

Continuous exposures with propensity scores

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2021-09-01

Warning! Propensity
score weights are
sensitive to positivity
violations for
continuous exposures.

The story so far

Propensity score weighting

- 1 Fit a propensity model predicting exposure x , $x + z$ where z is all covariates
- 2 Calculate weights
- 3 Fit an outcome model estimating the effect of x on y weighted by the propensity score

Continuous exposures

- 1 Use a model like `lm(x ~ z)` for the propensity score model.
- 2 Use `wt_ate()` with `.fitted` and `.sigma`; transforms using `dnorm()` to get on probability-like scale.
- 3 Apply the weights to the outcome model as normal!

Alternative: quantile binning

- 1 Bin the continuous exposure into quantiles and use categorical regression like a multinomial model to calculate probabilities.
- 2 Calculate the weights where the propensity score is the probability you fall into the quantile you actually fell into. Same as the binary ATE!
- 3 Same workflow for the outcome model

1. Fit a model for exposure ~ confounders

```
1 model <- lm(  
2   exposure ~ confounder_1 + confounder_2,  
3   data = df  
4 )
```

2. Calculate the weights with `wt_ate()`

```
1 model |>
2   augment(data = df) |>
3   mutate(wts = wt_ate(
4     exposure,
5     .fitted,
6     # .sigma is from augment()
7     .sigma = .sigma
8   ))
```


Does change in smoking intensity (**smkintensity82_71**) affect weight gain among lighter smokers?

```
1 nhfs_light_smokers <- nhfs_complete |>  
2   filter(smokeintensity <= 25)
```

1. Fit a model for exposure ~ confounders

```
1 nhefs_model <- lm(  
2   smkintensity82_71 ~ sex + race + age + I(age^2) +  
3   education + smokeintensity + I(smokeintensity^2) +  
4   smokeyrs + I(smokeyrs^2) + exercise + active +  
5   wt71 + I(wt71^2),  
6   data = nhefs_light_smokers  
7 )
```

2. Calculate the weights with `wt_ate()`

```
1 nhefs_wts <- nhefs_model |>
2   augment(data = nhefs_light_smokers) |>
3   mutate(wts = wt_ate(
4     smkintensity82_71,
5     .fitted,
6     .sigma = .sigma
7   ))
```

2. Calculate the weights with `wt_ate()`

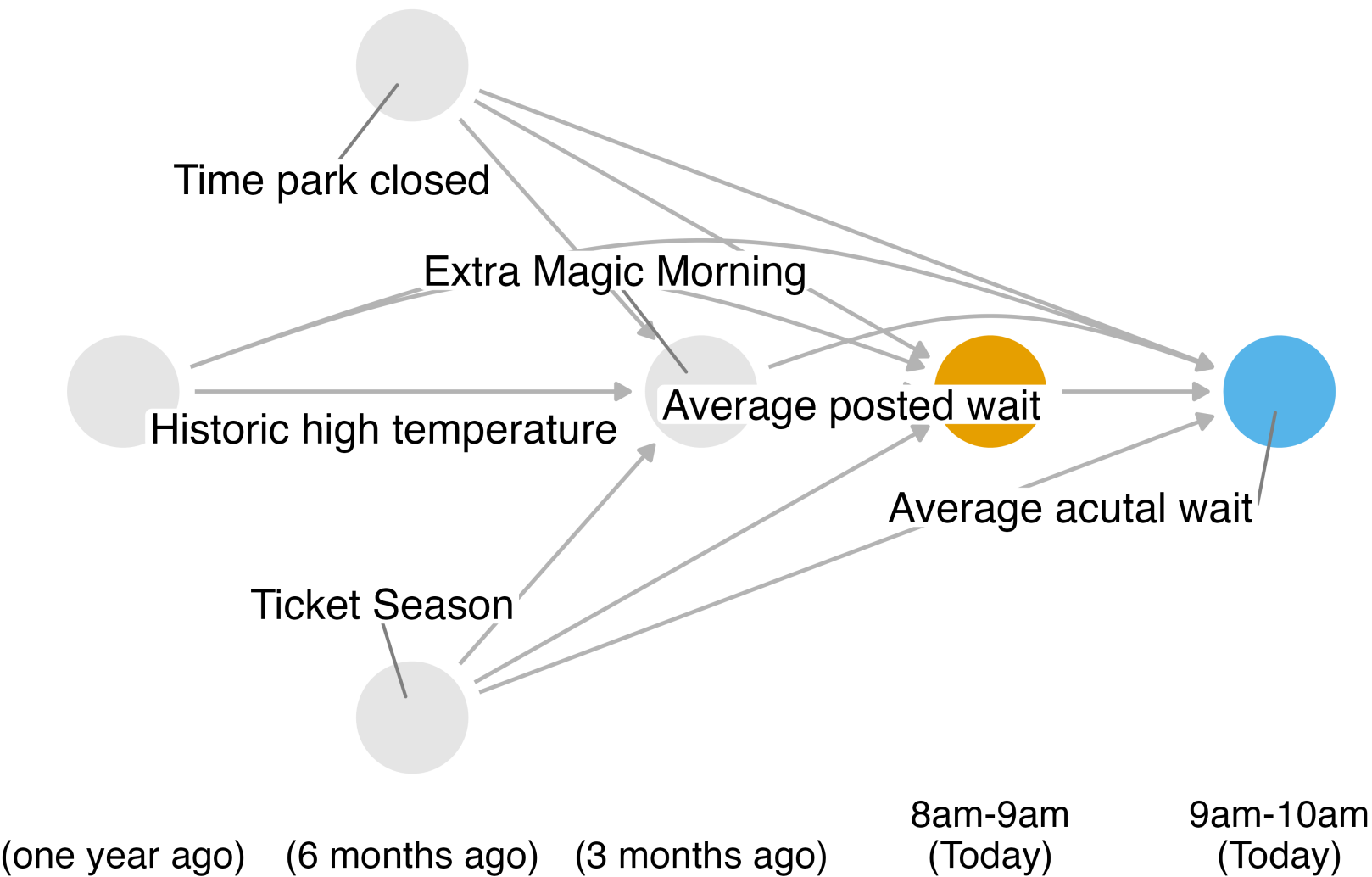
```
1 nhefs_wts
```

```
# A tibble: 1,162 × 74
```

