

# G-Computation

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Normal regression estimates associations. But we want *causal* estimates: what would happen if *everyone* in the study were exposed to x vs if *no one* was exposed.

# G-Computation/G-Formula

- 1 Fit a model for  $y \sim x + z$  where  $z$  is all covariates
- 2 Create a duplicate of your data set for each level of  $x$
- 3 Set the value of  $x$  to a single value for each cloned data set (e.g  $x = 1$  for one,  $x = 0$  for the other)

# G-Computation / G-Formula

# ***Advantages of the parametric G-formula***

Often more statistically precise than propensity-based methods

Incredibly flexible

Basis of other important causal models, e.g. causal survival analysis and TMLE

# Greek Pantheon data (greek\_data)

The name of a Greek god	A prognostic factor	The treatment, a heart transplant	The outcome, death
Rheia	0	0	0
Kronos	0	0	1
Demeter	0	0	0
Hades	0	0	0
Hestia	0	1	0
Poseidon	0	1	0
Hera	0	1	0
Zeus	0	1	1
Artemis	1	0	1
Apollo	1	0	1

+ 10 more rows

# 1. Fit a model for $y \sim a + 1$

```
1 greek_model <- lm(y ~ a + 1, data = greek_data)
```

# 2. Create a duplicate of your data set for each level of a

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Apollo	1	0	1

# 3. Set the value of **a** to a single value for each cloned data set

The name of a Greek god	A prognostic factor	a	The outcome, death
Rheia	0	0	0
Kronos	0	0	1
Demeter	0	0	0
Hades	0	0	0
Hestia	0	0	0
Poseidon	0	0	0
Hera	0	0	0
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Hera	0	1	0
Zeus	0	1	1
Artemis	1	1	1
Apollo	1	1	1

### 3. Set the value of **a** to a single value for each cloned data set

```
1 # set all participants to have a = 0
2 untreated_data <- greek_data |>
3   mutate(a = 0)
4
5 # set all participants to have a = 1
6 treated_data <- greek_data |>
7   mutate(a = 1)
```

## 4. Make predictions using the model on the cloned data sets

```
1 # predict under the data where everyone is untreated
2 predicted_untreated <- greek_model |>
3   augment(newdata = untreated_data) |>
4   select(untreated = .fitted)
5
6 # predict under the data where everyone is treated
7 predicted_treated <- greek_model |>
8   augment(newdata = treated_data) |>
9   select(treated = .fitted)
10
11 predictions <- bind_cols(
12   predicted_untreated,
13   predicted_treated
14 )
```

# 5. Calculate the estimate you want

```
1 predictions |>
2   summarise(
3     mean_treated = mean(treated),
4     mean_untreated = mean(untreated),
5     difference = mean_treated - mean_untreated
6   )
```

