# Brunswick Point Peep Models

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Roberts Bank, Delta, BC, is situated in the great Pacific Flyway and serves as an important stopover for peeps migrating north in the spring. It therefore hosts a large seasonal population of peeps: namely, Western sandpiper (WESA) and Dunlin (DUNL), that rely on the seasonal nutritional bounty provided by the Fraser River delta.

This document describes the suite of models used to estimate yearly changes in spatial distribution and abundance of peeps in the Roberts Bank estuary.

There are two datasets used in this modelling pipeline:

- 1. sr, which contains species ratio data (WESA:DUNL)
- 2. dat, which contains bird counts + environmental covariates

For an interactive interface with the dat dataset used in this document, see https://popovs.shinyapps.io/peepr/.

### Species composition model

The daily ratio of Western sandpiper (WESA) to Dunlin (DUNL) across the entire study period is first modelled using a dataset of known species ratios (species ratios are not measured during every survey).

The ratios are modelled using a binomial generalized linear mixed model (binomial GLMM). The resulting predicted ratios are then used to estimate the number of WESA vs. DUNL per day.

### sr data summary

```
survey_date
##
                                wesa
                                                  dunl
                                                                   total
##
    Min.
           :1997-04-21
                          Min.
                                      0.0
                                             Min.
                                                        0.0
                                                               Min.
                                                                       : 48.0
##
    1st Qu.:2005-04-20
                          1st Qu.: 126.8
                                             1st Qu.:
                                                       42.0
                                                               1st Qu.: 287.2
##
    Median :2009-04-23
                          Median: 355.0
                                             Median :
                                                       93.0
                                                               Median: 524.5
##
    Mean
            :2009-09-05
                          Mean
                                  : 470.1
                                             Mean
                                                    : 176.7
                                                               Mean
                                                                       : 646.8
##
    3rd Qu.:2015-04-16
                          3rd Qu.: 719.0
                                             3rd Qu.: 203.5
                                                               3rd Qu.: 943.8
##
    Max.
            :2022-05-04
                          Max.
                                  :2605.0
                                             Max.
                                                    :5000.0
                                                               Max.
                                                                       :5047.0
##
##
        p_wesa
                          p_dunl
                                              year
                                                          julian_day
##
    Min.
           : 0.00
                      Min.
                              :
                                 0.00
                                        2006
                                                : 23
                                                       Min.
                                                               :101.0
    1st Qu.: 53.04
                      1st Qu.:
                                 8.83
                                                       1st Qu.:112.0
##
                                        2019
                                                  23
    Median: 81.32
                      Median: 18.68
                                        2005
                                                       Median :117.0
##
                                                : 18
                                                               :117.6
##
    Mean
           : 68.94
                      Mean
                              : 31.06
                                        2007
                                                : 18
                                                       Mean
##
    3rd Qu.: 91.17
                      3rd Qu.: 46.96
                                        2008
                                                : 18
                                                       3rd Qu.:123.0
##
    Max.
            :100.00
                      Max.
                              :100.00
                                        2012
                                                : 18
                                                       Max.
                                                               :137.0
##
                                         (Other):200
##
           dos.V1
           :-2.2763470
##
    Min.
##
    1st Qu.:-0.7798519
##
    Median :-0.0996268
##
    Mean
            :-0.0221924
    3rd Qu.: 0.7166433
##
##
    Max.
           : 2.6212735
##
```

### Five models are built and compared

Response variable:

• y - WESA:DUNL ratio

Predictor variables:

