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Probability Assignment -III

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Question: Let X represent the difference between the number of heads and the number of tails obtained when a coin is tossed 6 times. What are possible values of X?

Solution:

Let, *H* represent random variable representing the no of heads in 6 coin tosses, (PMF) of *H* is given by

$$\Pr(H = k) = {}^{n} C_{k} \times \left(\frac{1}{2}\right)^{k} \times \left(\frac{1}{2}\right)^{6-k}, 0 \le H \le 6 \quad (1)$$

Let, H represent random variable representing the no of heads in 6 coin tosses, (PMF) of H is given by

$$\Pr(T = k) = {}^{n} C_{k} \times \left(\frac{1}{2}\right)^{k} \times \left(\frac{1}{2}\right)^{6-k}, 0 \le T \le 6$$
 (2)

X is random varible representing the difference between no of tails and heads (PMF) of X is

$$X = H - T, X = -6, -4, -2, 0, 2, 4, 6$$
 (3)

$$H = k \Rightarrow T = 6 - k \Rightarrow X = 2k - 6 \tag{4}$$

$$Pr(X = 2k - 6) = Pr(H = k) = Pr(T = 6 - k)$$
 (5)

$$=^{n} C_{k} \times \left(\frac{1}{2}\right)^{6} \tag{6}$$

k=0

$$\Pr(X = -6) = \left(\frac{1}{2}\right)^6 = \frac{1}{64} \tag{7}$$

k=1

$$\Pr(X = -4) = 6 \times \left(\frac{1}{2}\right)^6 = \frac{3}{32} \tag{8}$$

k=2

$$\Pr(X = -2) = 15 \times \left(\frac{1}{2}\right)^6 = \frac{3}{16} \tag{9}$$

k=3

$$\Pr(X = 0) = 20 \times \left(\frac{1}{2}\right)^6 = \frac{5}{16} \tag{10}$$

k=4

$$\Pr(X=2) = 15 \times \left(\frac{1}{2}\right)^6 = \frac{3}{16} \tag{11}$$

k=5

$$\Pr(X = 4) = 6 \times \left(\frac{1}{2}\right)^6 = \frac{3}{32} \tag{12}$$

k=6

$$\Pr(X=6) = \left(\frac{1}{2}\right)^6 = \frac{1}{64} \tag{13}$$

X	-6	-4	-2	0	2	4	6
Pr(X)	$\frac{1}{64}$	$\frac{3}{32}$	$\frac{3}{16}$	$\frac{5}{16}$	$\frac{3}{16}$	$\frac{3}{32}$	1 64