Lab 8

Functional languages: compilation for an abstract machine

Objective

Understand the semantics of a toy functional programing language, and:

- $\bullet \ \ discover \ an implementation \ of the \ compilation \ and \ execution \ of the \ abstract \ machine \ seen \ in \ the \ course.$
- · extend it.

First, download the archive.

8.1 Compiling Fun programs for an abstract machine

Discovering the toplevel In this week's archive, there is a toplevel for the compiler and virtual machine seen during the lectures. Hit make to compile it, it should generate a toplevel binary. When you run it, you get a toplevel where you can ask to compile expressions, run bytecode, or compile and run some expressions. The documentation of the options is available with ./toplevel --help. You can find examples of valid source in the repository tests/ of the archive, here is one 1:

```
$ ledit ./toplevel
> c 2 + 2
Cst 2; Cst 2; Add
> cr 2 + 2
> cr 17 + (3 + 42)
62
   Here is the abstract syntax of our (input) language:
(* Syntax of the input language of terms. *)
type expr =
 (* Arithmetic fragment *)
 | Constant of int
 | Addition of expr * expr
 (* Let fragment *)
 | Variable of variable
 | Let of variable * expr * expr (* [Let (x, a, b)] stands for [let x = a in b] *)
 (* Functional fragment *)
 | Function of variable * expr
 | Application of expr * expr
```

EXERCISE #1 \triangleright Abstract machine for Fun

The objective is is to complete the given code in order to be able to compile and execute the whole language:

1. Read the files main.ml syntax.ml and tP.ml in order to become familiar with the syntax of the language and the machine code, and the structure of the code. The compilation into the abstract machine and its evaluation are done in tP.ml.

¹ledit is a one-line editor written in OCaml. It provides line editing for the Caml toplevels, as well as other interactive Unix commands. On the ENS machines you can find it in /usr/bin/.

2. For local definitions, here is the expected output:

```
> c (let x = 1 in x+2)
Cst 1; Let "x"; Access "x"; Cst 2; Add; EndLet
> cr (let x = 1 in x+2)
3
```

Complete the following table that mimics the execution of the compiled program:

Ø Ø	Ø Vint(1)	push the constant on the stack
Ø	Vint(1)	on the stack
Ø	Vint(1)	
	(_)	

Now complete the TP. compile and TP. transition functions.

3. (This is the hardest question of the lab) First, implement the compilation of user-defined functions (declaration, application):

```
> c ((fun x -> x+1) 42)
Cst 42; Closure("x", Access "x"; Cst 1; Add; Ret); App
> c ((let y=2 in fun x -> x+y)) 40
Cst 40; Cst 2; Let "y"; Closure("x", Access "x"; Access "y"; Add; Ret); EndLet; App
```

The compilation of a given function thus only produces an element Closure(var, code).

Then, the objective is to implement the execution steps, so that to obtain:

```
> cr ((fun x -> x+1) 41)
42
> cr ((let y=2 in fun x -> x+y)) 40
42
```

For the execution, you have to use the VClosure of string * code * environment value type for functions, that links together the argument of the function, its code and the environment *at its definition point*. A bit of the execution scheme for functions is depicted in Figure 8.1.

Code	Env.	Stack	Code	Env.	Stack	Comment	
Closure(x,c');c	σ	S	С	σ	$(x,c')[\sigma].s$	a new closure	
						(x,c') on top	
						of stack	
App;c	σ	$(x,c')[\sigma'].v.s$	c'	$(x,v).\sigma'$	c.\sigma.s	push the	
						code and	
						initial env	
Ret;c	σ	$v.c'.\sigma'.s'$	c'	σ'	v.s	stack top	
						= returned	
						value	

Figure 8.1: Execution scheme for user-defined functions

First do the two following examples by hand:

Code	Env.	Stack
<pre>Cst 41;Closure("x",Acces x;Cst 1; Add; Ret);App)</pre>	Ø	Ø
Closure("x",Acces x;Cst 1; Add; Ret); App	Ø	Vint(41)

