Tutorial Introduction to Neural Networks with an eye towards linguistic applications

Shane Steinert-Threlkeld

January 25, 2019









Today's Plan

- 1. Neural Networks: computation
- 2. Neural Networks: learning
- 3. Hands-on experiment: learning quantifiers
- 4. Some practical tips
- 5. Further Topics + Resources

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- 1. Neural Networks: computation
- 2. Neural Networks: learning
- 3. Hands-on experiment: learning quantifiers
- 4. Some practical tips
- 5. Further Topics + Resources

Goals:

- enough background and material so that you can begin playing around with your own experimental ideas by the end of today
- develop a bit of a map of the field, with pointers to where to go next

Some mathematical notation/concepts from:

- Linear algebra (matrix multiplication, e.g.)
- Multivariate calculus (partial derivatives)
- Logic / formal semantics of natural language

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- Basic syntax in NumPy

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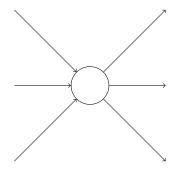
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- Basic syntax in NumPy

But: no formal requirements; all concepts and syntax can be explained intuitively, so please ask for clarification at all points!

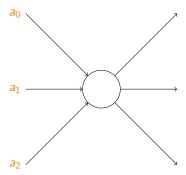
Materials: Slides + Jupyter Notebook

https://github.com/shanest/nn-tutorial

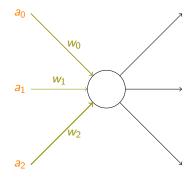
Artificial Neuron

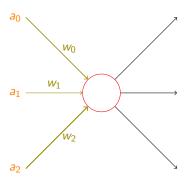


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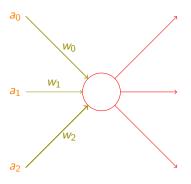


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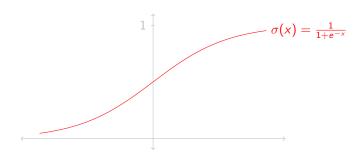




$$a = f(a_0 \cdot w_0 + a_1 \cdot w_1 + a_2 \cdot w_2)$$

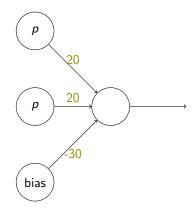


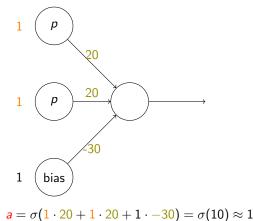
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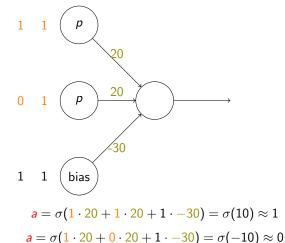
More on choosing activation functions later in the tutorial.

p	q	$p \wedge q$
1	1	1
1	0	0
0	1	0
0	0	0

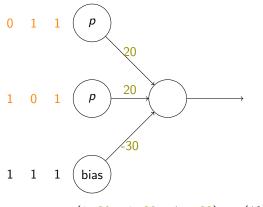




NNs: Computation 00000000000



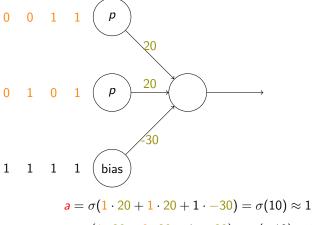
NNs: Computation



$$a = \sigma(1 \cdot 20 + 1 \cdot 20 + 1 \cdot -30) = \sigma(10) \approx 1$$
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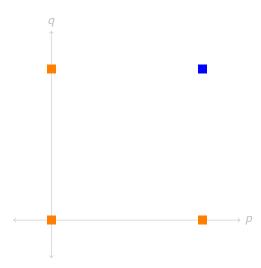
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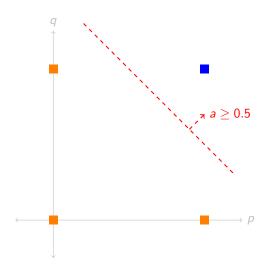


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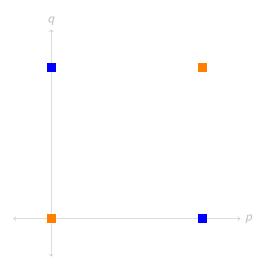
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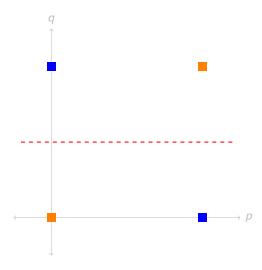
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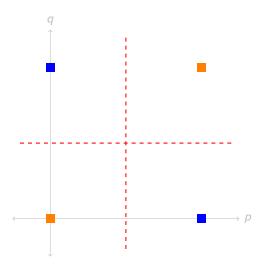


