UNIT I: NUMERICALS

Q1. A substance with face-centered cubic lattice has density 6250 kg/m^3 and molecular weight 60.2. Calculate the lattice constant a and the atomic radius r. Given Avogadro number $N = 6.02 \times 10^{26} \text{ (kg.mole)}^{-1}$.

Hints:
$$[a = \left(\frac{nM}{N\rho}\right)^{1/3}$$
, $a = \frac{4R}{\sqrt{2}}]$ [Ans: $a = 4 \times 10^{-10} \text{ m}$, $r = 1.414 \times 10^{-10} \text{ m}$].

Q2. NaCl crystals have an fcc crystal structure. The density of NaCl is $2.18 \times 10^3 \text{ kg/m}^3$, the atomic weight of Na is 23 and that of Cl is 35.5. Find the lattice constant. Given Avogadro number $N = 6.02 \times 10^{23} \text{ mole}^{-1}$.

Hints:
$$a = \left(\frac{nM}{N\rho}\right)^{1/3}$$
 [Ans: 5.63 Å].

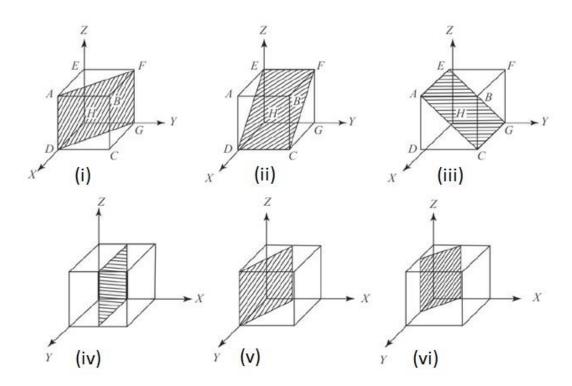
Q3. Assuming that the lattice points of lattice parameter *a* in a *bcc* structure are occupied by spherical atoms of radius r, calculate the free volume per unit cell.

Hints:
$$a = 4r/\sqrt{3}$$
 [Ans: $a^3 [1 - \frac{\pi\sqrt{3}}{8}]$.

Q4. Cs metal (atomic weight 130) has a cubic unit cell of side 6 Å. If the density of Cs is 2 g/cm³, determine whether the unit cell is simple, face centered or body centered.

[Ans: BCC].

Q5. Find the Miller indices of the following shaded planes



- Q6. Calculate the spacing between (1 0 0) and (1 1 1) planes of a cubic system of lattice parameter a. [Ans: a, $a/\sqrt{3}$].
- Q7. Draw the planes having miller indices (121), (231), (120), (030), (103).
- Q8. Draw the directions [1 2 3], [0 1 2].
- Q9. The inter-planar spacing of [1 1 0] plane is 2 Å for a FCC crystal. Find the atomic radius.

Hints:
$$[d = \frac{a}{\sqrt{h^2 + k^2 + l^2}}, a = \frac{4R}{\sqrt{2}}]$$
 [Ans: $\mathbf{r} = \mathbf{1} \, \mathring{\mathbf{A}}$].

Q10. Find the perpendicular distance between the two planes indicated by the Miller indices (1 2 1) and (2 1 2) in a unit cell of a cubic lattice with a lattice constant parameter 'a'.

Hints:
$$d_1 = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$$
; $d_2 = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$; $d = d_1 - d_2$ [Ans: 0.0749 Å].

Q 11. Aluminium is an fcc crystal with lattice constant a = 0.405 nm. Calculate the number of unit cells present in an aluminium foil of 0.005 cm thickness and two sides of 25 cm length.

[Ans. 4.7041×10^{22}].