Code	Env.	Stack
Cst 40;Cst 2; Let "y"; Closure("x",Acces x;Access	Ø	Ø
y; Add; Ret); EndLet; App (Let code be Acces x; Access		
y; Add; Ret)		
Closure("x",code); EndLet; App (where $fv(code) = \{x, y\}$)	<i>y</i> → 2	VInt40

Now, implement:

• To implement the closure $(x,c')[\sigma]$ that is pushed on the stack you have to produce an element of type VClosure of string * code * environment. The environment which is pushed is the current value of all free variables of the code, that you can compute using the following Ocaml function:

```
let rec fv = function
    | Access s :: rest -> s :: fv rest
    | Closure (_, code) :: rest ->
        fv code @ fv rest
    | _ :: rest -> fv rest
    | [] -> []
```

You only have to filter out the current environnement values to only get track of these free variable values.

- To implement the App part, you have to recover the VClosure and the argument on top of stack, localy bind the argument to its value in the environment. Use the following trick to push the remaining code c and the initial environment σ on the stack: push a VClosure("_", c, σ) (an anonymous special closure).
- For Ret, there should be a value followed by the special closure on top of stack. You only have to recover the initial environment and code, that are stored in this special closure.
- 4. Manually compile the expression print 2 (where print is to be considered as a variable name)
- 5. The VBuiltin value type is used to represent concrete operations (like print). Explain how the transition for the App instruction when the function is not a VClosure but a VBuiltin will be implemented.

An example of such builtins is print defined in TP.builtins, which is an initial environment the machine is loaded with when running code (See main.ml around line 80).

Implement the transition for the instruction App when there is a VBuiltin on the stack (instead of a VClosure). Check that this works on the compiled form of print 2:

```
> r Cst 2; Access "print"; App
2
0
```

6. Test your code against the examples in tests/ and write your own ones:

```
./toplevel <tests/arith.test
```

7. Introduce a mistake in your compiler, by adopting the following wrong transition rule for the App machine instruction:

Code	Environment	Stack	Code	Environment	Stack	
App;c	σ	$(x,c')[\sigma'].v.s$	c'	$(x, v).\sigma$	c.\sigma.s	

The mistake is in the Environment after the transition, right?

Invent a Fun program that, when run on this erroneous machine, yields an unexpected result, thus showing the bug.

8. Add references to the language by introducing a new kind of (stack) value: VRef of value ref. Add three builtins operations to the builtins list, namely ref, get and set that mimick the ML operations ref, ! and :=.

8.2 Recursion

EXERCISE #2 ► Adding recursive definitions.

We want here to extend our compiler to handle the definition of recursive functions of the following form: let rec $f = fun \ x \rightarrow e1 \ in \ e2$ where f can be used in e1 (and in e2, of course).

- 1. Suppose that we compile letrec like let (and hence a recursive function like a plain function). What will be the problematic transition in the abstract machine if we do so? (You can explain this on an example)
- 2. (*More difficult*) Extend the definitions in files syntax.ml and tP.ml to handle recursive definitions of the form given above.

For this, a solution is to have a new kind of value. In absence of recursion, values are either integers or closures of the form $(x,c)[\sigma]$ (see definition of type value in the file syntax.ml). To handle recursion, we also have values of the form $Rec(f)(x,c)[\sigma]$ (a closure to represent recursive function f).

The transition rule for instruction Access(x) is changed: instead of just looking up in the environment σ , and returning $\sigma(x)$:

- we return v in case $\sigma(x) = v$ and v is either an integer or a plain closure (as before);
- if on the other hand $\sigma(x) = Rec(f)(x,c)[\sigma]$, we return a closure $(x,c)[\sigma']$, where σ' is defined according to the behaviour we expect for a recursive definition.
- (a) Explain the run steps on the following example (that does not terminate):

```
let rec pr = fun n-> print n+pr (n+1) in pr 0
```

- (b) Describe the behaviour of Access(x) in the case where $\sigma(x) = Rec(f)(x,c)[\sigma]$ (this amounts to defining σ' as introduced above).
- (c) Accordingly, define the compilation of a recursive definition, in which a value of the new form is added to the environment.
- (d) Implement, test!
- (e) (hard) Is it possible to get rid of those $Rec(f)(x, c)[\sigma]$ values? (Only to keep regular closure).