

Introduction

→ Prime Mover.

- converts any natural energy into mechanical energy.

→ Classification on the basis of energy.

non-thermal

- Hydral
- Tidal
- Wind

thermal

- fuel (H.E.)
- Biogas
- Geothermal
- nuclear
- Solar

Prime mover

H.E (Heat Engine)

TCE (Internal Combustion Engine)

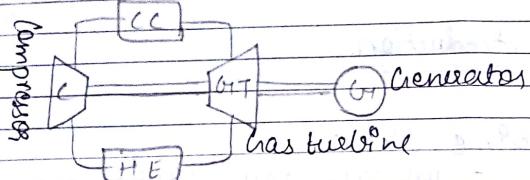
ECE (External Combustion Engine)

TCE
(reciprocating)
piston

Gas turbine
(open)

ST.
(rotatory)
Steam turbine

SE
Steam engine
(reciprocating)
gas turbine
(closed)



Heat Exchange.

→ Forces - A push or a pull applied on an object that affects its state of motion, direction or shape:

$$F = \frac{d(P)}{dt} = \frac{d(mv)}{dt} = m \frac{dv}{dt} = ma$$

Unit = N.

→ Pressure - It is an expression of force exerted on a surface per unit area.

$$P = \frac{F}{A} \quad \text{Unit} \text{z} \text{ N/m}^2$$

$1 \text{ N/m}^2 = 1 \text{ Pa}$. (Standard Unit of pressure.)

Atmospheric pressure is measured by Barometer. ΔP = pressure applied by atm. on the ground!

⇒ Standard atmospheric pressure, P_{atm} .

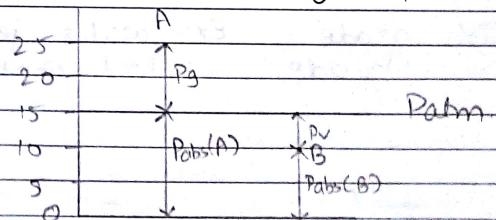
$$P_{atm} = 1.01325 \text{ bar} \\ = 760 \text{ mm of Hg.}$$

$$1 \text{ bar} = 10^5 \text{ Pa} \\ = 10^5 \text{ N/m}^2$$

$P_{atm} < P_g \Rightarrow P_g$ gauge pressure

$P_{atm} > P_v \Rightarrow P_v$ vacuum pressure.

⇒ Absolute pressure (P_{abs}) measured with reference to absolute zero pressure



$$P_{abs}(A) = P_{atm} + P_g$$

$$P_{abs}(B) = P_{atm} - P_v$$

$$\text{Power} \Rightarrow P = \frac{W}{t}, \text{ Unit: J/s}$$

Brake power (BP) - available at final shaft.

Indicated power (IP) - power generated within the cylinder

$$IP - BP = F.P$$

$$\eta = \frac{\text{Output}}{\text{Input}} = \frac{BP}{IP}, 0.$$

Energy is capacity to do work.
Unit: Joule

- High grade ex: water jet
- Low grade. ex: heat, combustion of fuel.

Stored energy

Energy in transmission

Internal Energy

Heat

Temperature

Enthalpy - change of state

Process - critical point

Path - triple point

Cycle

Ques A steam engine piston having an area of 140 cm^2 moves a distance of 160mm inside the cylinder. Find the amount of work done if pressure exerted upon the piston is 80 KN/m^2 is 650 kPa .

\star

$$A = 140 \text{ cm}^2 = 140 \times 10^{-4} \text{ m}^2 \quad W_2 = (?)$$

$$d = 160 \text{ mm} = 160 \times 10^{-3} \text{ m}$$

$$80 \text{ KN/m}^2 \quad 80 \text{ kPa}$$

$$W_1 = F \cdot d$$

$$= P_1 A \cdot d$$

$$= 80 \times 140 \times 10^{-4} \times 160 \times 10^{-3}$$

$$= 0.179 \text{ J}$$

$$650 \text{ kPa}$$

$$W_2 = F \cdot d$$

$$= P_2 A \cdot d$$

$$= 650 \times 140 \times 10^{-4} \times 160 \times 10^{-3}$$

$$= 1.456 \text{ J}$$

Ques

Determine the power developed by the water turbine if it receive 800 kg/sec water per second at the pressure of 2 bar .

