

American International University-Bangladesh

Experiment NO - 3

Title: Study of Nyquist bit rate formula and
Shannon capacity using MATLAB .

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Course title: Data Communication .

Section: L

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Experiment No: 3

Date: 03.11.2025

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Task 1: Example of Nyquist bit rate calculation for a noiseless channel.

Solution:

close all;

clc;

fs = 8000;

t = 0:1/fs:1-1/fs;

$$ex = 1.1 * \sin(2 * \pi * 100 * t) + 1.3 * \cos(2 * \pi * 300 * t) + 1.5 * \sin(2 * \pi * 2000 * t);$$

bandwidth = obw(ex, fs);

L = 2;

$$\text{BitRate} = 2 * \text{bandwidth} * \log_2(L)$$

Result: BitRate = 3.8019e+03

Task 3: Example of shannon capacity calculation for a noisy channel.

Solution:

close all;

clc;

fs = 8000;

f = 3;

t = 0:1/fs:1-1/fs;

A = 2;

s = 0.4;

$$x = A * \sin(2 * \pi * f * t);$$

ns = s * randn(size(signal));

S-N-R = snrc(x, ns);

bandwidth = obw(x, fs);

$$c = \text{bandwidth} * \log_2(1 + S/NR)$$

Result:

$\text{SNR} = C =$

$$6.6576e+04$$

Task 2: Calculation of SNR

close all;

clc;

fs = 8000;

f = 400;

t = 0:1/fs:1-1/fs;

A = 3.0

$$\text{powfund} = A^{2/2} \cdot$$

S = 0.1

Varnoise = S^2

Signal = A * sin(2 * pi * f * t);

Noise = S * randn(size(signal));

NoisySignal = Signal + Noise

SNR = snrc(NoisySignal)

$$\text{def SNR} = 10^{\log_{10}(\text{powfund}/\text{varnoise})}$$

Result:

$\text{SNR} =$

$$26.2571$$

$\text{def SNR} =$

$$26.5321$$

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Title: Study of Nyquist bit rate and shannon capacity using MATLAB

Objective: The aim of this experiment is to learn how MATLAB helps us to solve basic communication problems. hence we calculate the Nyquist bit rate for noiseless channel and the shannon capacity for noisy channel. We also calculate the SNR value of the noisy signal and can know the quality of the signal that means which is more corrupted. We can also know the shannon capacity of noisy signal and helping us to know the bandwidth also.

Working principle: In this experiment, we use the MATLAB to study how much data can be sent through the communication channel that means the bitrate. For noiseless channels the Nyquist formula helps us to find the maximum bitrate using bandwidth and number of signal levels (L).

$$\text{Bitrate} = 2 \times \text{bandwidth} \times \log_2(L)$$

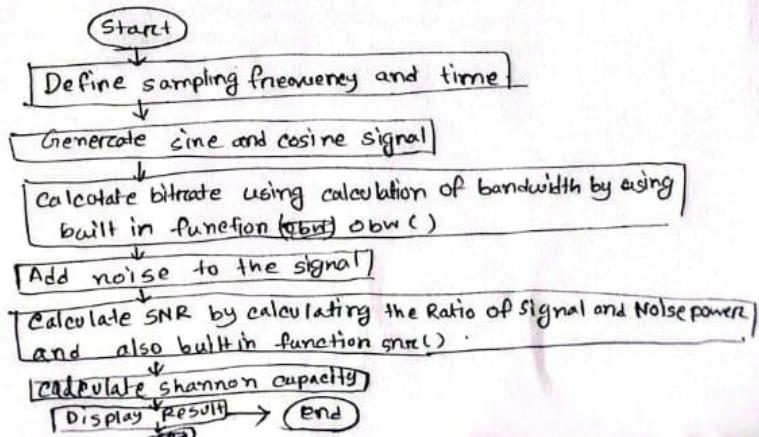
For noisy channel, the shannon capacity formula tells us the highest data rate of this channel. Capacity = bandwidth $\times \log_2(1+SNR)$. Here, SNR is the Signal to Noise Ratio.

$$SNR = \frac{\text{Average Signal power}}{\text{Average Noise power}}$$

A higher SNR means the signal is less corrupted by noise. And low SNR means the signal is more corrupted by noise.