- dos day of season (recentered/scaled Julian date)
- year year of survey

```
## Data: sr
## Models:
## lme5: y ~ 1 + (1 | year)
## lme4: y ~ dos + (1 | year)
## lme2: y ~ dos + I(dos^2) + (1 | year)
```

```
## lme3: y ~ dos + (dos | year)
## lme1: y ~ dos + I(dos^2) + (dos + I(dos^2) | year)
                                          Chisq Df Pr(>Chisq)
              AIC
                    BIC logLik deviance
          2 64756 64764 -32376
## lme5
                                  64752
## lme4
          3 25804 25815 -12899
                                   25798 38954.1 1
                                                        <2e-16 ***
## 1me2
          4 16295 16310 -8144
                                  16287 9510.6 1
                                                        <2e-16 ***
## 1me3
          5 22521 22540 -11255
                                   22511
                                            0.0 1
                                                             1
          9 11083 11117 -5532
                                  11065 11446.2 4
                                                        <2e-16 ***
## lme1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The best-fit model is lme1. The residuals from lme1 are appended to the sr dataset and another model is re-fit in order to estimate overdispersion. Because the standard deviation of the residuals is < 1, the model is deemed an appropriate candidate for predicting daily species ratios.

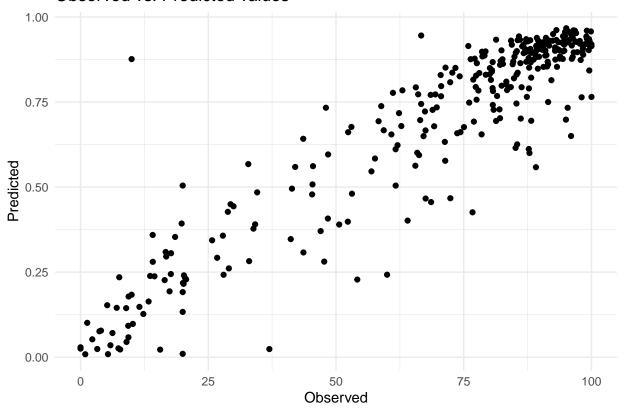
```
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
  Family: binomial (logit)
## Formula: y \sim dos + I(dos^2) + (dos + I(dos^2) | year) + (1 | resids)
##
      Data: sr
##
         AIC
                   BIC
                          logLik deviance
                                            df.resid
   3409.879 3447.499 -1694.939
                                 3389.879
                                                  308
## Random effects:
   Groups Name
                       Std.Dev. Corr
   resids (Intercept) 0.94716
##
##
   year
           (Intercept) 0.65139
##
           dos
                       0.06454
                               -1.00
                       0.41479 -0.65 0.68
##
           I(dos^2)
                                resids, 318; year, 24