\star

$$\frac{m}{t} = 800 \text{ kg/sec}$$

$$\text{Power} = (?)$$

$$P = 2 \times 10^5 \text{ Pa.}$$

$$\text{Power} = \frac{\omega}{t} \cdot F.d$$

$$= \frac{F \cdot d \cdot A}{A}$$

$$= P \cdot V$$

$$= 8 \times 10^5 \times 0.8$$

$$= 1.6 \times 10^5$$

$$= 160 \times 10^6 \text{ W}$$

$$V \cdot d \cdot A$$

$$\text{Power} = 160 \text{ kW}$$

Ques

In a water turbine, water is supplied at the rate 500 lit/sec under head of 20m it is discharge from the turbine at a velocity of 8 m/sec. Determine the power developed by the turbine.

$$m = 500 \text{ lit/sec.}$$

$$V = 8 \text{ m/sec}$$

$$g = 9.81 \text{ m/s}^2$$

$$h = 20 \text{ m}$$

$$\text{Power} = ?$$

$$P.E = mgh$$

$$= 500 \times 9.81 \times 20$$

$$= 98100 \text{ J}$$

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$$K.E = \frac{1}{2} m v^2 = \frac{1}{2} \times 500 \times 4 = 1000 \text{ J}$$

$$P.E - K.E = 98100 - 1000 \\ = 97100$$

$$P = 97100 \text{ Watt} \\ = 97.1 \text{ kW}$$

Ques

Steel having mass of 20 kg and the specific heat of 460 J/kg K is heated from 35°C - 150°C. Determine the heat required.

Ans

$$m = 20 \text{ kg}$$

$$T_1 = 35^\circ\text{C} = 308 \text{ K}$$

$$T_2 = 150^\circ\text{C} = 423 \text{ K}$$

$$c = 460 \text{ J/kg K}$$

$$Q = mc \Delta t$$

$$= mc (t_2 - t_1)$$

$$= 20 \times 460 \times (423 - 308)$$

$$= 20 \times 460 \times 115$$

$$= 1058000 \text{ J}$$

$$= 1058 \text{ kJ}$$

Specific Heat :- Amount of heat per unit mass required to raise the temperature by one degree Celsius

Ques 3000 m³ of water is to be delivered in 50 min to a vertical piston of 20 m. Find the power required. Neglect friction and other losses.

$$V = 3000 \text{ m}^3$$

$$h = 20 \text{ m}$$

$$t = 50 \text{ min}$$

$$\frac{P_2 w}{t} \rightarrow \frac{F \cdot d}{t}$$

$$F = mg \approx 3000 \times 10^3 \times 9.81$$

$$P_2 = \frac{3000 \times 10^3 \times 9.81 \times 20}{3000}$$

$$P_2 = 196.2 \text{ kW}$$

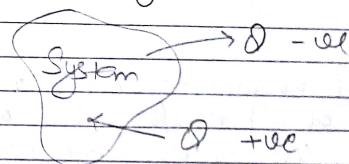
H System: region of a fixed quantity within space

Open System: mass, energy both can exchange etc.

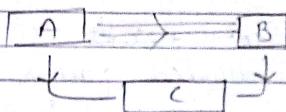
Closed System: energy can exchange

Isolated: system that cannot exchange either energy or matter outside the boundaries of the system.

An isolated system differs from a closed system by the transfer of energy. Closed systems are only closed to matter, energy can be exchanged across the system's boundaries.



Zeroth law: If two systems are in thermodynamic equilibrium with a third system, the two original systems are in thermal equilibrium with each other.



