

Capabilities for Effects

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Formalism by Aaron Craig as Undergraduate Thesis student at VUW in
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CAPABILITY-FLAVOURED EFFECTS

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Capability Safety

- Capability-safe languages prohibit ambient authority
 - All authority derives from previous authority, starting at the entry point of the program
 - A component can't exercise authority unless you give it a capability to do so
- Can be used to quantify risk of executing code [Drossopolou] and ensure least privilege [Saltzer]
- Do capabilities help existing formal reasoning techniques, such as effects?

Effects

- Describe “intensional information” about how a program executes (Neilson & Nelson)
 - $\text{Int} \rightarrow \text{Int}$ (unannotated function type)
 - $\text{Int} \dashv\!\!\!-\{\text{File.write}\} \rightarrow \text{Int}$ (annotated function type)
- Limited mainstream use; too verbose? (Rytz)
- Inference helps reduce verbosity
 - Need to analyse source code
 - Back to manual reasoning if it fails

Capability-Flavoured Effects

- In a capability-safe setting, any effect on a resource must happen through a capability
 - By tracking capabilities, we also track effects
 - What can we say at the boundary where annotated code passes capabilities into unannotated code?
-
- `import(File.append)
 logger: String -{File.append}→ Unit
in
 e // arbitrary, unannotated code`

Capability-Flavoured Effects

- Can safely determine effects of unannotated code by inspecting the capabilities we give it
 - Only have to inspect its type, not its source code
- Effect-conscious capability-safe code can reason about what untrusted, capability-safe code will do
- Our work: formulates a minimal, sound lambda calculus and type system to demonstrate this

Imports

```
import(File.append)
  log: String -{File.append}→ Unit
in
  log("doing some logging")
```

- Pass in capabilities, execute unannotated code
- Unannotated code must type with *exactly* the free variables imported
- Programmer *selects* authority as {File.*}
- Statically: accept/reject, if {File.*} is a safe upper-bound on effects

Multiple Imports

```
import(File.*)
  makeFile: Unit -{File.create}→ Unit
  pureApply: (Unit -Ø→ Unit) -Ø→ Unit
in
  pureApply(makeFile)
```

- Input to `pureApply` has same type as `makeFile` (modulo effect annotations)
- Don't want `pureApply` to violate its annotation by incurring a `File.create` effect in the unannotated code
- Need to ensure all imports are allowed the selected authority before passing them in

Higher-Order Effects

- Regular effect: you possess capability for effect
- Higher-order effect: allowed to incur effect, but you need to be given the capability

```
... // some omitted set up code
def log(msg: String, sock: Socket) =
    file.append("hello")
    sock.append("they're logging")
```

- Assuming this typechecks...
 - `File.append` is a regular effect
 - `Socket.append` is higher order

Higher-Order Safety

- An annotated type τ is *higher-order safe* for a set of effects ε if $\varepsilon \subseteq \text{ho-effects}(\tau)$
- Intuitively: an expression of type τ must be allowed to incur the effects in ε
- To safely check an import, all imports must be higher-order safe for the selected authority

```
import(File.create)
  makeFile: Unit -{File.create}→ Unit
  pureApply: (Unit -Ø→ Unit) -Ø→ Unit
in
  pureApply(log)
```

Return Types

- Unannotated code might return a function/capability
- Need to annotate it with effects to safely effect-check rest of annotated code

```
let result =  
  import(File.*)  
  f: {File}  
  in  
    def tricky(): Unit =  
      f.write("hello")  
  result()
```

- The type of `tricky` is `Unit → Unit`, which annotates as `Unit -{File.*}→ Unit`

Return Types

- Unannotated code might return a function that can later be used elsewhere in the annotated world
- Need to understand what effects it has to safely effect-check annotated code using it

```
import(File.*)
f: {File}

in

def tricky(): Unit =
  f.write("hello")
```

- The type of `tricky` is `Unit → Unit`, which annotates as `Unit -{File.*}→ Unit`

Returning Higher-Order Effects

```
import(File.*)
      f: {File}

in

def myFunc(msg: String, s: Socket): Unit =
  s.write("they're logging")
  f.write(msg)
```

