Actor Critic

Sanjiban Choudhury



Vanilla REINFORCE

Start with an arbitrary initial policy $\pi_{\theta}(a \mid s)$

while not converged do

Roll-out
$$\pi_{\theta}(a \mid s)$$
 to collect trajectories $D = \{s_0^i, a_0^i, r_0^i, ..., s_{T-1}^i, a_{T-1}^i, r_{T-1}^i\}_{i=1}^N$

Compute reward-to-go for each timestep for each trajectory $\hat{Q}^{\pi_{\theta}}(s_t^i, a_t^i) = \sum_{t=0}^{T-1} r(s_{t'}^i, a_{t'}^i)$

$$\hat{Q}^{\pi_{\theta}}(s_t^i, a_t^i) = \sum_{t'=t}^{T} r(s_{t'}^i, a_{t'}^i)$$

Compute gradient
$$\nabla_{\theta} J(\theta) = \frac{1}{N} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \; \hat{Q}^{\pi_{\theta}}(s_t^i, a_t^i) \right]$$

Update parameters $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

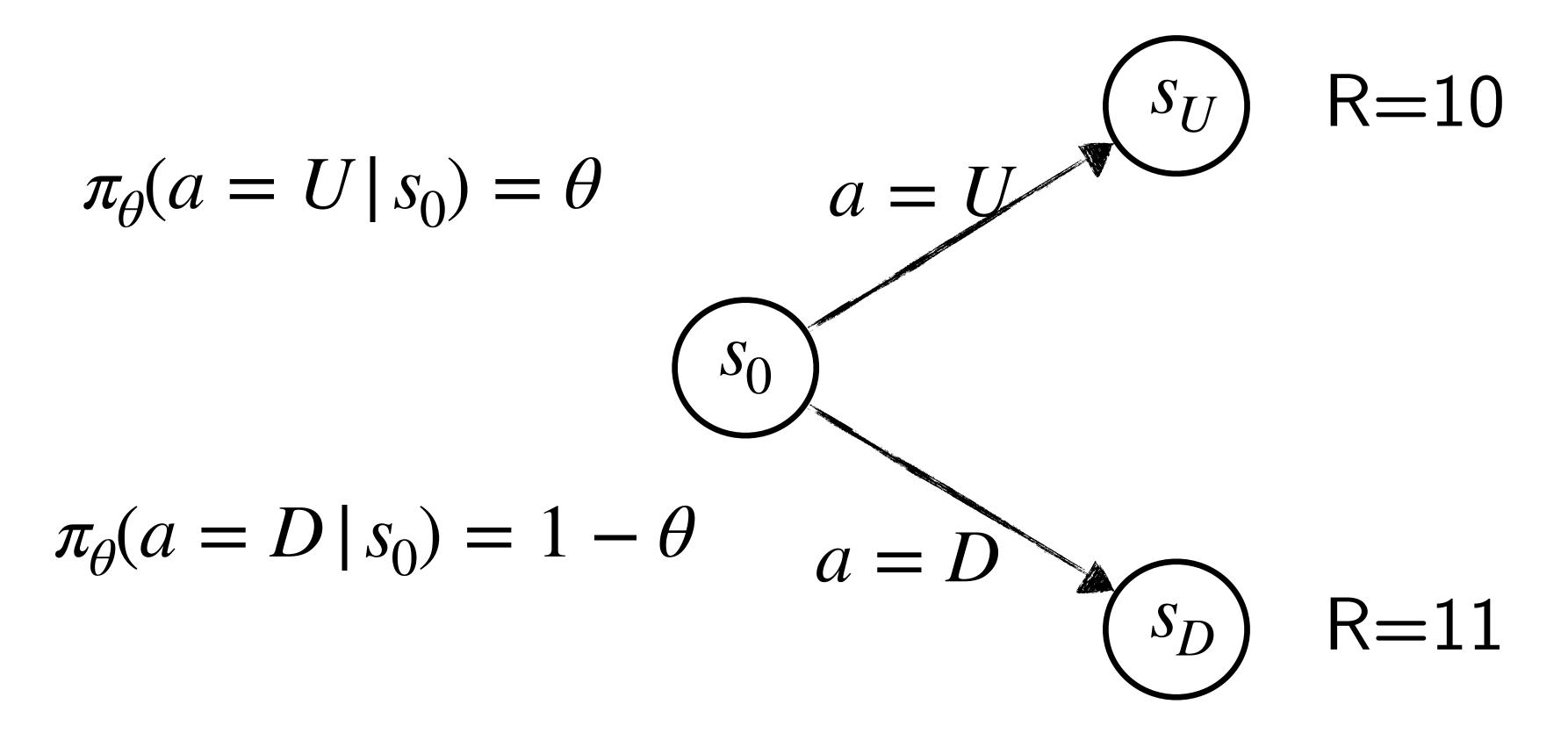
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

Three major nightmares with policy gradients

Nightmare 1:

High Variance

Consider the following MDP

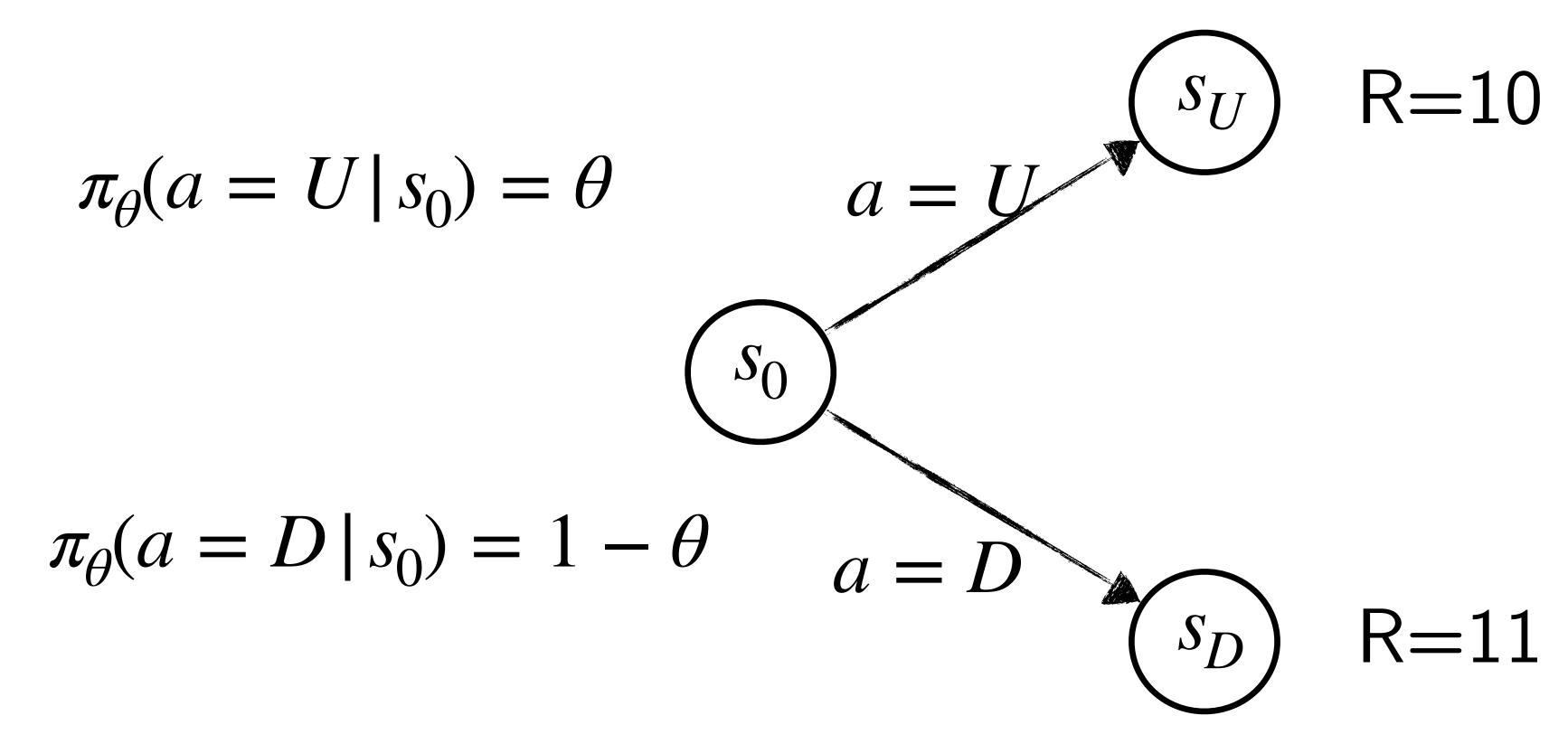


Suppose we init $\theta = 0.5$, and draw 4 samples with our policy And then apply PG