# A tibble: 1 × 3

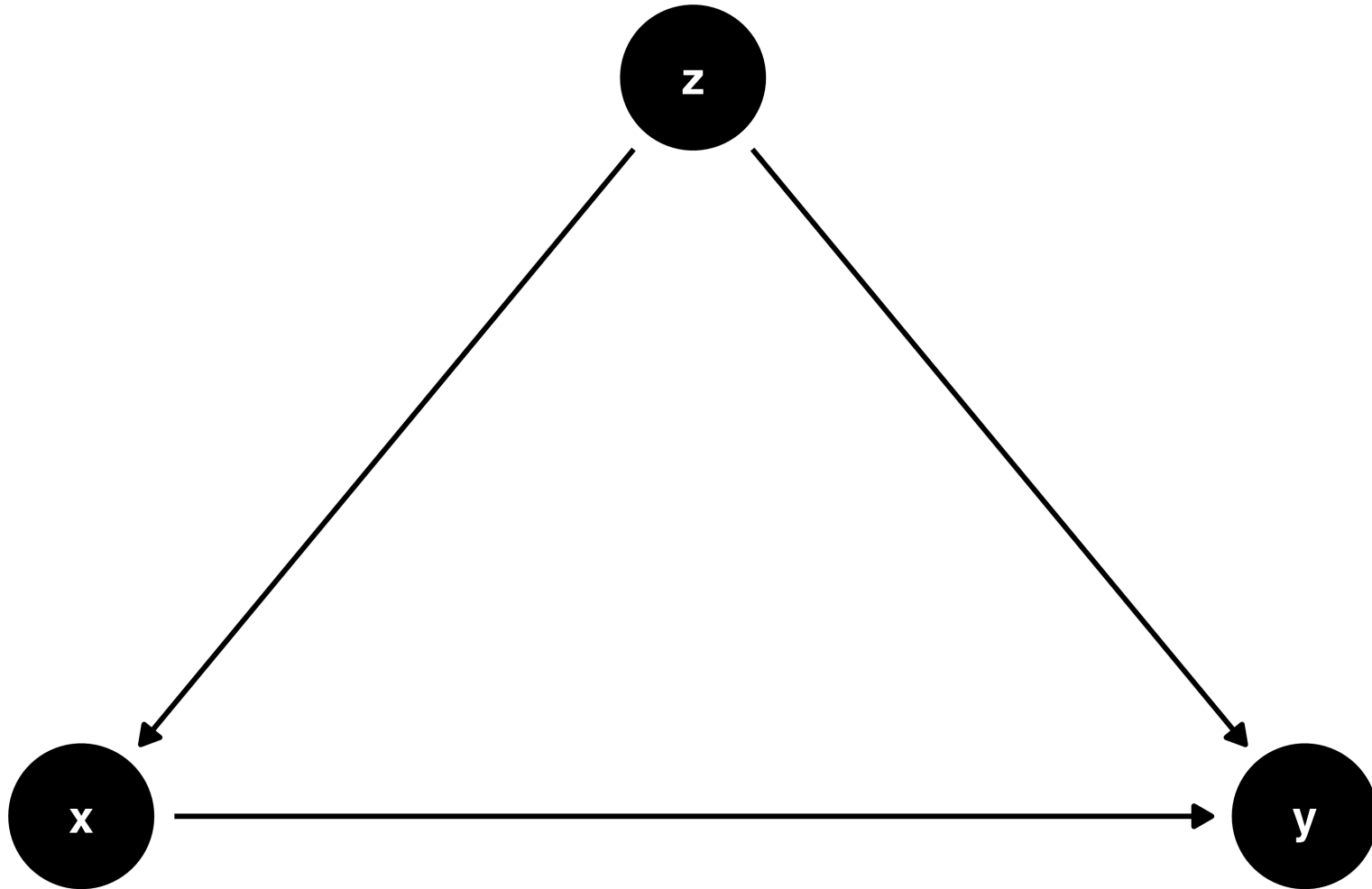
	mean_treated	mean_untreated	difference
	<dbl>	<dbl>	<dbl>
1	0.5	0.5	0

