

## Assignments 1

Date: chhawan 04

(2021)

1. What do you mean by law of demand? Explain factors influencing demand.



Demand for a commodity refers to the desire backed by ability to pay and willingness to buy it. If a person below poverty to buy it, it is only desire not a demand. If a rich man wants to buy a car, it is demand as he will be able to pay for the car. Thus, desired backed by purchasing power is demand. The demand for any commodity mainly depends on the price of the commodity. The demand for any commodity depends on the price of that commodity (~~or it's~~). The other determinants include price of related commodities, income of consumers, taste and preferences (~~affection~~) of consumers, and wealth of consumers. Hence, demand function can be written as:

$$D_x = f(P_x, P_s, Y, T, W)$$

Where,  $D_x$  - demand for good x

$P_x$ : Price of good x

$P_s$ : Price of related goods

$Y$ : income

$T$ : taste and preferences of consumer

$W$ : Wealth of consumer

### Law of demand

The law of demand states that there is negative or inverse relationship between the price and quantity demanded of a commodity over period of time.

"Adam Smiths was 18<sup>th</sup> century father of modern economics"

Alfred Marshall stated that 'the greater the amount sold, the smaller must be the price at which it is offered, in order that it may find purchasers; or in other words, the amount demanded increases with a fall in price and diminishes with rise in price'

According to Ferguson, the law of demand is that the quantity demanded varies inversely with price

Thus the law of demand states that people will buy more at lower prices and buy less at higher prices, other things remains the same. By other things remaining the same, we mean the following assumptions.

Assumption of the law:

1. No change in the consumer's income
2. No change in the consumer's tastes and preference
3. No change in the prices of other related goods.
4. No new substitutes for the goods have been discovered
5. People do not feel that the present fall in price is prelude (जिस तरफ होती है) to further decline of Price.

The factors influencing demands are:

1. Price of commodity
2. Income of consumer (उत्तमि)
3. Price of related goods (competitive or complementary)
4. Weather
5. customer and fashion
6. Size of Population
7. Future expectation

(31/5/21)

What do you mean by law of supply? Explain factors influencing supply.

Supply means the good offered for sale at a price during a specified period of time. It is the capacity and intention of the producer to produce goods and service for sale at a specific price.

The supply of a commodity at a given price may be defined as the amount of it which is actually offered for sale per unit of time at that price.

The law of supply establishes a direct relationship between price and supply. Firms will supply less at lower prices and more at higher prices. Other things remaining the same, as the price of commodity rises, its supply rises and as the price falls, its supply contracts.

#### factors determining supply

- Production technology
- Prices of factors
- Price of other products
- Number of producers or firms
- Future price expectation
- Taxes and subsidies
- Non-economic factors

All other things being equal, demand price and quantity varies inversely with time.

5. What do you mean by utility and marginal utility? State and explain the law of diminishing marginal utility with suitable example and figure.

### ① Utility:

- The level or power of satisfaction to a consumer by consuming goods and services
- Utility is defined as the power of commodity or a service to satisfy a human want. Utility is a subjective or psychological concept

Eg: for a vegetarian, mutton has no utility.

### ② Total utility

The sum of utilities of all units of a commodity consumed.

Ex: If a consumer consumes ten biscuits, then total utility is the sum of satisfaction of consuming all the ten biscuits.

### ③ Marginal utility

The addition made to the total utility by consuming one more unit of a commodity

Ex: If a consumer consumes 10 biscuits, the marginal utility is the utility derived from the 10th unit. It is nothing but the total utility of 10 biscuits minus the total utility of 9 biscuits.

Thus

$$MU_n = TU_n - TU_{n-1}$$

↴ total utility of  $n-1$  units  
 ↴ Total utility of  $n$  units  
 ↴ Marginal utility of ' $n^{\text{th}}$ ' commodity.

The Law of diminishing marginal utility states that in the process of fulfilling human wants, when a consumer consumes additional units of commodity, the utility derived from each successive unit of the commodity goes decreasing.

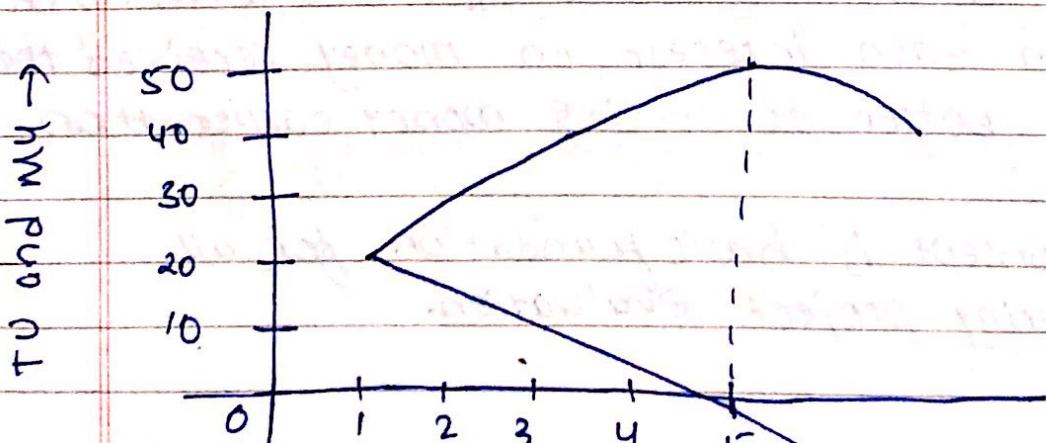
If a consumer takes more and more units of commodity the additional utility he derives from an extra unit of commodity goes on falling. Thus according to law: The marginal utility decreases, the total utility increases at diminishing rate.

Example :

units of Apple	Total utility	Marginal utility
1	20	20
2	35	15
3	45	10
4	50	5
5	50	0
6	45	-5
7	35	-10

Suppose, Mr. X is hungry, and eats apple one by one. The first apple give him great pleasure as he is hungry; when he takes second apple, the extent of his hunger will reduce, therefore he will derive less utility from the second apple.

If he continues to take additional apples, the table shows total utility and marginal utility.



4. Define Engineering Economics. What are the basic principle of engineering economics.

→ Engineering Economics is the applications of economic techniques to the evaluation of engineering alternatives. The role of engineering economics is to assess the appropriateness of a given project, estimates its value and justify it from an engineering standpoint - John M. Watts

It deals with the concepts and techniques of analysis useful in evaluating the worth of system, products and services in relation to their cost.

The principles of Engineering Economics are

A. According to Chan S. Park

Principles unite the concepts and techniques presented in any engineering economic book, thereby allowing us to focus on the logic underlying the practice of engineering economics.

There are 4 principles

a. Time value of money

- A nearby penny is worth a distant dollar.
- Money has a time value associated with it, because we can earn interest on money received today, it is better to receive money earlier than later
- This concept is basic foundation for all engineering project evaluation.

(contd)

(contd)

b. differential (incremental) cost and revenue

- All that counts are the differences among alternatives
- An economic decision should be based on the differences among the alternatives considered. All that is common is irrelevant to the decision.
- Whenever a choice is made, something is given up. The opportunity cost of a choice is the value of the best alternative given up.

c. Marginal revenues must exceed marginal cost

- Marginal revenue means the additional revenue made possible by increasing the activity by one unit (or small unit). Marginal cost has an analogous definition
- Any increased economic activity must be justified on the basis of the fundamental economic principle that marginal revenue must exceed marginal cost.

d. The trade-off between risk and reward

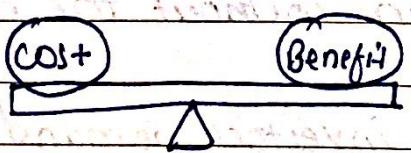
- Additional risk is not taken without the expected additional return.
- for delaying consumption, investors demand a minimum return that must be greater than the anticipated rate of inflation or any perceived risk
- if they didn't receive enough to compensate for anticipated inflation and the perceived investment risk, inventors risk

According to W. Sullivan

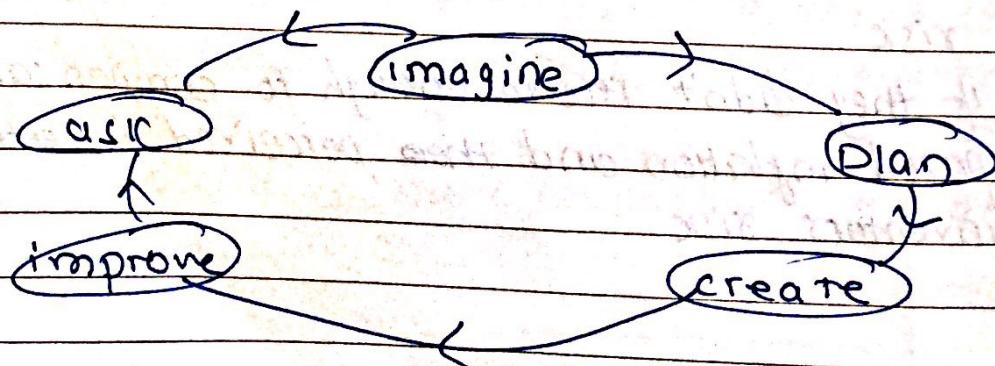
1. Develop Alternatives
  2. Focus on the differences
  3. Use a consistent viewpoint [Economic Viewpoint]
  4. Use common unit of measure
  5. Consider all relevant criterial social and environmental aspects)
  6. Make uncertainty explicit
  7. Revisit your decision (Self evaluation)
- 5. Why do you think studying the course is important for engineering students? Justify.**

Engineering Economy is a subset of economy for application to engineering projects. Engineers seek solutions to problems, and the economic viability of each potential alternative or design is normally considered along with the technical aspects.

Engineering economy involves the evaluation of the costs and benefits of proposed projects.



Engineers play a major role in investment by making decisions based on economic analysis and design considerations.



- Engineering economy analysis presents the best estimates of what is expected to occur

### Steps

- understand the problem
  - collect all relevant data/information
  - define the feasible alternative
  - evaluate each alternative
  - select the best alternative
  - implement and monitor
- 
- Engineering students should prepare themselves with economic empowerment so that they could manage their wealth, help them in starting their own business or during managerial period.
  - It is because, money is one of important factor in completing a project. Furthermore, fresh graduate also need to manage their wealth well since a lot of graduates facing problem because lack of information about the loans that they have made.
  - for profit making organization have to go for more money - now and in the future
  - Not for-profit must remain financially sound.