## Number of obs: 318, groups:
## Fixed Effects:
## (Intercept)
                        dos
                                I(dos^2)
##
        1.8826
                     1.3770
                                 -0.8085
```

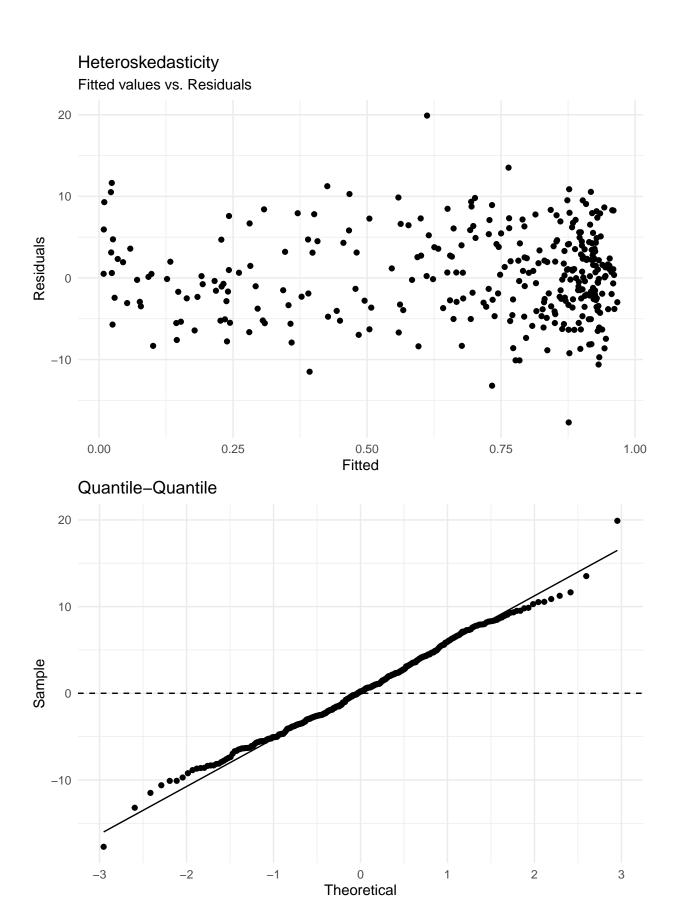
#### Summary of best fit model (lme1)

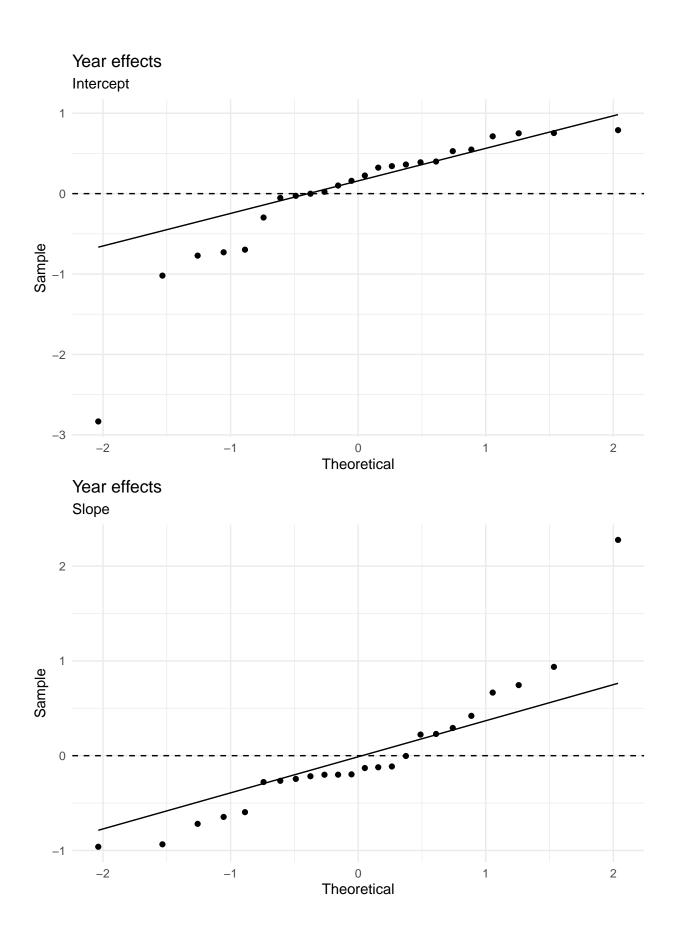
```
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
  Family: binomial (logit)
## Formula: y \sim dos + I(dos^2) + (dos + I(dos^2) | year)
##
     Data: sr
##
##
        AIC
                BIC
                      logLik deviance df.resid
##
  11082.7 11116.6 -5532.4 11064.7
##
## Scaled residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -23.5674 -3.5412
                      0.2172
                               3.6901 21.7396
##
## Random effects:
                      Variance Std.Dev. Corr
##
   Groups Name
   year
          (Intercept) 0.6045
                              0.7775
                      0.4629
                               0.6803
##
          dos
                                         0.18
##
          I(dos^2)
                      0.6650
                              0.8155
                                        -0.71 -0.53
## Number of obs: 318, groups: year, 24
## Fixed effects:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 1.7477
                           0.1593 10.974 < 2e-16 ***
                                   9.558 < 2e-16 ***
## dos
                1.3365
                           0.1398
## I(dos^2)
                           0.1676 -4.874 1.09e-06 ***
                -0.8168
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
##
            (Intr) dos
## dos
            0.177
## I(dos^2) -0.705 -0.522
```

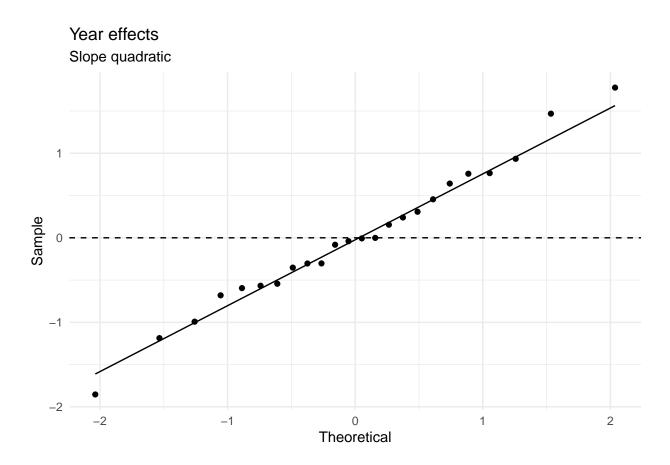
# Check assumptions of best fit model





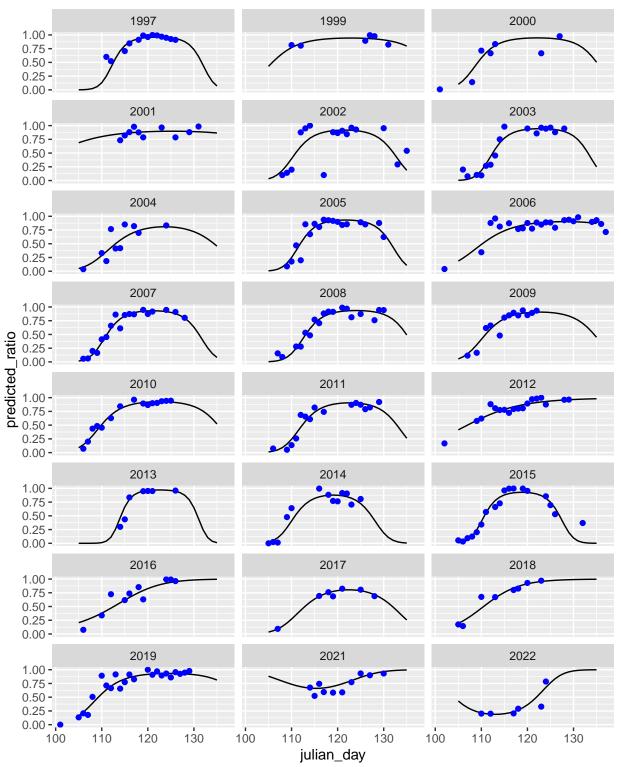






## Predict WESA/DUNL population

Using the derived binomial GLMM above, we will predict the amount of WESA and DUNL each day. For any years that are missing from the bGLMM we will assign the mean proportion of WESA:DUNL.