## *Your Turn*

**Work through Your Turns 1-3 in `07-g-computation-exercises.qmd`**

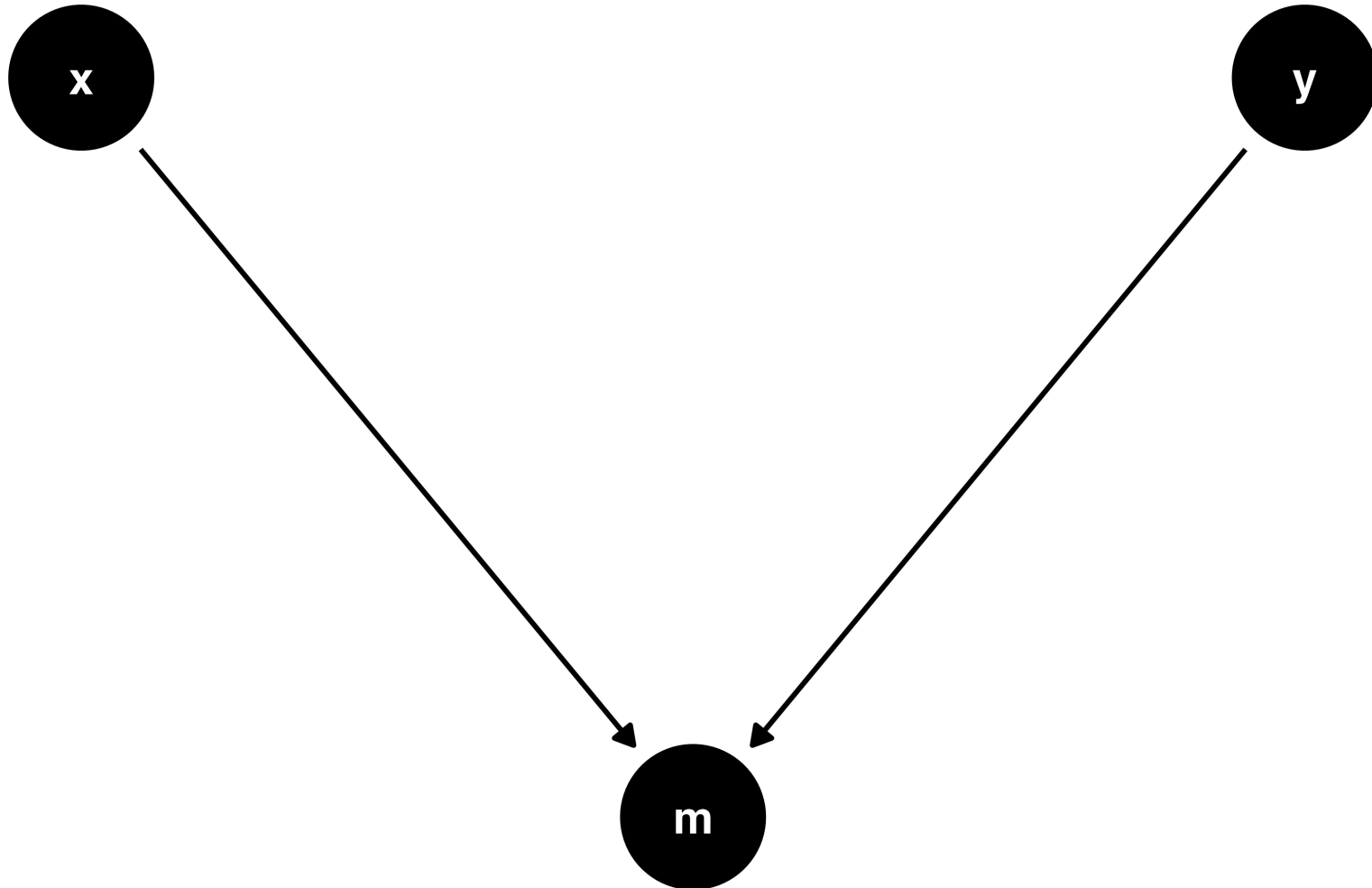
# **Detour:** Colliders, selection bias, and loss to follow-up