When Q values for all rollouts in a batch are high?

$$\nabla_{\theta} J = E_{s \sim d^{\pi_{\theta}}(s), a \sim \pi_{\theta}(a|s)} \left[\nabla_{\theta} \log \pi_{\theta}(a|s) Q^{\pi_{\theta}}(s, a) \right]$$

Recall that one of the reasons for the high variance is that the algorithm does not know how well the trajectories perform compared to other trajectories. Therefore, by introducing a baseline for the total reward (or reward to go), we can update the policy based on how well the policy performs compared to a baseline



Suppose we subtracted of $V^{\pi}(s_0) = 10.5$ from the reward to go

$$\nabla_{\theta} J = E_{d^{\pi_{\theta}}(s)} E_{\pi_{\theta}(a|s)} \left[\nabla_{\theta} \log(\pi_{\theta}(a|s)) \left(Q^{\pi_{\theta}}(s,a) - V^{\pi_{\theta}}(s) \right) \right]_{\tau}$$

$$\nabla_{\theta} J = E_{d^{\pi_{\theta}}(s)} E_{\pi_{\theta}(a|s)} \left[\nabla_{\theta} \log(\pi_{\theta}(a|s)) \left(Q^{\pi_{\theta}}(s,a) - V^{\pi_{\theta}}(s) \right) \right].$$

We can prove that this does not change the gradient

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$$\nabla_{\theta} J = E_{d^{\pi_{\theta}}(s)} E_{\pi_{\theta}(a|s)} \left[\nabla_{\theta} \log(\pi_{\theta}(a|s) A^{\pi_{\theta}}(s,a)) \right]$$

But turns Q values into advantage (which is lower variance)

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But turns Q values into advantage (which is lower variance)

Can we justify this move using the PDL?

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$$\hat{Q}^{\pi_{\theta}}(s_t^i, a_t^i) = \sum_{t'=t}^{1} r(s_{t'}^i, a_{t'}^i)$$

Compute gradient
$$\nabla_{\theta} J(\theta) = \frac{1}{N} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \; \hat{Q}^{\pi_{\theta}}(s_t^i, a_t^i) \right]$$

Update parameters $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

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Fix #1: Subtract baseline

Start with an arbitrary initial policy $\pi_{\theta}(a \mid s)$

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Fit value function
$$\hat{V}^{\pi_{\theta}}(s_t^i) \approx \sum_{t'=t}^{T-1} r(s_{t'}^i, a_{t'}^i)$$
 How??

Compute advantage $\hat{A}^{\pi_{\theta}}(s_t^i, a_t^i) = \hat{Q}^{\pi_{\theta}}(s_t^i, a_t^i) - \hat{V}^{\pi_{\theta}}(s_t^i)$

radient
$$\nabla_{\theta} J(\theta) = \frac{1}{N} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi_{\theta}(a_t^i \mid s_t^i) \hat{A}^{\pi_{\theta}}(s_t^i, a_t^i) \right]$$

Update parameters

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

Two ways to fit critic

Monte-Carlo

$$\left(V(s_t) - \sum_{t'=t}^{T} \gamma^{t'-t} r_t'\right)^2$$

Needs full time-horizon trajectories

Temporal Difference

$$\left(V(s_t) - \left[r_t + \gamma V(s_t)\right]\right)^2$$

Works with partial segments! (s,a,r,s')

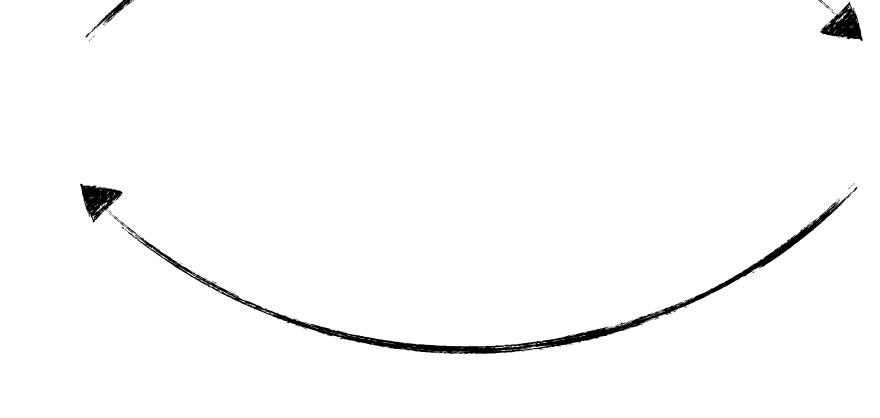
Actor-Critic Framework

Actor



Critic





Policy improvement of π

Estimates value functions V^{π}

Actor-Critic Framework (Infinite Horizon)

Start with an arbitrary initial policy $\pi_{\theta}(a \mid s)$

while not converged do

Roll-out $\pi_{\theta}(a \mid s)$ to collect trajectories $D = \{s^i, a^i, r^i, s^i_+\}_{i=1}^N$

Fit value function $\hat{V}^{\pi_{\theta}}(s^i)$ using TD, i.e. minimize $(r^i + \gamma \hat{V}^{\pi_{\theta}}(s^i) - \hat{V}^{\pi_{\theta}}(s^i))^2$

Compute advantage $\hat{A}^{\pi_{\theta}}(s^i, a^i) = r(s^i, a^i) + \gamma \hat{V}^{\pi_{\theta}}(s^i) - \hat{V}^{\pi_{\theta}}(s^i)$

Compute gradient
$$\nabla_{\theta} J(\theta) = \frac{1}{N} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \, \hat{A}^{\pi_{\theta}}(s^i, a^i) \right]$$

Update parameters
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

Important Actor Critic Algorithms

1. Soft Actor-Critic

- Stochastic policy
- Off-policy algorithm
- Adds entropy to reward to encourage exploration

