Continuous exposures with propensity scores Malcolm Barrett

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Warning! Propensity score weights are sensitive to positivity violations for continuous exposures.

The story so far

Propensity score weighting

- Fit a propensity model predicting exposure x, x + z where z is all covariates
- 2 Calculate weights
- Fit an outcome model estimating the effect of x on y weighted by the propensity score

Continous exposures

- ① Use a model like $lm(x \sim z)$ for the propensity score model.
- Use wt_ate() with .fitted and .sigma; transforms using dnorm() to get on probability-like scale.
- 3 Apply the weights to the outcome model as normal!

Alternative: quantile binning

- Bin the continuous exposure into quantiles and use categorical regression like a multinomial model to calculate probabilities.
- Calculate the weights where the propensity score is the probability you fall into the quantile you actually fell into. Same as the binary ATE!
- 3 Same workflow for the outcome model

1. Fit a model for exposure ~ confounders

```
1 model <- lm(
2 exposure ~ confounder_1 + confounder_2,
3 data = df
4 )</pre>
```

2. Calculate the weights with wt_ate()

```
1 model |>
2  augment(data = df) |>
3  mutate(wts = wt_ate(
4  exposure,
5  .fitted,
6  # .sigma is from augment()
7  .sigma = .sigma
8  ))
```

Does change in smoking intensity (smkintensity82_71) affect weight gain among lighter smokers?

```
1 nhefs_light_smokers <- nhefs_complete |>
2 filter(smokeintensity <= 25)</pre>
```

1. Fit a model for exposure ~ confounders

```
1 nhefs_model <- lm(
2 smkintensity82_71 ~ sex + race + age + I(age^2) +
3 education + smokeintensity + I(smokeintensity^2) +
4 smokeyrs + I(smokeyrs^2) + exercise + active +
5 wt71 + I(wt71^2),
6 data = nhefs_light_smokers
7 )</pre>
```

2. Calculate the weights with wt_ate()

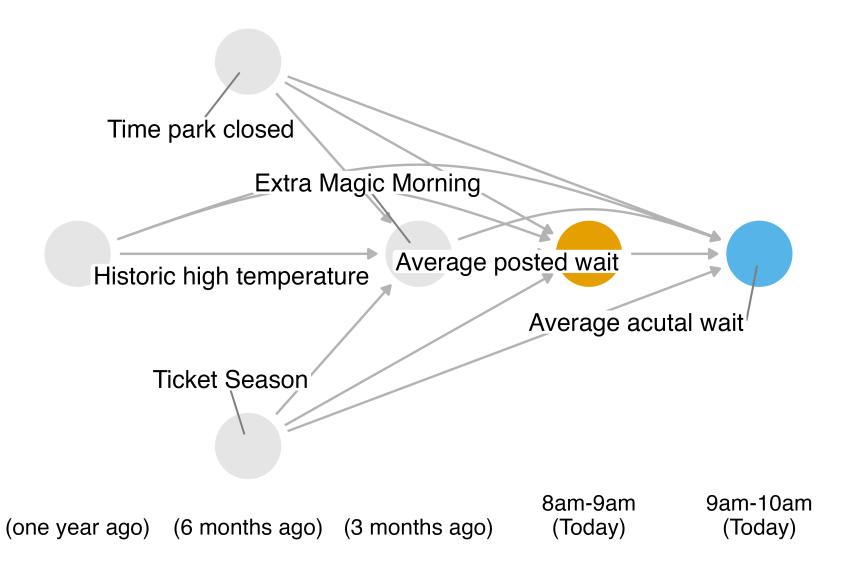
```
1 nhefs_wts <- nhefs_model |>
2 augment(data = nhefs_light_smokers) |>
3 mutate(wts = wt_ate(
4 smkintensity82_71,
5 .fitted,
6 .sigma = .sigma
7 ))
```

2. Calculate the weights with wt_ate()

1 nhefs_wts

```
# A tibble: 1,162 × 74
    segn qsmk death yrdth modth dadth sbp
                                               dbp sex
   <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <fct>
     235
                                         123
                                                80 0
             0
                        NA
                              NA
                                    NA
                   0
    244
                                         115
                                                75 1
                        NA
                              NA
                                    NA
 3
    245
                        85
                                                78 0
                                    14
                                         148
    252
                        NA
                              NA
                                    NA
                                         118
                                                77 0
 5
    257
                                         141
                                                83 1
                        NA
                              NA
                                    NA
    262
                                         132
                                                69 1
 6
                        NA
                              NA
                                    NA
    266
                                         100
                                                53 1
                        NA
                              NA
                                    NA
 8
     419
                        84
                              10
                                    13
                                         163
                                                79 0
 9
     420
                        86
                              10
                                    17
                                         184
                                               106 0
10
                                         127
     434
                   0
                        NA
                              NA
                                    NA
                                                80 1
```

Do posted wait times at 8 am affect actual wait times at 9 am?



Fit a model using lm() with wait_minutes_posted_avg as the outcome and the confounders identified in the DAG.