6. "Engineering Economics is all about decision making" Explain.

Engineering economic decision refers to all investment decisions relating to engineering projects. The most interesting fact of an economic decision, from an engineer's point of view, is the evaluation of costs and benefits associated with making a capital investment.

The types of engineering economic decision are:

- ① Service or quality improvement
- ② New products or product expansion
- ③ Equipment and process selection
- ④ Cost reduction
- ⑤ Equipment replacement

Engineers play a vital role in capital investment decisions based on their ability and experience to design, analyze, and synthesize.

Engineering economy involves formulating, estimating and evaluating the expected economic outcome of alternatives designed to accomplish a defined purpose. Mathematical techniques simplify the economic evaluation of alternatives.

Because the formulas and techniques used in engineering economics are applicable to all type of money matter they are equally useful in business and government as well as for individuals.

Engineering economics teaches us

- engineering economics analysis
- capital allocation study
- economic analysis

The numbers used in engineering economy are best estimates of what is expected to occur.

## 7. Explain primary application of Engineering Economics

The primary application of engineering economy are

### 1. Seeking of New objectives

→ Engineers all over the world are constantly seeking new and wider application of their technical knowledge for the benefit of mankind.

### 2. Discovery of factors

→ Engineering Economy seeks to discover so-called limiting factors which may hinder the success of a project

### 3. Investment of capital

→ with the exception of few cases, capital is invested to earn profit for the owners of the capital.

→ EE enables engineers to consider all the aspects of the investment from both technical and financial viewpoints.

Assignment: 2Shrawan OC

1. Explain Concepts of manufacturing and non-manufacturing cost with suitable example.

→ In Engineering economics, cost is used in many different ways because there are many types of costs, each classified differently according to the immediate needs of management:

A. Manufacturing Cost

B. Non-Manufacturing cost

① Manufacturing Cost

→ Manufacturing cost is the sum of costs of all resources consumed in the process of making a product.

→ In converting raw materials into products (finished goods), a manufacturer incurs various costs - associated with operating a factory.

→ The manufacturing cost is classified into 3 categories:

② Direct raw materials costs

- Direct raw materials are any materials that are used in the final products and that can be easily traced to it. Some examples are wood in furniture, steel in bridge construction, paper in printing firms and fabric for clothing manufacturers.

- It is important to note that finished product of one company can become the raw materials of another company.

Ex: Computer chips produced by Intel are a raw material for Dell in its personal computers.

### b. Direct Labor Cost

- The direct labor cost is the cost of workers who can be easily identified by with the unit of production.
- direct labor incurs cost that go into the production of a product
- The labor costs of assembly-line workers  
Ex: welders in metal-fabricating industries  
Carpenters or bricklayers in home building etc

### c. Manufacturing overhead

Manufacturing overhead, the third element of manufacturing cost includes all the cost of manufacturing except the cost of direct materials and direct labor.

It includes:

- i) indirect labor costs: supervisors, material handling team
- ii) indirect material costs: lubricants, grease and water
- iii) other indirect: land rent, property insurance.

### (ii) Non-Manufacturing cost

- Two additional costs incurred in supporting any manufacturing operation are: ① Marketing or selling cost  
② Administrative cost
- Marketing cost include all the costs necessary to secure customer orders and get the finished product or service into the hands of the customer.
- Overhead: Heat and light, property taxes, depreciation
- Marketing: Advertising, shipping, sales travel, sales commission, sales salaries.
- Administrative function: Executive compensation, general accounting, public relation and Secretarial support.

2. Explain the different types of cost involved in manufacturing of products with suitable example

Manufacturing costs are the costs necessary to convert raw material into products. In converting raw materials into finished goods, a manufacturer incurs various costs associated with operating a factory.

Manufacturing costs are typically divided into three categories...

1. Direct raw material cost.
2. Direct labor cost
3. Manufacturing overhead.

Example:

Consider a Noodle factory. we will discuss the cost relating with noodle factory.

#### ① Direct material cost:

This is the cost of the materials which become the part of the finished product

Example: the cost of wheat, starches, water, salt, flavor are considered as direct material cost

#### ② Direct-labor-cost

This is the cost of wages of the individuals who are physically involved in the converting raw into a finished product

Example: wages of the person cooking food, putting on machine, packaging noodle etc (Assembly line workers)

### ⑩ Manufacturing overhead

The all other cost incurred in the manufacturing activity which cannot be directly traced to physical units in an economically feasible way.

Example : depreciation of the factory equipment  
property taxe

insurance on manufacturing facilities

## Overtime premiums

3. Write short notes on :

## (i) Differential cost

## (11) Sunk cost

## (ii) Differential revenue

### (v) Marginal Cost

## (ii) Opportunity cost

### a. Differential cut:

- In business decisions, each alternative has certain costs and benefits that must be compared with the costs and benefit of the other available alternatives.
  - A difference in cost between any two alternatives is called differential cost.
  - A differential cost is also known as an incremental cost, although technically an incremental cost should refer only to an increase in cost from one alternative to another.
  - In particular, they are useful in making a variety of short-term operational decisions.
  - Some common examples of short-run problems are:
    - method changes
    - operations planning
    - make-or-buy decision

## Opportunity Cost:

Opportunity cost may be defined as a potential benefit that is given up if you select an alternative course of action. In fact, virtually every alternative has some opportunity cost associated with it. For example, suppose you have a part time job while attending college that pays you Rs 20,000 per month, you would like to spend 2 months Annapurna Trail Spring break, and your employer has agreed to give you the month off.

The Rs 20,000 in lost wages would be an opportunity cost.

Opportunity cost could also mean contribution to income that is forgone by not using a limited resource in the best way possible.

Or we may view opportunity cost as cash flows that could be generated from an asset the firm already owns, provided that such flows are not used for the alternative in question.

## Sunk Cost (Retrospective opp. of prospective)

A sunk cost is a cost that has already been incurred by past action. Sunk cost are not relevant to decision, because they cannot be changed regardless of what decision is made now or in the future. The only costs relevant to decision, because they do not change among the alternative courses of action being considered.

To illustrate a sunk cost, suppose you have a very old motorcycle that requires frequent

repairs. You want to sell it, and you figure that the current market value would be about Rs 1,20,000 at best. While you are in the process of advertising the bike, you find that the engine is leaking. You decided to have the engine repaired which cost you Rs 8,000. A friend of yours is interested in buying your bike and has offered Rs 1,20,000 for it. Would you take the offer, or would you decline it simply because you cannot recoup the repair costs on that offer?

Here, Rs 8,000 is a sunk cost.

A sunk cost is a cost that has already been incurred and cannot be recovered.

### Marginal cost:

Another cost term useful in cost-volume analysis is marginal cost. We define marginal cost as the added cost that would result from increasing the rate of output by a single unit. The accountant's differential cost concept can be compared to the economist's marginal cost concept.

In speaking of changes in cost and revenue, the economist employs the term marginal cost and marginal revenue.

- The revenue that can be obtained from selling one more unit of product is called marginal revenue. The cost involved in producing one more unit of product is called marginal cost.

## Manufacturing cost vs Non Manufacturing cost (MC) (NMC)

- |  |   |
|--|---|
| <p>→ MC is the sum of costs of all resources consumed in the process of making a product.</p> <p>→ MC refers to those that are spent to transform material into finished goods</p> <p>→ This cost is easily traced in the final product.</p> <p>→ The types are:</p> <ul style="list-style-type: none"> <li>① Direct raw material cost</li> <li>② Direct labor</li> <li>③ Manufacturing overhead</li> </ul> <p>→ It is also called factory cost or production cost</p> <p>→ The cost of (salary) for the front line workers are considered as Manufacturing cost</p> | <p>NMC refer to those incurred outside the factory or production department.</p> <p>→ NMC refers to that cost invested beside directly on the product</p> <p>→ This cost is not easily traced in the final product.</p> <p>→ The types are:</p> <ul style="list-style-type: none"> <li>④ Marketing cost</li> <li>⑤ Administrative cost</li> </ul> <p>→ It is also called period cost</p> <p>→ The executive salaries are considered as Non-manufacturing cost</p> |
|--|---|

→ The level of Manufacturing cost are directly related to the level of production and directly involved in the creation of product and service.

→ Example of MC are:  
factory supplies  
Salary of factory workers  
freight-in

→ The level of non-manufacturing cost are not directly related to the level of production but related to the administration, sales and promotion related cost

Example of NMC are!  
Legal expense  
Advertising  
freight-out (delivery expen)

2017 Fall

(2-a)

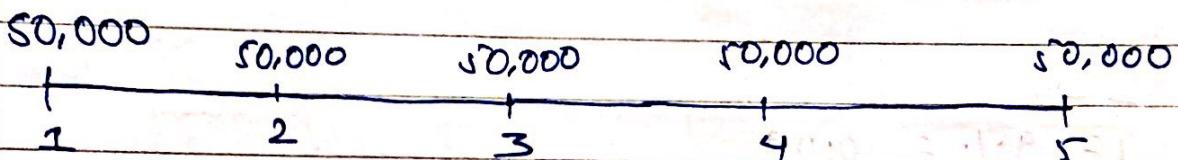
Calculate the future worth of the following cash flows deposited at 8.1% compounded continuously for 5 years.

- (i) Rs 50,000 at the beginning of each year.
- (ii) Rs. 50,000 at the end of each year.