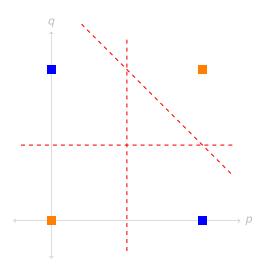


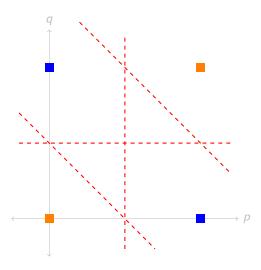
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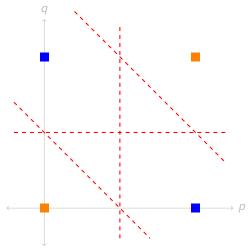




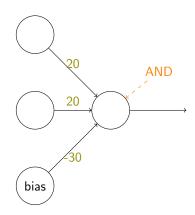


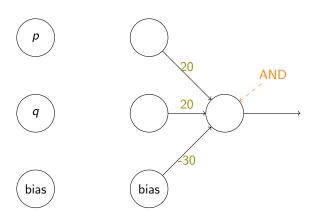


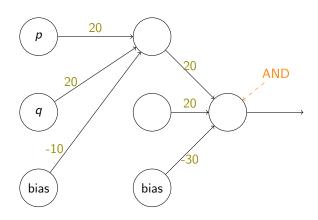


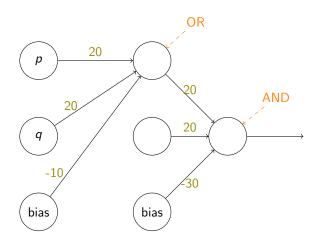


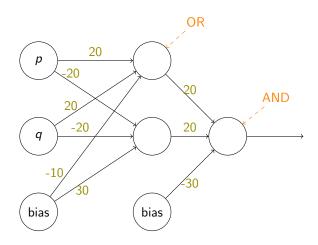
xor is not *linearly separable*

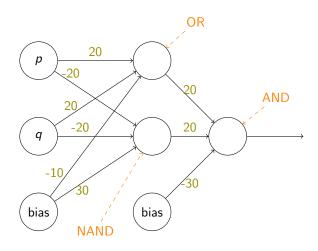


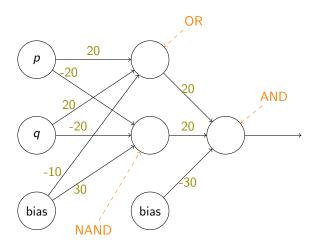




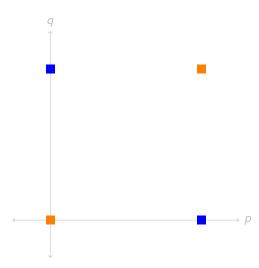




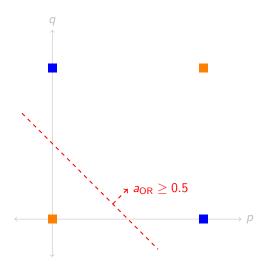




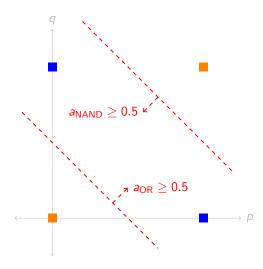
Exercise: show that the hidden units behave as labeled.



Computing 'xor'



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Computing Many Examples

NNs: Computation 00000000000

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Exercises:

NNs: Computation

- write down W^1 and W^2 for the xor network.
- re-write the above as f(xW) by adding a column of 1s to x and a new row to W.

Hidden Representations

Key idea: hidden layers of a neural network can encode high-level/abstract features of the input.

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The last step is done via gradient descent (and refinements thereof).

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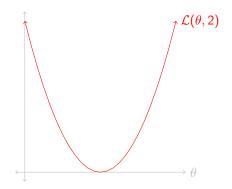
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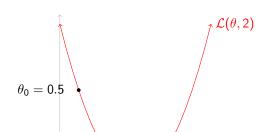
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Loss function:

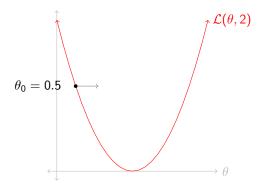
$$\mathcal{L}(\theta, y) = (\hat{y}(\theta) - y)^2$$



