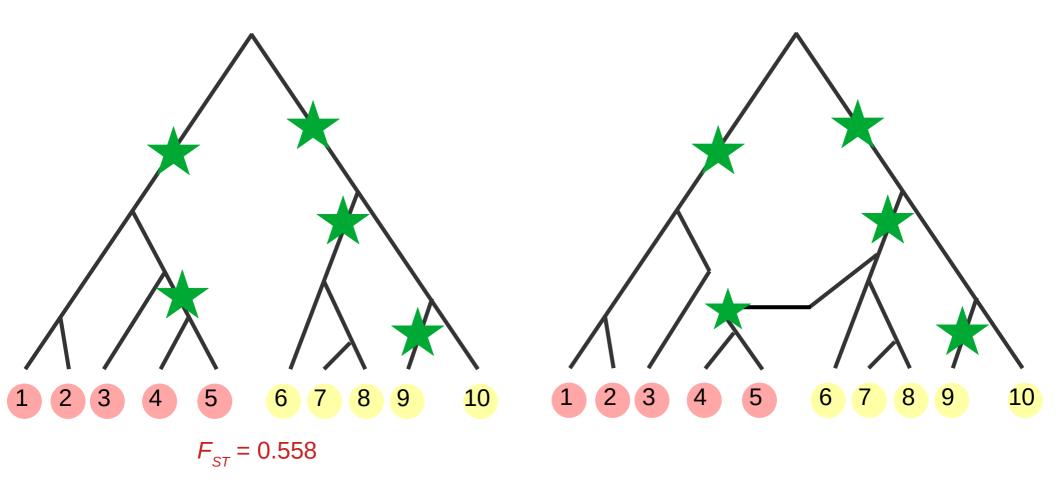
The effect of migration on  $F_{{\scriptscriptstyle ST}}$ 



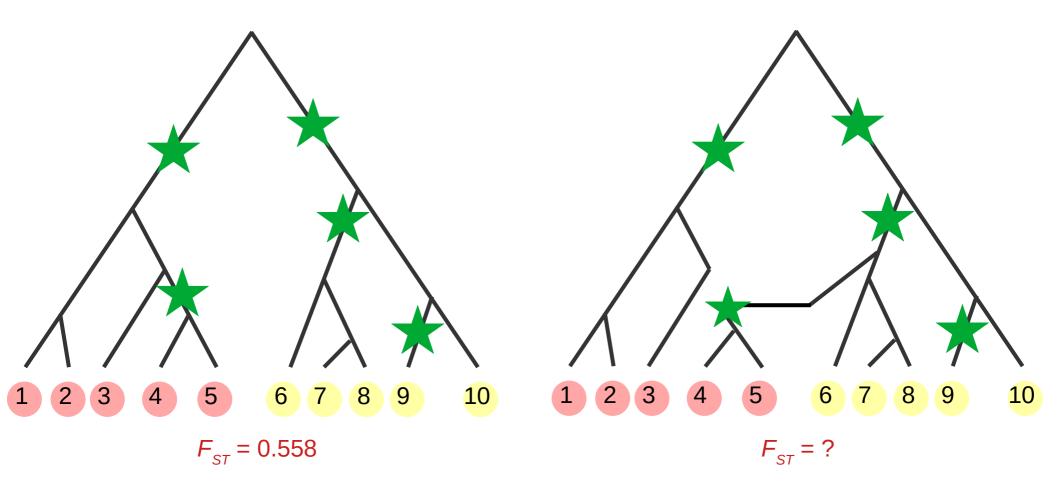
The effect of migration on  $F_{{\scriptscriptstyle ST}}$ 