(i) Beginning of each year

$$N(\text{time}) = 5 \text{ years}$$

$$\text{Rate } (i) = 8.1\% = 0.08$$



here all annuity earn certain amount as interest

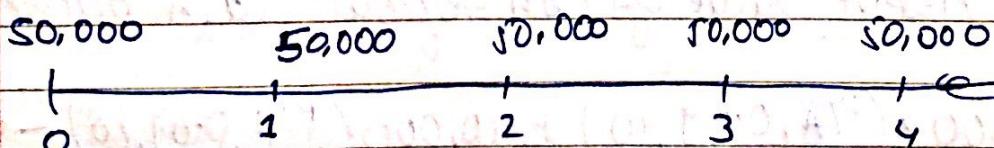
$$\text{Future worth (FW)} = A * (F/A, i, N)$$

$$= A * \left[ \frac{(1+i)^N - 1}{i} \right]$$

$$= 50,000 * \left[ \frac{(1+0.08)^5 - 1}{0.08} \right]$$

$$= 293,330.048$$

(ii) End of each year



here Annuity (0, 1, 2, 3) earn but the 4th one was at the end, so it cannot earn any extra amount.

future worth ( $PW$ ) =  $A + (F/A, i, N) + 50,000$

$$50,000 * \left( \frac{(1+i)^N - 1}{i} \right) + 50,000$$

275305.6

I am confused at rate, continuously ~~annual~~  $\rightarrow$   $e^r$ ,  
 rate may be  $r = e^{m-1}$   
 $r = e^{0.08-1} = 8.32\% = 0.833$

(21b)

$$\rightarrow i = g \cdot l = 0.09$$

Initial investment ( $I$ ) = Rs. 50,000

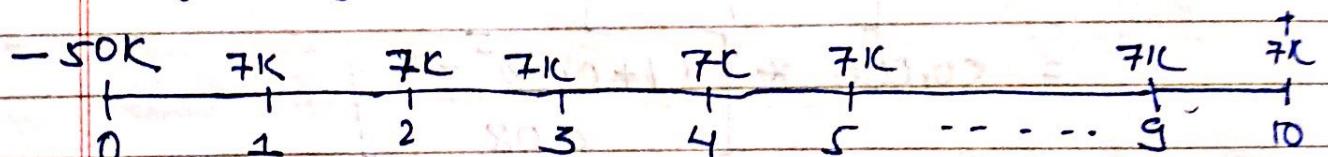
Operating cost (Expense ( $AE$ )) = Rs. 2000

Annual Income / Revenue ( $AR$ ) = Rs. 7000

Net profit ( $P$ ) Annuity =  $AR - AE =$  Rs. 7,000

Salvage value ( $S$ ) = Rs. 10,000

useful life ( $N$ ) = 10 years



find a. Is this investment worth investing?

$NPW = \text{Present value of (Cash inflow - Cash outflow)}$

$$= 7,000 * (P/A, 0.09, 10) + 10,000 * (P/f, 0.09, 10) - 50,000$$

$$= 7000 * \frac{1.09^{10} - 1}{0.09 * 1.09^{10}} + 10,000 * \frac{1}{1.09^{10}} - 50,000$$

$$= -852$$

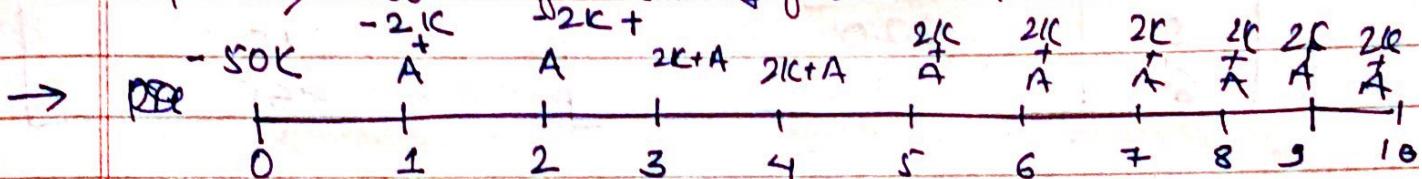
Hence  $NPW < 0$ , it is not worth investing.

b. What should be min. annual benefit for making it a worthy of investment at g.i. rate of return

• present worth of cash inflow ~~= A(P/A, g.i., 10)~~  
~~A(2)~~ = ~~A \* 6.418 +~~



• present worth of cash outflow = \$50,000



let  $A$  be the min. annual benefit for making it worthy

- present value of cashflow =

$$= A * (P/A, i, N) + 10,000 + (P/F, g.i., 10)$$

$$= A * \left[ \frac{(1+i)^N - 1}{i(1+i)} \right] + 10,000 * \frac{1}{(1+i)^{10}}$$

$$= A * \frac{1.09^{10} - 1}{0.09 + 1.09^{10}} + 10,000 / 1.09^{10}$$

$$= A(6.418) + 4224.108$$

- Present value of cashoutflow =

$$= A * (P/A, i, N) + 50,000$$

$$= 2000 * (6.418) + 50,000$$

$$= 62836$$

In this case, for minimum annual benefit

~~proj QD~~ Net present worth = 0

Cash inflow - Cash outflow = 0

Cash inflow = Cash outflow

$$A(6.418) + 4224.108 = 62836$$

$$6.418 * A = 5861.892$$

$$A = \cancel{9132.44} \quad 9140.96$$

(3-a) Evaluate the following project whose cash flows are given below. Use simple payback period, present worth and future worth method. [MARR = 10% p.a.]

Year	Net cash flow	Cumulative cash flow
0	-600	-600
1	-500	-1100
2	125	-975
3	300	-675
4	1000	325
5	220	545
6	320	865

a. Simple payback period method:

Simple payback period =

minimum year + Amount to be recovered

~~Upcoming year cash flow~~

$$3 + \frac{675}{1000}$$

3.675

Conclusion:

for six year project, the payback period is 3.675 which is good (वर्ति अच्छा करता रहा)

b. Present worth method:

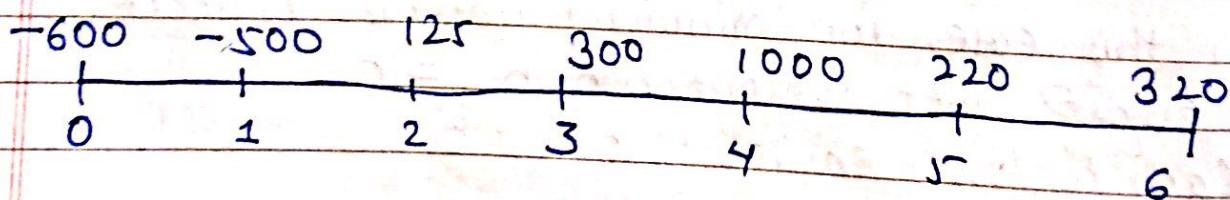


Fig: Cash flow diagram.

$$\text{MARR} = 10\% = 0.1$$

$$\begin{aligned} \text{Net present worth} &= -\frac{600}{(1+i)^0} + \frac{-500}{(1+i)^1} + \frac{125}{(1+i)^2} + \frac{300}{(1+i)^3} \\ &\quad + \frac{1000}{(1+i)^4} + \frac{220}{(1+i)^5} + \frac{320}{(1+i)^6} \\ &= -600 \text{ put } i = 0.1 \end{aligned}$$

$$\begin{aligned} \text{NPW} &= -600 + (-454.545) + 103.30 + 225.394 + \\ &\quad 683.013 + 136.602 + 180.631 \\ &= 274.395 \end{aligned}$$

NPW is  $> 0$ , so accept the project

### C. Future worth method

$$\begin{aligned} \text{future worth} &= -600 (\text{FIP}, 0.1, 0) - 500 (\text{FIP}, 0.1, 5) + \\ &\quad 125 (\text{FIP}, 0.1, 4) + 300 (\text{FIP}, 0.1, 3) + 1000 (\text{FIP}, 0.1, 2) \\ &\quad + 220 (\text{FIP}, 0.1, 1) + 320 (\text{FIP}, 0.1, 0) \\ &= -600 (1+0.1)^6 - 500 (1+0.1)^5 + 125 \times (1+0.1)^4 + 320 \times (1+0.1)^3 + \\ &\quad 1000 \times (1+0.1)^2 + 220 \times (1+0.1)^1 + 320 \times (1+0.1)^0 \\ &= -1062.9366 - 805.257 + 183.0125 + 425.92 + \\ &\quad 1210 + 202 + 320 \\ &= 512.7409 \end{aligned}$$

Since, Future worth  $> 0$ , so accept the project.

(31b) Select which project is feasible to invest.

MARR is 12.1% per year.

use IRR method and incremental cash analysis

Particulars	Project A (Rs)	Project B (Rs)
Initial Investment	6,50,000	5,00,000
Net Annual revenue	2,50,000	2,00,000
Net Annual cost	50,000	40,000
Salvage value	75,000	50,000
Useful life	8 years	8 years

→ A. IRR method

a. Project A

(i) Trial at 12.1% per year

$$NPW = -650,000 + 250,000 (P/A, 0.12, 8) - 50,000 (P/A, 0.12, 8) + 75,000 (P/F, 0.12, 8)$$

$$= -650,000 + (250,000 - 50,000) (P/A, 0.12, 8) + 75,000 (P/F, 0.12, 8)$$

$$= -650,000 + 200,000 \times \left[ \frac{1 - 1.12^8}{0.12} \right] + 75,000 \times \frac{1}{1.12^8}$$

$$= 1673,819.19 \text{ or } 373819.19 \text{ Rs}$$

(ii) Trial at 10% per year

$$NPW = -650,000 + (250,000 - 50,000) (P/A, 0.1, 8) + 75,000 (P/F, 0.1, 8)$$

$$= 147723.20 \text{ Rs}$$

Note: दामीलाई ग्राही थेटी NPI उत्तम नहीं होता  
 & क्रैट की value की sign alternate होती है  
 ie at 12% , NPI is +ve  
 at ?%, NPI is -ve  
 So we can interpolate.

(iii) Trial at 30% per year

$$\begin{aligned} NPI &= -650,000 + (250,000 - 50,000)(P/A, 0.3, 8) \\ &\quad + 75,000(P/F, 0.3, 8) \\ &= -34,768 \text{ [तो फिर कौन सी positive तरफ]} \end{aligned}$$

So rate of return must be in between 12% to 30%.

Note:

IRR is calculate when  $NPI = 0$  ie cash inflow - cash outflow are equal.