2. TD3

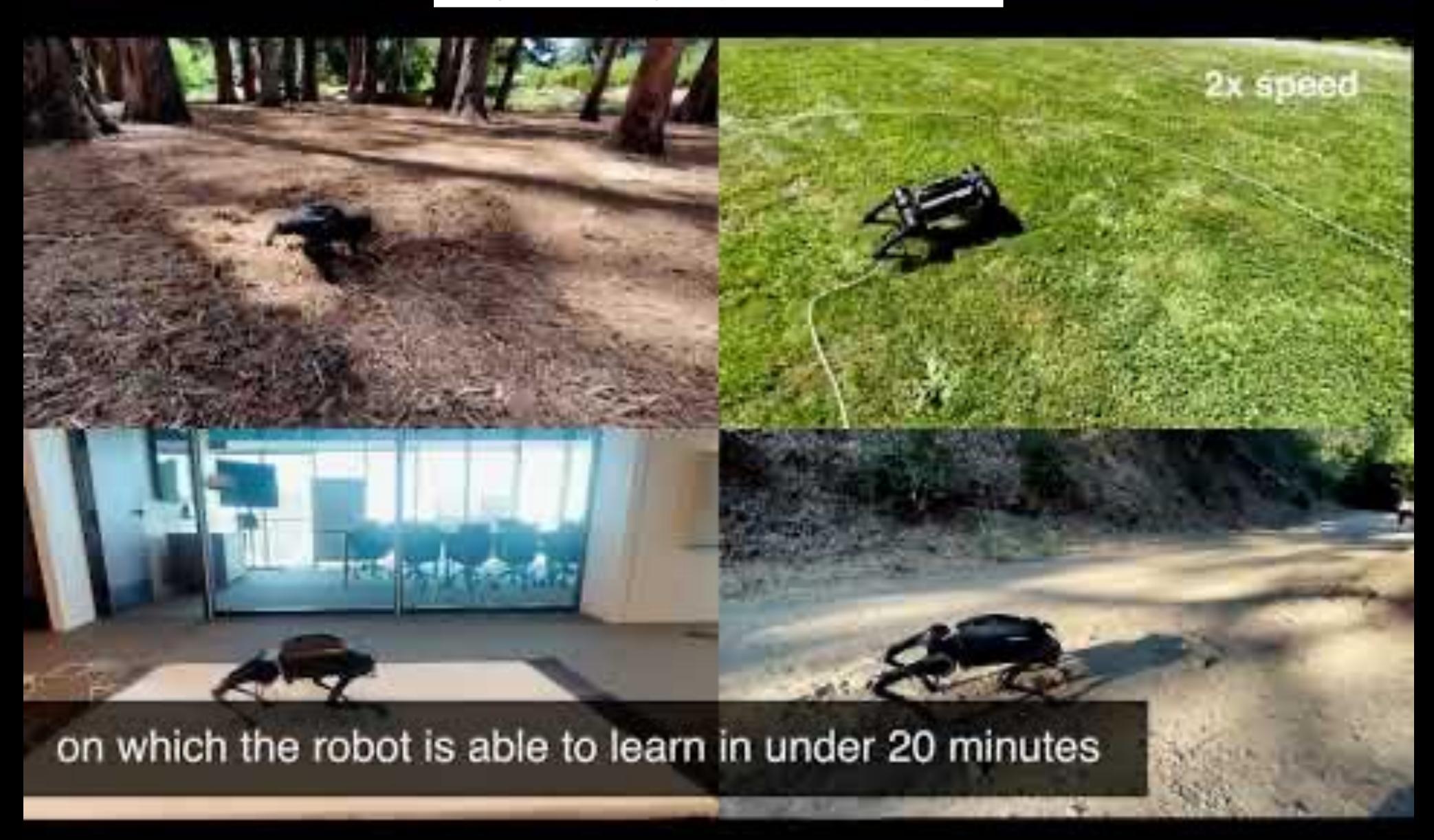
- Deterministic policy
- Off-policy algorithm
- Trains two Q networks to combat overestimation

3. PPC

- Stochastic policy
- On-policy algorithm
- We will cover this next!

Demonstrating a Walk in the Park: Learning to Walk in 20 Minutes With Model-Free Reinforcement Learning

Laura Smith*1, Ilya Kostrikov*1, Sergey Levine1
*Equal contribution 1Berkeley AI Research, UC Berkeley
{smithlaura, kostrikov}@berkeley.edu, svlevine@eecs.berkeley.edu



Details

State-Action Space: The state is 30 dimensional containing the joint positions (12 values), joint velocities (12 values), roll and pitch of the torso and binary foot contact indicators (4 values). The action space is 12 dimensional corresponding to the target joint position for the 12 robot joints. The predicted target joint angles $a = \hat{\mathbf{q}} \in \mathbb{R}^{12}$ is converted to torques $\boldsymbol{\tau}$ using a PD controller with target joint velocities set to 0.

Reward:

$$r(s,a) = r_v(s,a) - 0.1v_{yaw}^2$$

where v_{yaw} is an angular yaw velocity and

$$r_v(s,a) = egin{cases} 1, & ext{for } v_x \in [v_t, 2v_t] \ 0, & ext{for } v_x \in (-\infty, -v_t] \cup [4v_t, \infty) \ 1 - rac{|v_x - v_t|}{2v_t}, & ext{otherwise.} \end{cases}$$

Algorithm:

Soft Actor-Critic

Nightmare 2:

Distribution Shift

What happens if your step-size is large?

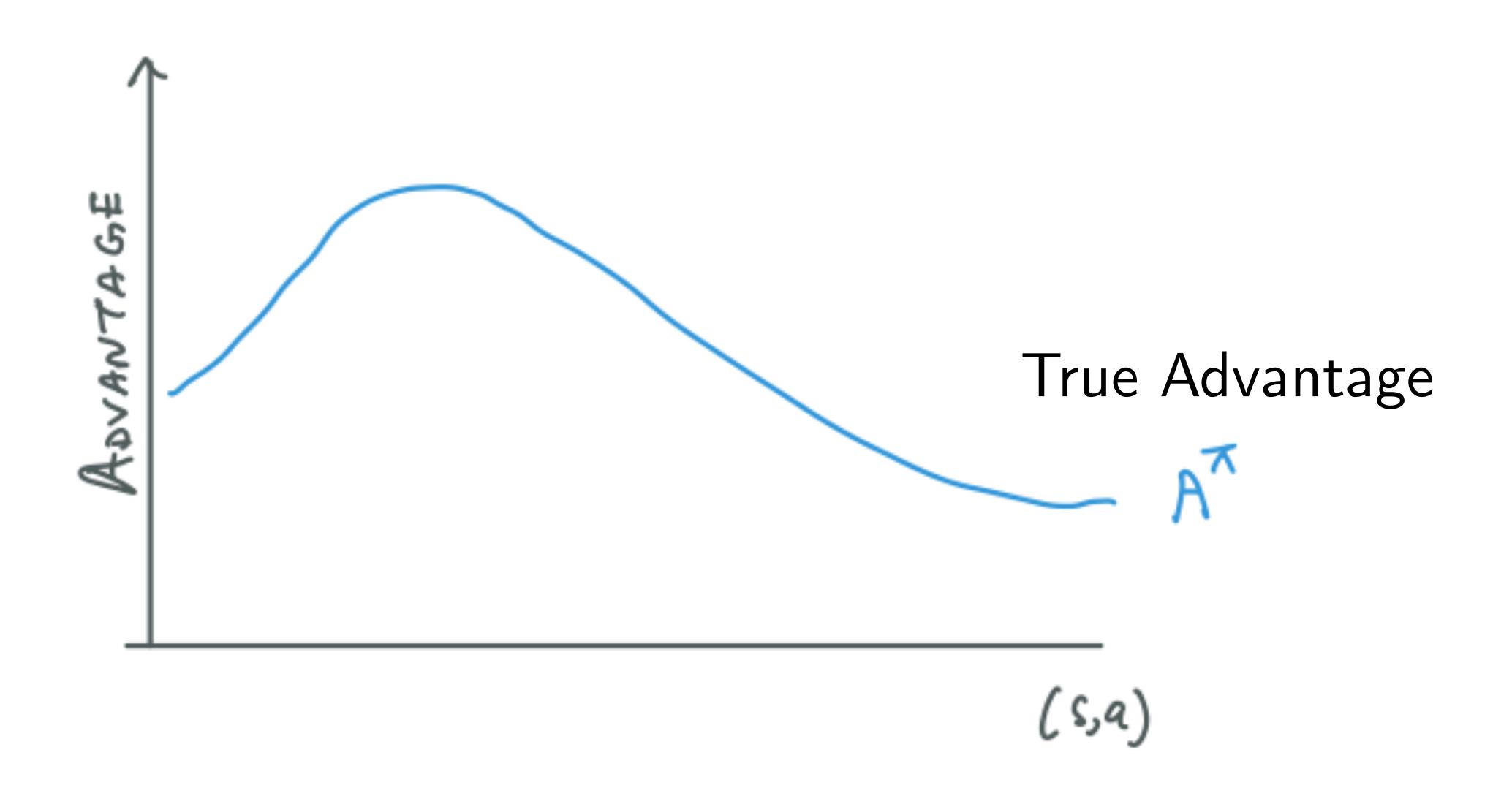
$$\nabla_{\theta} J = E_{d^{\pi_{\theta}}(s)} E_{\pi_{\theta}(a|s)} \left[\nabla_{\theta} \log(\pi_{\theta}(a|s) A^{\pi_{\theta}}(s,a)) \right]$$