First Law - The total energy of an isolated system is constant; Energy can be transformed from one form to another, but can be neither created nor destroyed.

$$\eta_{th} = \frac{35 \times 10^3}{1.194 \times 10^5} = 29.3\%$$

Ques A gas in a cylinder is at the pressure of 9 bar. It is expanded at a constant pressure from $0.5 \rightarrow 1.8 \text{ m}^3$. Determine the work done.

$$P_1 = 9 \text{ bar}, \quad V_1 = 0.5 \rightarrow 1.8 \text{ m}^3$$

$$\begin{aligned} W &\geq P \Delta V \\ &\geq P(V_2 - V_1) \\ &\geq 9 \times 10^5 (1.8 - 0.5) \\ &\geq 11.4 \times 10^5 \end{aligned}$$

Ques A diesel engine consumes a fuel at the rate of 10 kg/h . The engine is developed in 55 kW power. Calorific value of fuel is 43 MJ/kg . Calculate thermal efficiency.

$$\eta_{th} = \frac{\text{Output power}}{\text{Input power}}$$

= Break power
Indicated power.

$$I.P = m \times C.V$$

$$= \frac{10}{3600} \times 43 \times 10^6 = 0.1194 \times 10^6$$

$$= 1.194 \times 10^5$$

Ques To pump 200 kg of water in a boiler $150 \times 10^3 \text{ Nm}$ of work is required. Find the pressure in the boiler.

$$\begin{aligned} M &= 200 \text{ kg} & 1 \text{ m}^3 &= 1000 \text{ lit} \\ W &= 150 \times 10^3 \text{ nm} & 1 \text{ lit} &= 1 \text{ kg} \end{aligned}$$

$$\begin{aligned} W &\geq F.d \\ &\geq F \cdot d \cdot f \\ &\geq \frac{F \cdot d \cdot f}{A} \end{aligned}$$

$$\begin{aligned} &\geq PAV \\ &\geq (1) \geq 200 \text{ kg} \\ &\geq 200 \text{ lit} \end{aligned}$$

$$\begin{aligned} 1 \text{ m}^3 &= 1000 \text{ lit} \\ (1) &= 2000 \text{ lit} \end{aligned}$$

$$150 \times 10^3, P \times 0.2$$

$$P_2 = 750 \times 10^3, \text{ MPa}$$

Ques In a compressor work done on the air 150 kJ, the heat rejected to the surrounding is 60 kJ. Find the change in internal energy.

$$\begin{aligned} Q_2 &= U + W \\ Q_2 - W &= U \\ -150 + 60 &= U \end{aligned}$$

$$U = 90 \text{ kJ}$$

Ques 10 kg of air at 90°C is heated at constant pressure then at constant volume to final temperature 300°C if 1800 kJ of heat is supplied. Find the temperature at the end of constant pressure may be $C_p = 1.005 \text{ kJ/kg K}$, $C_v = 0.715 \text{ kJ/kg K}$.

$$\begin{aligned} C_p &= 1.005 \text{ kJ/kg K} \\ C_v &= 0.715 \text{ kJ/kg K} \\ m &= 10 \text{ kg} \\ Q &= 1800 \text{ kJ} \end{aligned}$$

$$90^\circ\text{C} \xrightarrow[1]{P \rightarrow C} t_2 \xrightarrow[2]{V \rightarrow C} 300^\circ\text{C}$$

$$\Delta Q = mc \Delta t + mC_v \Delta t$$

$$Q_2 = m(C_p(t_2 - t_1) + C_v(V_3 - V_2))$$

$$Q_2 = 10 \times 1.005(t_2 - 363) + 10 \times 0.715(573 - t_2)$$

$$Q_2 = 10[1.005t_2 - 364.875 + 409.695 - 0.715t_2]$$

$$Q_2 = 10[0.29t_2 + 44.88]$$

$$Q_2 =$$

$$1800 = 2.9t_2 + 448.8$$

$$1800 - 448.8 = 2t_2$$

$$2.9$$

$$t_2 = 192$$

Ques In a cyclic process there are four heat transfer process which are as under
 $Q_{12} = 92.5 \text{ kJ}$
 $Q_{23} = -110 \text{ kJ}$
 $Q_{34} = -770 \text{ kJ}$
 $Q_{41} = 220 \text{ kJ}$