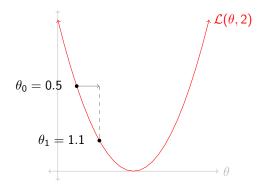
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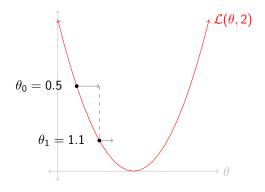
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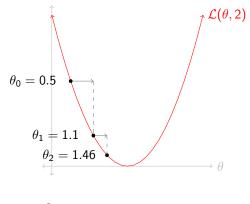
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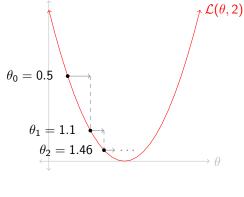
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A neural network computes a complex function of its input. For an L-layer feed-forward network:

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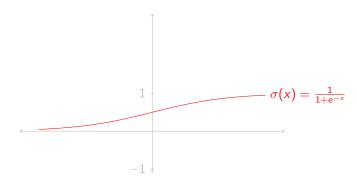
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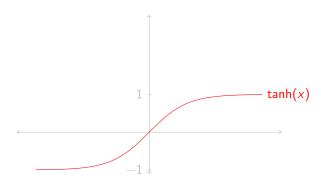
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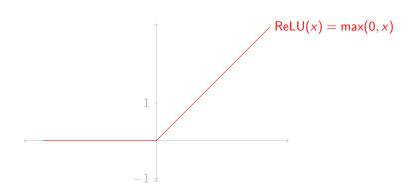
The (negative) gradient tells us which direction in 'parameter space' to walk in order to make the loss (\mathcal{L}) smaller, i.e. to make the network's output closer to the true output.

Activation Functions



Activation Functions





ReLUs are incredibly popular at the moment, as are refinements: softplus, leaky ReLU, exponential linear (ELU), gaussian linear (GLU), ...

Hahnioser et al. 2000; Glorot, Bordes, and Bengio 2011

Loss Functions

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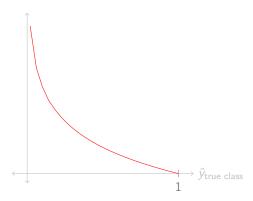
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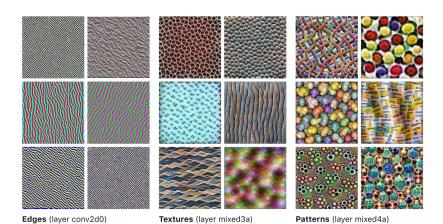
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Example of Learned Hidden Layers



Olah, Mordvintsev, and Schubert 2017; Yosinski et al. 2014 https://distill.pub/2017/feature-visualization/

Learned Representations

Key idea: a neural network can learn *which* high-level/abstract features of the input are useful in helping it solve its task. (Features are learned, instead of engineered by us.)

Anatomy of a DL Experiment

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 - Measure your variables of interest
 - Monitor train/test loss
 - Early stopping [later in tutorial]
- Analyze
 - quantitative
 - qualitative behavior

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NOTE: keep detailed records about what you're doing! For guidance on keeping records and writing up results, see these lecture notes from Sam Bowman.

To the code!

https://github.com/shanest/nn-tutorial/blob/master/tutorial.ipynb

Balancing the Data

For classification tasks, it's very important to *balance the training data*, so that it contains (roughly) equal numbers of examples for each class. Otherwise, a network can very quickly get stuck in a local minimum, where it uniformly guesses the most-frequent class.

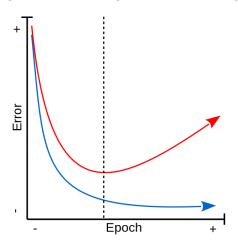
Two methods:

- ① Downsampling: randomly sample as many examples from each class as in your least-frequent class
- ② Upsampling: repeat examples from your less-frequent classes until you have as many as the most-frequent

Over-fitting: detection

Neural networks, especially very large, deep ones, run the risk of *over-fitting* ("memorizing") their training data.

Evidence: training loss continues to go down, while testing loss rises.

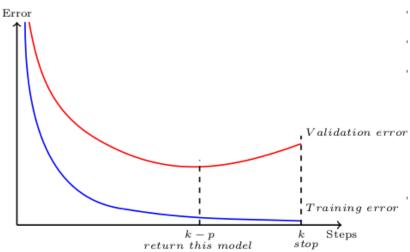


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How do you know how many epochs to train for? One common method: A LOT, but put in a condition for *early stopping*.

- Record test performance every N epochs
- Save best performing model.
- If performance doesn't improve after P epochs, quit training.
 [Note: P for 'patience']

Over-fitting: avoidance (regularization)

Two very popular and successful *regularization* techniques to combat over-fitting (and generally make your life better):

- L2 regularization: add a term $\lambda ||\theta||_2^2$ to loss function.
- Dropout (Srivastava et al. 2014): randomly 'turn off' (set to 0) a certain percentage of input nodes to this layer
- Batch normalization (loffe and Szegedy 2015): scale the inputs to the layer so that they're roughly averaged around 0 and normally distributed.