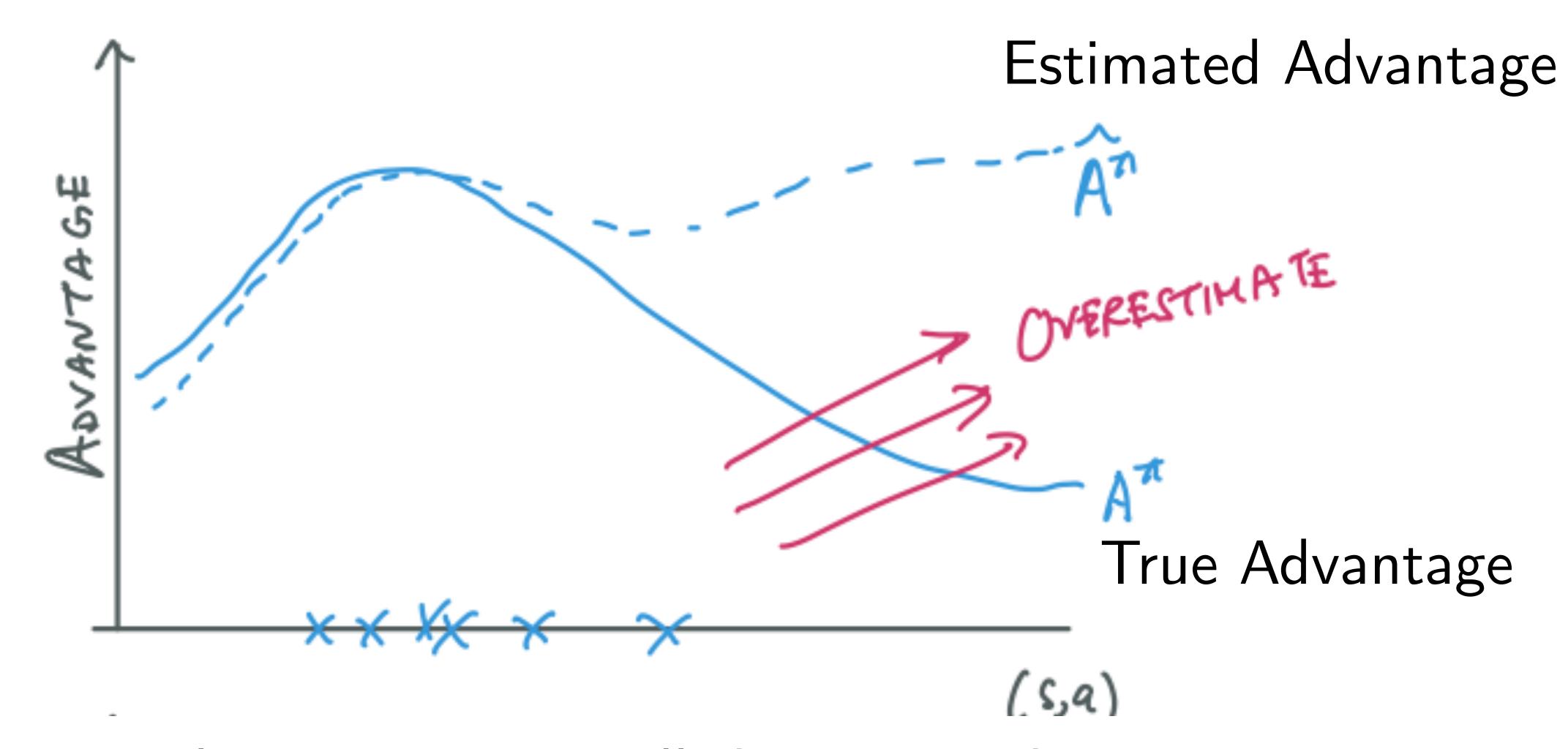
What happens if your step-size is large?

$$abla_{ heta} J = E_{d^{\pi_{ heta}}(s)} E_{\pi_{ heta}(a|s)} \left[\nabla_{\theta} \log(\pi_{\theta}(a|s) A^{\bullet}(s,a)) \right]$$