# Confounders and chains

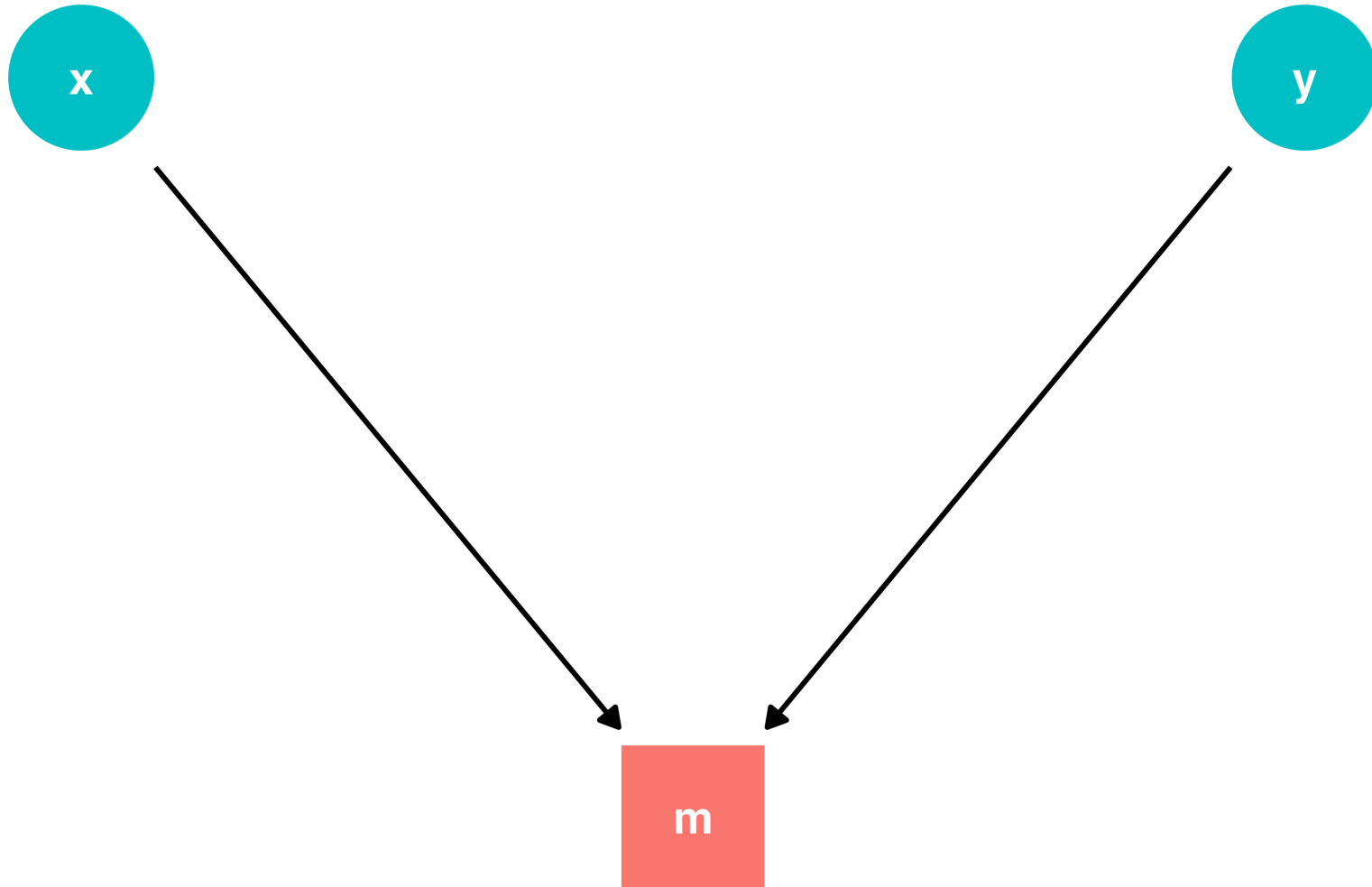




# Colliders



# Colliders



# Let's prove it!

```
1 set.seed(1234)
2 collider_data <- collider_triangle() |>