Now interpolating

$$\begin{aligned} IRR &= \text{lower rate} + \frac{\text{Amount at LR}}{\text{Amount at LR} + \text{Amount at HR}}(HR - LR) \\ &= 0.12 + \frac{373819.1955}{373819.1955 + 343768}(0.3 - 0.12) \\ &= 0.12 + 0.0937 \\ &= 0.2137 \end{aligned}$$

$$At IRR - IRR = 21.37\%$$

## Project B

(i) Trial at 12%.

$$NPW = -\$500,000 + (200,000 - 40,000)(P/A, 0.12, 8)$$
$$+ 50,000 (P/F, 0.12, 8)$$

$$= -\$500,000 + 1,60,000 * \frac{1.12^8 - 1}{0.12 * 1.12^8} + 50,000 * \frac{1}{(1+0.12)^8}$$
$$= 315016.5241$$

(ii) Trial at 20%.

$$NPW = -\$500,000 + 1,60,000 * \frac{1.2^8 - 1}{0.2 * 1.2^8} + \frac{50,000}{(1+0.2)^8}$$
$$= 1,25,573.9705$$

(iii) Trial at 30%.

$$NPW = -\$500,000 + 1,60,000 * \frac{1.3^8 - 1}{0.3 * 1.3^8} + \frac{50,000}{1.3^8}$$
$$= -25,918.245$$

Interpolate is between 12% and 30%.

Lower rate (LR) = 0.12, Amt = 315016.5241  
higher rate (HR) = 30%, Amt = -25,918.245

$$IRR = LR + \frac{|Amt at LR| (HR - LR)}{|Amt at LR| + |Amt at HR|}$$

$$\begin{aligned}
 IRR &= 0.12 + \frac{315016.5241 \times (0.3 - 0.12)}{315016.5241 + 25918.245} \\
 &= 0.12 + 0.1663 \\
 &= 0.2863
 \end{aligned}$$

$$IRR = 28.63\%$$

Conclusion

(प्रोजेक्ट की शैर्ट एवं डिप्पे राशि) का नक्षत्र rate of return  
मानना हमें कहलाता है investment return  $\approx 21.37\%$

Since IRR of Proj A ( $21.37\%$ ) < IRR of Proj. B ( $28.63\%$ ). So, I accept project A

### → B. Incremental Analysis:

$$\text{IRR of A} = 21.37\%$$

$$\text{IRR of B} = 28.63\%$$

Take A as the base project alternative

- Ques 1. Sorting the project in order of increasing capital investment

B	Project	I	IRR
A	B	500,000	28.63%
	A	6,50,000	21.37%

Take B as the base project

Ques A-B

15,00	150,000
	50,000
	10,000

Ques

(i) At 12% for 8 years (trial 1)

$$NPW_{A-B} = -150,000 + (50,000 - 10,000)(P/A, 0.12, 8)$$

$$+ 25,000 + (P/F, 0.12, 8)$$

$$= -150,000 + 40,000 * \frac{1.12^8 - 1}{0.12 * 1.12^8} + 25,000 * \frac{1}{1.12^8}$$

$$= 58802.67137$$

(ii) At 20% for 8 years (trial 2)

$$NPW_{A-B} \text{ at } 20\% = -150,000 + 40,000 * (P/A, 0.2, 8) + \\ 25,000 * (P/F, 0.2, 8) \\ = 9300.5931$$

(iii) At 25% for 8 years (trial 3)

$$NPW_{A-B} \text{ at } 25\% = -150,000 + 40,000 * (P/A, 0.25, 8) + \\ 25,000 * (P/F, 0.25, 8) \\ = -12649.2416$$

Interpolating in between 12% and 25%

$$IRR_{A-B} = LR + \frac{Amt \text{ at } LR (HR - LR)}{Amt \text{ at } LR + Amt \text{ at } HR}$$

$$= 0.12 + \frac{58802.67137 (0.25 - 0.12)}{58802.67137 + 12649.2416}$$

$$= 0.2269$$

$$= 22.69\%$$

$$IRR_{A-B} = 22.69\% > MARR$$

## Decision Rule :

If  $\DeltaIRR > MARR$ , choose higher cost alternative

If  $\DeltaIRR < MARR$ , choose lower cost alternative

## Conclusion

here  $\DeltaIRR_{A-B} > MARR$ , choose higher cost

alternative that is project A.

(4b) find simple payback period and discounted cash flow information

→ Given

Initial Investment ( $I$ ) = Rs. 4,00,000

Annual Revenue ( $AR$ ) = Rs. 150,000

Annual cost ( $AC$ ) = Rs. 30,000

Salvage value ( $S$ ) = Rs. 1,00,000

Useful life ( $N$ ) = 5 years

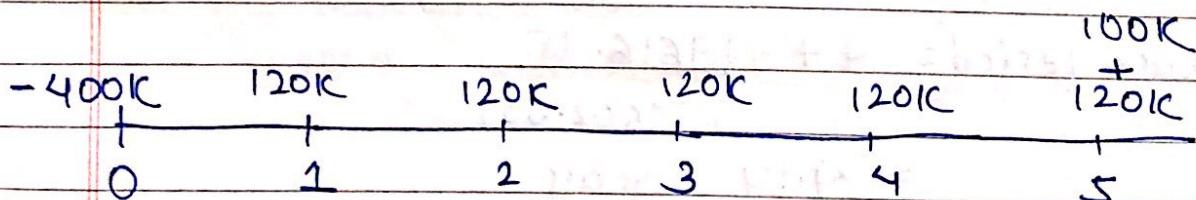
$MARR = 10\% = 0.1$

Annual = 150,000

Profit = 30,000  
1,20,000

a. Simple payback information

Cash flow	Amount	Action	Cumulative cash flow
- 4,00,000		I	- 4,00,000
+ 150,000		AR	- 250,000
- 30,000		AC	- 220,000
+ 1,00,000		S	0



### a. Simple payback period method

Year	Particulars	Net cash flow	cummulative cash flow
0		-4,00,000	-4,00,000
1		+120,000	-280,000
2		+120,000	-160,000
3		+120,000	-40000
4		+120,000	80,000
5		+220,000	3,00,000

simple payback period = min year + Amount to be recovered  
upcoming year cash flow

$$= 3 + \frac{40000}{120,000}$$

$$= 3 + 0.333$$

$$= 3.333$$

### b. discounted payback period method ( $MARR = 10\%$ )

Year	Net cash flow	A $\frac{1}{(1+i)^N}$	(X)	(A * X)	$\sum(A * X)$	cummulative cash flow
0	-4,00,000	$(1+0.1)^0 = 1$	-4,00,000	-4,00,000	-4,00,000	
1	+120,000	$(1+0.1)^1 = 0.909$	109090.909	109090.909	-290909.090	
2	+120,000	$(1+0.1)^2 = 0.8264$	99173.55	99173.55	-191735.54	
3	+120,000	$(1+0.1)^3 = 0.75131$	90157.77	90157.77	-101577.77	
4	+120,000	$(1+0.1)^4 = 0.6830$	81961.614	81961.614	-19616.15	
5	+220,000	$(1+0.1)^5 = 0.6209$	136602.691	136602.691	116986.534	

$$\text{payback period} = 4 + \frac{19616.15}{136602.691}$$

$$= 4.14 \text{ years}$$

## (S1a) Solution.

Given:

Initial investment ( $I$ ) = Rs. 1,00,000Salvage value ( $S$ ) = Rs. 30,000Useful life ( $N$ ) = 10 years

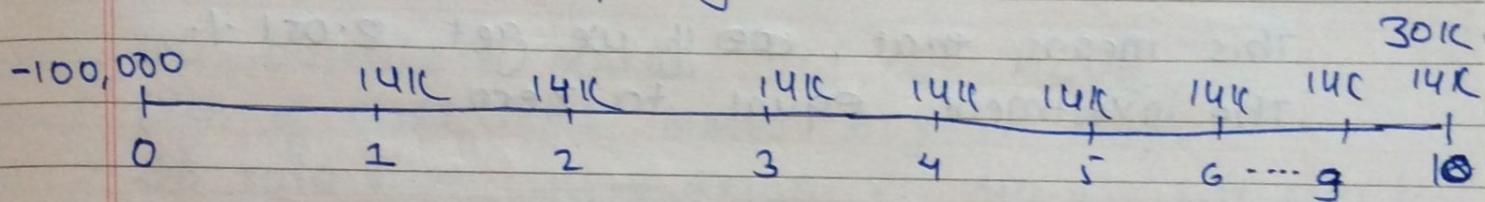
Annual revenue (AR) = 20,000 p.a

Annual expenses (AE) = 6,000 p.a

MARR  $\rho = 8\%$  p.a $\alpha IRR = ?$ 

Now

Net profit = AR - AE = 14,000 per annum

~~(i) Trial at 8% per year~~

(i) Trial at 8% per year

$$NPW = -1,00,000 + 14,000 \left( P/A, 0.08, 10 \right) + 30,000 \left( P/F, 0.08, 10 \right)$$

$$= -100000 + 14000 \times \frac{(1+0.08)^{10} - 1}{0.08 \times (1+0.08)^{10}} + \frac{30,000}{(1+0.08)^{10}}$$

$$= 7836.944$$

(ii) Trial at 15% per year

$$NPW = -1,00,000 + 14000 \left( P/A, 0.15, 10 \right) + 30,000 \left( P/F, 0.15, 10 \right)$$

$$= -100000 + 14000 \times \frac{1.15^{10} - 1}{0.15 \times 1.15^{10}} + \frac{30,000}{1.15^{10}}$$

$$= -99066.67$$

Interpolating in between 8% and 15%.

$$LR = 0.08; \text{ Amount} = 7836.944$$

$$HR = 0.15; \text{ Amount} = -99066.67$$

$$\begin{aligned} IRR &= LR + \frac{[Amt \text{ at } LR] (HR - LR)}{[Amt \text{ at } LR] + [Amt \text{ at } HR]} \\ &= 0.08 + \frac{7836.944 (0.15 - 0.08)}{7836.944 + 99066.67} \\ &= 0.08 + 0.05131 \\ &= 0.08051 \\ &= 8.051\% > MARR \end{aligned}$$

This means that, if we get 8.051%,  
The investment equal to zero

At 8.051%, The net present value of all the cash flows from a project equal to zero.

Decision Rule,

Hence the IRR (ie 8.051%) which is greater than MARR (8%), so we accept the project

(Slb) A construction equipment has initial cost and annual saving per year are of Rs 100,000 - 40,000 a Rs 20,000 resp with O&M cost of Rs 7000 <sup>per year</sup>; it will depreciate by MACRS method and will have no salvage value. ( $N = 5$  years). Estimate before and tax cash flow. The company pays income tax @ 40%.

MACRS: Modified Accelerated Cost Recovery System  
Allows the taxpayers to deduct greater amounts during first few years of an asset life.