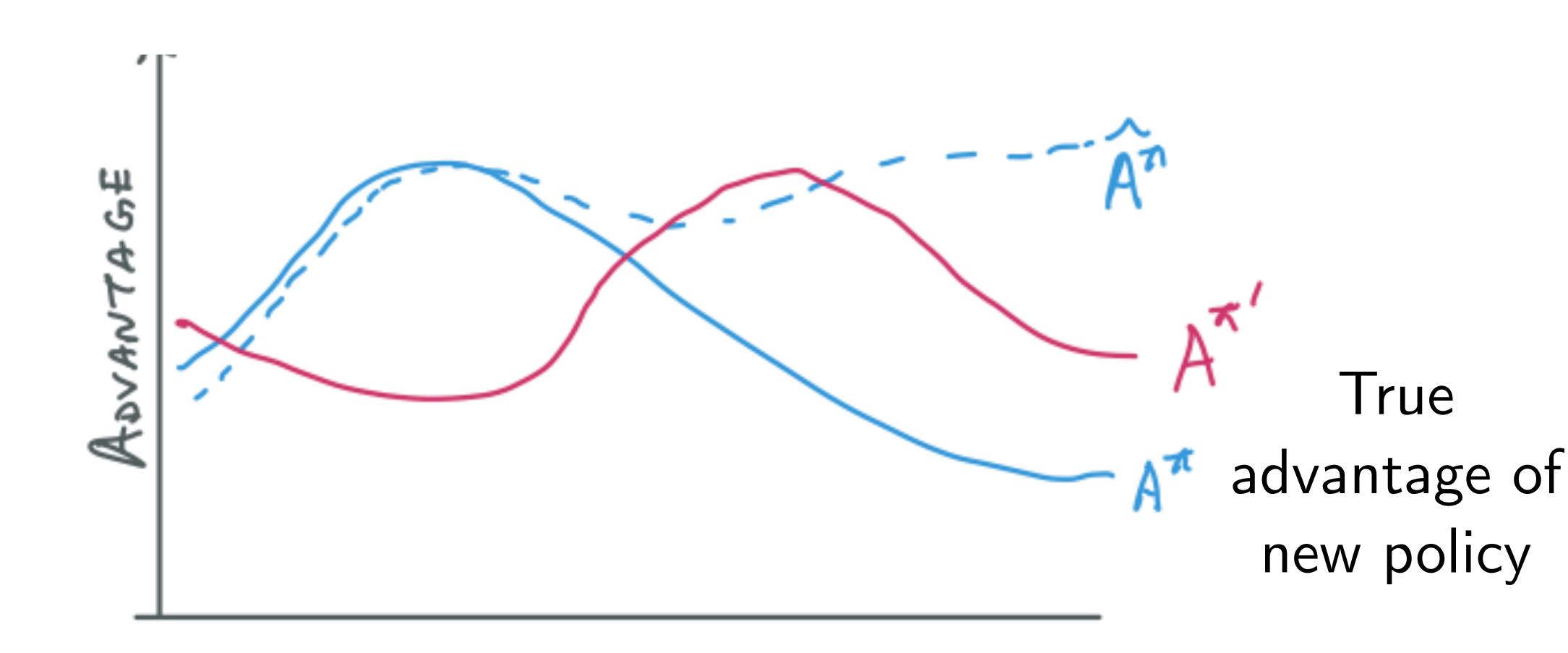
$$\hat{A}^{\pi_{\theta}}(s,a)$$

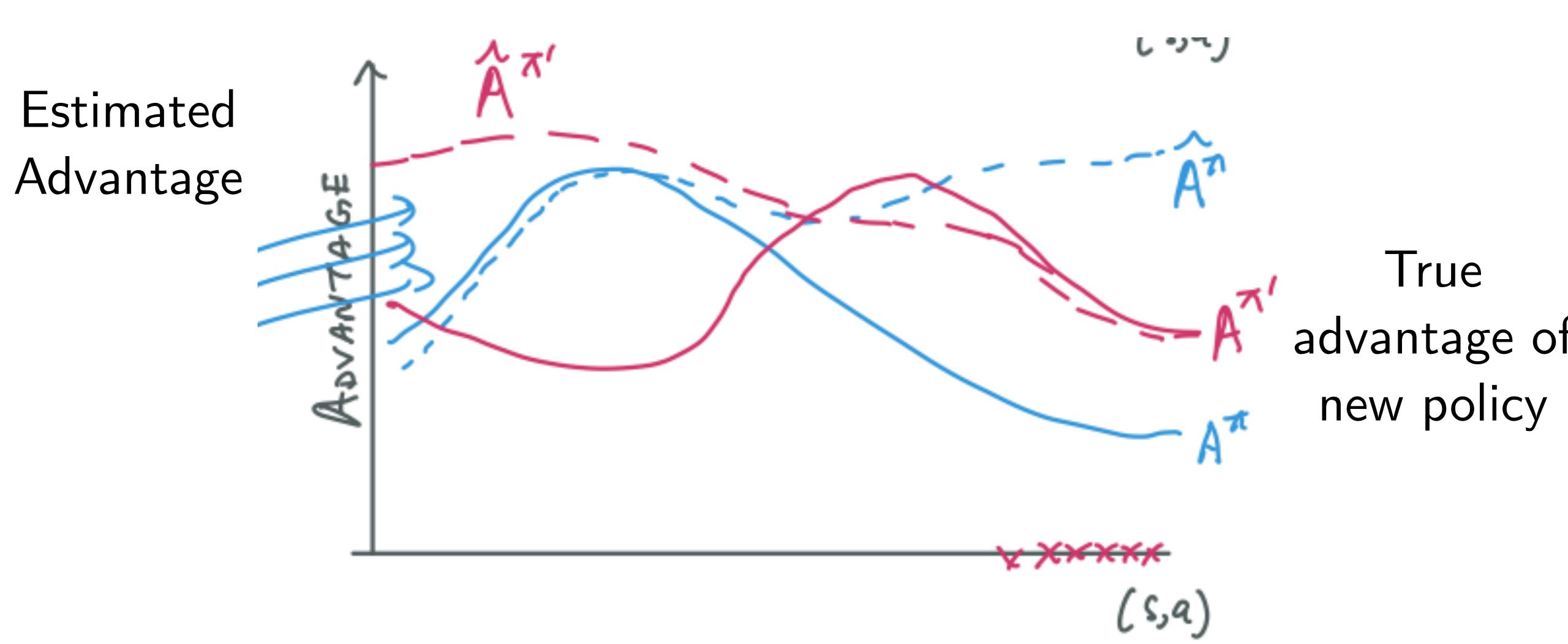
We are estimating the advantage from roll-outs





Our new policy wants to go all the way to the RIGHT





Our new policy wants to go all the way to the LEFT

Recap: Problem with Approximate Policy Iteration

$$V^{\pi^+}(s_0) - V^{\pi}(s_0) = \sum_{t=0}^{T-1} \mathbb{E}_{s_t \sim d_t^{\pi^+}} A^{\pi}(s_t, \pi^+)$$

PDL requires accurate Q^{π}_{θ} on states that π^+ will visit! $(d^{\pi^+}_t)$

But we only have states that π visits (d_t^{π})

If π^+ changes drastically from π , then $|d_t^{\pi^+} - d_t^{\pi}|$ is big!

Be stable

Slowly change policies

Keep $d_t^{\pi^+}$ close to d_t^{π}



Goal: Change distributions slowly

$$\max_{\Delta\theta} J(\theta + \Delta\theta)$$

s.t. $d^{\pi_{\theta+\Delta\theta}}$ is close to $d^{\pi_{\theta}}$

How do we measure distance between distributions?

Goal: Change distributions slowly

$$\max_{\Delta\theta} J(\theta + \Delta\theta)$$

s.t.
$$KL(d^{\pi_{\theta+\Delta\theta}} \mid d^{\pi_{\theta}}) \leq \epsilon$$

Fix #2: Take small steps

Start with an arbitrary initial policy $\pi_{\theta}(a \mid s)$

while not converged do

Roll-out $\pi_{\theta}(a \mid s)$ to collect trajectories $D = \{s^i, a^i, r^i, s^i_+\}_{i=1}^N$

Fit value function $\hat{V}^{\pi_{\theta}}(s^i)$ using TD, i.e. minimize $(r^i + \gamma \hat{V}^{\pi_{\theta}}(s^i) - \hat{V}^{\pi_{\theta}}(s^i))^2$

Compute advantage $\hat{A}^{\pi_{\theta}}(s^i, a^i) = r(s^i, a^i) + \gamma \hat{V}^{\pi_{\theta}}(s^i) - \hat{V}^{\pi_{\theta}}(s^i)$

Compute gradient

$$\nabla_{\theta} J(\theta) = \frac{1}{N} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \, \hat{A}^{\pi_{\theta}}(s^i, a^i) \right] \qquad \text{s.t. } KL(\pi(\theta + \Delta \theta) | | \pi(\theta)) \leq \epsilon$$

Update parameters
$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$$

s.t.
$$KL(\pi(\theta + \Delta\theta) | | \pi(\theta)) \le \epsilon$$

How??

Natural Gradient Descent (rediscovered as TRPO)

Start with an arbitrary initial policy $\pi_{\theta}(a \mid s)$

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Update parameters
$$\theta \leftarrow \theta + \alpha G(\theta)^{-1} \nabla_{\theta} J(\theta)$$

$$\nabla_{\theta} J(\theta) = \frac{1}{N} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \, \hat{A}^{\pi_{\theta}}(s^i, a^i) \right] \qquad \frac{\text{s.t. } KL(\pi(\theta + \Delta \theta) | |\pi(\theta)) \leq c}{\approx \Delta \theta^T G(\theta) \Delta \theta \leq c}$$

 $G(\theta)$ is Fischer Information Matrix

$$G(\theta) = \mathbb{E}_{\pi_{\theta}} \left[\nabla_{\theta} \log \pi_{\theta} \nabla_{\theta} \log \pi_{\theta}^{T} \right]$$

Proximal Policy Optimization (PPO)

Computing Fischer Information matrix is expensive and slow!

