

Continuous exposures and g-computation

Malcolm Barrett

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Normal regression estimates associations. But we want *causal* estimates: what would happen if *everyone* in the study were exposed to x vs if *no one* was exposed.

G-Computation/G-Formula

- 1 Fit a model for $y \sim x + z$ where z is all covariates
- 2 Create a duplicate of your data set for each level of x
- 3 Set the value of x to a single value for each cloned data set (e.g $x = 1$ for one, $x = 0$ for the other)

G-Computation / G-Formula

Advantages of the parametric G-formula

Often more statistically precise than propensity-based methods

Incredibly flexible

Basis of other important causal models, e.g. causal survival analysis and TMLE

Greek Pantheon data (greek_data)

| The name of a Greek god | A prognostic factor | The treatment, a heart transplant | The outcome, death |
|-------------------------|---------------------|-----------------------------------|--------------------|
| Rheia | 0 | 0 | 0 |
| Kronos | 0 | 0 | 1 |
| Demeter | 0 | 0 | 0 |
| Hades | 0 | 0 | 0 |
| Hestia | 0 | 1 | 0 |
| Poseidon | 0 | 1 | 0 |
| Hera | 0 | 1 | 0 |
| Zeus | 0 | 1 | 1 |
| Artemis | 1 | 0 | 1 |
| Apollo | 1 | 0 | 1 |

+ 10 more rows

1. Fit a model for $y \sim a + 1$

```
1 greek_model <- lm(y ~ a + 1, data = greek_data)
```

2. Create a duplicate of your data set for each level of **a**

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3. Set the value of **a** to a single value for each cloned data set

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3. Set the value of **a** to a single value for each cloned data set

```
1 # set all participants to have a = 0
2 untreated_data <- greek_data |>
3   mutate(a = 0)
4
5 # set all participants to have a = 1
6 treated_data <- greek_data |>
7   mutate(a = 1)
```

4. Make predictions using the model on the cloned data sets

```
1 # predict under the data where everyone is untreated
2 predicted_untreated <- greek_model |>
3   augment(newdata = untreated_data) |>
4   select(untreated = .fitted)
5
6 # predict under the data where everyone is treated
7 predicted_treated <- greek_model |>
8   augment(newdata = treated_data) |>
9   select(treated = .fitted)
10
11 predictions <- bind_cols(
12   predicted_untreated,
13   predicted_treated
14 )
```

5. Calculate the estimate you want

```
1 predictions |>
2   summarise(
3     mean_treated = mean(treated),
4     mean_untreated = mean(untreated),
5     difference = mean_treated - mean_untreated
6   )
```

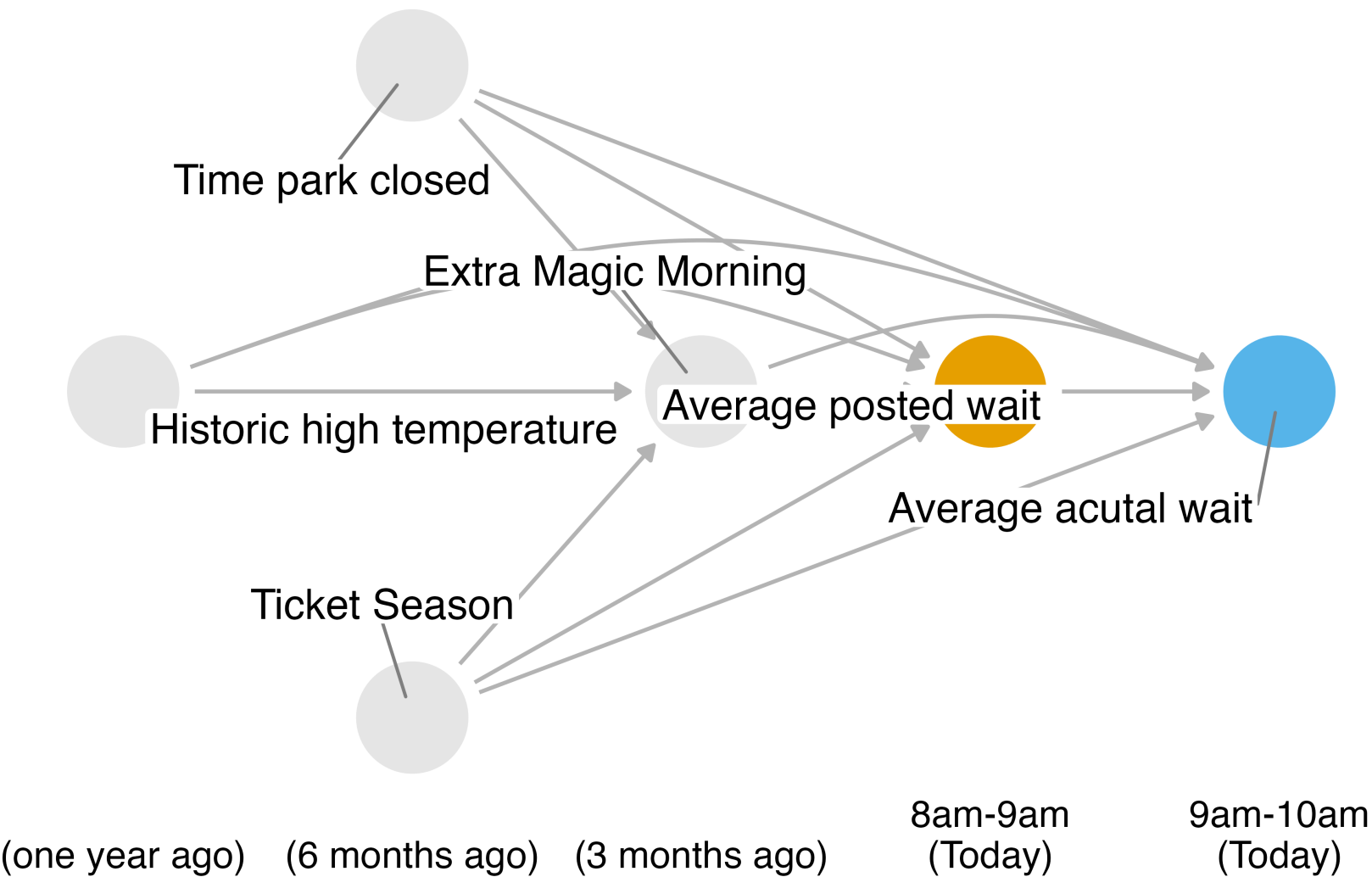
A tibble: 1 × 3

| | mean_treated | mean_untreated | difference |
|---|--------------|----------------|------------|
| | <dbl> | <dbl> | <dbl> |
| 1 | 0.5 | 0.5 | 0 |

Continuous exposures

**We recommend g-computation
over propensity scores for
continuous exposures because of
stability issues**

Do *posted* wait times at 8 am affect *actual* wait times at 9 am?



Your Turn

**Work through Your Turns 1-3 in 10-
continuous-g-computation-
exercises.qmd**

10:00