→ Given

Income

$$\text{Tax} = 40\%$$

$$N = 5 \text{ years}$$

Year	BT(F)
0	-40,000
1	
2	
3	
4	
5	

(MACRS किन ताकि ग्रन्ति)

GOT it

TO calculate MACRS %, we have

Life of Asset ( $N$ ) = MACRS 5 year class

$$\text{DB rate } \alpha = \frac{1}{N} + 2 * 100 = 40\% \text{ (At } N=5\text{)}$$

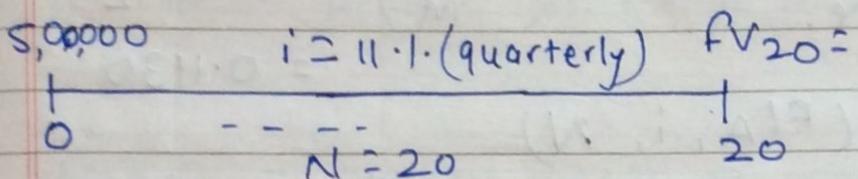
Year	calculation	MACR %
1		
2		
3		
4		
5		

Annual profit =  $20,000 - 7000 = 13000$

Year	BTCF	Macr Dep	Depreciation	Taxable income BTCF - Depr	Income tax (40%)	ATCF
0	-Rs 40,000	-	-	-	-	-40,000
1	$13000 * 0.5$ = 6500	20.1.	8,000	-1500	No Tax	6500
2	13,000	32.1.	12,800	200	80	12,920
3	13,000	19.2.1.	7620	5380	2152	10,848
4	13,000	11.52				
5	13,000	11.52				
6	$13000 * 0.5$ = 6500	5.76				

2016 spring

- (21b) A man aged 40 years now had borrowed Rs. 500,000 from bank for his further studies at the age of 20 years. Interest was charged at 11.1 per year compounded quarterly. He wish to pay semiannual equal installment with the first installment begining 5 year after receiving the loan. He has just clear his loan now what amt did he pay in each installments.



$$FV_{20} = \$50,000 * (1+i)^N$$

$$= \$50,000 *$$

$$i_{eff} = \left(1 + \frac{r}{M}\right)^M - 1$$

$$= \left(1 + \frac{0.11}{4}\right)^4 - 1$$

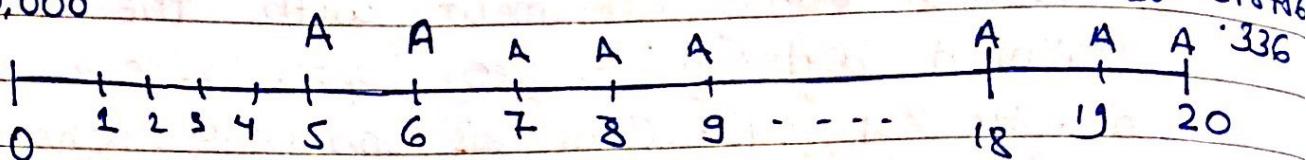
$$= 0.1146$$

$$\begin{aligned}\therefore FV_{20} &= 500000 * (1 + 0.1146)^{20} \\ &= 500000 * 8.7575 \\ &= 4378756.336\end{aligned}$$

The man have to pay is 4378756.336 in total, he started paying from after 5 years to 20 years equally to contribute 4378756.336

let he pay 'A' amount after 5 years of borrowed time (ie 5) to until now (20)  
ie  $n = 15$

- \$,00,000



$$i_{\text{eff}} = \left(1 + \frac{r}{m}\right)^{\frac{m}{n}} - 1 = \left(1 + \frac{0.11}{2}\right)^2 - 1 = 0.1130$$

Now we have,

$$FV_{20} = A(F/A, i, n)$$

$$= A(F/A, 0.1130, 16)$$

$$4378756 \cdot 336 = A * \left[ \frac{(1+i)^N - 1}{i} \right]$$

$$4378756 \cdot 336 = A * \frac{1.1130^{16} - 1}{0.1130}$$

$$A = \frac{4378756 \cdot 336}{40.2236}$$

$$A = 108860.3229$$

He paid 108860.3229 in each installment

(3b) Determine both types of BIC ratio using present and annual worth if rate is 12%.

$$I = 6,00,000$$

$$\text{life} = 8 \text{ years}$$

$$AR = 2,00,000 \rightarrow \text{benefit}$$

$$AE = 60,000 \rightarrow 0.02M$$

$$S = 2,00,000$$

(i) Present worth formulation

$$\text{benefit} = 200,000 - 60,000 = 140,000$$

PW(B) = present worth of benefit

$$= 200,000 (P/A, 0.12, 8)$$

$$= 200,000 + \frac{1.12^8 - 1}{0.12 * 1.12^8}$$

$$= 695469.5674 - 993527.9534$$

PW(I) = present worth of initial investment

$$= 600,000$$

PW(S) = present worth of salvage value

$$= 200,000 + (P/F, 0.12, 8)$$

$$= 200,000 * (1 + 0.12)^{-8}$$

$$= 80776.6456$$

PW(OM) = present worth of operation & maintenance cost

$$= 60,000 * (P/A, 0.12, 8)$$

$$= 60,000 + \frac{1.12^8 - 1}{0.12 * 1.12^8}$$

$$= 298058.386$$

BIC (Conventional) = PW(B)

$$\frac{PW(I) - PW(S) + PW(OM)}{}$$

$$= \underline{993527.9534}$$

$$600,000 - 80776.6456 + 298058.386$$

$$= 1.1163$$

BIC (Modified) = PW(B) - PW(OM)

$$\frac{PW(I) - PW(S)}{}$$

$$= \underline{993527.9534 - 298058.386}$$

$$600,000 - 80776.6456$$

$$= 1.17$$

### (b) Annual worth formulation

$$AW(I) = 6,00,000 (AIP, 0.12, 8)$$

$$\begin{aligned} &= 6,00,000 * \left[ \frac{(1+i)^N - 1}{(1+i)^N - 1} \right] \\ &= 600000 * \frac{1.12^8 + 0.12}{1.12^8 - 1} \\ &= 120781.7048 \end{aligned}$$

$$AW(B) = 2,00,000$$

$$AW(08M) = 60,000$$

$$AW(J) = 200000 * (AIF, 0.12, 8)$$

$$\begin{aligned} &= 200000 * \left[ \frac{i}{(1+i)^N - 1} \right] \\ &= 200000 * \frac{0.12}{1.12^8 - 1} \\ &= 16260.568 > \underline{\underline{100\%}} \end{aligned}$$

Now

$$B/C \text{ (conventional)} = \frac{AW(B)}{AW(I) - AW(J) + AW(08M)}$$

$$= \frac{200000}{120781.7048 - 16260.568 + 60,000}$$

$$= 1.2156$$

$$B/C \text{ (Modified)} = \frac{AW(B) - AW(08M)}{AW(I) - AW(J)}$$

$$= \frac{200000 - 60000}{120781.7048 - 16260.568}$$

$$= 1.3394 > 0 \quad \underline{\underline{100\%}}$$

(u/a) Use Repeatability Assumptions to recommend the best project

Project

Initial Investment (R<sub>0</sub>)

Net Annual Revenue (R<sub>t</sub>)

Salvage value (R<sub>t</sub>)

Life

MARR

A

40,000

15,000

5,000

3

15·1.

B

50,000

20,000

6,000

5

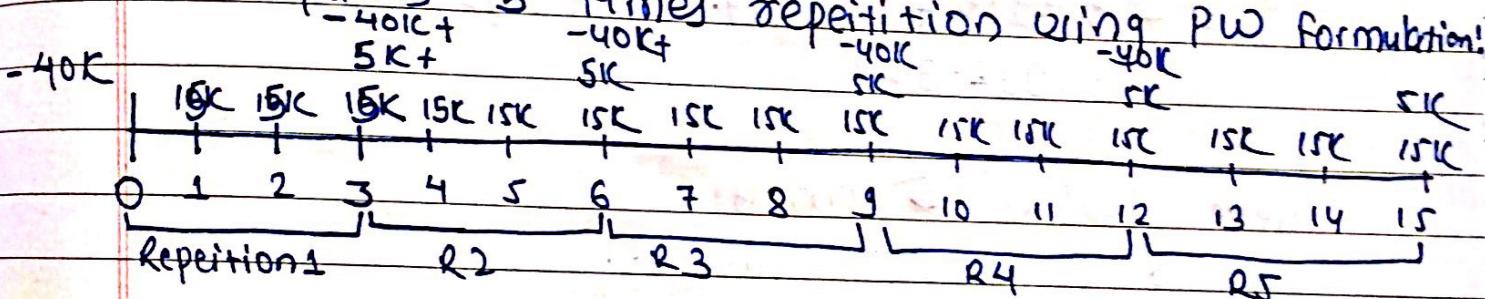
15·1.