- Safe to execute this code
- Unsafe to annotate return type with `{File.*}`
- Must make sure return type doesn't ask for a capability (`Socket`) whose effects haven't been selected
 - This example rejects because `String → Socket → Unit` has the higher-order effects `{Socket.*}`

Polymorphic Types

- Polymorphic types let you write type-generic code
- Polymorphic effects let you write effect-generic code

```
// Define a new effect to simplify function definition
effect write = {File.write, Socket.write}

// Takes a write function, uses it to write a message, logs
def writeData<φ ⊑ write>(s: String, write: String -φ→ Unit) =
  write(s)
  file.append("wrote to writer")

type WriteDataFunc = typeof(writeData)
```

Polymorphic Imports

```
effect write = {File.write, Socket.write}
import(File.append, File.write, Socket.write)
    writeData: WriteDataFunc<write>
    fwriter: String -{File.write, File.append}→ Unit
in
e
```

- Can approximate effects of `writeData` with its polymorphic upper bound `{File.write, Socket.write}`
- Can approximate effects of the unannotated code as `{File.append, File.write, Socket.write}`

Polymorphic Imports

- Lots of generic code doesn't have an upper bound on its possible effects
 - map, fold/reduce, filter, zip, collections
- To incur an effect with generics you must instantiate with something concrete that can invoke the effect
 - Capability for the effect must have been imported
- Can tighten the upper-bound by looking at other capabilities that have been imported

Polymorphic Imports

```
effect write = {File.write, Socket.write}
import(File.append, File.write, Socket.write)
  writeData: WriteDataFunc<write>
  fwriter: String -{File.write, File.append}→ Unit
in
  e
```

- Nothing imported can incur `Socket.write` so we can ignore that as a possibility for `writeData`
- Upper-bound on `writeData` tightens to `{File.write}`
- Better approximation of effects of `e` is `{File.write, File.append}`

Overall

- Capability-safe design enables reasoning at module boundaries about the effects of unannotated code
- Must restrict capabilities passed in based on their higher-order effects
- Finer reasoning needed for useful polymorphics

Paper by Aaron Craig, Alex Potanin, Lindsay Groves, and Jonathan Aldrich
at ICFEM 2018 conference

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Motivation

- Consider a program which calls a logger component:

```
1 module def logger(f:{File}):Logger  
2 def log(x: String): Unit
```

```
1 module def client(logger: Logger)  
2 def run(): Unit = logger.log(x)
```

- We pass the logger a file expecting it to append to it.
- But how do we ensure that is all it does?
- In Java, once the logger has the file, it can do anything it wants: “ambient authority”.
- Capabilities have been used informally to reason about resource use — can we use them formally?

Approach

- We look at adding capability-based reasoning to a formal system for reasoning about resource use.
- Specifically, a small effect calculus based on the λ -calculus, with operations on resources.
- Rich enough to capture examples written in a subset of a capability-safe language, Wyvern.
- Look at how we can minimise the need for effect annotations in order to make such a system easier to use.
- Using capabilities allows us to bound the effects of unannotated code without needing to annotate it.

Basic Language

We start with a very simple language with operations on resources.

$e ::=$	<i>exprs :</i>	$\tau ::=$	<i>types :</i>
x	<i>variable</i>	$\{r\}$	<i>resource set</i>
v	<i>value</i>	$\tau \rightarrow \tau$	<i>function</i>
$e e$	<i>application</i>		
$e.\pi$	<i>operation</i>		
$v ::=$	<i>values :</i>	$\Gamma ::=$	<i>type ctx :</i>
r	<i>resource literal</i>	\emptyset	<i>empty ctx</i>
$\lambda x : \tau. e$	<i>abstraction</i>	$\Gamma, x : \tau$	<i>binding</i>

- Semantics uses reduction relation $e \rightarrow e$ (ignoring operations).
- Type system has judgements: $\Gamma \vdash e : \tau$.
- Shows types of inputs and outputs, but nothing about effects.

Adding Effects

Add annotations to function types to show the effects that *may* occur.

