

American International University-Bangladesh

Experiment No-3

Title: Study of Nyquist bit rate ~~formula~~ and
Shannon capacity using MATLAB.

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Course title: Data Communication.

Section: L

Date of submission: 08-11-2025.

Experiment No: 3

Date: 03.11.2025

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Task 1: Example of Nyquist bit rate calculation for a noiseless channel.

Solution

close all;

clc;

fs = 8000;

t = 0:1/fs:1-1/fs;

cx = 1.1 * sin(2 * pi * 100 * t) + 1.3 * cos(2 * pi * 300 * t) + 1.5 * sin(2 * pi * 2000 * t);

bandwidth = obw(cx, fs);

L = 2;

BitRate = 2 * bandwidth * log2(L)

Result: BitRate = 3.8019e+03

Task 3: Example of Shannon capacity calculation for a noisy channel.

Solution

close all;

fs = 8000;

f = 3;

t = 0:1/fs:1-1/fs;

A = 2;

S = 0.4;

X = A * sin(2 * pi * f * t);

ns = S * randn(size(signal));

S-N-R = snr(x, ns);

bandwidth = obw(x, fs);

C = bandwidth * log2(1 + SNR)

Result:

SNR = C =

6.6576e+04

Task 2: Calculation of SNR

close all;

clc;

fs = 8000;

f = 400;

t = 0:1/fs:1-1/fs;

A = 3.0

powfund = A^2/2;

S = 0.1

varnoise = S^2

Signal = A * sin(2 * pi * f * t);

noise = S * randn(size(signal));

noisySignal = signal + noise

SNR = snr(noisySignal)

defSNR = 10 * log10(powfund/varnoise)

Result:

SNR =

26.2571

defSNR =

26.5321

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Titles Study of Nyquist bit rate and Shannon capacity using MATLAB

Objective: The aim of this experiment is to learn how MATLAB helps to solve basic communication problems. Here we calculate the Nyquist bit rate for noiseless channel and the Shannon capacity for noisy channel. We also calculate the SNR value of the noisy signal and can know the quality of the signal that means which is more corrupted. We can also know the Shannon capacity of noisy signal and helping us to know the bandwidth also.

Working principle: In this experiment, we use the MATLAB to study how much data can be sent through the communication channel that means the bit rate. For noiseless channel, the Nyquist formula helps us to find the maximum bit rate using bandwidth and number of signal levels (L).

$$\text{Bitrate} = 2 \times \text{bandwidth} \times \log_2(L)$$

For noisy channel, the Shannon capacity formula tells us the highest data rate of this channel. $\text{Capacity} = \text{bandwidth} \times \log_2(1 + \text{SNR})$

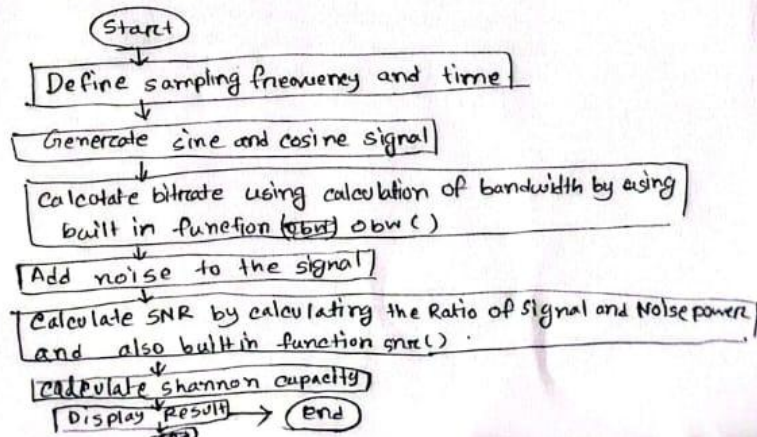
Here, SNR is the Signal to Noise Ratio. Power Ratio.

$$\text{SNR} = \frac{\text{Average Signal power}}{\text{Average Noise power}}$$

A higher SNR means the signal is less corrupted by noise, and low SNR means the signal is more corrupted by noise.

By using MATLAB, this experiment determines all of this above and gives us the clear knowledge.