By using MATLAB, this experiment determine all of this above and gives us the clear knowledge.

Flowchart:



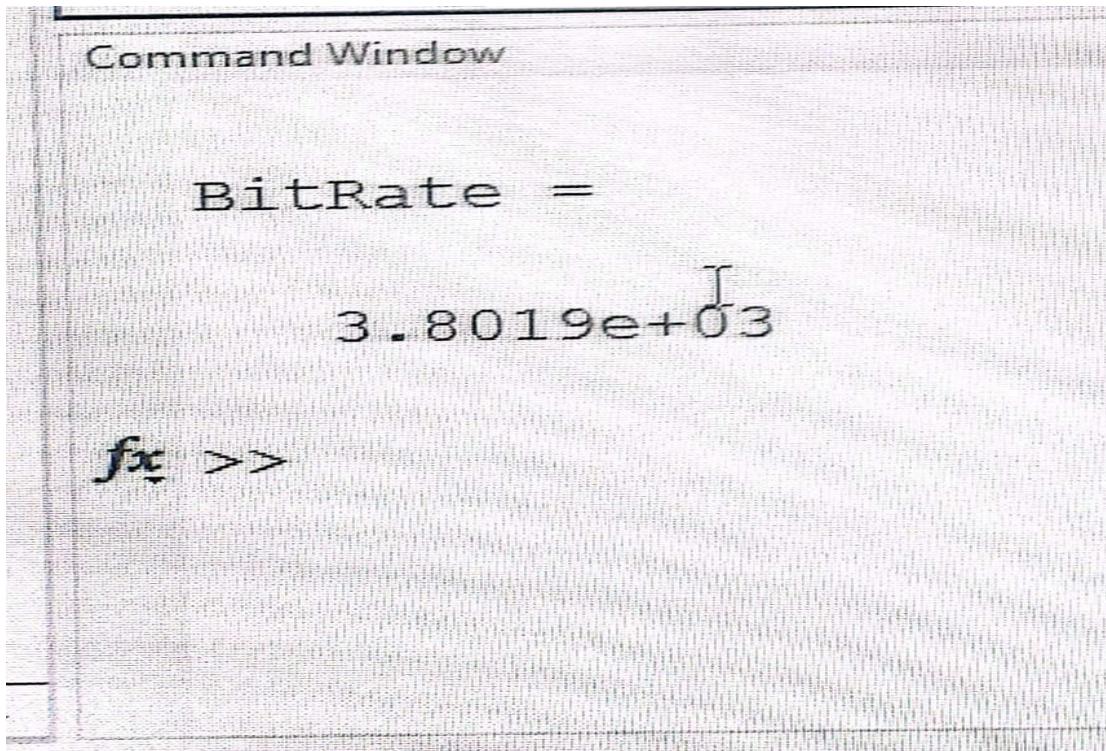
MATLAB CODE AND RESULT:

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Problem 1: Example of Nyquist bit rate calculation for a noiseless channel:

```
close all;  
clc;  
fs = 8000; % Sampling frequency  
t = 0:1/fs:1-1/fs; % Time duration  
cx = 1.1*sin(2*pi*100*t) + 1.3*cos(2*pi*300*t) + 1.5*sin(2*pi*2000*t);  
bandwidth = obw(cx,fs); % Bandwidth of the signal  
L=2; % Level of the signal  
BitRate = 2*bandwidth*log2(L)
```