The work done during the process

$$W_{12} = 40 \text{ kJ}$$

$$W_{23} = -50 \text{ kJ}$$

$$W_{34} = 170 \text{ kJ}$$

$W_{41} = ?$. Calculate work done during process (34) find out the change in internal energy during cyclic process.

$$\begin{aligned} Q - W &= 0 \\ Q &= W \\ \oint Q &= \oint W \end{aligned}$$

$$Q_{12} + Q_{23} + Q_{34} + Q_{41}, \quad W_{12} + W_{23} + W_{34} + W_{41}$$

$$q_{23} = -110 - 110 + 220 = 70 - 50 + W_{34} + 170$$

$$W_{34} = 265 - 40 + 50 - 170 \\ = 75$$

$$Q_{12} = U_{12} + W_{12}$$

$$U_{12} = q_{12} - w_{12} = 865$$

$$U_{23} = -110 + 50 = -60$$

$$U_{34} = -170 + 75 = -845$$

$$U_{41} = 220 - 170 = 50$$

$$\Delta U = U_{12} + U_{23} + U_{34} + U_{41} \\ = 865 - 60 - 845 + 50 \\ = 0$$

Ques
In a compression process 3 kJ of mechanical work is supplied. If 5 kJ of working substance, the heat rejected to the cooling jacket 700 J. Calculate the specific internal energy.

A
Work done on the system $\Rightarrow W_2 = 3 \text{ kJ}$
 $m = 5 \text{ kg}$
heat is rejected $\therefore Q_2 = -700 \text{ J}$

$$W_2 = 3 \times 10^3 \text{ J}$$

$$Q_2 = -700 \text{ J}$$

$$\begin{aligned} Q_2 &= U + W \\ U_2 &= Q_2 - W \\ &= -700 + 3 \times 10^3 \\ &= 2300 \\ &= 2.3 \text{ kJ} \end{aligned}$$

Specific internal energy $\Rightarrow \frac{U}{m}$

$$= \frac{2.3 \times 10^3}{5}$$

$$= 0.46$$

$$= 460 \text{ J}$$

Ques
A gas enters in a system at an initial pressure of 0.1 MPa and flow rate of 0.15 m³/s leaves the system at the pressure of 0.95 MPa and flow rate 0.09 m³/sec. during the process change in enthalpy is 23 kJ/sec calculate the change in enthalpy.

$$\begin{aligned}
 \Delta H &= \Delta U + \Delta PV \\
 &= (U_2 + P_2 V_2) - (U_1 + P_1 V_1) \\
 &= U_2 - U_1 + P_2 V_2 - P_1 V_1 \\
 &= 22 + 0.5 \times 0.15 \times 10^6 - 0.45 \times 10^6 \times 0.09 \\
 &= 22 + 10^6 (0.075 - 0.085) \\
 &= 22 \times 10^3 + 0.1605 \times 10^6 \\
 &= 22 \times 10^3 + 10.5 \times 10^3 \\
 &= 32.5 \times 10^3 \\
 &= 32.5 \text{ kJ}
 \end{aligned}$$

Properties of Gases

Perfect or Ideal Gas.

- The gas in which property remains unchanged when temperature and pressure changes.
- The gas which obeys Charles law, Boyle's law and Gay Lussac law is called ideal gas.
(Real gases doesn't obey these laws).
- Every real gas if subjected to min. P and max. T behaves like perfect gas.

41 Boyle's law ($T = c$)

$$V \propto \frac{1}{P_{\text{abs}}}$$

$$V_2 = \frac{C}{P}$$

$$PV_2 = C$$

$$P_1 V_1 = P_2 V_2$$

Charles Law ($P=c$)

$$\nabla \propto T_{\text{abs}}$$

$$N_2 \propto T$$

$$\frac{\nabla}{T} = c$$

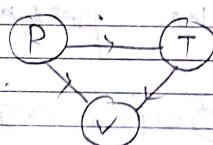
$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