3   simulate_data(-.6)
```

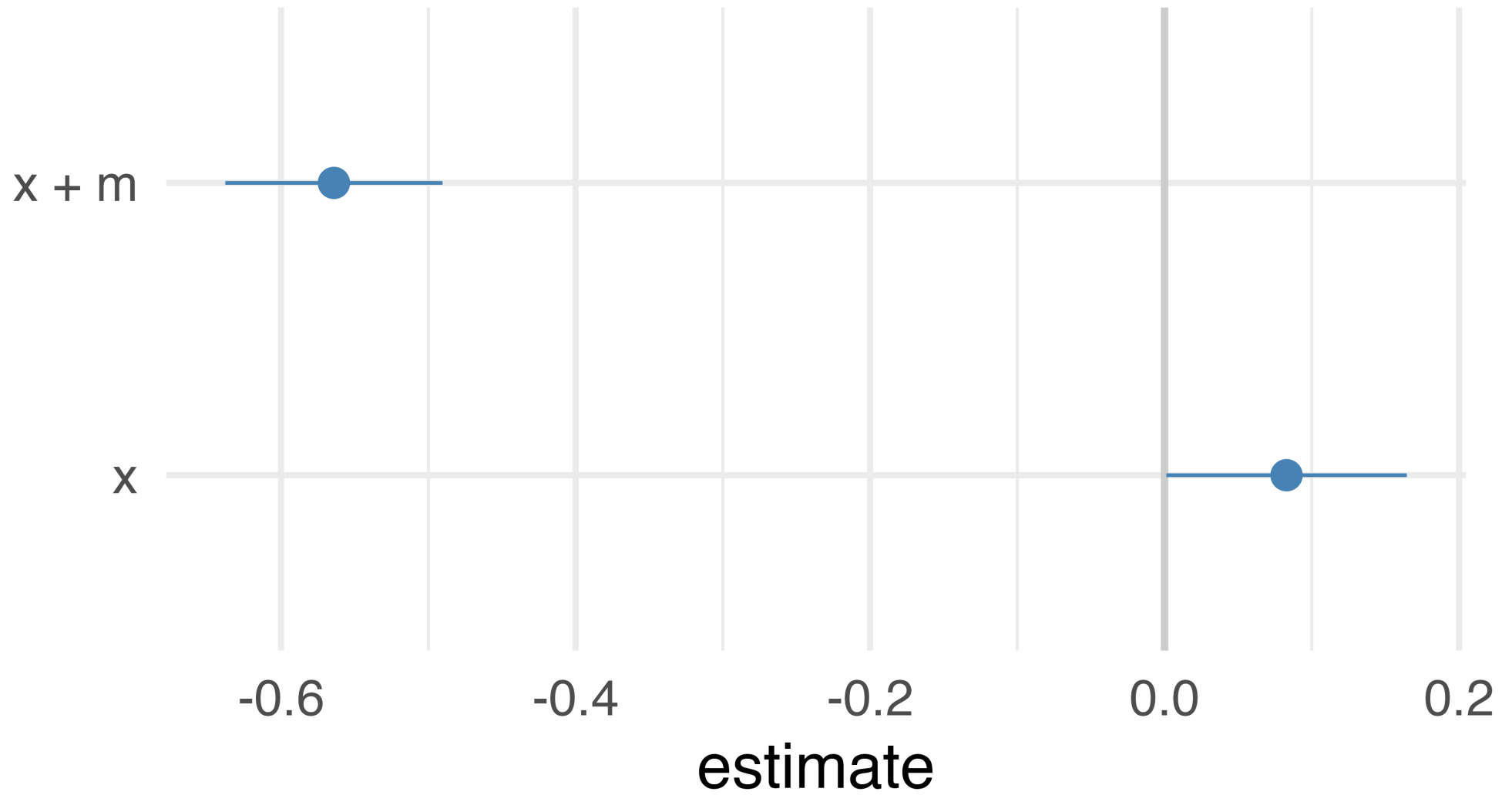
# Let's prove it!

```
1 collider_data
```

```
# A tibble: 500 × 3
```