Flowchart:

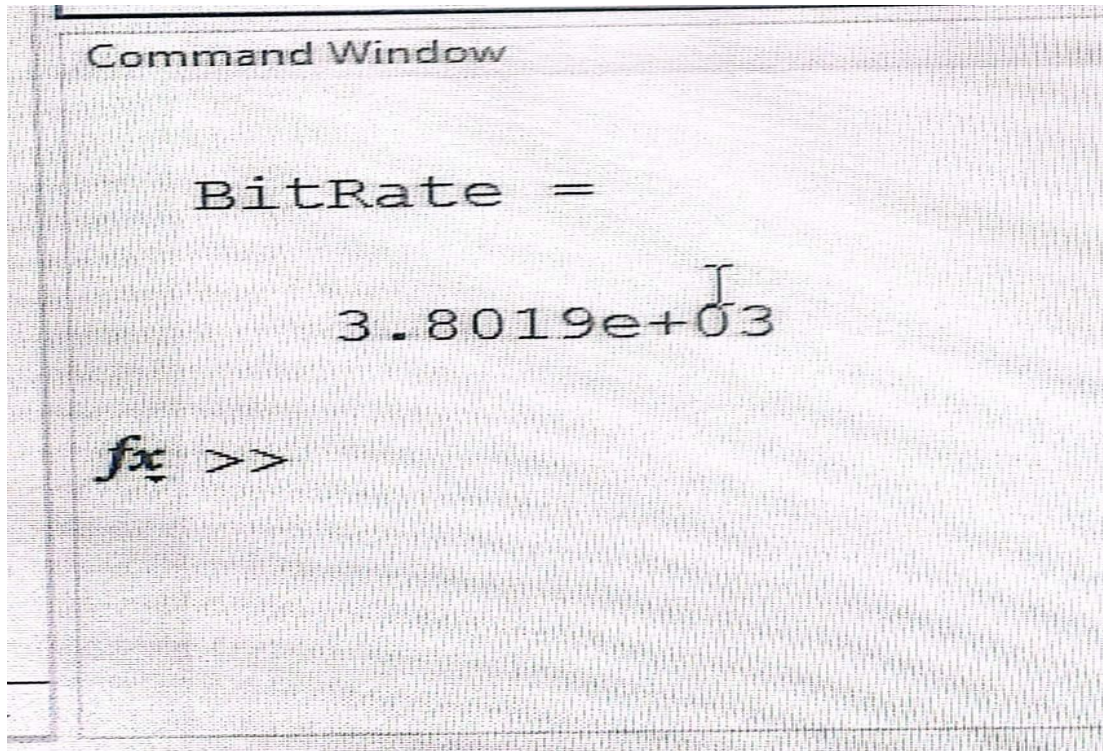


MATLAB CODE AND RESULT:

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Problem 1: Example of Nyquist bit rate calculation for a noiseless channel:

```
close all;  
clc;  
fs = 8000; % Sampling frequency  
t = 0:1/fs:1-1/fs; % Time duration  
cx = 1.1*sin(2*pi*100*t) + 1.3*cos(2*pi*300*t) + 1.5*sin(2*pi*2000*t);  
bandwidth = obw(cx,fs); % Bandwidth of the signal  
L=2; % Level of the signal  
BitRate = 2*bandwidth*log2(L)
```

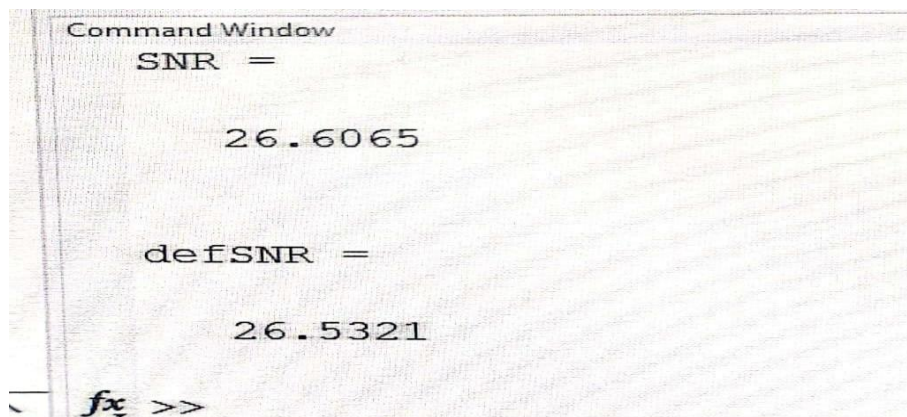
Result:

A screenshot of the MATLAB Command Window. The title bar reads "Command Window". The output displayed is "BitRate =" followed by "3.8019e+03" on the next line. At the bottom left, the prompt "fx >>" is visible.