	seqn	qsmk	death	yrdth	modth	dadth	sbp	dbp	sex
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<fct>
1	235	0	0	NA	NA	NA	123	80	0
2	244	0	0	NA	NA	NA	115	75	1
3	245	0	1	85	2	14	148	78	0
4	252	0	0	NA	NA	NA	118	77	0
5	257	0	0	NA	NA	NA	141	83	1
6	262	0	0	NA	NA	NA	132	69	1
7	266	0	0	NA	NA	NA	100	53	1
8	419	0	1	84	10	13	163	79	0
9	420	0	1	86	10	17	184	106	0
10	434	0	0	NA	NA	NA	127	80	1

```
" " 1 150
```

Do *posted* wait times at 8 am affect *actual* wait times at 9 am?



Your Turn 1

Fit a model using `lm()` with `avg_spostmin` as the outcome and the confounders identified in the DAG.

Use `augment()` to add model predictions to the data frame

In `wt_ate()`, calculate the weights using `avg_postmin`, `.fitted`, and `.sigma`

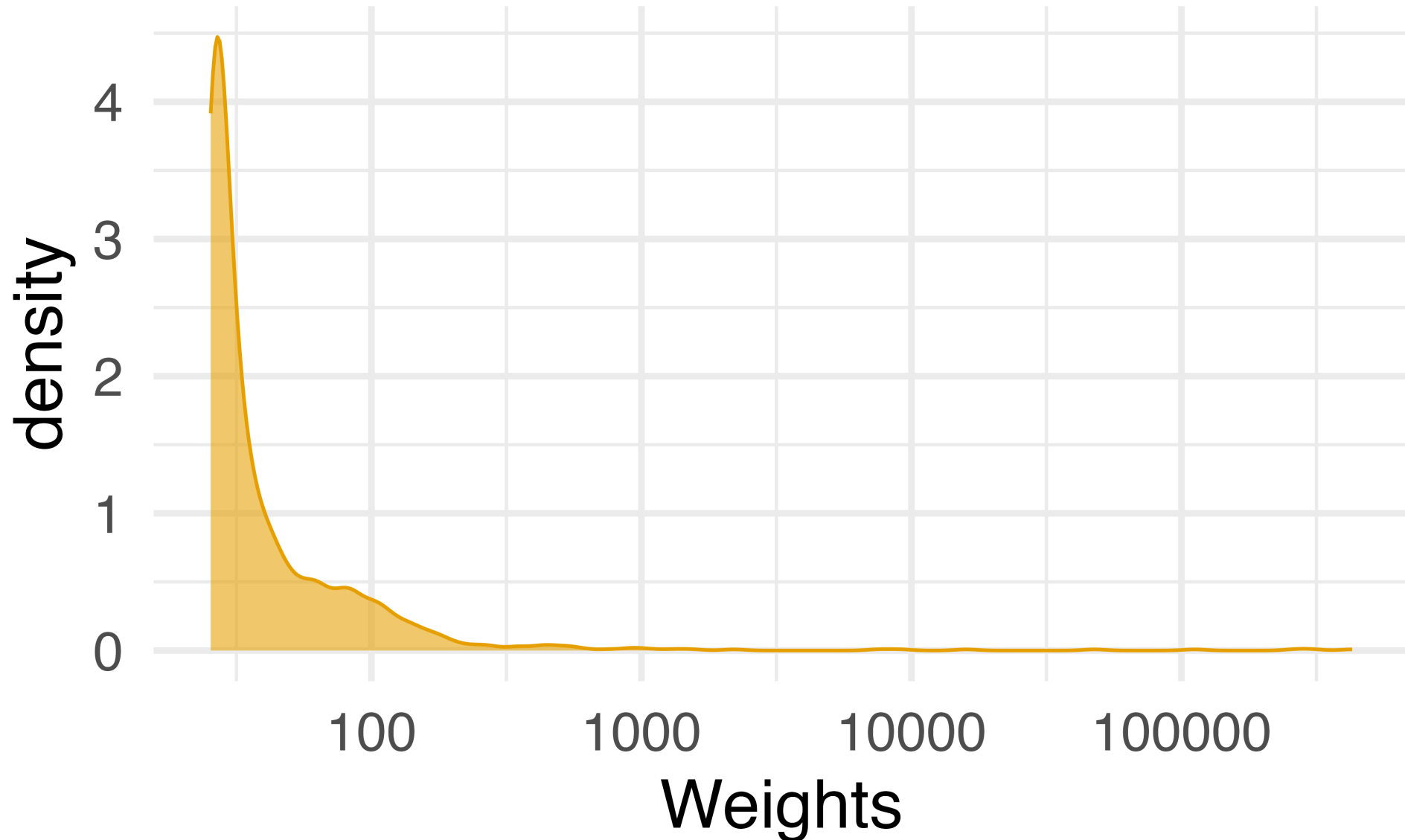
Your Turn 1

```
1 post_time_model <- lm(  
2   avg_spostmin ~  
3     close + extra_magic_morning +  
4     weather_wdwhigh + wdw_ticket_season,  
5   data = wait_times  
6 )
```

Your Turn 1

```
1 wait_times_wts <- post_time_model |>
2   augment(data = wait_times) |>
3   mutate(wts = wt_ate(
4     avg_spostmin, .fitted, .sigma = .sigma
5   ))
```