a. Repeatability project

LCM of 3 and 5 years = 15 years

for project A

it requires 5 times repetition using PW formulation:



$$PW(15\%) = -40,000 - 40,000(P/F, 0.15, 3) - 40,000(P/F, 0.15, 6)$$

$$- 40,000(P/F, 0.15, 9) - 40,000(P/F, 0.15, 12) +$$

$$15,000(P/A, 0.15, 15) + 5,000(P/F, 0.15, 3) +$$

$$5,000(P/F, 0.15, 6) + 5,000(P/F, 0.15, 9) +$$

$$5,000(P/F, 0.15, 12) + 5,000(P/F, 0.15, 15)$$

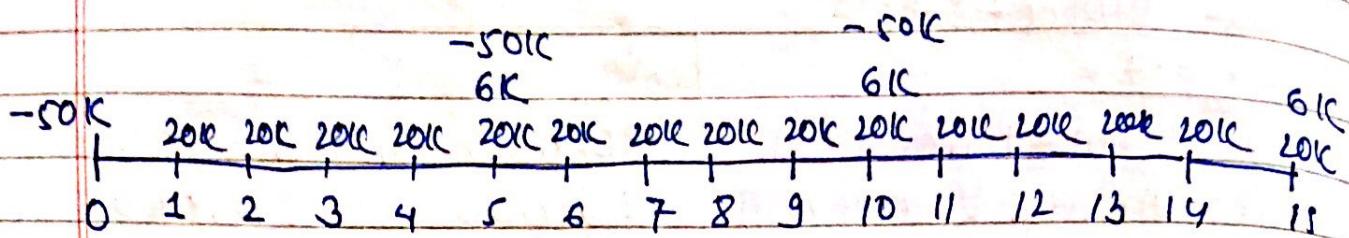
$$= -40,000 - 26,300 \cdot 6.4 - 17,293 \cdot 10 - 11,370 \cdot 4.9 - 7,476 \cdot 2.8$$

$$+ 8,7710 \cdot 5.5 + 3,287 \cdot 5.8 + 2,161 \cdot 6.3 + 1,421 \cdot 3.12 +$$

$$934 \cdot 5.3 + 614 \cdot 4.7$$

$$= -6310.438$$

for project B : it has 3 repetition



$$\begin{aligned}
 PW(15\%) &= -50000 - 50000(P/F, 0.15, 5) - 50000 \\
 &\quad (P/F, 0.15, 10) + 20000 \times (P/A, 0.15, 15) + 6000(P/F, 0.15, \\
 &\quad + 6000(P/F, 0.15, 10) + 6000(P/F, 0.15, 15) \\
 &= -50 - 50,000 - 24858.83 - 12359.23 + 116947.40 \\
 &\quad 20000 + 3945.09 + 2593.96 + 1705.57 + 298 \\
 &\quad 121.44 + 737.36 + 2983.06 + 1483.10 + 737.36 \\
 &= -87218 + 116947.402 + 5203.52 \\
 &= 34932.922
 \end{aligned}$$

here  $PW(A) \leq PW(B)$

so B is better than A.

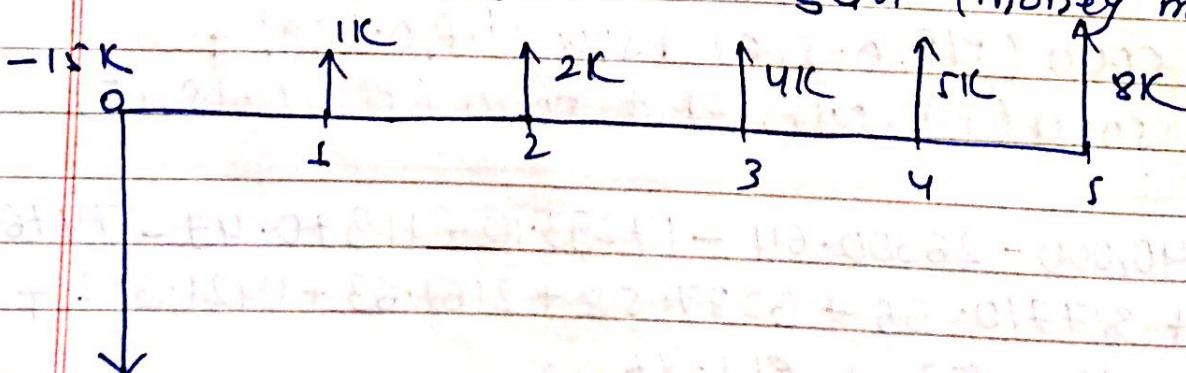
(4)(b) Find IRR, MIRR, both payback period

MARR = 10%

Year	0	1	2	3	4	5
Amount	(15000)	1000	2000	4000	5000	8000

↳ -ve cash flow

coz invest profit income  $\frac{\text{P}}{\text{C}}$  (money makes money)



(i) Internal rate of return (IRR)

Trial at 10%.

$$\text{NPW} = -15000 + \frac{1000}{1.1^1} + \frac{2000}{1.1^2} + \frac{4000}{1.1^3} + \frac{5000}{1.1^4} + \frac{8000}{1.1^5}$$

$$= -1050.3194$$

Trial at 5%.

$$\text{NPW} = -15000 + \frac{1000}{1.05^1} + \frac{2000}{1.05^2} + \frac{4000}{1.05^3} + \frac{5000}{1.05^4} + \frac{8000}{1.05^5}$$

$$= 1603.512$$

Interpolating between 10% and 5%.

$$LR = 5\% \quad \text{Amt} = 1603.512$$

$$HR = 10\% \quad \text{Amt} = -1050.3194$$

$$\begin{aligned} IRR &= LR + \frac{|\text{Amt at LR}|(HR-LR)}{|\text{Amt at LR}| + |\text{Amt at HR}|} \\ &= 0.05 + \frac{1603.512 \times 0.05}{1603.512 + 1050.3194} \\ &= 0.05 + 0.03021 \\ &= 0.0802 \\ &= 8.02\% < MARR \end{aligned}$$

Not a good project. So Reject.

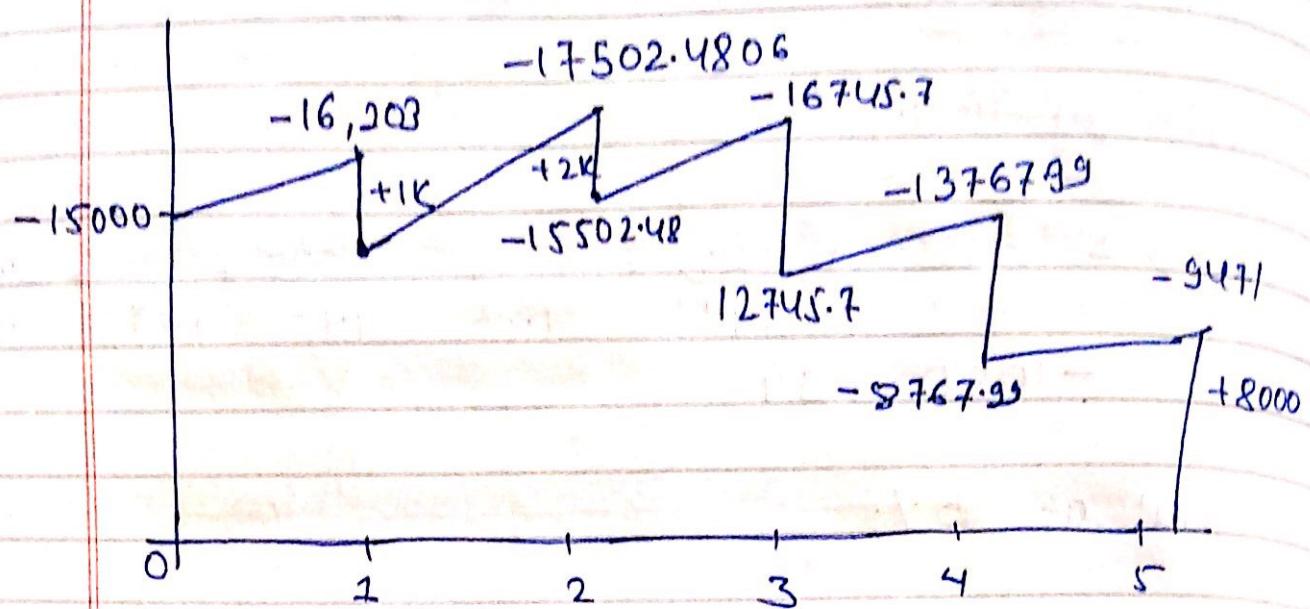


Fig: Investment balance Diagram

(ii) MIRR.

$$PV \text{ of outflow} = \frac{FV \text{ of inflow}}{(1+MIRR)^N}$$

$$PV \text{ of outflow} = -15000$$

$$\begin{aligned} FV \text{ of inflow} &= 1000 \times 1.1^4 + 2000 \times 1.1^3 + 4000 \times 1.1^2 + \\ &\quad 5000 \times 1.1^1 + 8000 \times 1.1^0 \\ &= 22466.1 \end{aligned}$$

$$MIRR = ?$$

Now

$$PV_0 = \frac{FV_i}{(1+MIRR)^N}$$

$$-15000 = \frac{22466}{(1+MIRR)^5} \Rightarrow 1+MIRR = \sqrt[5]{22466/15000}$$

$$MIRR = 8.414\%$$

### (iii) Simple payback period

EOY	Cash Flow Amount	cummulative frequency
0	-15000	-15000
1	1000	-14000
2	2000	-12000
3	4000	-8000
4	5000	-3000
5	8000	5000

Payback period = minimum year +  $\frac{\text{Amt to be recovered}}{\text{upcoming yr cash flow}}$

$$= 4 + \frac{3000}{8000}$$

$$= 4.375$$

### (iv) Discounted payback period

EOY	Net cash flow	Interest factor	Discount cash flow	cummulative cash flow
0	-15000	$1.1^0 = 1$	-15000	-15000
1	1000	$1.1^1 = 0.9090$	909.0909	-14090.9091
2	2000	$1.1^2 = 0.8264$	1652.8925	-12438.01
3	4000	$1.1^3 = 0.7513$	3005.2592	-9432.75
4	5000	$1.1^4 = 0.6830$	3415.0672	-6017.68
5	8000	$1.1^5 = 0.6209$	4967.37	-1050.3128

Not feasible for discounted

(5/b) Find annual depreciation and book value of each year by SL, DB, SVD and sinking fund method

Initial cost (I) = Rs. 7000 Salvage value = Rs. 2000

useful life (N) = 5 years MARR = 10%

### (i) straight line method

$$\text{Annual depreciation} = \frac{I - S}{N} = \frac{7000 - 2000}{5}$$

$$= \frac{5000}{5} = \text{Rs. } 1000$$

$$\text{rate of depreciation} = \frac{1}{N} \times 100 = \frac{1}{5} \times 100 = 20\%$$

To find Book value

Year	Book value Beginning	Depreciation	Book value at end
0	7000	-	7000
1	7000	1000	6000
2	6000	1000	5000
3	5000	1000	4000
4	4000	1000	3000
5	3000	1000	2000

### (ii) Declining Balance method

we define

relationship

$$B = I - dR$$

$$R = r [0 to 1]$$

$$r = N$$

d = depreciation

BV<sub>k</sub> = Book value

$$d_1 = B(R)$$

$$d_{k+1} = B(1-R)^{k-1} * R \quad \text{--- (1)}$$

$$d_k^* = B[1 - (1-R)^k] \quad \text{--- (2)}$$

$$BV_k = B(1-R)^k \quad \text{--- (3)}$$

Using ①, ② and ③, we can calculate annual depreciation, cumulative depreciation and book value.