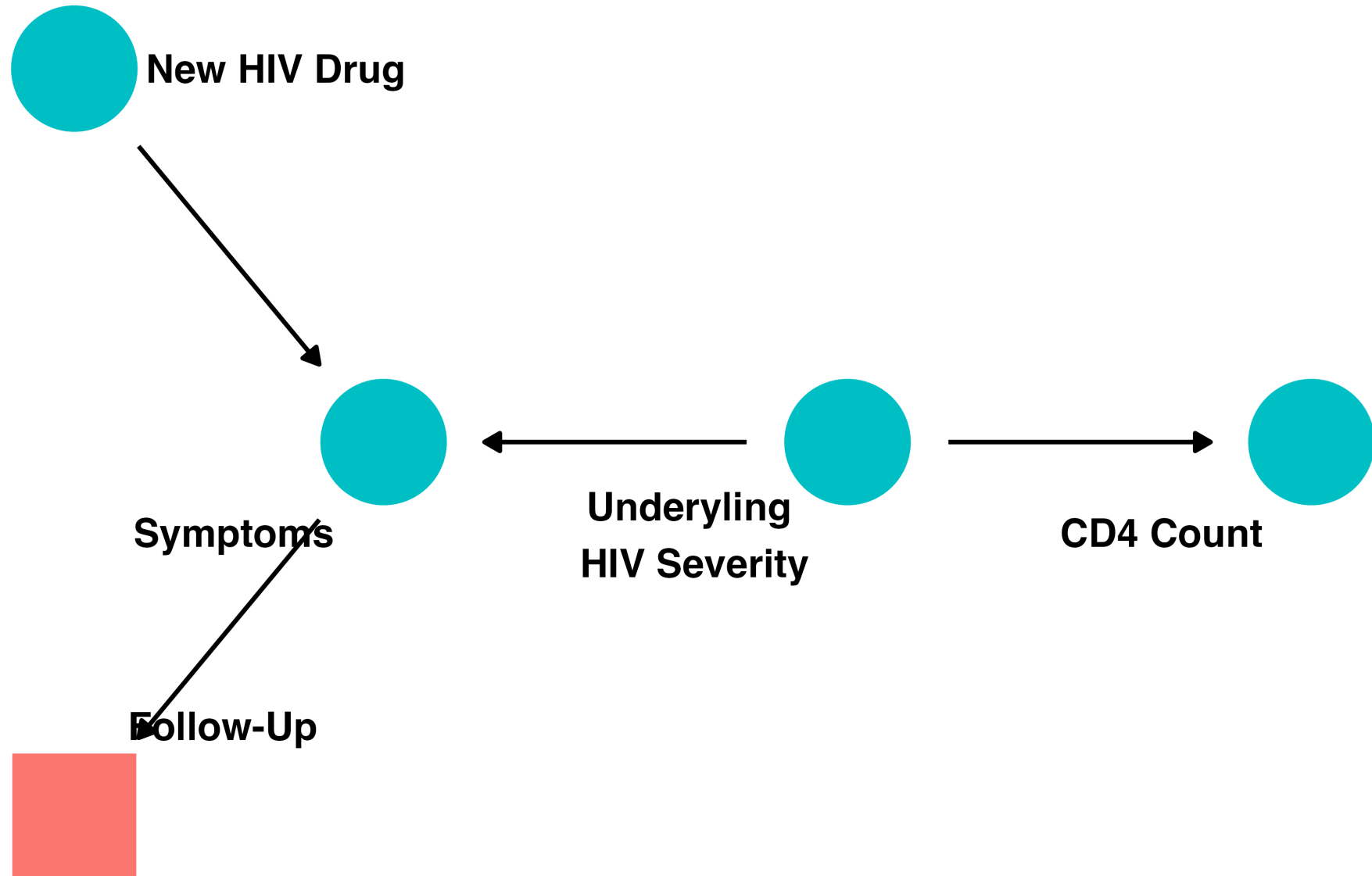
	m	x	y
	<dbl>	<dbl>	<dbl>
1	-0.829	0.359	1.75
2	0.184	0.619	-1.11
3	1.47	-0.940	0.0642
4	-2.43	1.55	1.39
5	0.219	-1.69	0.832
6	1.01	0.199	-0.145
7	-0.811	1.29	-0.872
8	-0.464	0.0675	0.763
9	-0.357	0.264	0.766
10	-0.978	0.531	0.506
" . . . . .			

# Let's prove it!



correct effect size: 0

# Loss to follow-up



# Adjusting for selection bias

- 1 Fit a probability of censoring model,  
e.g. *glm(censoring ~ predictors, family  
= binomial())*
- 2 Create weights using inverse  
probability strategy
- 3 Use weights in your causal model

**We won't do it here, but you can include many types of weights in a given model. Just take their product, e.g. *multiply inverse propensity of treatment weights by inverse propensity of censoring weights.***



## *Your Turn*

**Work through Your Turns 4-6 in 07-g-computation-exercises.qmd**