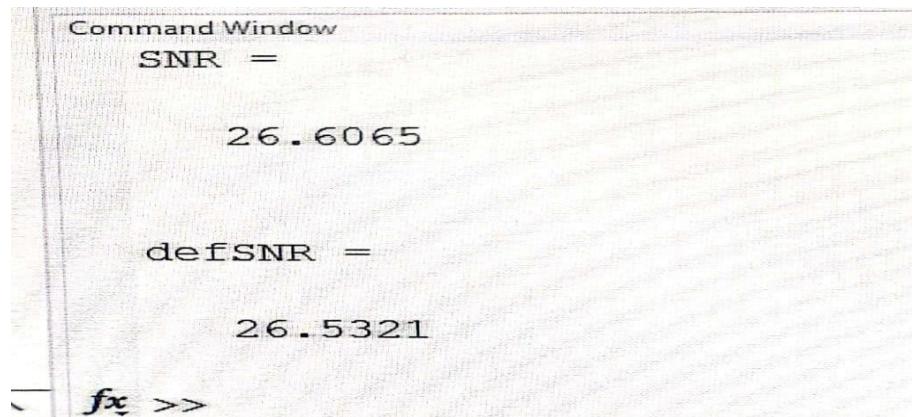
Result:



Problem 1: Example: Calculation of SNR

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```
close all;  
clc;  
%Define number of samples to take  
fs = 8000; % Sampling frequency  
f = 400; %Hz  
%Define signal  
t = 0:1/fs:1-1/fs;  
A = 3.0;  
powfund = A^2/2  
s = 0.1;  
varnoise = s^2;  
signal = A*sin(2*pi*f*t);  
%noise  
noise = s*randn(size(signal));  
%noisy signal  
noisySignal = signal + noise;  
SNR = snr(noisySignal) %Calculation of SNR using snr function  
defSNR = 10*log10(powfund/varnoise) %Calculation of SNR following the definition
```

Result:

The image shows a screenshot of the MATLAB Command Window. The window title is "Command Window". The command entered was "SNR =", followed by the output "26.6065". Below that, the command "defSNR =" was entered, followed by the output "26.5321". At the bottom of the window, there is a prompt "fx >>".

```
Command Window
SNR =
26.6065

defSNR =
26.5321

fx >>
```

Task 1:

Name: Poroma Basak, ID: 23-51662-2

Similar task can be done considering a noisy composite signal. Suppose our composite signal is,

```
signal = 1.5*sin(2*pi*2*t)+0.9*cos(2*pi*10*t)+1.1*sin(2*pi*20*t) + 0.13*randn(size(t));
```

*****Calculate the SNR value of the signal.

Solution:

```
close all;
```

```
clc;
```

```
% Sampling frequency
```

```
fs = 8000;
```

```
% Time vector
```

```
t = 0:1/fs:1-1/fs;
```

```
% Signal parameters
```

```
A1 = 1.5; f1 = 2;
```

```
A2 = 0.9; f2 = 10;
```

```
A3 = 1.1; f3 = 20;
```

```
% Noise parameters
```

```
s = 0.13; % standard deviation of noise
```

```
varnoise = s^2; % noise variance
```

```
% Composite clean signal
```

```
signal = A1*sin(2*pi*f1*t) + A2*cos(2*pi*f2*t) + A3*sin(2*pi*f3*t);
```

```
% Add noise
```

```
noise = s * randn(size(signal));
```

```
noisySignal = signal + noise;
```

```
% Signal power (theoretical)
```

```
powfund = (A1^2 + A2^2 + A3^2) / 2;
```

```
% SNR using built-in function
```

```
SNR = snr(signal, noise);
```

```
% SNR using definition
```

Name: Poroma Basak, ID: 23-51662-2

```
defSNR = 10*log10(powfund / varnoise);
```

```
% Display output in your desired format
```

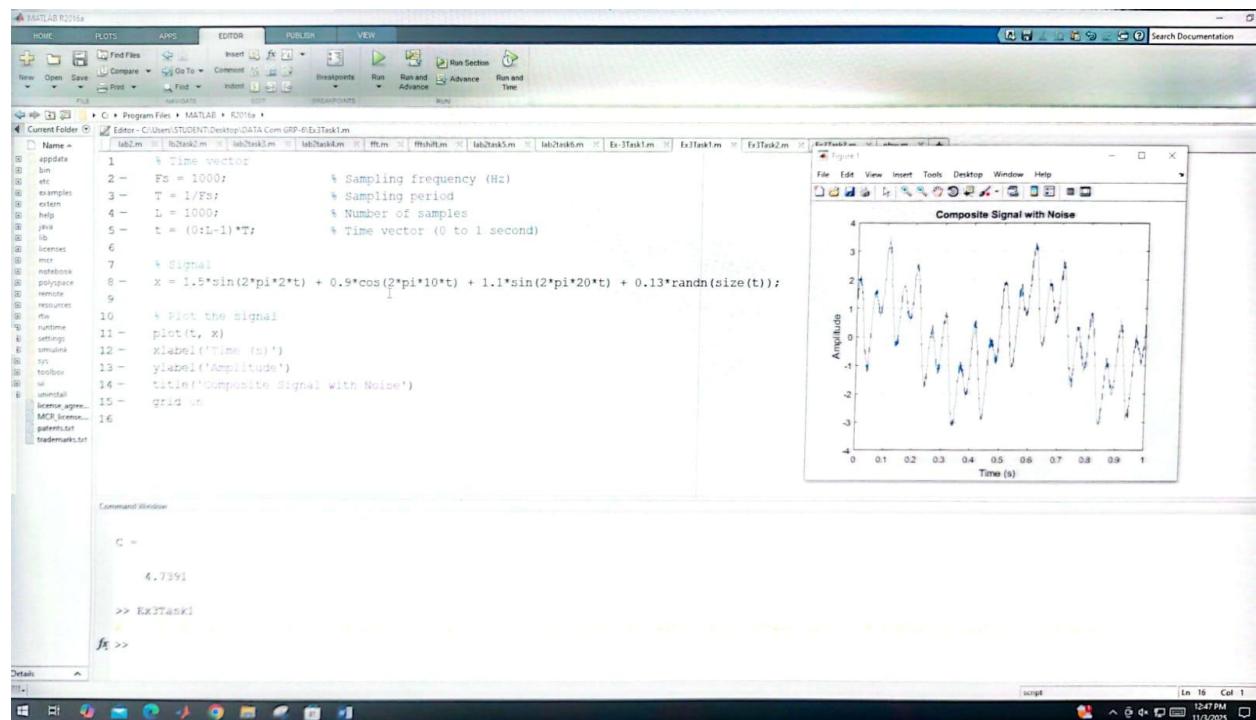
```
disp(['SNR = ', num2str(SNR)]);
```

```
disp(['defSNR = ', num2str(defSNR)]);
```

Result:

SNR = 21.0835

defSNR = 21.0219



Problem 3:

Example of Shannon capacity calculation for a noisy channel:

```
clc
close all
fs = 8000; % Sampling frequency
f = 3; %Hz
%Define signal
t = 0:1/fs:1-1/fs;
```

```

A = 2;
s = 0.4;
%signal
x = A*sin(2*pi*f*t);
%noise
ns = s*randn(size(signal));
S_N_R = snr(x,ns);
bandwidth = obw(x,fs); % Bandwidth of the signal
%capacity
C = bandwidth*log2(1+SNR) % Capacity of the channel

```

Result:

Command Window

C =

4.7391

fz >>

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Discussion: In this experiment, we used MATLAB to study how noise affects the data transmission. We calculate the Nyquist bit rate for a noiseless channel and Shannon capacity for a noisy channel. The results show that higher SNR gives a clear signal and higher channel capacity. The results show that higher SNR gives a clear signal and less corrupted signal. It also shows that bandwidth and signal levels are used to calculate Bitrate.

Conclusion: This experiment helped us understand the limits of data transfer in channels. We learned how Nyquist bit rate and Shannon capacity are affected by noise, bandwidth and signal levels. Higher SNR improves signal quality and low SNR make the signal more corrupted or noisy.