### North-South distribution model

The primary goal of this analysis is to determine whether melt flow regimes alter the north-south distribution of peeps. Birds are surveyed from a route of standardized survey stations. Any birds counted in or north of the "view corner" are labelled as  $\mathbb{N}$ , while any birds counted south of the "view corner" are labelled as  $\mathbb{S}$  for this analysis.<sup>1</sup>

The dat dataset, which contains survey data and associated environmental covariates, will be used in this model. The dat dataset can be explored in greater detail in the PeepR Shiny app.

<sup>&</sup>lt;sup>1</sup>For now, this includes birds counted in Canoe Pass, but those will be excluded in a later analysis to compare results.

#### dat filtering

The dat dataset underwent some filtering steps to exclude unwanted data prior to this analysis. First, only data that was originally included in Canham et al. (2021) is extracted from the bppeeps database. While survey data oftentimes includes multiple sweeps, low-quality or reconnaissance sweeps were excluded from the daily totals used in Canham et al. (2021). As such, they were excluded from this dataset as well.

The total bird count for several surveys were obtained by taking the average total count from multiple sweeps. In these cases, it is difficult to obtain accurate location-level numbers because birds often moved locations between sweeps. These records are excluded for now (45 survey dates out of a total of 538).

Additionally, certain survey dates only included a total bird count for the day, but no location-level information. These records were excluded from the initial database query (24 survey dates out of a total of 538).

After excluding these surveys, the initial dataset queried from the bppeeps dataset included 2207 records from a total of 469. This is termed the 'full dataset' and was filtered further in R.

Filtering step	No. survey dates	No. reco	No. survey ordkates lost	No. records lost
Full dataset	469	2207	NA	NA
Remove NA count records	469	2198	0	-9
Exclude dates where total $\#$ of birds $< 1000$	443	2085	-26	-113
Exclude dates outside of survey period (<04-15 or >05-15)	430	2023	-13	-62
Exclude Intercauseway and NA stations (e.g. location was	429	1892	-1	-131
simply 'inner mud', 'mumblies', 'flying', etc.) Exclude records where only bird count occurs in location that spans >2 stations (e.g., 'BP to CP')	425	1882	-4	-10

### dat data summary after filtering