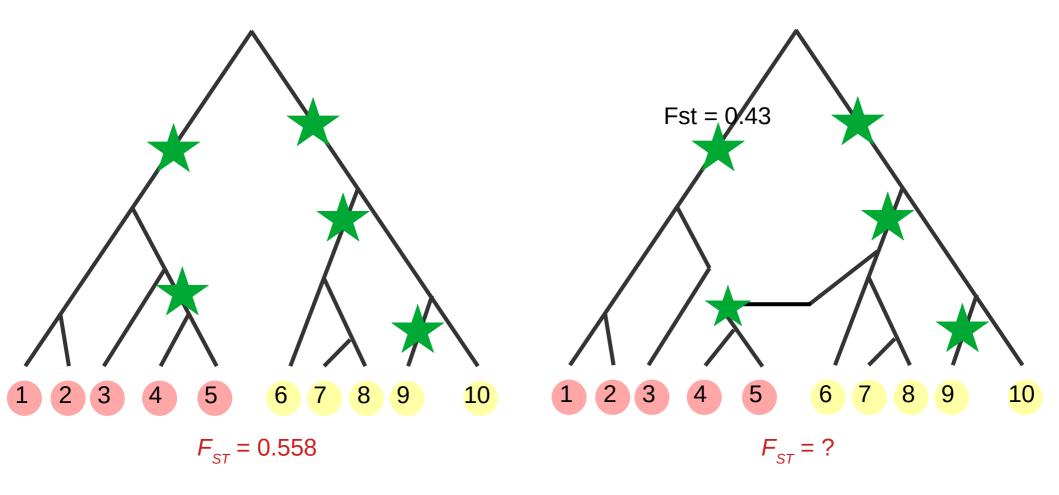
The effect of migration on  $F_{{\scriptscriptstyle ST}}$ 



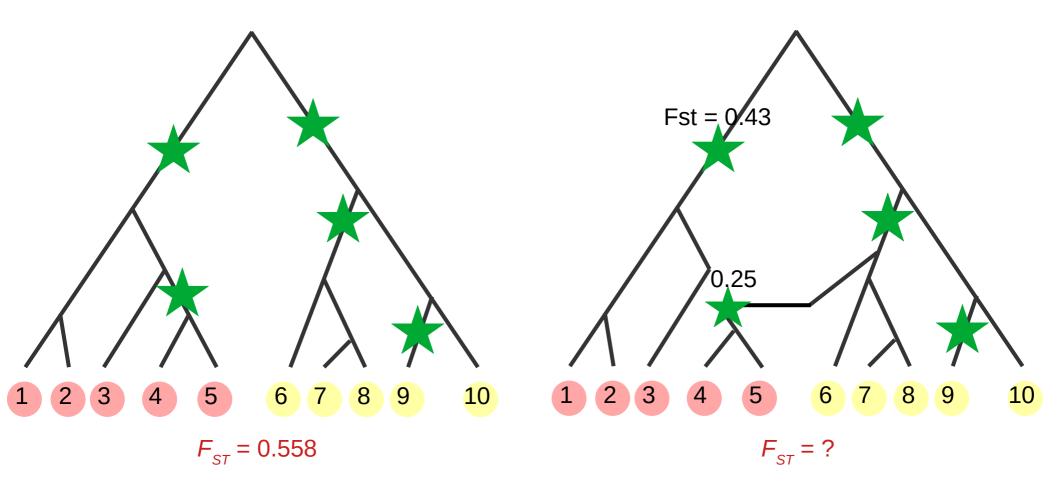
## The effect of migration on $F_{\rm ST}$



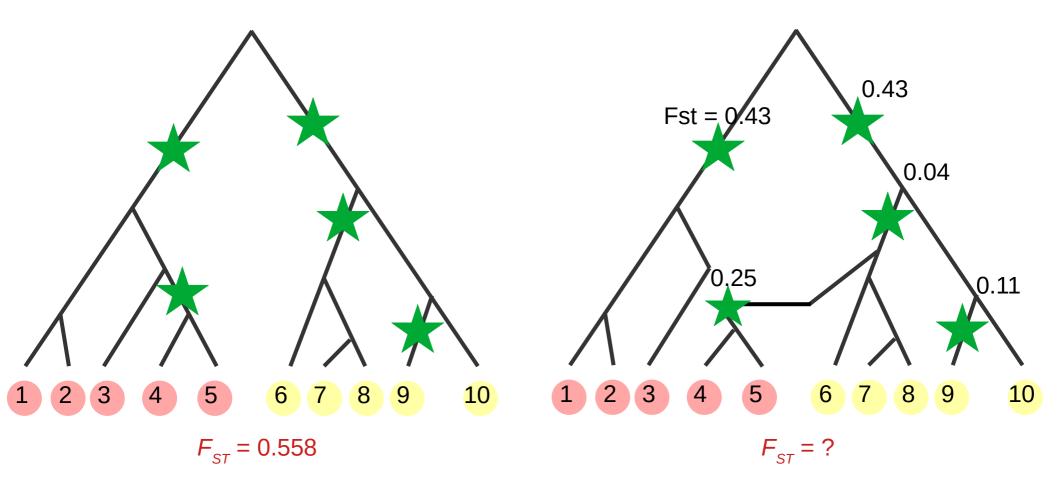
## The effect of migration on $F_{{\scriptscriptstyle ST}}$