$e ::=$	$exprs :$	$\tau ::=$	$types :$
	<i>variable</i>	$ \quad \{\bar{r}\}$	<i>resource set</i>
	<i>value</i>	$ \quad \tau \rightarrow_{\varepsilon} \tau$	<i>function</i>
	<i>application</i>		
	<i>operation</i>		
$v ::=$	$values :$	$\Gamma ::=$	$type\ ctx :$
	<i>resource literal</i>	$ \quad \emptyset$	<i>empty ctx.</i>
	<i>abstraction</i>	$ \quad \Gamma, x : \tau$	<i>binding</i>
		$\varepsilon ::=$	$effects :$
		$ \quad \{\overline{r.\pi}\}$	<i>effect set</i>

Effects are sets of resource-operation pairs.

Adding Effects

- Semantics uses reduction relation $e \longrightarrow e \mid \varepsilon$, where ε is the effects that occur during evaluation of e .
- Type/effect system has judgements: $\Gamma \vdash e : \tau$ with ε .
So we can check what effects may occur during evaluation of e .
- But this requires extensive annotation, which is tedious in practice.
E.g. Java unchecked exceptions are often criticised and often misused.
- Also, we may want to import third-party code which is not annotated.

Adding Capabilities

- Key idea is to combine annotated and unannotated code.
 - Allow annotated code to import unannotated code.
 - passing it the capabilities (resources) it needs.
 - and specifying the effects they are permitted to have.
- Combine the languages of unannotated and annotated code.
using hat (e.g. \hat{e}) in the formalism to distinguish them.
- Add a new statement: $\text{import}(\varepsilon_s) x = \hat{e} \text{ in } e$
 - e is the unannotated code being imported
 - \hat{e} is the capability being passed to e , which is bound to x in e .
 - ε_s is the set of effects which e is allowed to have (“selected authority”).
- E.g. $\text{import}(\text{File.append}) x = \text{File} \text{ in } \lambda y : \text{Unit}. x.\text{write}.$
This logger exceeds its authority so will be rejected!

Adding Capabilities

- Semantics uses reduction relation $\hat{e} \rightarrow \hat{e} \mid \varepsilon$.
We are only concerned with executing annotated code.
- To execute unannotated code which is imported, we annotate it with the selected authority.

$$\frac{}{\text{import}(\varepsilon_s) \ x = \hat{v} \text{ in } e \rightarrow [\hat{v}/x]\text{annot}(e, \varepsilon_s) \mid \emptyset} (\text{E-IMPORT2})$$

- $\text{annot}(e, \varepsilon_s)$ just adds ε_s to function arrows in e .

Example: Importing Logger

```
1 let MakeLogger =
2   ( $\lambda f$ : File.
3     import (File.append)  $f = f$  in
4        $\lambda x$ : Unit.  $f.append$ ) in
5
6
7 let MakeClient =
8   ( $\lambda logger$ : Logger.
9      $\lambda x$ : Unit. logger unit) in
10
11
12 let MakeMain =
13   ( $\lambda f$ : File.
14     let loggerModule = MakeLogger  $f$  in
15     let clientModule = MakeClient loggerModule in
16     clientModule unit) in
17
18
19 MakeMain File
```

Note: `let` expression is usual syntactic sugar.

Example: Higher Order Effects

```
1 let malicious =
2   (import(∅) y=unit in
3     λf: Unit → Unit. f()) in
4
5 let plugin =
6   (λf: {File}.
7     malicious(λx:Unit. f.read)) in
8
9 let MakeMain =
10  (λf: {File}.
11    plugin f) in
12
13 MakeMain File
```

Type and Effect Checking for Imports

Most type and effect rules are straightforward, but...

For import, we want a rule of the form:

$$\frac{\dots}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \dots \text{ with } \dots} (\varepsilon\text{-IMPORT})$$

- What type and effects does the import expression have?
- What assumptions do we need?

Typing Imports – First Attempt

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) \ x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon_s \cup \varepsilon_1} (\varepsilon\text{-IMPORT1})$$

- Assume arbitrary type and effect for \hat{e} .
- Must be able to type e , given just that x has type $\hat{\tau}$, to ensure e uses only the capabilities provided to it.
- e is unannotated while $\hat{\tau}$ is annotated, so we erase the annotations from $\hat{\tau}$.
- e has type τ — but τ is unannotated, so we annotate with ε_S .
- Evaluating e has all effects in ε_1 and ε_S .