Gay-Lussac's Law ($V=c$)

$$P \propto T_{\text{abs}}$$

$$P_2 \propto T$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$



Combined Gas Law

$$\nabla \propto \frac{1}{P} \quad (\text{Boyle's Law})$$

$$\nabla \propto T \quad (\text{Charles Law})$$

$$\Rightarrow \nabla \propto \frac{T}{P}$$

$$PV = RT \quad (R = \text{specific gas constant})$$

or characteristic gas constant

$$V = \frac{V}{m} \quad (\text{specific volume})$$

$$PV = mRT$$

$$R = 287 \text{ J/kg K} \quad (\text{Air})$$

$$R_o = mR$$

$$M = \text{molecular mass}$$

$$R = \frac{J}{\text{kg K}}$$

$$R_o = \frac{J}{\text{mol K}}$$

$$PV = MRT$$

$$PV = R_o T$$

$$R_o = 8.314 \times 10^3$$

NTP

T₂ 25°C

P₂ 1 bar

STP

T₁ 0°C

P₁ 1 bar

$$1 \text{ bar} = 1.01325 \times 10^5 \text{ Pa.}$$

$$\cdot PV_2 = P_0 T$$

$$V_2 = \frac{P_0 T}{P} = \frac{8.314 \times 10^3 \times 273}{1.01325 \times 10^5}$$

$$= 22.4 \text{ liter} = \frac{\text{m}^3}{\text{mol}}$$

$$1 \text{ liter} = 1 \text{ m}^3$$

Relation b/w C_p & C_v .

O₂ U+w (Ind law of Thermodynamics)

$$mc_p(t_2 - t_1) = mc_v(t_2 - t_1) + P(V_2 - V_1)$$

$$mC_p(t_2 - t_1) = mC_v(t_2 - t_1) + mR(t_2 - t_1)$$

$$C_p = C_v + R$$

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$$C_p - C_v = R$$

Meyer's Eqn ↑

Dividing above eqn by C_v

$$\frac{C_p}{C_v} - 1 = \frac{R}{C_v}$$

$$\frac{C_p}{C_v} - 1 = \frac{R}{C_v}$$

$$\gamma = 1 + \frac{R}{C_v} \quad [C_p = \gamma C_v]$$

$$C_v = \frac{R}{\gamma - 1} \quad \text{g_2 adiabatic index.}$$

$$= \frac{0.887}{1.4 - 1}$$

$\gamma = 1.67$ (monatomic)
 $= 1.4$ (diatomic)
 $= 1.33$ (polyatomic)

$$[C_v = 0.715]$$

$$[C_p = 1.00]$$

flow and Non-flow processes

⇒ Flow processes

- applicable to open system
- mass can flow from system to surrounding & vice-versa

⇒ Non-flow processes

- applicable to closed system
- mass cannot flow

⇒ types of non-flow processes.

i) $V = C$ (isochoric)

ii) $P = C$ (isobaric)

iii) $T = C$ (isothermal)

v) reversible adiabatic (isentropic)
 $\delta Q = 0$, entropy = C_{S}

v) polytropic

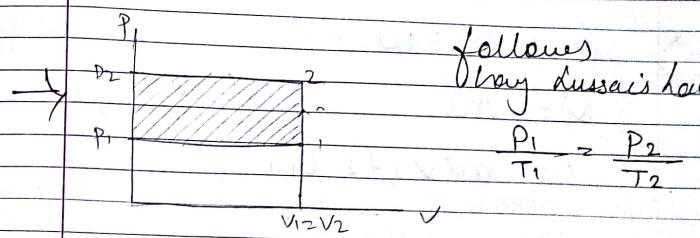
$$PV^{\gamma} = C$$

⇒ constant Volume Process.