Stabilizing extreme weights



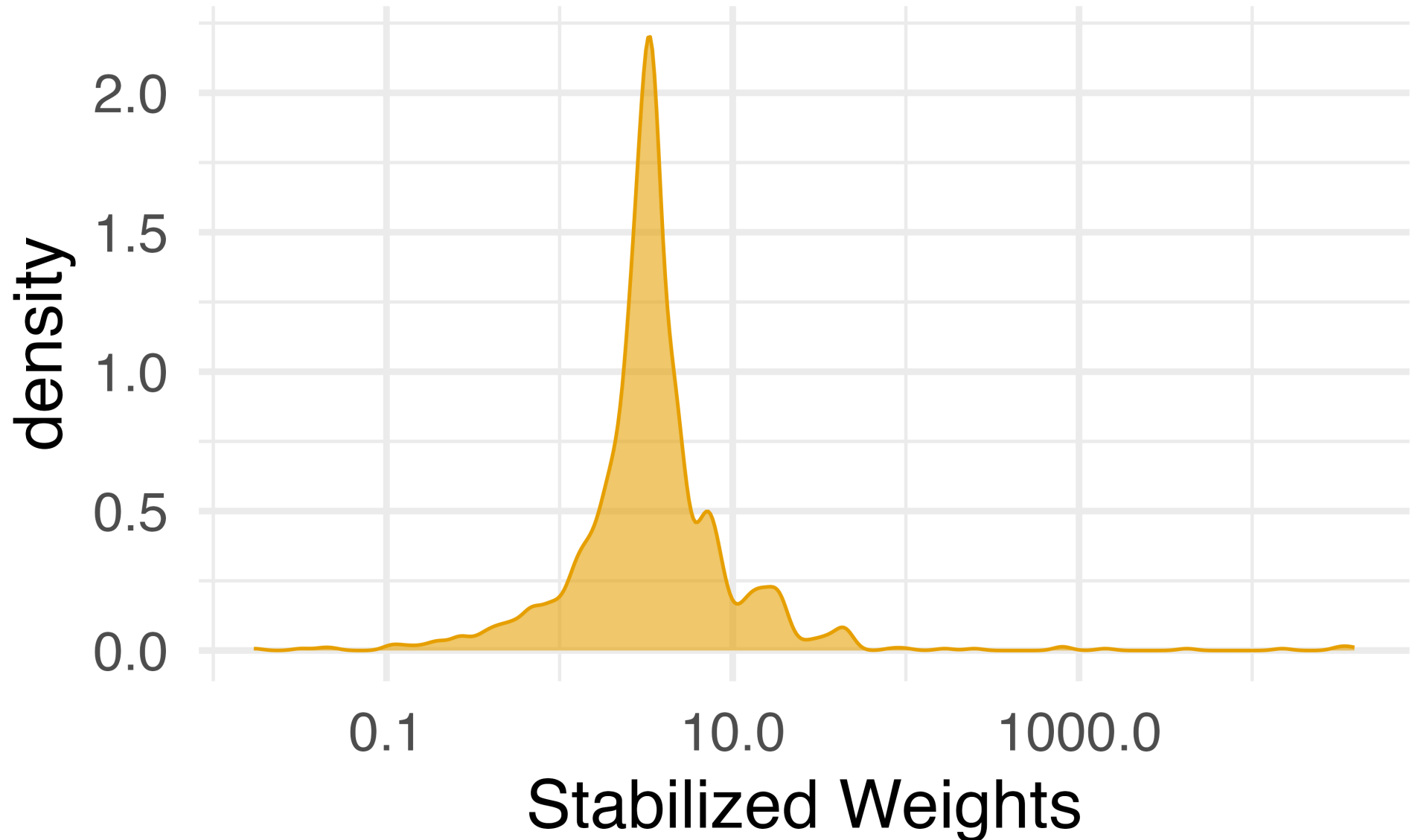
Stabilizing extreme weights

- 1 Fit an intercept-only model (e.g. `lm(x ~ 1)`) or use mean and SD of x
- 2 Calculate weights from this model.
- 3 Divide these weights by the propensity score weights.
`wt_ate(..., stabilize = TRUE)` does this all!

Calculate stabilized weights

```
1 nhefs_swts <- nhefs_model |>
2   augment(data = nhefs_light_smokers) |>
3   mutate(swts = wt_ate(
4     smkintensity82_71,
5     .fitted,
6     .sigma = .sigma,
7     stabilize = TRUE
8   ))
```

Stabilizing extreme weights



Your Turn 2

Re-fit the above using stabilized weights

Your Turn 2

```
1 wait_times_swts <- post_time_model |>
2   augment(data = wait_times) |>
3   mutate(swts = wt_ate(
4     avg_spostmin,
5     .fitted,
6     .sigma = .sigma,
7     stabilize = TRUE
8   ))
```

Fitting the outcome model

- 1 Use the stabilized weights in the outcome model. Nothing new here!

```

1  lm(
2    wt82_71 ~ smkintensity82_71,
3    weights = swts,
4    data = nhfs_swts
5  ) |>
6    tidy() |>
7    filter(term == "smkintensity82_71") |>
8    mutate(estimate = estimate * -10)

```

A tibble: 1 × 5

	term	estimate	std.error	statistic	p.value
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>
1	smkintensity82_71	1.99	0.0316	-6.30	4.33e-10

Your Turn 3

Estimate the relationship between posted wait times and actual wait times using the stabilized weights we just created.

Your Turn 3

```
1 lm(  
2   avg_sactmin ~ avg_spostmin,  
3   weights = swts,  
4   data = wait_times_swts  
5 ) |>  
6 tidy() |>  
7 filter(term == "avg_spostmin") |>  
8 mutate(estimate = estimate * 10)
```

A tibble: 1 × 5

	term	estimate	std.error	statistic	p.value
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>
1	avg_spostmin	-3.47	0.0836	-4.15	0.0000805

Diagnosing issues

- 1 Extreme weights even after stabilization
- 2 Bootstrap: non-normal distribution
- 3 Bootstrap: estimate different from original model

More info

[**https://github.com/LucyMcGowan/writing-positivity-continous-ps**](https://github.com/LucyMcGowan/writing-positivity-continous-ps)