Problem 1: Example: Calculation of SNR

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```
close all;
clc;
%Define number of samples to take
fs = 8000; % Sampling frequency
f = 400; %Hz
%Define signal
t = 0:1/fs:1-1/fs;
A = 3.0;
powfund = A^2/2
s = 0.1;
varnoise = s^2;
signal = A*sin(2*pi*f*t);
%noise
noise = s*randn(size(signal));
%noisy signal
noisySignal = signal + noise;
SNR = snr(noisySignal) %Calculation of SNR using snr function
defSNR = 10*log10(powfund/varnoise) %Calculation of SNR following the definition
```

Result:

A screenshot of the MATLAB Command Window. The window title is "Command Window". It displays the results of the MATLAB script: "SNR =" followed by the value "26.6065", and "defSNR =" followed by the value "26.5321". At the bottom left, the prompt "fx >>" is visible.

```
Command Window
SNR =

    26.6065

defSNR =

    26.5321

fx >>
```

Task 1:

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Similar task can be done considering a noisy composite signal. Suppose our composite signal is,

$\text{signal} = 1.5 \cdot \sin(2\pi \cdot 2 \cdot t) + 0.9 \cdot \cos(2\pi \cdot 10 \cdot t) + 1.1 \cdot \sin(2\pi \cdot 20 \cdot t) + 0.13 \cdot \text{randn}(\text{size}(t));$

*****Calculate the SNR value of the signal.

Solution:

```
close all;
```

```
clc;
```

```
% Sampling frequency
```

```
fs = 8000;
```

```
% Time vector
```

```
t = 0:1/fs:1-1/fs;
```

```
% Signal parameters
```

```
A1 = 1.5; f1 = 2;
```

```
A2 = 0.9; f2 = 10;
```

```
A3 = 1.1; f3 = 20;
```

```
% Noise parameters
```

```
s = 0.13;          % standard deviation of noise
```

```
varnoise = s^2;    % noise variance
```

```
% Composite clean signal
```

```
signal = A1*sin(2*pi*f1*t) + A2*cos(2*pi*f2*t) + A3*sin(2*pi*f3*t);
```

```
% Add noise
```

```
noise = s * randn(size(signal));
```

```
noisySignal = signal + noise;
```

```
% Signal power (theoretical)
```

```
powfund = (A1^2 + A2^2 + A3^2) / 2;
```

```
% SNR using built-in function
```

```
SNR = snr(signal, noise);
```

% SNR using definition

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```
defSNR = 10*log10(powfund / varnoise);
```