Use augment() to add model predictions to the data frame

In wt_ate(), calculate the weights using wait_minutes_posted_avg, .fitted, and .sigma

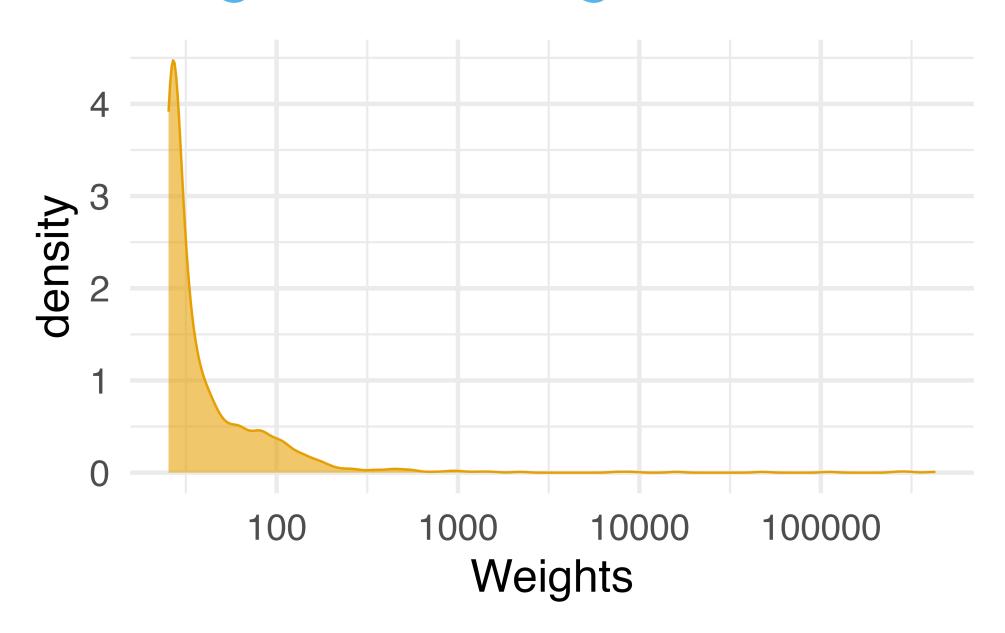
```
post_time_model <- lm(
wait_minutes_posted_avg ~

park_close + park_extra_magic_morning +
park_temperature_high + park_ticket_season,

data = wait_times

)</pre>
```

Stabilizing extreme weights



Stabilizing extreme weights

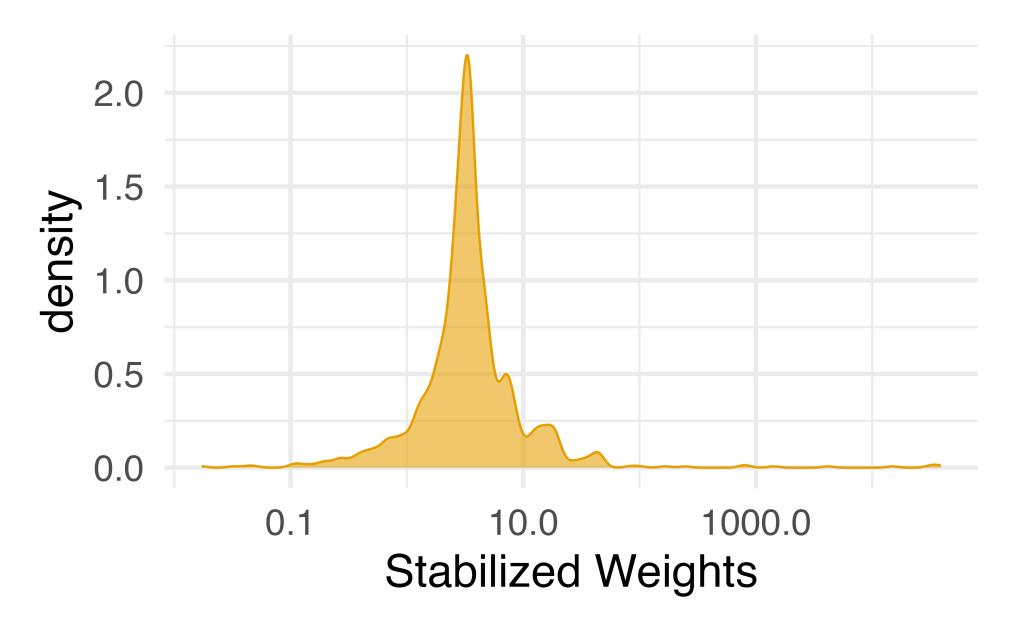
- Fit an intercept-only model (e.g. lm(x)~ 1)) or use mean and SD of x
- 2 Calculate weights from this model.
- Divide these weights by the propensity score weights.

 wt_ate(.., stabilize = TRUE) does this all!

Calculate stabilized weights

```
1 nhefs_swts <- nhefs_model |>
2 augment(data = nhefs_light_smokers) |>
3 mutate(swts = wt_ate(
4 smkintensity82_71,
5 .fitted,
6 .sigma = .sigma,
7 stabilize = TRUE
8 ))
```

Stabilizing extreme weights



Re-fit the above using stabilized weights

Fitting the outcome model

Use the stabilized weights in the outcome model. Nothing new here!

```
1 lm(
2  wt82_71 ~ smkintensity82_71,
3  weights = swts,
4  data = nhefs_swts
5 ) |>
6  tidy() |>
7  filter(term == "smkintensity82_71") |>
8  mutate(estimate = estimate * -10)

# A tibble: 1 × 5
term  estimate std.error statistic p.value
```

1 smkintensity82 71 1.99 0.0316 -6.30 4.33e-10

<chr>

Estimate the relationship between posted wait times and actual wait times using the stabilized weights we just created.

1 wait_minutes_posted_... 2.39 0.0659 3.63 4.93e-4

Diagnosing issues

- Extreme weights even after stabilization
- 2 Bootstrap: non-normal distribution
- Bootstrap: estimate different from original model

More info

https://github.com/LucyMcGowan/writingpositivity-continous-ps