```
survey_date
                         start_time
                                            station
   Min. :1997-04-21
##
                        Length: 1882
                                          Length: 1882
   1st Qu.:2004-04-19
                        Class :character
                                          Class : character
   Median: 2008-05-07
                        Mode :character
                                          Mode :character
   Mean :2009-03-12
##
   3rd Qu.:2014-04-18
##
   Max. :2022-05-04
##
##
             station_n
                                  station_s
                                               mumblies_yn
                                                                mud_yn
##
   Coal Port
                :536
                                      :
                                          70
                                               Mode :logical
                                                               Mode :logical
                         Bend
   Pilings
##
                  :465
                         Coal Port
                                          55
                                               FALSE: 1700
                                                               FALSE: 1697
   Brunswick Point:311
                         View corner
                                          45
                                               TRUE : 182
                                                               TRUE: 185
   34th St pullout:204
##
                         34th St pullout:
                                          17
   View corner
                  :174
                         Pilings
                                       : 15
##
   Bend
                  :118
                         (Other)
                                           1
##
   (Other)
                  : 74 NA's
                                       :1679
    marsh_yn
##
                   tide_edge_yn
                                  flying_yn
                                                   final_count
  Mode :logical
                 Mode :logical
                                  Mode :logical
                                                  Min. :
##
  FALSE: 1815
                   FALSE: 1807
                                  FALSE: 1866
                                                  1st Qu.:
                                                             500
   TRUE :67
                   TRUE :75
                                  TRUE :16
                                                  Median: 4125
                                                  Mean : 12745
##
##
                                                  3rd Qu.: 14500
##
                                                  Max. :222500
##
##
                       elev_min
                                       elev_max
                                                     elev_median
       p_wesa
##
   Min. : 0.00
                    Min. :-0.040
                                    Min. :3.960
                                                    Min. :2.240
                    1st Qu.: 0.830
   1st Qu.: 52.32
                                    1st Qu.:4.300
                                                    1st Qu.:3.071
   Median: 80.66
                    Median : 1.210
                                   Median :4.430
                                                    Median :3.255
   Mean : 68.69
##
                    Mean : 1.223
                                    Mean :4.418
                                                    Mean :3.239
##
   3rd Qu.: 90.97
                    3rd Qu.: 1.620
                                    3rd Qu.:4.560
                                                    3rd Qu.:3.415
   Max. :100.00
                    Max. : 2.420
                                    Max. :4.850
                                                    Max. :3.735
##
   NA's
          :589
     {\tt elev\_mean}
                                                  total_precip
##
                     elev range
                                       flow
                                                                  mean temp
##
  Min. :2.660
                   Min. :1.870
                                  Min. : 996
                                                 Min. : 0.00
                                                                Min. : 3.80
   1st Qu.:2.967
                   1st Qu.:2.712
                                  1st Qu.:2430
                                                 1st Qu.: 0.00
                                                                 1st Qu.: 9.20
   Median :3.037
                   Median :3.210
                                  Median :3090
                                                 Median: 0.00
                                                                 Median :10.50
##
                                                 Mean : 2.09
   Mean :3.041
                   Mean :3.195
                                  Mean :3227
                                                                 Mean :10.64
##
   3rd Qu.:3.118
                   3rd Qu.:3.607
                                   3rd Qu.:3990
                                                 3rd Qu.: 2.00
                                                                 3rd Qu.:11.90
   Max. :3.422
                   Max. :4.640
                                  Max.
                                         :7830
                                                 Max.
                                                        :28.20
                                                                 Max. :17.50
##
                                  NA's
                                         :5
                                                 NA's
                                                        :4
                                           windspd
##
                                                            wind_deg
                            7.7
         11
         :-19.8067
                      Min. :-42.3467
                                        Min. : 5.292
                                                         Min. :-177.35
   1st Qu.: -3.8058
                      1st Qu.: -9.9586
                                        1st Qu.:10.542
                                                         1st Qu.: -77.07
##
                      Median : -0.4341
   Median : -1.0261
                                        Median :12.958
                                                         Median : -22.79
##
                                                         Mean : 15.03
##
   Mean : -0.7134
                      Mean : -1.8065
                                        Mean :14.309
   3rd Qu.: 2.5179
                      3rd Qu.: 8.0889
                                        3rd Qu.:16.906
                                                         3rd Qu.: 117.95
##
   Max. : 15.0489
                     Max. : 20.4541
                                        Max. :43.750
                                                       Max. : 179.93
##
##
   station_n_no
                    station_s_no
                                    station_diff
                                                      year
                                                                  julian_day
  Min. :1.000
                   Min. :3.000
                                  Min. :0.00
                                                 2008
                                                        : 124
                                                               Min. :105
                   1st Qu.:5.000
                                  1st Qu.:1.00
                                                 2019
                                                                1st Qu.:112
## 1st Qu.:4.000
                                                        : 121
## Median :5.000
                 Median:6.000
                                  Median :1.00
                                                 2012
                                                       : 120
                                                               Median:118
```