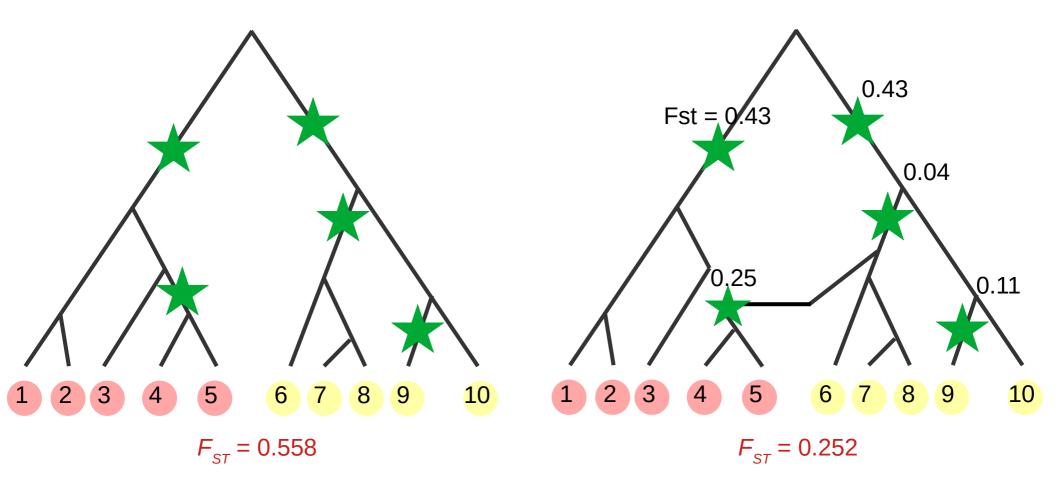
## The effect of migration on $F_{{\scriptscriptstyle ST}}$



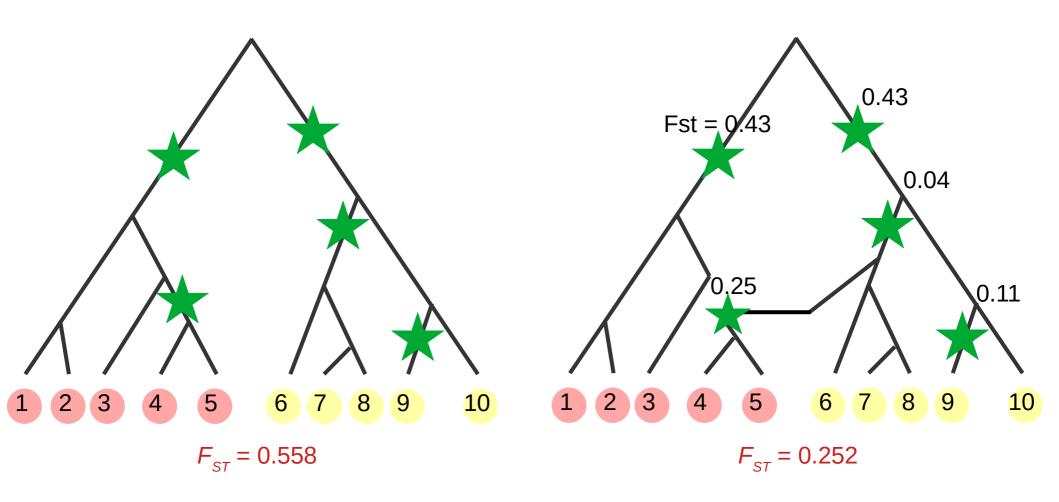
#### The effect of migration on $F_{\rm ST}$