Typing Imports – Second Attempt

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad x : \underline{\text{erase}}(\hat{\tau}) \vdash e : \tau \quad \text{effects}(\hat{\tau}) \subseteq \varepsilon_s}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon \cup \varepsilon_1} (\varepsilon\text{-IMPORT2})$$

- First version allows any capability to be passed to e .
- Restrict \hat{e} so that its effects are contained in ε_s .
- effects collects all the effects captured by its argument.

$$\text{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$$

$$\text{effects}(\hat{\tau}_1 \rightarrow_{\varepsilon} \hat{\tau}_2) = \text{effects}(\hat{\tau}_1) \cup \varepsilon \cup \text{effects}(\hat{\tau}_2)$$

```
1 import (File.*)
2 go = λx: Unit →∅ Unit. x unit
3 f = File
4 in
5 go (λy: Unit. f.write)
```

Typing Imports – Third Attempt

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad \text{effects}(\hat{\tau}) \subseteq \varepsilon_s}{\boxed{\text{ho-safe}(\hat{\tau}, \varepsilon_s)} \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau} \frac{}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon \cup \varepsilon_1} (\varepsilon\text{-IMPORT3})$$

$$\text{effects}(\{\bar{r}\}) = \{r.\pi \mid r \in \bar{r}, \pi \in \Pi\}$$

$$\text{effects}(\hat{\tau}_1 \rightarrow_{\varepsilon} \hat{\tau}_2) = \text{ho-effects}(\hat{\tau}_1) \cup \varepsilon \cup \text{effects}(\hat{\tau}_2)$$

$$\text{ho-effects}(\{\bar{r}\}) = \emptyset$$

$$\text{ho-effects}(\hat{\tau}_1 \rightarrow_{\varepsilon} \hat{\tau}_2) = \text{effects}(\hat{\tau}_1) \cup \text{ho-effects}(\hat{\tau}_2)$$

- Need to distinguish “direct” effects from “higher-order” effects.
- And ensure safe use of resources: imported capabilities must be expecting the effects they are passed by unannotated code.

Typing Imports – Fourth (and Final) Attempt

$$\text{effects}(\hat{\tau}) \cup \text{ho-effects}(\text{annot}(\tau, \emptyset)) \subseteq \varepsilon_s$$

$$\frac{\hat{\Gamma} \vdash \hat{e} : \hat{\tau} \text{ with } \varepsilon_1 \quad \text{ho-safe}(\hat{\tau}, \varepsilon_s) \quad x : \text{erase}(\hat{\tau}) \vdash e : \tau}{\hat{\Gamma} \vdash \text{import}(\varepsilon_s) x = \hat{e} \text{ in } e : \text{annot}(\tau, \varepsilon_s) \text{ with } \varepsilon_s \cup \varepsilon_1} (\varepsilon\text{-IMPORT})$$

Distinction between direct and higher-order effects needs to be pushed further!

$$\boxed{\text{safe}(\hat{\tau}, \varepsilon)}$$

$$\underline{\{r.\pi \mid r \in \bar{r}, \pi \in \Pi\} \subseteq \varepsilon} \text{ (SAFE-RESOURCE)}$$

$$\frac{\varepsilon \subseteq \varepsilon' \quad \text{ho-safe}(\hat{\tau}_1, \varepsilon) \quad \text{safe}(\hat{\tau}_2, \varepsilon)}{\text{safe}(\hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2, \varepsilon)} \text{ (SAFE-ARROW)}$$

$$\boxed{\text{ho-safe}(\hat{\tau}, \varepsilon)}$$

$$\overline{\text{ho-safe}(\{\bar{r}\}, \varepsilon)} \text{ (HOSAFE-RESOURCE)}$$

$$\frac{\text{safe}(\hat{\tau}_1, \varepsilon) \quad \text{ho-safe}(\hat{\tau}_2, \varepsilon)}{\text{ho-safe}(\hat{\tau}_1 \rightarrow_{\varepsilon'} \hat{\tau}_2, \varepsilon)} \text{ (HOSAFE-ARROW)}$$

Conclusions

- We can now check examples like the ones given earlier and safely reject ones that violate the granted authority.
- Doesn't require programmers to add effect annotations.
- Relies on type checking, not effect checking — doesn't require unannotated expressions to be analysed for their effects.