```
## Mean :5.554 Mean :6.094
                              Mean :1.01
                                           2005 : 116 Mean :118
## 3rd Qu.:8.000 3rd Qu.:8.000
                              3rd Qu.:1.00
                                           2001 : 109 3rd Qu.:124
## Max. :8.000 Max. :8.000
                              Max. :2.00
                                           2006 : 95
                                                        Max. :135
##
                 NA's :1679
                              NA's :1679
                                           (Other):1197
##
         dos.V1
                    n_s
## Min. :-1.8238057
                   N: 559
## 1st Qu.:-0.8404703
                    S:1323
## Median : 0.0023885
## Mean : 0.000000
## 3rd Qu.: 0.8452474
## Max. : 2.3904887
##
```

#### Build and test model

In this initial analysis, the model will be kept relatively simple: use the same model as in Canham et al. (2021), but add a "north vs. south" term. The response variable will be the total count for that location/day \* the predicted WESA ratio generated by the bGLMM above.

#### Base model

Response variable:

• log wesa - Log-transformed predicted WESA count

Predictor variables:

```
• year c - Scale-transformed survey year
```

• dos - Scale-transformed Julian date, aka Day of Season

```
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: log_wesa ~ year_c + dos + I(dos^2) + (dos + I(dos^2) | year)
##
      Data: dat
##
## REML criterion at convergence: 9666.4
##
## Scaled residuals:
                1Q Median
##
       Min
                                3Q
                                       Max
  -2.9584 -0.3512 0.2321 0.6717
##
## Random effects:
                         Variance Std.Dev. Corr
   Groups
             Name
##
                                  0.6815
##
   year
             (Intercept) 0.4644
                                  0.6859
                         0.4704
                                            0.05
##
             dos
                                  0.4033
##
             I(dos^2)
                         0.1626
                                           -0.51 0.03
                         9.5098
                                  3.0838
##
   Residual
## Number of obs: 1882, groups:
                                 year, 24
##
## Fixed effects:
                                         df t value Pr(>|t|)
##
               Estimate Std. Error
## (Intercept)
               7.91981
                           0.17559 14.09445
                                             45.104
                                                     < 2e-16 ***
## year c
                0.43653
                           0.13529 21.39075
                                              3.227
                                                      0.00398 **
## dos
                0.05938
                           0.16521 17.09441
                                              0.359 0.72368
## I(dos^2)
               -1.28574
                           0.12112 11.08547 -10.615 3.79e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##
            (Intr) year_c dos
## year_c
            -0.049
## dos
             0.034 0.025
## I(dos^2) -0.577 0.018 0.031
```

#### Full model

**NOTE**: at the time of this writing, IR is *unavaible* in this model. I have not gotten any response from the team that manages the UBC Totem Station data.

Response variable:

• log\_wesa - Log-transformed predicted WESA count

Predictor variables:

- year\_c Scale-transformed survey year
  dos Scale-transformed Julian date, aka Day of Season
  elev\_range Tidal amplitude (m)
  total\_precip Total daily precipitation (mm)
  mean\_temp Daily mean temperature (C°)
  flow Fraser River discarge (m^3/s)
- u, v Westerly and Southerly wind vectors (km/h)
  n\_s Location ('North' or 'South')

Additionally, the dataset is reduced down to only complete cases of all predictor variables of interest (1882 -> 1873).