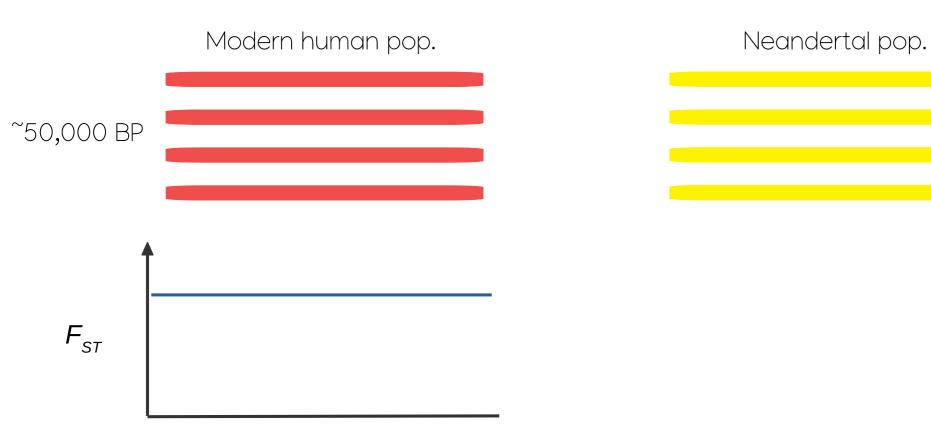
## The effect of migration on $F_{{\scriptscriptstyle ST}}$

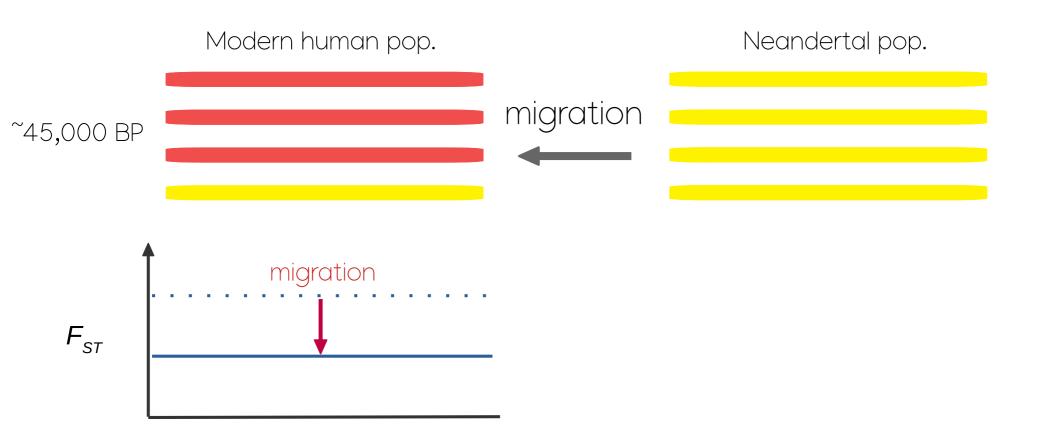


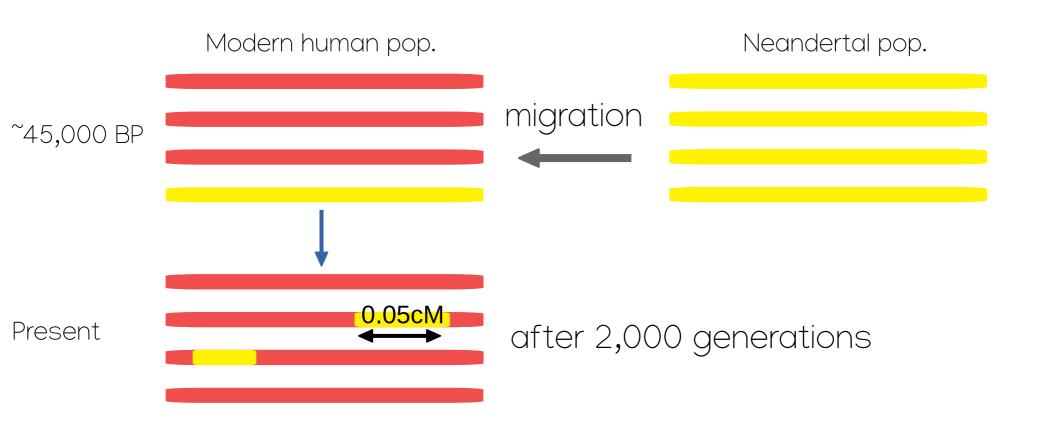
#### The effect of migration on $F_{\rm ST}$