$$\text{DB rate} = \frac{1}{N} * 200 = 20\% = 0.1\%$$

$$\begin{aligned} d_5 &= \text{depreciation at year } 5 \\ &= B(1-R)^{n-1} * R \\ &= 7000 * (1-0.1)^4 * (0.1) \\ &= 459.27 \end{aligned}$$

$$\begin{aligned} d_5^* &= B[1 - (1-R)^n] = 7000 * [1 - (1-0.1)^5] \\ &= 2407 - 2866.52 \end{aligned}$$

$$\begin{aligned} BV_5 &= B(1-R)^n = 7000 * (1-0.1) \\ &= 4133.43 \end{aligned}$$

EOT	BV begin	$0.1 * BV_{\text{begin}}$	$BV_{\text{begin}} - dr$	BV end
0	-	-		7000
1	7000	700		6300
2	6300	630		5670
3	5670	567		5103
4	5103	510.3		4592.7
5	4592.7	459.27		4133.43

## 1) Sum of year digit (SOYD)

$$SOYD = \frac{N(N+1)}{2} = \frac{5*6}{2} = 15$$

Depreciation portion for each year = ~~5:4:3:2:1~~ 5:4:3:2:1

$SYD = \text{remaining useful year}$  (I-S)

$SYD$  total life

here

$I = \text{Rs. } 7000$

$S = \text{Rs. } 2000$

$SYD$  total life = 15

remaining useful life, 5: 4: 3: 2: 1

Year	Book value Beginning	Depreciation Proportion	SYD Depreciation	Book value at end
0	0 -	-	-	7000
1	7000	5	$\frac{5}{21} \times 7000$	5809.53
2	5809.53	4	$\frac{4}{21} \times 5000$	4857.15
3	4857.15	3	$\frac{3}{21} \times 5000$	4142.86
4	4142.86	2	$\frac{2}{21} \times 5000$	3666.66
5	3666.66	1	$\frac{1}{21} \times 5000$	3428.57 (wrong)

#### (iv) Sinking Fund method

Year	BV begin	Depr Portion	SOPA Depreciation	Book value at E
0	-	-	-	
1	7000	5	$5 \times (7000 - 2000)/15$ = 1666.67	7000 5333.33
2	5333.33	4	$4 \times 5000/15$ = 1333.33	4000
3	4000	3	$3 \times 5000/15$ = 1000	3000
2	3000	2	$2 \times 5000/15$ = 666.67	2333.33
1	2333.33	1	$5000/15$ = 333.33	2000

#### (iv) Sinking Fund method:

$$\text{Fixed Annual depreciation } (A) = (I-S) \times (A/F, i\% \cdot, n)$$

$$= (7000 - 2000) \left[ \frac{1}{(1+i)^N - 1} \right] = 5000 \times 0.163 \\ = 818.98$$

Net depreciation for year  $k$

$$d_{ik} = (I-S) (A/F, i\%, k) \times (F/P, i\%, N-k)$$

Book value at end of year  $k$ ,

$$BV_k = I - (I-S) \times (A/F, i\%, N) \times (F/A, i\%, k)$$

classmate  
Date \_\_\_\_\_  
Page \_\_\_\_\_

$$(A/F, 0.1, 5) = 0.1637$$

using this formula,

(A)

Year	Fixed depreciation (A)	Net (deci) depreciation	Book value on end (BVC)
0	818.98	-	7000
1	818.98	818.5	6181.5
2	818.98	900.35	5281.15
3	818.98	990.385	4290.765
4	818.98	1089.42	3201.34
5	818.98	1198.36	≈ 2000.2

(6b) perform Sensitivity analysis using PW

$$I = 100,000$$

$$AR = 40,000$$

$$AE = 5000$$

$$S = 1000$$

$$N = 6 \text{ years}$$

$$MARR = 12\% = 0.12$$

[Done in brinde's Assignment]

It should be given

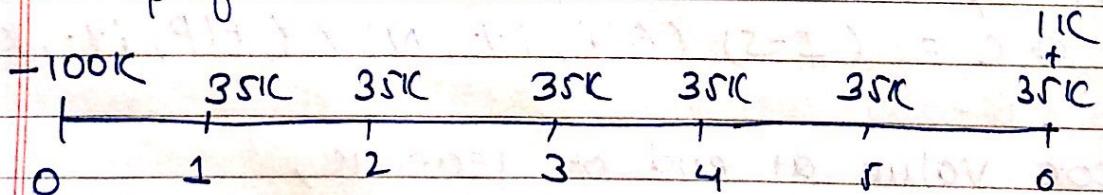
fluctuate  $\pm 1\% = \pm 20\%$

→ Solution

$$AR = 40,000$$

$$AE = -5,000$$

$$\text{Net profit} = 35,000$$



$$\text{Present worth}(12\%) = -100000 + 35000(P/A, 0.12, 6)$$

$$+ 1000(P/F, 0.12, 6)$$

$$= -100000 + 35000 \frac{1 - 1.12^6}{0.12 \times 1.12^6} + 1000 \frac{1}{1.12^6}$$

PW(12%) = 73185.73

when Initial Investment varies by  $\pm 20\%$ , we have

$$\begin{aligned} \text{At } I(+20\%) &= -100000 \times 1.2 + 35000(P/A, 0.12, 6) + 1000 \\ &\quad (P/F, 0.12, 6) \\ &= 53185.7387 \end{aligned}$$

$$\begin{aligned} \text{At } I(-20\%) &= -100000 \times 0.8 + 35000(P/A, 0.12, 6) + 1000(P/F, 0.12, 6) \\ &= 93185.738 \end{aligned}$$

when AR varies by  $\pm 20\%$ , we have

$$\begin{aligned} \text{At } AR(+20\%) &= -100000 + 40000 \times 1.2 \times (P/A, 0.12, 6) \\ &\quad - 5000(P/A, 0.12, 6) + 1000(P/F, 0.12, 6) \\ &= -100000 + (48000 - 5000) \times 4.111 + 1000 \times 0.5066 \\ &= -100000 + 176773 + 506.6 \\ &= 77279.6 \end{aligned}$$

$$\begin{aligned} \text{At } AR(-20\%) &= -100000 + 40000 \times 0.8 \times (P/A, 0.12, 6) \\ &\quad - 5000(P/A, 0.12, 6) + 1000(P/F, 0.12, 6) \\ &= -100000 + 131552 - 20555 + 506.6 \\ &= 11503.6 \end{aligned}$$

When useful life varies by  $\pm 20\%$ .

$$\begin{aligned} \text{At } +20\%, \quad N &= 6 + 0.2 \times 6 = 7.2 \\ \text{At } -20\%, \quad N &= 6 - 0.2 \times 6 = 4.8 \end{aligned}$$

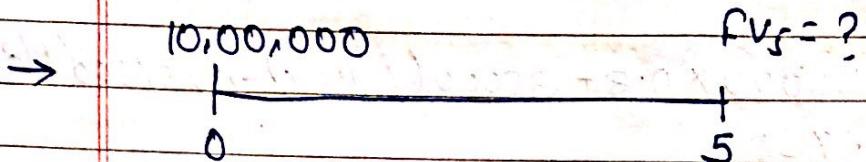
$$\begin{aligned} \text{At } N(+20\%) &= -100000 + 35000(P/A, 0.12, 7.2) \\ &\quad + 1000(P/F, 0.12, 7.2) \\ &= 63130.46 \end{aligned}$$

$$\text{At } N(-20\%) = 22953.59$$

2016 Fall

(2(a)) Sabina deposits a sum of Rs. ~~10,00,000~~ + 1000 in a bank in an bank at an  $i = 12\% \text{ p.a.}$  what will be future amount after 5 years if compounded:

- (i) weekly
- (ii) quarterly
- (iii) Annually



$$I = 10,00,000$$

$$i = 0.12$$

$$N = 5 \text{ years}$$

(i) weekly ( $M = 52$  weeks in a year)

$$I_{eff} = \left(1 + \frac{i}{M}\right)^M - 1$$

$$= \left(1 + \frac{0.12}{52}\right)^{52} - 1$$

$$= 0.1273 \\ = 12.73\%$$

$$FV_5 = P(F/P, 0.1273, 5)$$

$$= 10,00,000 * (1 + 0.1273)^5$$

$$= 1820528.722$$

(ii) quarterly ( $M = 4$ )

$$i_{eff} = \left(1 + \frac{0.12}{4}\right)^4 - 1 = 0.1255$$

$$\begin{aligned} FV_5 &= P(F/P, 0.1255, 5) \\ &= 10,00,000 \times (1 + 0.1255)^5 \\ &= 1806040.548 \end{aligned}$$

(iii) Annually

$$\begin{aligned} FV_5 &= P(F/P, 0.12, 5) \\ &= 10,00,000 \times (1 + 0.12)^5 \\ &= 1762341.683 \end{aligned}$$

(21b) Use simple payback period, PW and FW.

If MARR is 12%.

EOY	0	1	2	3	4	5	6
Net cash flow	-700	-400	125	200	800	220	320

(i) Simple payback

EOY	Cash Flow	CF
0	-700	-700
1	-400	-1100
2	125	-975
3	200	<u>-775</u>
4	<u>800</u>	25
5	220	245
6	320	565

$PP = \text{min year} + \frac{\text{recover}}{\text{upcoming}}$

$$\text{payback period} = 3 + \frac{775}{800} = 3.968 \text{ yrs.}$$

(ii)

$$\begin{aligned}
 \text{NPW} &= \frac{-700}{1.12^0} - \frac{400}{1.12^1} + \frac{125}{1.12^2} + \frac{200}{1.12^3} + \frac{800}{1.12^4} \\
 &\quad + \frac{220}{1.12^5} + \frac{320}{1.12^6} \\
 &= -700 - 357.142 + 99.64 + 142.35 + 508.414 \\
 &\quad + 124.83 + 162.121 \\
 &= -19.787
 \end{aligned}$$

(iii) Decision

NPW &lt; 0, reject the project

(iii)

$$\text{NFCW} = \text{NPW}(F/P, 0.12, 5)$$

$$= -19.787 * (1+0.12)^5$$

 $= -34.871 < 0$ , reject the project

(3(a))

Use Repeatability with PW formulation if MARR is 10.1% to evaluate two feasible investment A and B.

