Report for Programming Assignment 2 (Fifteen Puzzle)

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Abstract

We consider the performance of two algorithms, A* search and rbfs, on finding solutions to a generic fifteen puzzle. We compared their performance with respect to computation time and optimality of solution for various levels of scrambling of the board and with respect to two different heuristics.

1 Introduction

In this paper, we examine the performance of two search algorithms, Compassion A* and RBFS, using a 4x4 puzzle as a representation. The environment is randomized to ensure optimal exploration. To enhance efficiency, we introduce a random algorithm designed to avoid repeating the same steps.

2 Environment Descriptions

We consider the setting of the fifteen puzzle. In this setting, a four by four grid contains fifteen (15) tiles, where the tiles can be slid to move the empty square around. The tiles are each numbered and the goal of the program is to find a sequence of moves that will return the tiles to their correct order after being scrambled in the minimum moves with the minimum amount of calculation time.

2.1 Heuristic function

We used the Manhattan distance as one of our heuristics. For this, we considered each tile to have a target location, and counted the total number of squares each tile must be moved to reach that location. This is equivalent to assuming each tile can be moved through other tiles.

We also used a heuristic suggested by Michael Kim, on his blog at https://michael.kim/blog/puzzle, where the Manhattan distance is augmented by an addition of two moves for each location that has two tiles next to each other that need to be directly swapped. This is because it takes at least three moves to swap two tiles. This is no longer an admissible heuristic because it assumes that each swap must happen independently.

This is not quite the same as what is reccomended by Mr. Kim, since he does not mention anythin about what to do with vertical swaps. We treated vertical swaps differently because the correct offset between vertical tiles is 4 instead of 1.

2.2 A* search

We implement the A* search algorithm for finding the paths between initial states to a given goal state in the problem of puzzle 4x4. It is a variant of the uniform cost search by using a heuristic function for each node in addition to path costs.

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```
Algorithm 1 Programmatic Description of A* search
openlist = [Node(nodeState, 0, nodeState.manhdist())] // Start with the initial state
closedlist = []
totalHeuristic = 0 // keep running total of heuristic time
while openlist is not empty: do
   currentnode = node with minimum fscore in openlist
   currentnode.state.checkcanmove()
   remove currentnode from openlist
   add currentnode to closedlist
   if currentnode.heuristic is 0 then
       return currentnode, length of closedlist, totalHeuristic // Return the goal node and the number
of nodes expanded
   for move in ["up", "down", "left", "right"] do
       successorstate = copy of currentnode.state
       cannotmove = currentnode.state.checkcanmove()
       if move in cannotmove: then
           continue
       if move is "up": then
           successorstate.moveUp()
       if move is "down": then
           successorstate.moveDown()
       if move is "left": then
           successorstate.moveLeft()
       if move is "right": then
           successorstate.moveRight()
       cost = currentnode.cost + 1 // Assume uniform cost for each move
       heuristicTic = time.perfcounter()
       if funType is "other": then
           heuristic = successorstate.otherHeuristic()
       else
           heuristic = successorstate.manhdist()
       heuristicToc = time.perfcounter()
       totalHeuristic += heuristicToc - heuristicTic
       successornode = Node(successorstate, cost, heuristic, currentnode)
       if successornode not in closedlist: then // This would prefer a better equality
           add successornode to openlist
   return None
```

2.3 Recursive Best-First Search (RBFS)

Recursive Best-First Search (RBFS) operates by maintaining an f-limit variable, tracking the f-value of the best alternative path from any ancestor node to the current node. This f-limit guides the algorithm in determining which subtree of the problem tree to explore, balancing between the current path and the best alternative path. RBFS dynamically updates the f-values of nodes during recursion unwinding to ensure search functionality, thereby allowing consideration of forgotten subtrees in future exploration.

RBFS offers the advantage of requiring less memory compared to A* search, as it utilizes linear space. Unlike A*, which stores all explored nodes, RBFS only retains "relevant" nodes in memory. However,

RBFS may expand more nodes than A* due to redundancy. Since RBFS doesn't store all explored nodes, it can potentially revisit and re-expand the same nodes, leading to increased computation time.

```
if node.state isgoal() then
   return node, flimit
successors = []
for move in ["up", "down", "left", "right"] do
   if move is not in node.state.checkcanmove() then
       successorstate = copy of node.state
       performmove(move, successorstate) // Execute the move on the state
       cost = node.cost + 1
       heuristic = calculateheuristic(successorstate) // Calculate heuristic value for the successor
state
       successornode = create Node with successorstate, cost, heuristic, and parent node
       add successornode to successors list
if successors is empty then
   return None, infinity
while true do
   sort successors by fscore
   best = first node in successors
   if best.fscore > flimit then
       return None, best.fscore
   alternative = second node's fscore if successors has more than one node else infinity
   result, best.fscore = RBFS(best, min(flimit, alternative))
   if result is not None then
       return result, best.fscore
```

3 Experimental setup

4 Results

5 Discussion

- 1. Is there a clear preference ordering among the heuristics you tested considering the number of nodes searched and the total CPU time taken to solve the problems for the two algorithms?
- 2. Can a small sacrifice in optimality give a large reduction in the number of nodes expanded? What about CPU time?
- 3. Is the time spent on evaluating the heuristic a significant fraction of the total problem-solving time for any heuristic and algorithm you tested?
- 4. How did you come up with your heuristic evaluation function? We looked to the literature for suggestions.
- 5. How do the two algorithms compare in the amount of search involved and the cpu-time?