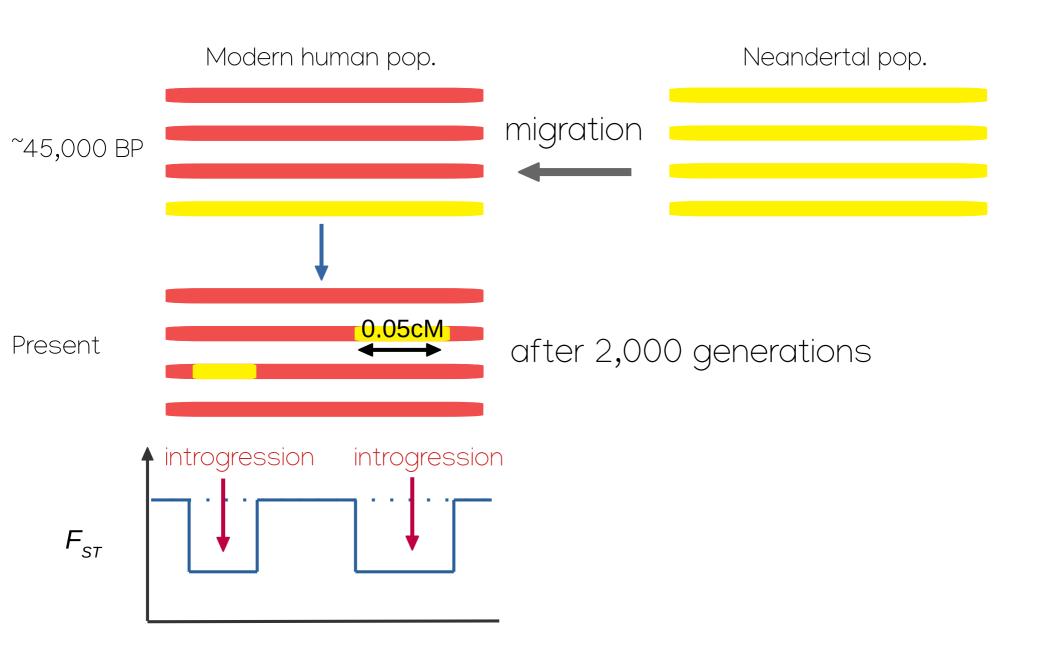


Migration  $\nearrow$   $F_{ST}$ 









#### The Wahlund effect

```
q1=1-p1
q2=1-p2
q3=1-p3
p = (p1+p2+p3)/3
q = (q1+q2+q3)/3
fAa 1 = 2*p1*q1
fAa 2 = 2*p2*q2
fAa 3 = 2*p3*q3
fAa = 2 * p * q
sigma sqr = (1/3) * ((p1-p)**2 + (p2-p)**2 + (p3-p)**2)
res = round(c(fAa 1, fAa 2, fAa 3, fAa, sigma sqr, sigma sqr/(p*q), (fAa 1+fAa 2+fAa 3)/3 + 2*sigma sqr), 2)
names(res) = c('fAa (pop 1)', 'fAa (pop 2)', 'fAa (pop 3)', 'fAa (tot. pop)', 'sigma sqr', 'Fst', 'mean(fAa) + 2 sigma sqr')
tmp = paste("\n\#pop. 1\nAA\tAa\taa\n", p1**2, "\t", 2*p1*q1, "\t", q1**2, "\n", sep="")
cat(tmp)
tmp = paste("\n\#pop. 2\nAA\tAa\taa\n", p2**2, "\t", 2*p2*q2, "\t", q2**2, "\n", sep="")
cat(tmp)
tmp = paste("\n#pop. 3\nAA\tAa\taa\n", p3**2, "\t", 2*p3*q3, "\t", q3**2, "\n", sep="")
cat(tmp)
tmp = paste("\n\#pop. total\nAA\tAa\taa\n", p**2, "\t", 2*p*q, "\t", q**2, "\n", sep="")
cat(tmp)
return(t(t(res)))
```