```
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula:
## log_wesa ~ year_c + dos + I(dos^2) + scale(elev_range) + scale(total_precip) +
       scale(mean_temp) + scale(flow) + scale(u) + scale(v) + n_s +
##
       (dos + I(dos^2) | year) + (scale(flow) | n_s)
##
##
      Data: dat2
##
## REML criterion at convergence: 9295.4
##
## Scaled residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -3.6037 -0.3664 0.1907 0.6530
                                   2.6563
##
## Random effects:
   Groups
                         Variance Std.Dev. Corr
##
             Name
             (Intercept) 0.62485 0.7905
##
   year
##
                         0.58201 0.7629
                                            0.02
             dos
                         0.18182 0.4264
                                           -0.49 0.18
##
             I(dos^2)
##
             (Intercept) 6.57361
                                 2.5639
             scale(flow) 0.07199 0.2683
##
                                           0.99
##
  Residual
                         7.85024 2.8018
## Number of obs: 1873, groups: year, 24; n_s, 2
##
## Fixed effects:
                                                      df t value Pr(>|t|)
##
                         Estimate Std. Error
## (Intercept)
                        8.151e+00 1.950e+00
                                              1.950e-08
                                                           4.180
                                                                   1.0000
## year_c
                        4.857e-01 1.488e-01
                                              2.043e+01
                                                           3.265
                                                                   0.0038 **
## dos
                       -7.627e-04 2.049e-01 3.067e+01
                                                        -0.004
                                                                   0.9971
## I(dos^2)
                       -1.339e+00 1.219e-01 1.169e+01 -10.990 1.63e-07 ***
```

```
## scale(elev range)
                       3.994e-01 7.721e-02 9.786e+02
                                                         5.173 2.79e-07 ***
## scale(total_precip) 4.194e-02 7.384e-02 1.774e+03
                                                                0.5701
                                                        0.568
## scale(mean temp)
                       1.680e-01 8.911e-02 9.056e+02
                                                         1.885
                                                                0.0597 .
## scale(flow)
                       1.741e-02 2.457e-01 2.140e+00
                                                         0.071
                                                                0.9496
## scale(u)
                       8.213e-02 8.665e-02
                                            1.377e+03
                                                         0.948
                                                                0.3434
## scale(v)
                       2.105e-01 8.887e-02 1.581e+03
                                                               0.0180 *
                                                        2.368
## n sS
                                                               1.0000
                       6.674e-01 1.376e+00 1.977e-08
                                                        0.485
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
                                   I(d^2) scl(l_) scl(t_) scl(m_) scl(f) scal()
##
              (Intr) year_c dos
## year_c
              -0.004
               0.011 0.024
## dos
## I(dos^2)
              -0.052 0.019 0.051
## scl(lv_rng) -0.001 0.012 -0.050 0.036
## scl(ttl_pr) 0.008 -0.009 -0.013 0.014 0.044
## scl(mn tmp) 0.000 -0.061 -0.151 0.003 -0.070
                                                   0.068
## scale(flow) 0.667 -0.005 -0.306 0.074 0.035
                                                  0.020
                                                           0.014
               0.000 -0.039 0.021 -0.068 -0.102
## scale(u)
                                                 -0.042
                                                           0.071
                                                                  0.025
## scale(v)
              -0.006 -0.015  0.042 -0.066  0.018 -0.251 -0.079
                                                                  0.000 0.522
## n sS
              -0.354 -0.002 -0.011 -0.007 -0.002 -0.023 -0.002
                                                                  0.104 0.010
              scl(v)
##
## year_c
## dos
## I(dos^2)
## scl(lv_rng)
## scl(ttl_pr)
## scl(mn_tmp)
## scale(flow)
## scale(u)
## scale(v)
## n_sS
               0.025
## optimizer (nloptwrap) convergence code: 0 (OK)
## unable to evaluate scaled gradient
## Model failed to converge: degenerate Hessian with 1 negative eigenvalues
```

#### Backwards step-wise selection