($N = C$)

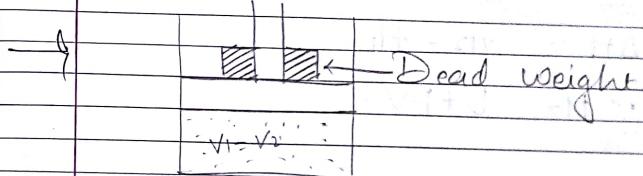
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follows
Davy Russel's law

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$



→ work done, W

$$W = P \Delta V$$

$$\rightarrow P(V_2 - V_1)$$

$$[W > 0]$$

→ Internal Energy, A_u .

$$\Delta U = mcv \Delta t$$

$$\rightarrow mcv(t_2 - t_1)$$

$$\rightarrow Q = \Delta U + W$$

$$Q = \Delta U \quad [W=0]$$

$$\rightarrow Q = mc_v(t_2 - t_1)$$

~~heat supplied at const Volume~~

$$\rightarrow \Delta H = H_2 - H_1$$

$$\therefore H_2 = U + PV.$$

$$\Rightarrow \Delta H_2 = (U_2 + P_2 V_2) - (U_1 + P_1 V_1)$$

$$= (U_2 - U_1) + (P_2 V_2 - P_1 V_1)$$

$$= \Delta U + V(P_2 - P_1)$$

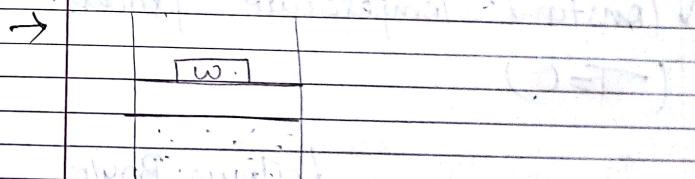
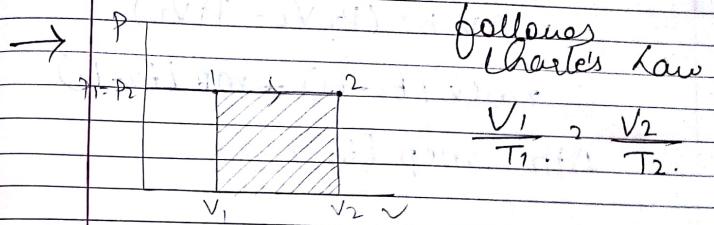
$$\Rightarrow mc_v(t_2 - t_1) + mR(t_2 - t_1)$$

$$= mcv(t_2 - t_1) + mR(t_2 - t_1)$$

$$= mR(t_2 - t_1)(v + R)$$

$$\boxed{\Delta H_2 = mC_p(t_2 - t_1)}$$

ii) Constant pressure process.
($P=c$)



$$\rightarrow \text{Work done, } W = P(V_2 - V_1)$$

$$W = mR(t_2 - t_1)$$

$$\rightarrow \Delta U = mc_v(t_2 - t_1)$$

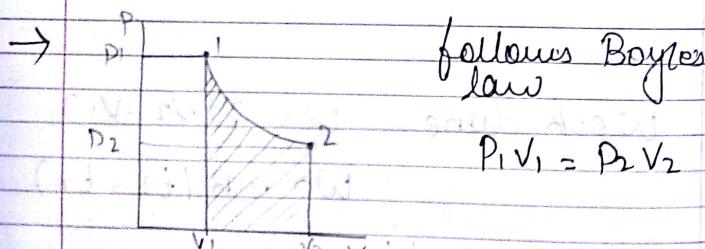
$$\rightarrow Q_2 = U + W$$

$$= mcv(t_2 - t_1) + mR(t_2 - t_1)$$

$$Q_2 = mC_p(t_2 - t_1)$$

$\rightarrow \Delta H_2 = H_2 - H_1$
 $= (U_2 + P_2 V_2) - (U_1 + P_1 V_1)$
 $\Rightarrow \Delta U + (P_2 V_2 - P_1 V_1)$
 $\Rightarrow mcv(t_2 - t_1) + mR(t_2 - t_1)$
 $\Delta H_2 = mcp(t_2 - t_1)$

