

Operations with matrices using c#

The resulting program is able to:

- Add — adding two matrices of the same size.
- Mult — multiplying two matrices of the same size.
- Inverse — matrix inverse.
- Det — compute the determinant of a matrix.

For adding and multiplying the algorithm is direct. The complexity of mult is $O(n^3)$. There is also a Strassen algorithm with complexity $O(n^{2.8})$ which works better on big square matrices, but I decided not to use it.

Inverse:

For the matrix inverse, I used the adjugate matrix (also called the classical adjoint) and the cofactor matrix. There is a theorem which says:

$$A^{-1} = 1/\det(A) \cdot \text{adj}(A)$$

Testing data:

6 6 6

0 12 12

0 0 18

Result:

6 -3 0

0 3 -2

0 0 2

Determinant:

For finding the determinant I use a recursive algorithm, the complexity of which is $O(n!)$. It finds determinants of smaller sizes ($n-1$, $n-2$, ... up to 1) and use Laplace expansion.

Testing data:

2 4 6

2 4 4

3 3 7

Result: -12.

2 0 1

3 4 5

7 0 8

Result: 36.