Idea: Instead of taking small steps, change the loss function so there is no benefit in taking large steps!

Proximal Policy Optimization (PPO)

Computing Fischer Information matrix is expensive and slow!

Idea: Instead of taking small steps, change the loss function so there is no benefit in taking large steps!

Instead of defining gradient, we will define a surrogate loss function (Lets say we are at iteration k)

$$\mathscr{L}(\theta) = \mathbb{E}_{s,a \sim \pi_{\theta_k}} \left[\frac{\pi_{\theta}}{\pi_{\theta_k}} A^{\pi_{\theta_k}}(s,a) \right]$$

Proximal Policy Optimization (PPO)

Computing Fischer Information matrix is expensive and slow!

Idea: Instead of taking small steps, change the loss function so there is no benefit in taking large steps!

Clip the loss if the policy π_{θ} deviates too much from π_{θ_n}

$$\mathscr{L}(\theta) = \mathbb{E}_{s,a \sim \pi_{\theta_k}} \left[\min \left(\frac{\pi_{\theta}}{\pi_{\theta_k}} A^{\pi_{\theta_k}}(s,a), \operatorname{clip} \left(\frac{\pi_{\theta}}{\pi_{\theta_k}}, 1 - \epsilon, 1 + \epsilon \right) A^{\pi_{\theta_k}}(s,a) \right) \right]_{34}$$

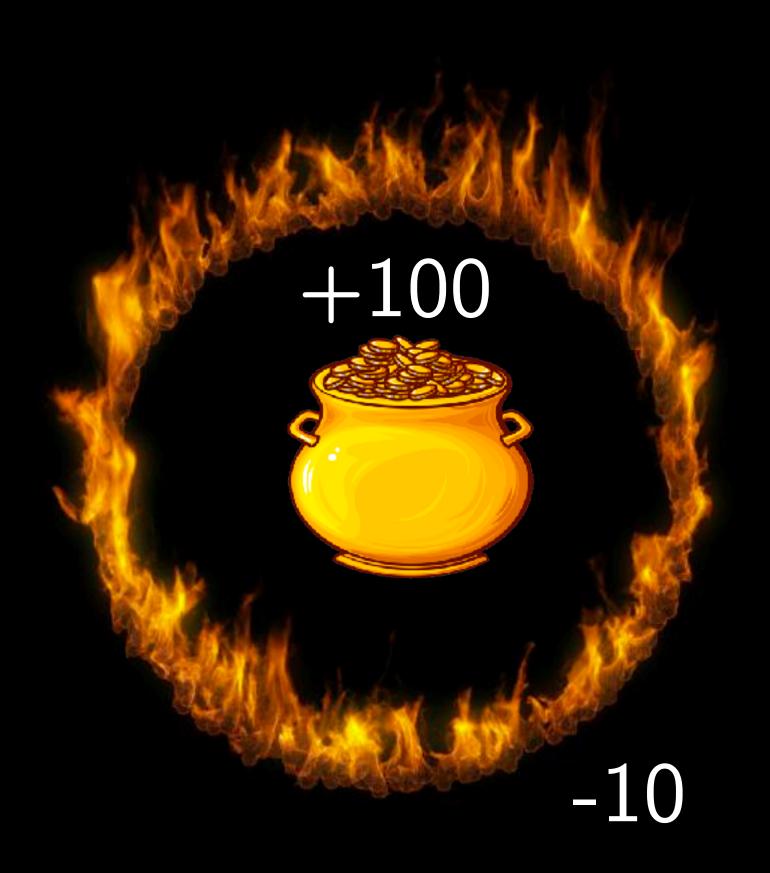
Nightmare 3:

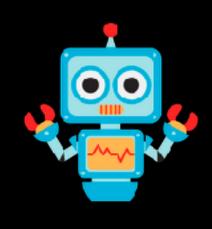
Local Optima

The Ring of Fire

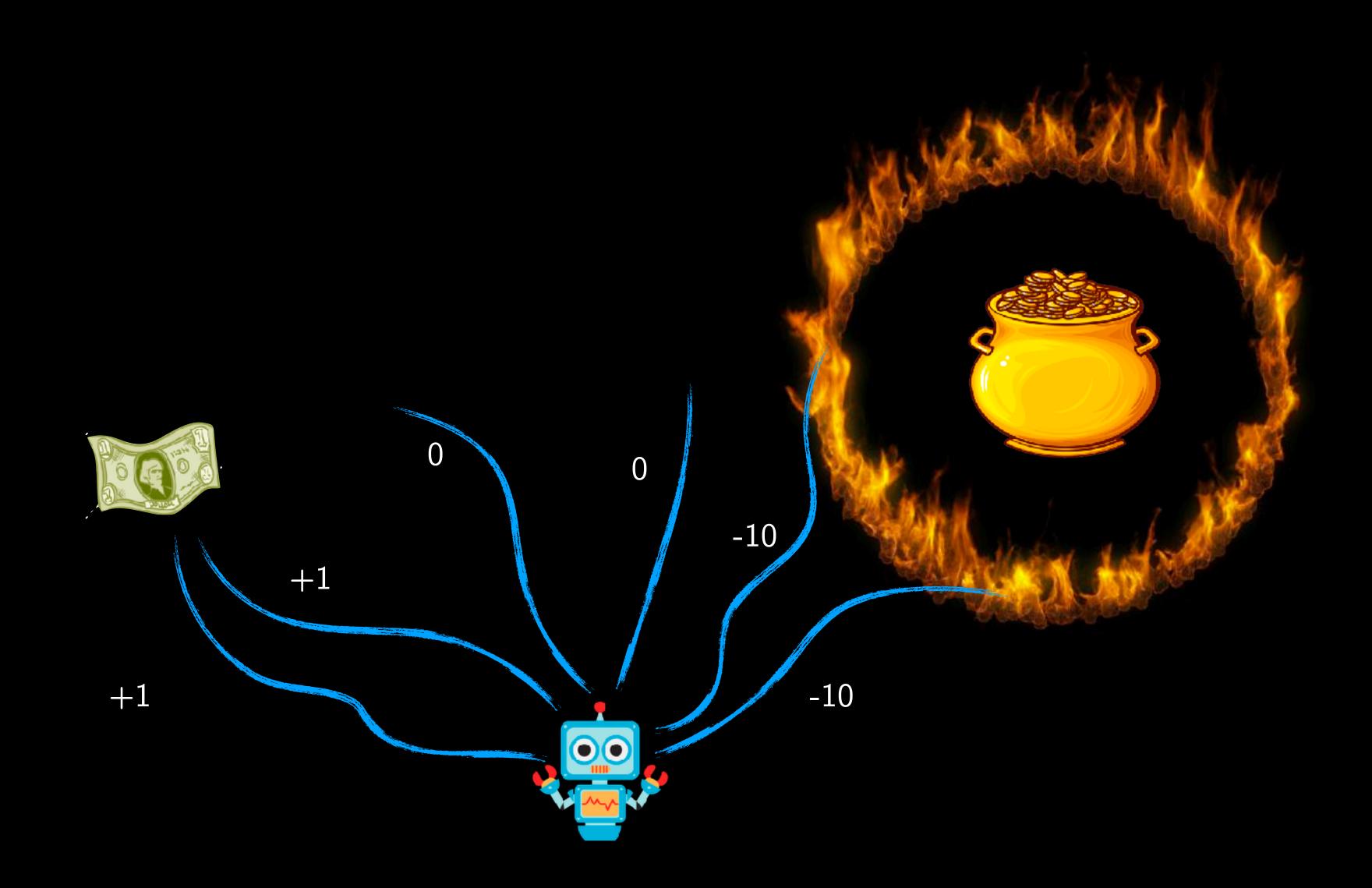
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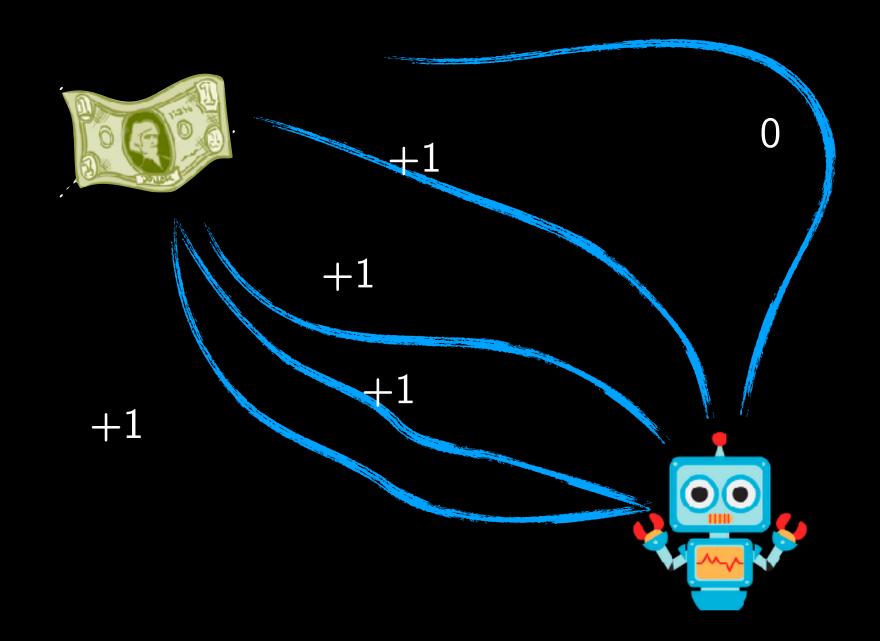