III) Constant Temperature Process.
 $(T = C)$



$W_2 = \int_1^2 P dV = \int_1^2 \frac{C}{V} dV = C \left[\ln V \right]_1^2 = C [\ln V_2 - \ln V_1] = C \ln \frac{V_2}{V_1}$
 $\Rightarrow P_1 V_1 \ln \frac{V_2}{V_1} = P_2 V_2 \ln \frac{V_2}{V_1}$
 $\Rightarrow mRT_1 \ln \frac{V_2}{V_1} = mRT_2 \ln \frac{V_2}{V_1}$
 $\Rightarrow mRT_1 \ln \frac{P_1}{P_2} = mRT_2 \ln \frac{P_1}{P_2}$
 $\Rightarrow P_1 V_1 \ln \frac{P_1}{P_2} = P_2 V_2 \ln \frac{P_1}{P_2}$

$$\rightarrow U_2 = mcv(t_2 - t_1)$$

$$= 0$$

$$\rightarrow Q_2 = U + W$$

$$= W$$

$$\rightarrow \Delta H_2 = mc_p(t_2 - t_1)$$

$$= 0$$

W) Adiabatic Process (Isentropic)
(Q=0)

$$dQ = du + dw = 0$$

$$\therefore du = mcv dt$$

$$\Rightarrow (cv dt + P dv) = 0 \quad [m_2 \text{ kg}]$$

$$Pv^r = R t$$

$$Pdv + Vdp = Rdt$$

$$dt = \frac{Pdv + Vdp}{R}$$

$$cv \left[\frac{Pdv + Vdp}{R} \right] + Pdv = 0$$

$$cv Pdv + cv Vdp + c_p Pdv - w Pdv = 0$$

$$\frac{cv Vdp}{Pv cv} + \frac{c_p Pdv}{Pv cv} = 0$$

$$\frac{dp}{P} + \gamma \frac{dv}{v} = 0$$

$$\ln P + \gamma \ln v = \ln C$$

$$\ln P + \ln v^\gamma = \ln C$$

$$\ln P v^{\gamma} = \ln C$$

$$[Pv^{\gamma} = C]$$

Adiabatic Law

$$\frac{P_1}{P_2} = \left(\frac{V_2}{V_1} \right)^\gamma$$

$$\frac{P_1}{P_2} = \frac{T_1}{T_2} = \frac{V_2}{V_1}$$

$$\frac{T_1}{T_2} = \left(\frac{V_2}{V_1} \right)^{\gamma-1} \Rightarrow \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} = \frac{T_2}{T_1}$$

$$\Rightarrow W_2 = \int_1^2 P dV$$

$$= \frac{C}{V^\gamma} \cdot dV \quad [PV^\gamma = C \Rightarrow P_2 \frac{C}{V^\gamma}]$$

$$= C \int_1^2 \frac{1}{V^\gamma} dV$$

$$= C \int_1^2 V^{-\gamma} dV$$

$$= C \left[\frac{V^{\gamma+1}}{-\gamma+1} \right]_1^2$$

$$W_2 = \frac{C}{1-\gamma} \left[V_2^{-\gamma+1} - V_1^{-\gamma+1} \right]$$

$$= \frac{C}{1-\gamma} \left[V_2^{-\gamma+1} - V_1^{-\gamma+1} \right]$$

$$= \frac{1}{1-\gamma} \left[C V_2^{-\gamma+1} - C V_1^{-\gamma+1} \right]$$

$$= \frac{1}{1-\gamma} \left[P_2 V_2^{\gamma-1} - P_1 V_1^{\gamma-1} \right]$$

$$= \frac{1}{1-\gamma} \left[P_2 V_2 - P_1 V_1 \right]$$

$$W_2 = \frac{P_2 V_2 - P_1 V_1}{\gamma-1}$$

$$W = \frac{m R (t_1 - t_2)}{\gamma-1}$$

$$W = m C_v (t_1 - t_2)$$

$$\because C_p = C_v \frac{R}{C_v}$$

$$C_v = \frac{R}{\gamma-1}$$

$$\rightarrow \Delta U_2 = mC_V(t_2 - t_1)$$

$$\rightarrow Q_2 = U + \omega$$

$$Q_2 = U + W$$

$$U_2 = -W$$

$$\rightarrow \Delta H_2 = mC_p(t_2 - t_1)$$

Q A tank contains 3m^3 air at 25 bar, pressure. This air is pulled until its pressure and temp. decreases to 15 bar and 21°C . Determine change in internal energy, change in enthalpy and heat transfer. Take $C_p = 1.005 \text{ kJ/kgK}$ and $C_v = 0.718 \text{ kJ/kgK}$.