Implementation by Justin Lubin as Undergraduate RA at CMU in the summer of 2018

APPROXIMATING POLYMORPHIC EFFECTS WITH CAPABILITIES

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Goal

Allow *secure* and *ergonomic* mixing of effect-unannotated code with effect-annotated code in a *realistic* capability-safe programming language.

Object Capabilities

Capabilities

Unforgeable objects that give particular parts of the code access to sensitive resources

Capability-safe language

A language in which the only way to access sensitive resources is via capabilities

```
module def logger(myFile : File)
...
module def main(platform : Platform)
  val myFile = file(platform)
  val myLogger = logger(myFile)
  ...

```

Effect Systems

Effect system

Annotations on methods describing effects they can incur

Capability-based effect system

Way of formally reasoning about capabilities (*awesome!*)

Downside: verbosity

Capability-Safe Import Semantics

Prior work (*Craig et al.*)

Import semantics for capability-safe lambda calculus

Limitation

Does not handle mutable state nor effect polymorphism

Our goal

Scale up to a more realistic programming language

The Problem

Effect polymorphism *and* mutability

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The Problem

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit

  module def reversePlugin(name : String)
    var logger : Logger = ...
    def setLogger(newLogger : Logger) : Unit
      logger = newLogger
    def run(s : String) : String
      val t = s.reverse()
      logger.append(name + ":" + s + " -> " + t)
      t
```

Question: How will annotated code use `reversePlugin`?

Effect polymorphism + mutability
⇒ `log` effect could be *anything!*

The Problem

```
resource type Logger  
effect log  
def append(contents : String) : {log} Unit
```

```
module def reversePlugin(name : String)  
var logger : Logger = ...  
def setLogger(newLogger : Logger) : Unit  
logger = newLogger  
def run(s : String) : String  
val t = s.reverse()  
logger.append(name + ":" + s + " -> " + t)  
t
```



Question: How will annotated code use **reversePlugin**?

Effect polymorphism + mutability
⇒ **log** effect could be *anything!*

The Problem

```
resource type Logger  
effect log  
def append(contents : String) : {log} Unit
```

```
module def reversePlugin(name : String)  
var logger : Logger = ...  
def setLogger(newLogger : Logger) : Unit  
logger = newLogger  
def run(s : String) : String  
val t = s.reverse()  
logger.append(name + ":" + s + " -> " + t)  
t
```

Question: How will annotated code use `reversePlugin`?

Effect polymorphism + mutability
⇒ `log` effect could be *anything!*

Solution

Quantification lifting

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Quantification Lifting: Idea

```
resource type Logger  
effect log  
def append(contents : String) : {log} Unit
```

```
module def reversePlugin(name : String)  
var logger : Logger = ...  
def setLogger(newLogger : Logger) : Unit  
  logger = newLogger  
def run(s : String) : String  
  val t = s.reverse()  
  logger.append(name + ":" + s + " -> " + t)  
  t
```

```
resource type Logger[effect E]  
def append(contents : String) : {E} Unit
```

```
module def reversePlugin[effect E](name : String)  
var logger : Logger[E] = ...  
def setLogger(newLogger : Logger[E]) : {E} Unit  
  logger = newLogger  
def run(s : String) : {E} String  
  val t = s.reverse()  
  logger.append(name + ":" + s + " -> " + t)  
  t
```

- *Lift* effect polymorphism from inside ML-style module functor to the functor itself
- Collapse each universal effect quantification into single quantified effect E
 - Serves as effect bound for all methods in module

Quantification Lifting: Idea

```
resource type Logger  
effect log  
def append(contents : String) : {log} Unit
```

```
module def reversePlugin(name : String)  
var logger : Logger = ...  
def setLogger(newLogger : Logger) : Unit  
  logger = newLogger  
def run(s : String) : String  
  val t = s.reverse()  
  logger.append(name + ":" + s + " -> " + t)  
  t
```

```
resource type Logger[effect E]  
def append(contents : String) : {E} Unit
```

```
module def reversePlugin[effect E](name : String)  
var logger : Logger[E] = ...  
def setLogger(newLogger : Logger[E]) : {E} Unit  
  logger = newLogger  
def run(s : String) : {E} String  
  val t = s.reverse()  
  logger.append(name + ":" + s + " -> " + t)  
  t
```



- *Lift* effect polymorphism from inside ML-style module functor to the functor itself
- Collapse each universal effect quantification into single quantified effect E
 - Serves as effect bound for all methods in module

Quantification Lifting: Usage