The Ring of Fire



The Ring of Fire

Get's sucked into a local optima!!

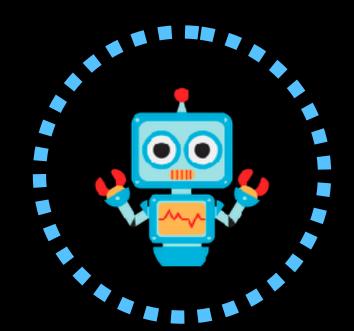


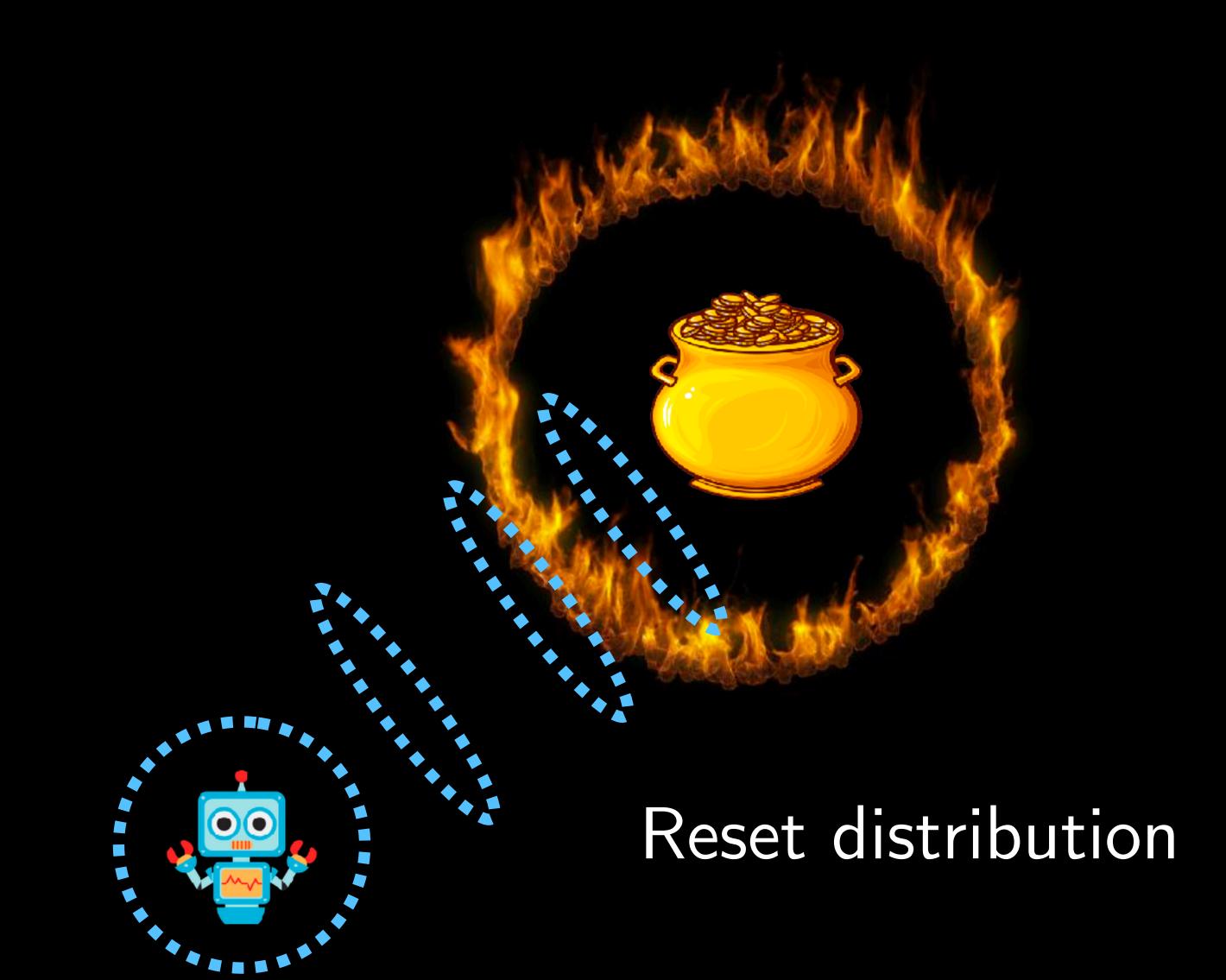






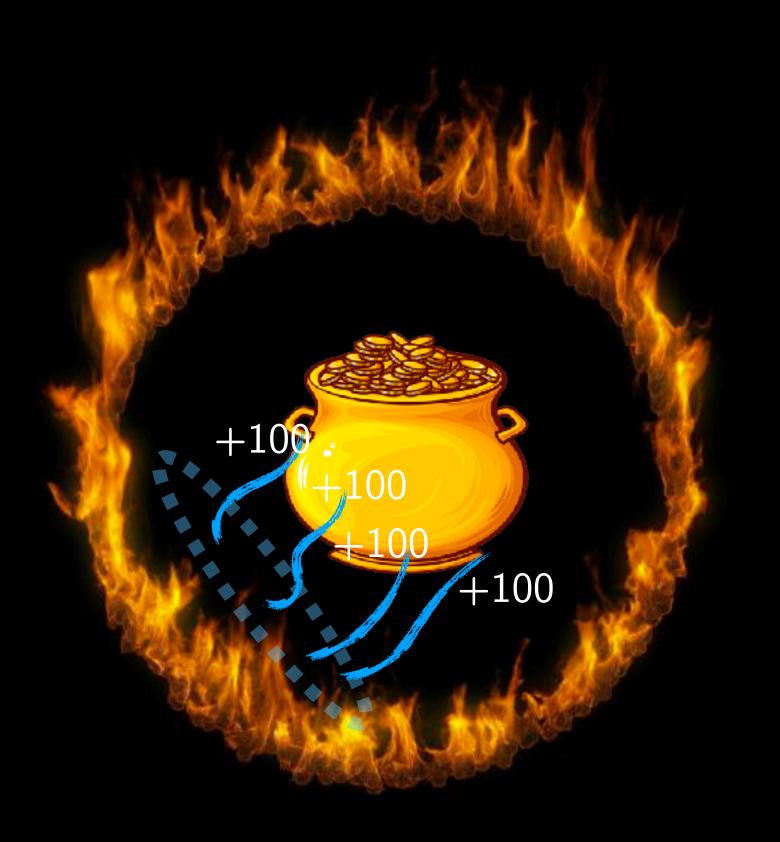


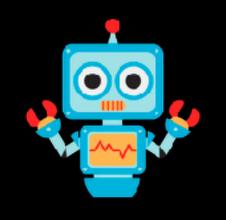






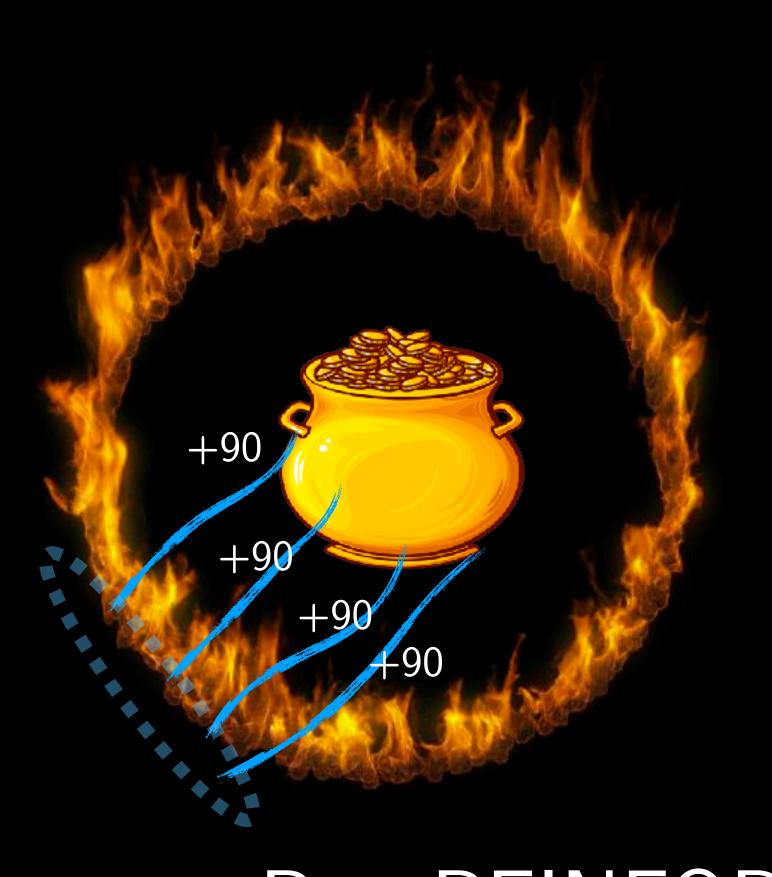


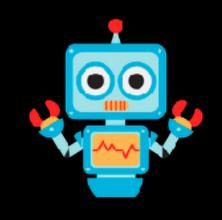




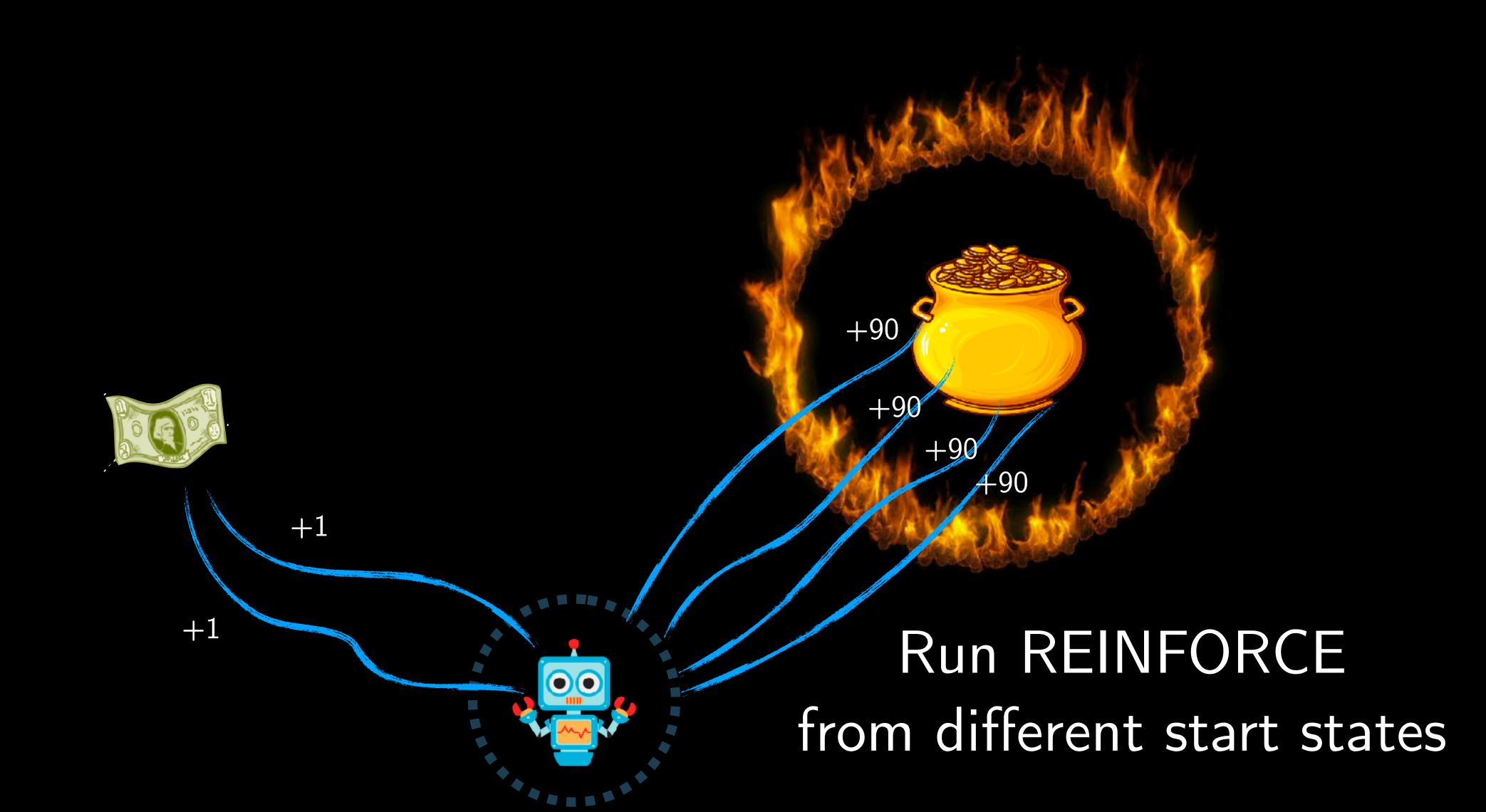
Run REINFORCE from different start states







Run REINFORCE from different start states



Fix #3: Use a reset distribution

Start with an arbitrary initial policy $\pi_{\theta}(a \mid s)$

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Instead of rolling out from the start state, rollout from states expert visits

Compute gradient

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Update parameters $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

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