$$V_1 = 3\text{m}^3 \quad P_2 = 15 \text{ bar}, \\ P_1 = 25 \text{ bar}, \quad T_2 = 21^\circ\text{C}$$

$$C_p = 1.005 \text{ kJ/kgK} \\ C_v = 0.718 \text{ kJ/kgK}$$

$$\therefore \Delta U = ? \\ \therefore \Delta H = ? \\ \therefore Q = ?$$

Q) 1 kg of air at 7 bar pressure and temp. 90°C undergoes polytropic process. The law of expansion is $PV^{1.1} = C$. The pressure falls to 1.4 bar. Calculate final temp., work done, change in internal energy, heat exchange. Take $R = 287 \text{ J/kg K}$, $\gamma = 1.4$ for air.

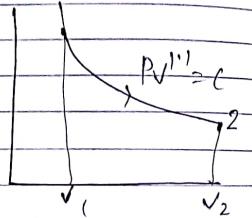
$$n = 1.4$$

$$m = 1 \text{ kg}$$

$$P_1 = 7 \text{ bar}$$

$$T_1 = 90^\circ\text{C}$$

$$P_2 = 1.4 \text{ bar}$$



$$\text{As } PV^{1.1} = C$$

law of expansion
 $V_1 < V_2$

$$PV^n = C \Rightarrow n = 1.1$$

$$\Rightarrow \frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}}$$

$$T_2 = (90 + 273) \left(\frac{1.4}{7}\right)^{\frac{1.1-1}{1.1}}$$

$$T_2 = 313.6 \text{ K}$$

$$W = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$= mR(t_2 - t_1)$$

$$= (1)(287) \left[\frac{(90+273) - (313.6)}{1.1-1} \right]^{363}$$

$$W = 141.8 \text{ KJ}$$

$$\Delta U = m c_v (t_2 - t_1)$$

$$= 1 \times (0.718) (313.6 - 363)$$

$$\Delta U = -35.47 \text{ KJ}$$

$$\Delta U = \left(\frac{\gamma-n}{\gamma-1}\right) \times W$$

$$\text{or } \Delta U = U + W \\ = -35.47 + 141.8$$

$$= \left(\frac{1.4 - 1.1}{1.4 - 1}\right) \times 141.8$$

$$\Delta U = 106.33 \text{ KJ}$$

$$\Delta U = 106.35 \text{ KJ}$$

Q A balloon of spherical shape have 6 m in diameter filled with hydrogen gas at a pressure of 1 bar and temperature of 20°C . At the later time pressure of gas is 94% of initial pressure at same temperature.

1) What mass of original gas must have escaped if dimension of balloon is not changed?

ii) Find the amount of heat to be removed for the same condition if volume is constant.

Take molecular weight of hydrogen 2 kg/mol, specific heat at constant volume, $C_V = 10400 \text{ J/kg K}$.

$$M = 2 \text{ kg/mol}$$

$$C_V = 10400 \text{ J/kg K}$$

$$D = 6 \text{ m}$$

$$P_1 = 1 \text{ bar}$$

$$T_1 = 20^\circ\text{C}$$

$$P_2 = 94\% \text{ of } P_1 \\ = 0.94 P_1$$

$$\frac{4}{3} \pi r^3, V$$

$$V = \frac{4}{3} \pi r^3$$

$$= 113.04 \text{ m}^3$$

$$P_1 V_1 = m_1 R T_1$$

$$P_2 V_2 = m_2 R T_2$$

$$-\textcircled{1}$$

$$-\textcircled{2}$$

$$\text{mass} \quad \text{made}$$

$$P_1 V_1 - P_2 V_2 = (m_1 - m_2) R T$$