# Comparative population genomics in animals uncovers the determinants of genetic diversity

J. Romiguier<sup>1,2</sup>, P. Gayral<sup>1,3</sup>, M. Ballenghien<sup>1</sup>, A. Bernard<sup>1</sup>, V. Cahais<sup>1</sup>, A. Chenuil<sup>4</sup>, Y. Chiari<sup>5</sup>, R. Dernat<sup>1</sup>, L. Duret<sup>6</sup>, N. Faivre<sup>1</sup>, E. Loire<sup>1</sup>, J. M. Lourenco<sup>1</sup>, B. Nabholz<sup>1</sup>, C. Roux<sup>1,2</sup>, G. Tsagkogeorga<sup>1,7</sup>, A. A.–T. Weber<sup>4</sup>, L. A. Weinert<sup>1,8</sup>, K. Belkhir<sup>1</sup>, N. Bierne<sup>1</sup>, S. Glémin<sup>1</sup> & N. Galtier<sup>1</sup>



#### RESEARCH ARTICLE

#### Natural Selection Constrains Neutral Diversity across A Wide Range of Species

Russell B. Corbett-Detig1,2, Daniel L. Hartl1, Timothy B. Sackton1\*

- 1 Department of Organismic and Evolutionary Biology, Harvard University, Cambridge Massachusetts, United States of America, 2 Department of Integrative Biology, University of California, Berkeley, Berkeley, California, United States of America
- \* tsackton@oeb.harvard.edu

# Statistical evaluation of alternative models of human evolution

Nelson J. R. Fagundes<sup>†‡§</sup>, Nicolas Ray<sup>§</sup>, Mark Beaumont<sup>¶</sup>, Samuel Neuenschwander<sup>§|</sup>, Francisco M. Salzano<sup>‡††</sup>, Sandro L. Bonatto<sup>†,††</sup>, and Laurent Excoffier<sup>§††</sup>

<sup>†</sup>Laboratório de Biologia Genômica e Molecular, Faculdade de Biociências, Pontifícia Universidade Católica do Rio Grande do Sul (PUCRS), 90619-900 Porto Alegre, RS, Brazil; <sup>‡</sup>Departamento de Genética, Universidade Federal do Rio Grande do Sul, 91501-970 Porto Alegre, RS, Brazil; <sup>§</sup>Computational and Molecular Population Genetics (CMPG), Zoological Institute, University of Bern, CH-3012 Bern, Switzerland; <sup>¶</sup>School of Animal and Microbial Sciences, University of Reading, Reading RG6 6AJ, United Kingdom; and <sup>¶</sup>Department of Ecology and Evolution, University of Lausanne, Biophore, CH-1015 Lausanne, Switzerland

Contributed by Francisco M. Salzano, August 31, 2007 (sent for review August 1, 2007)



#### RESEARCH ARTICLE

# Shedding Light on the Grey Zone of Speciation along a Continuum of Genomic Divergence

Camille Roux<sup>1,2,3</sup>\*, Christelle Fraïsse<sup>1,2,4</sup>, Jonathan Romiguier<sup>1,2,3</sup>, Yoann Anciaux<sup>1,2</sup>, Nicolas Galtier<sup>1,2</sup>, Nicolas Bierne<sup>1,2</sup>

1 Université Montpellier, Montpellier, France, 2 CNRS Institut des Sciences de l'Évolution, CNRS-UM-IRD-EPHE, Montpellier, France, 3 Department of Ecology and Evolution, University of Lausanne, Lausanne, Switzerland, 4 Institute of Science and Technology, Klosterneuburg, Austria

\* camille.roux.1983@gmail.com



#### nature ecology & evolution

Explore content > About the journal > Publish with us > Subscribe

nature > nature ecology & evolution > articles > article

Published: 13 January 2017

# Experimental test and refutation of a classic case of molecular adaptation in *Drosophila melanogaster*

Mohammad A. Siddiq, David W. Loehlin, Kristi L. Montooth & Joseph W. Thornton ⊡

Nature Ecology & Evolution 1, Article number: 0025 (2017) Cite this article

5223 Accesses | 16 Citations | 181 Altmetric | Metrics



#### RESEARCH ARTICLE

# Adaptive Protein Evolution in Animals and the Effective Population Size Hypothesis

#### Nicolas Galtier\*

Institut des Sciences de l'Evolution UMR5554, Université Montpellier-CNRS-IRD-EPHE, Montpellier, France

\* nicolas.galtier@univ-montp2.fr