Particulars

Investment

Invest A (Rs)

Invest B (Rs)

Net Annual revenue

50000

150000

Net annual cost

25000

70000

Salvage value

3000

2000

Useful life

15,000

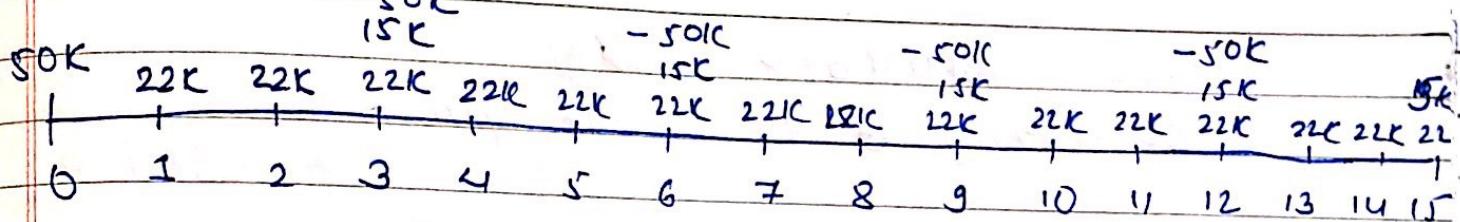
40,000

3

5 yrs

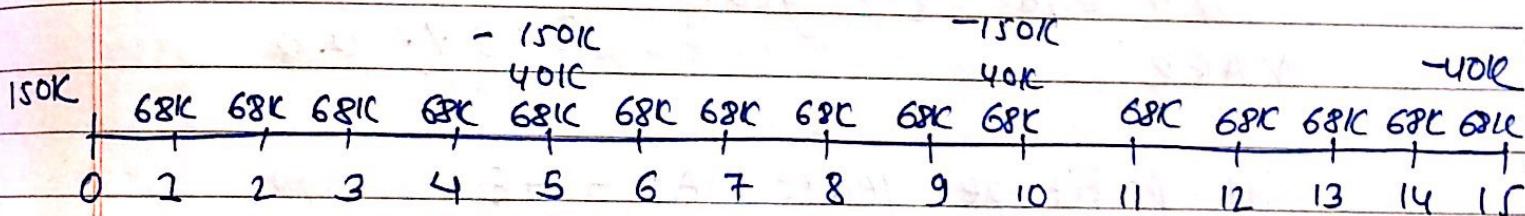
→ Using Repeatability with PW formulation

$$LCM = 15 \text{ yrs}$$



$$\text{Profit} = AR - AE = 25000 - 3000 = 22,000$$

Fig: Cash flow Diagram for project A



$$\text{Net profit} = 70000 - 2000 = 68000$$

Fig: Cash flow Diagram for Invest B

$$\begin{aligned}
 NPU(A) &= -50000 + (50000 + 15000)(P/F, 0.1, 3) + \\
 &\quad (-50000 + 15000)(P/F, 0.1, 6) + (-50000 + 15000)(P/F, 0.1, 9) \\
 &\quad + (-50000 + 15000)(P/F, 0.1, 12) + 15000(P/F, 0.1, 15) \\
 &\quad + 22000(P/A, 0.1, 15)
 \end{aligned}$$

$$\begin{aligned}
 NPW(B) &= -150000 + (-150000 + 40000) \\
 &\quad (P/F, 0.1, 15) + (-150000 + 40000)(P/F, 0.1, 10) \\
 &\quad + 40000 (P/F, 0.1, 15) + 68000 (P/A, 0.1, 15) \\
 &= -150000 - 68301.34 - 42409.76 + 9575.68 \\
 &\quad + 517213.4064 \\
 &= 266077.9864
 \end{aligned}$$

Here  $NPW(B) > NPW(A)$

Selecting B is best option.

### (3b) Evaluate IRR

$$I = \text{Rs } 6,00,000$$

$$N = 10 \text{ yrs}$$

$$AR = \text{Rs } 2,50,000$$

$$AE = 50,000$$

$$\text{Repair & maintenance cost at } 4^{\text{th}} \text{ and } 8^{\text{th}} \text{ year} = \text{Rs } 30,000$$

$$MARR = 10\% \text{ p.a}$$

$$\text{Net profit per year} = AR - AE$$

$$= 250,000 - 50,000$$

$$= 200,000$$

	-6,00,000	-30IC	-30IC
0	200K	200K	200K
1	1	2	3
2	4	5	6
3	7	8	9
4			
5			
6			
7			
8			
9			
10			

$$i = 10\% = 0.1$$

→ Solution:

Trial at 10%

$$NPW(10\%) = -600000 - 30000(P/F, 0.1, 4) - 30000(P/A, 0.1, 10)$$

$$= -600000 - \frac{30000 \times 1.1^4}{0.1 \times 1.1^{10}} - \frac{30000 \times 1.1^8}{0.1 \times 1.1^{10}} + \frac{200000}{0.1 \times 1.1^{10}}$$

$$= -600000 - \cancel{30000 \times} - 20490.40 - 13995.22$$

$$+ 1228913.421$$

$$= 594427.8011$$

$$NPW(20\%) = -60000 - 30000(P/F, 0.2, 4) - 30000(P/F, 0.2, 8) + 200000(P/A, 0.2, 10)$$

$$= 217049.78$$

$$NPW(30\%) = 4126.38$$

$$NPW(35\%) = -68742.75035$$

We get two NPW which have alternate sign

$$LR = 10\% \quad Amt = 594427.8011$$

$$HR = 35\% \quad Amt = 68742.75$$

$$IRR = LR + \frac{|Amt at LR| (HR - LR)}{|Amt at LR| + |Amt at HR|}$$

$$= 0.1 + \frac{594427.8011 \times 0.25}{594427.8011 + 68742.75}$$

$$= 0.1 + 0.2240$$

$$= 0.3240$$

$$= 32.40\% \quad \text{yes it is feasible}$$

coz IRR > MARR

(u/a) Use SL and SOYD if

$$I = 100,000 \quad N = 10 \text{ yrs}$$

$$S = 20000$$

→ Using Straight Line method

$$\text{depreciation} = \frac{I-S}{N} = \frac{80000}{10} = 8000$$

$$\text{rate of depreciation} = \frac{1}{N} * 100 = 10\%$$

SY	Book value at begining	Depreciation	Book value at end
0	—	—	100,000
1	100,000	8000	92000
2	92000	8000	84000
3	84000	8000	76000
4	76000	8000	68000
5	68000	8000	60000
6	60000	8000	52000
7	52000	8000	44000
8	44000	8000	36000
9	36000	8000	28000
10	28000	8000	20000

→ Using SOYD

$$\text{SOYD} = \frac{n(n+1)}{(n+1)} = \frac{10 \times 11}{11} = 55 \text{ %}$$

Depreciation portion: 10:9:8:7:6:5:4:3:2:1

$$\text{SOYD} = \frac{\text{remaining useful years}}{\text{total life}} = \frac{I-S}{I}$$

$$I - S = 80,000$$

Year	SOYD Calculation	=	Depreciation	Book Value at End of Year
0	-	-	-	100,000
1	10 * 80000 / 55		14545	85455
2	9 * 80000 / 55		13090.90	72364.1
3	8 * 80000 / 55		11636.36	60727.74
4	7 * 80000 / 55		10181.81	50545.93
5	6 * 80000 / 55		8727.27	41818.66
6	5 * 80000 / 55		7272.72	34545.95
7	4 * 80000 / 55		5818.18	28727.76
8	3 * 80000 / 55		4363.63	24364.13
9	2 * 80000 / 55		2909.09	21455.04
10	1 * 80000 / 55		1454.54	20000

### 2015 Spring (21a)

(21a) Mrs. Sharma is planning for her retired life and has 10 more years of service. She would like to deposit 20% of her salary, which is Rs 4000 at the end of first year and thereafter she wishes to deposit it the amt with an annual increase of Rs 1000 for 9 next years with interest of 10%. Find total amount at the end of 10<sup>th</sup> yr.

$$\begin{array}{cccccccccc}
 & 1000+ & 1000+ & 1000+ & 1000+ & 1000+ & 1000+ & 1000+ & 1000+ & 1000 \\
 4000 & 4000 & 4000 & 4000 & 4000 & 4000 & 4000 & 4000 & 4000 & 4000 \\
 \hline
 PV \rightarrow & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\
 FV \rightarrow & 9 & 8 & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0
 \end{array}$$

$$\begin{aligned}
 FV_{10} &= 4000 * (F/A, 0.1, 9) + 1000 * (F/A, 0.1, 8) \\
 &= 4000 * \frac{1.1^9 - 1}{0.1} + 1000 * \frac{1.1^8 - 1}{0.1} \\
 &= 65753.79574
 \end{aligned}$$

(6(b)) following information has be obtained

Particulars	Standard motor	New motor
size	100 hp	100hp
cost	130000	156000
life	20	20
salvage	0	0
efficiency	89.1%	93.1%
Annual O&M	8000	2500
Annual tax/insurance	2.1% of investment	
MARR	10.1% per year.	

find at what operating hours are they equivalent

Solution: for Motor standard

Calculating annual equivalent cost :

$$\text{Capital recovery cost} = 130000 \left( AIP, 10.1\%, 20 \right)$$

$$= 130000 * \frac{0.1 * 1.1^{20}}{1.1^{20} - 1}$$

$$= 15269.75$$

$$\text{Maintenance cost} = 8000$$

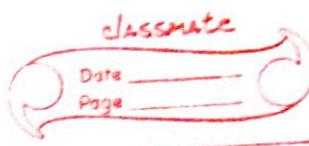
$$\text{Annual tax \& insurance} = 2.1 \% \text{ of } 130000$$

$$= 2600$$

Operating expenses for power (electricity cost)  
let  $x$  be the no: of hours of operation  
per year.

$$\text{Operating expense} = \text{Input} * \text{rate} * \frac{\text{hours}}{\text{output}} * \text{rate} * \text{hours of operation}$$

$$= \frac{\text{output}}{\text{Efficiency}} * \text{rate} * \text{hours of operation}$$



20/04/2024

Note: 1 hp = 0.746 kilowatt

$$= \left( \frac{100}{0.74} \right) * 0.746 *$$