```
## Backward reduced random-effect table:
##
##
                                       Eliminated npar logLik
                                                                  AIC
                                                                         I.R.T Df
## <none>
                                                    21 -4647.7 9337.4
## dos in (dos + I(dos^2) | year)
                                                0
                                                    18 -4668.6 9373.3 41.822 3
## I(dos^2) in (dos + I(dos^2) | year)
                                                0
                                                    18 -4651.2 9338.4 6.943 3
## scale(flow) in (scale(flow) | n s)
                                                0
                                                    19 -4650.2 9338.4 4.964 2
##
                                       Pr(>Chisq)
## <none>
## dos in (dos + I(dos^2) | year)
                                        4.376e-09 ***
## I(dos^2) in (dos + I(dos^2) | year)
                                          0.07373 .
## scale(flow) in (scale(flow) | n_s)
                                          0.08360 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Backward reduced fixed-effect table:
## Degrees of freedom method: Satterthwaite
##
##
                        Eliminated Sum Sq Mean Sq NumDF
                                                             DenDF F value
                                                                                Pr(>F)
## n s
                                      1.85
                                              1.85
                                                              0.00
                                                                    0.2352 1.000000
                                  1
## scale(flow)
                                      0.09
                                               0.09
                                                              1.97
                                                                     0.0116 0.924327
                                      2.49
## scale(total_precip)
                                               2.49
                                                        1 1773.49
                                                                     0.3179 0.572966
                                  3
## scale(u)
                                  4
                                      7.46
                                              7.46
                                                        1 1405.21
                                                                     0.9517 0.329455
## scale(mean_temp)
                                  5 24.48
                                              24.48
                                                        1 961.84
                                                                     3.1231 0.077505
## year_c
                                  0 78.39
                                              78.39
                                                        1
                                                             20.45 10.0000 0.004806
                                     0.93
## dos
                                  0
                                              0.93
                                                             22.76
                                                                    0.1188 0.733482
                                                        1
## I(dos^2)
                                  0 869.36 869.36
                                                             11.26 110.9087 3.584e-07
                                                        1
## scale(elev_range)
                                  0 227.24 227.24
                                                       1 1067.75 28.9905 8.942e-08
## scale(v)
                                  0 57.11
                                            57.11
                                                      1 1663.84 7.2857 0.007021
##
## n_s
## scale(flow)
## scale(total_precip)
## scale(u)
## scale(mean_temp)
## year_c
## dos
## I(dos^2)
## scale(elev_range)
                        ***
## scale(v)
                        **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Model found:
## \log_{\text{wesa}} \sim \text{year_c} + \text{dos} + I(\text{dos}^2) + \text{scale}(\text{elev\_range}) + \text{scale}(\text{v}) + (\text{dos} + I(\text{dos}^2) | \text{year}) + (\text{scale})
```

#### Summary of best-fit model

```
## Linear mixed model fit by REML. t-tests use Satterthwaite's method [
## lmerModLmerTest]
## Formula: log_wesa ~ year_c + dos + I(dos^2) + scale(elev_range) + scale(v) +
       (dos + I(dos^2) | year) + (scale(flow) | n_s)
##
     Data: dat2
##
## REML criterion at convergence: 9290.9
##
## Scaled residuals:
##
      Min 1Q Median
                               3Q
## -3.5926 -0.3549 0.1977 0.6622 2.6351
##
## Random effects:
## Groups
            Name
                        Variance Std.Dev. Corr
            (Intercept) 0.66453 0.8152
##
   year
##
                        0.56830 0.7539
                                          -0.06
##
            I(dos^2)
                        0.21228 0.4607
                                          -0.51 0.14
            (Intercept) 2.40110 1.5495
## n_s
##
            scale(flow) 0.04795 0.2190
                                          1.00
                        7.83853 2.7997
## Residual
## Number of obs: 1873, groups: year, 24; n_s, 2
## Fixed effects:
                      Estimate Std. Error
                                                  df t value Pr(>|t|)
                                 0.81189
                                             4.70595 10.448 0.000196 ***
## (Intercept)
                       8.48259
                       0.47802
                                  0.15116
                                           20.44910
                                                      3.162 0.004806 **
## year_c
                                                      0.345 0.733482
## dos
                       0.06505
                                  0.18871
                                            22.76153
## I(dos^2)
                      -1.33576
                                  0.12684
                                            11.26124 -10.531 3.58e-07 ***
## scale(elev range)
                       0.41344
                                  0.07679 1067.75043 5.384 8.94e-08 ***
## scale(v)
                       0.19582
                                  0.07255 1663.83794 2.699 0.007021 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
              (Intr) year_c dos
                                   I(d^2) scl(_)
              -0.013
## year_c
## dos
               0.353 0.016
## I(dos^2)
              -0.213 0.022 0.068
## scl(lv_rng) -0.043 0.008 -0.048 0.026
## scale(v)
              0.011 0.001 0.013 -0.032 0.091
## optimizer (nloptwrap) convergence code: 0 (OK)
## boundary (singular) fit: see help('isSingular')
```

# Check assumptions of best fit model