% Display output in your desired format

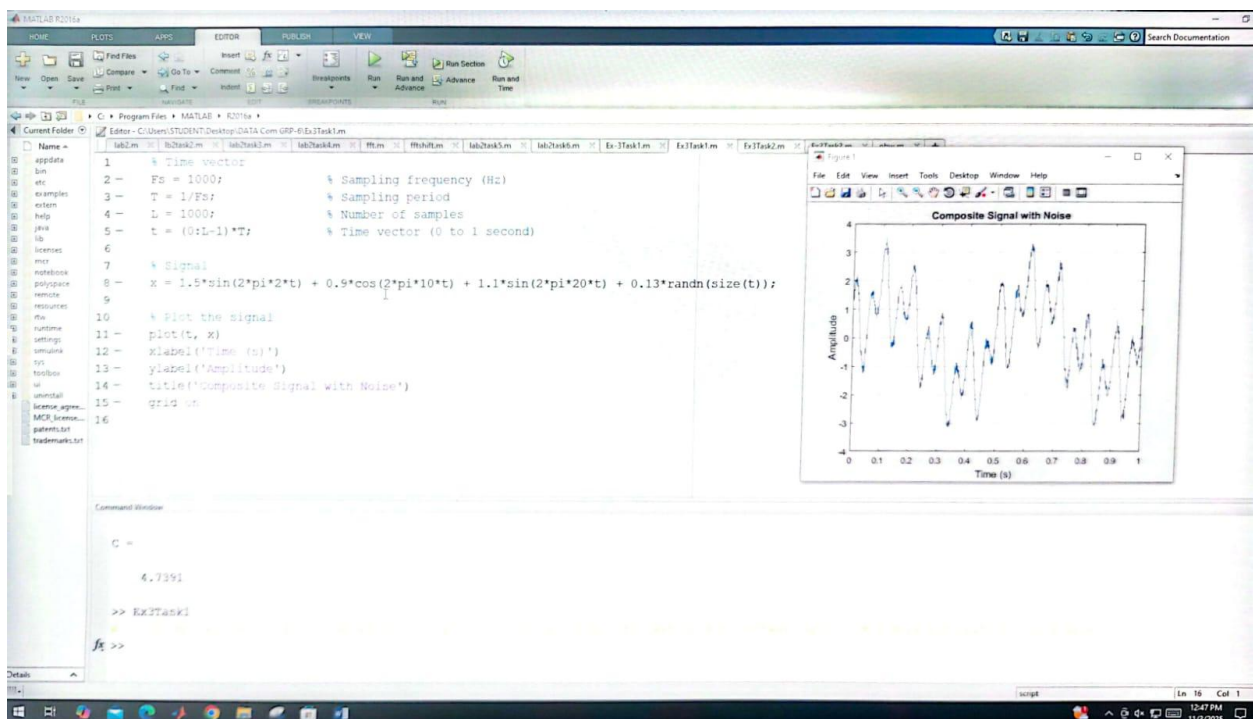
```
disp(['SNR = ', num2str(SNR)]);
```

```
disp(['defSNR = ', num2str(defSNR)]);
```

Result:

SNR = 21.0835

defSNR = 21.0219



Problem 3:

Example of Shannon capacity calculation for a noisy channel:

```
clc
```

```
close all
```

```
fs = 8000; % Sampling frequency
```

```
f = 3; %Hz
```

```
%Define signal
```

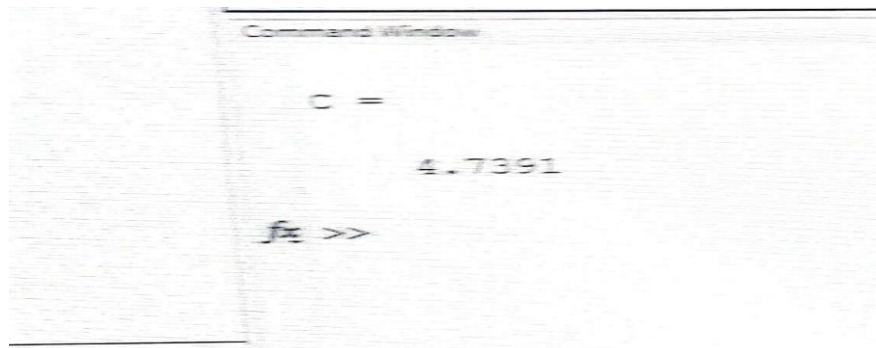
```
t = 0:1/fs:1-1/fs;
```

```

A = 2;
s = 0.4;
%signal
x = A*sin(2*pi*f*t);
%noise
ns = s*randn(size(signal));
S_N_R = snr(x,ns);
bandwidth = obw(x,fs); % Bandwidth of the signal
%capacity
C = bandwidth*log2(1+SNR) % Capacity of the channel

```

Result:



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Discussion: In this experiment, we used MATLAB to study how noise affects the data transmission. We calculate the Nyquist bit rate for a noiseless channel and Shannon capacity for a noisy channel. The results show that higher SNR gives a clear signal and higher channel. The results show that higher SNR gives a clear signal and less corrupted signal. It also shows that bandwidth and signal levels are used to calculate Bitrate.

Conclusion: This experiment helped us understand the limits of data transfer in channels. We learned how Nyquist bit rate and Shannon capacity are affected by noise, bandwidth and signal levels. Higher SNR improves signal quality and low SNR make the signal more corrupted or noisy.