(I've found BN very useful in my own research.)

Note: .eval() and .train() on a PyTorch nn.Module turn these sorts of methods off/on based on whether you are in training or 'inference' / prediction mode.

Hyper-parameter Tuning

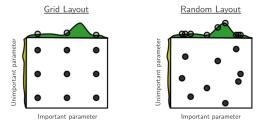
How do you decide how to set the parameters of your experiment? There are so many knobs to turn! (Listed roughly in order of importance of turning them.)

- 1 Network architecture: depth (number of layers) and width (size of layers)
 [architecture | different network types alterether]
- [or even different network types altogether]
- 2 Activation functions
- Optimizers
 - Learning rates + other parameters here
- 4 . . .

Hyper-parameter Tuning (cont.)

Main idea: try a whole bunch of settings! Choose the setting that performs best. Some notes:

- This requires a third set, a *development (dev)* set, in addition to training/testing.
 - You choose the best hyper-parameters based on best performance (however measured) on the *dev* set. Then you evaluate that model on the *test* set.
- Random search in parameter space better than 'grid' search:



Bergstra and Bengio 2012

Scaling Up

Once models and datasets become non-trivially sized, your personal computer likely won't suffice to run experiments.

A common paradigm: prototype locally, experiment externally on a 'cluster'.

Two most critical components:

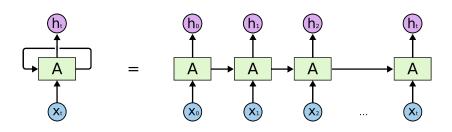
- Large RAM for storing big models and datasets
- GPUs (Graphics Processing Units)!
 These are made to massively parallelize linear algebra of the kind computed by networks, so can dramatically speed up training and inference.

If you can't access these things via your institution, you can buy compute time on appropriate machines via Amazon Web Services or Google Cloud Platform.

NNs: Computation

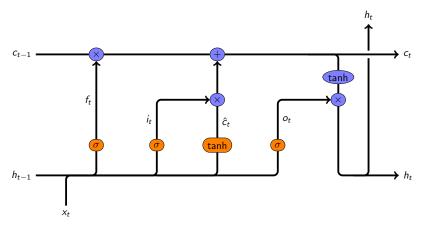
Processing Sequences: Recurrent Neural Networks

Processing sequences (of variable length) is crucial for applying neural networks to text!



http://karpathy.github.io/2015/05/21/rnn-effectiveness/ http://colah.github.io/posts/2015-08-Understanding-LSTMs/

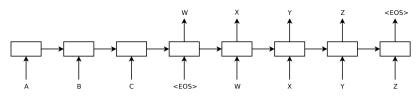
Long Short-Term Memory Network



Hochreiter and Schmidhuber 1997

Sequence-to-Sequence Models

Widely used in machine translation, dependency parsing, semantic parsing, . . .



Sutskever, Vinyals, and Le 2014

Semi-Supervised + Transfer Learning

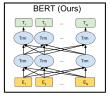
• (Un-/Semi-)supervised: no 'true output', predict some piece of the input from some other piece.

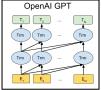
E.g.: *language modeling*, predict $P(w_t|w_{t-k},...,w_{t-1})$.

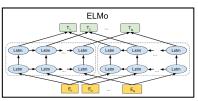
Semi-Supervised + Transfer Learning

- (Un-/Semi-)supervised: no 'true output', predict some piece of the input from some other piece.
 - E.g.: language modeling, predict $P(w_t|w_{t-k},...,w_{t-1})$.
- Transfer learning: train a model on one task, 'fine tune' it on the task you care about.
 - Very successful in computer vision.
 - "NLP's ImageNet moment has arrived."
 - (https://thegradient.pub/nlp-imagenet/)

Transfer Learning in NLP



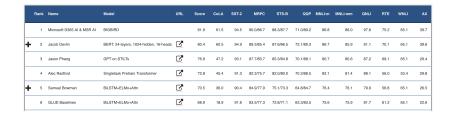




Devlin et al. 2018; Radford et al. 2018; Peters et al. 2018 http://jalammar.github.io/illustrated-bert/

Further Topics + Resources

Transfer Learning in NLP



https://gluebenchmark.com/

Further Resources

General references:

- Nielsen 2015
- Goodfellow, Bengio, and Courville 2016
- http://3blue1brown.net/neural-networks

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Bleeding edge papers:

- arXiv [cs.CL, cs.LG, cs.Al]
- Conference proceedings: ACL, EMNLP, NeurIPS, ICML, ICLR

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Google is your friend (and GitHub too)! Blog posts (incl. from places like OpenAI, DeepMind, Google Brain, AllenAI) are very popular in the DL world, often including break-downs and sample implementations of models from papers.

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