```
import fileLogger, databaseLogger, reversePlugin
val logger1 = fileLogger(...)
val logger2 = databaseLogger(...)
val plugin = reversePlugin[logger1.log]("archive")
def main() : {logger1.log} Unit
  plugin.setLogger(logger1)
  // plugin.setLogger(logger2) <-- not allowed!
```

```
resource type MyPlugin
  def setLogger(newLogger : Logger') : {logger1.log} Unit
  def run(s : String) : {logger1.log} String

resource type Logger'
  effect log = {logger1.log}
  def append(contents : String) : {log} Unit
```

Quantification Lifting: Import Bounds

```
resource type Logger  
effect log  
def append(contents : String) : {log} Unit
```

```
module def reversePlugin(name : String)  
var logger : Logger = ...  
def setLogger(newLogger : Logger) : Unit  
logger = newLogger  
def run(s : String) : String  
val t = s.reverse()  
logger.append(name + ":" + s + " -> " + t)  
t
```

```
resource type Logger[effect E]  
def append(contents : String) : {E} Unit
```

```
module def reversePlugin[effect E](name : String)  
var logger : Logger[E] = ...  
def setLogger(newLogger : Logger[E]) : {E} Unit  
logger = newLogger  
def run(s : String) : {E} String  
val t = s.reverse()  
logger.append(name + ":" + s + " -> " + t)  
t
```

- *Something to be careful about:* bounds on new universally-quantified polymorphism
 - *Upper bound:* Craig et al. import semantics
 - *Lower bound:* Capability-safety

E
1

Quantification Lifting: Type-Level Transformation

Benefit

Don't need code ahead of time, only type signature

- Dynamic loading (plugins)
- Compiled code
- Third-party libraries

Drawback

Over-approximation of possibly-incurred effects

Quantification Lifting: Type-Level Transformation

Before: $\tau_1 \rightarrow \tau_2$

After: $\forall \varepsilon (L \subseteq \varepsilon \subseteq U) . \tau_1 \rightarrow (\tau_2)_\varepsilon$

Related Work

Effect inference

- Operates on *expressions*
- Gives exact bound on effects that can be incurred

Algebraic effects

- Has a different goal
- We use the effect system to formally/statically reason about capabilities

Observations

- *Capabilities* are good way of managing non-transitive access to system resources
- *Effect systems* can formalize capability-based reasoning, but can be verbose
- Craig et al.'s *import semantics* work great for lambda calculus
- *Quantification lifting* handles tricky interaction between effect polymorphism and mutable state

Example Summary

```
resource type Logger
  effect log
  def append(contents : String) : {log} Unit
```

```
module def reversePlugin(name : String)
  var logger : Logger = ...
  def setLogger(newLogger : Logger) : Unit
    logger = newLogger
  def run(s : String) : String
    val t = s.reverse()
    logger.append(name + ":" + s + " -> " + t)
    t
```

```
import fileLogger, databaseLogger, reversePlugin
val logger1 = fileLogger(...)
val logger2 = databaseLogger...
val plugin = reversePlugin[logger1.log]("archive")
def main() : {logger1.log} Unit
  plugin.setLogger(logger1)
  // plugin.setLogger(logger2) <-- not allowed!
```

```
resource type Logger[effect E]
  def append(contents : String) : {E} Unit
```

```
module def reversePlugin[effect E](name : String)
  var logger : Logger[E] = ...
  def setLogger(newLogger : Logger[E]) : {E} Unit
    logger = newLogger
  def run(s : String) : {E} String
    val t = s.reverse()
    logger.append(name + ":" + s + " -> " + t)
    t
```

```
resource type MyPlugin
  def setLogger(newLogger : Logger') : {logger1.log} Unit
  def run(s : String) : {logger1.log} String
```

```
resource type Logger'
  effect log = {logger1.log}
  def append(contents : String) : {log} Unit
```

Thank you for the course!



CAPITAL THINKING.
GLOBALLY MINDED.
MAI TE IHO KI TE PAE



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