Quadrupole Pairing Two-body Hamiltonian $H_Q = -\frac{\chi}{2} \sum_{\mu} Q_{\mu} Q_{\mu}^+$ $H_p = -GT(2) T(-2)$ $Q_{\mu} = \sum_{\nu,\nu'} \langle \nu \mid r^2 Y_{2\mu} \mid \nu' \rangle c_{\nu}^+ c_{\nu}$ $T(2) = \sum_{\nu>0} c_{\nu}^{+} c_{\bar{\nu}}^{+} = T^{+}(-2)$ Associated average field $V_Q = -\sum_{\mu} K_{\mu} Q_{\mu} \quad (\mu = 0, \pm 1, \pm 2)$ $V_p = -\sum_{\alpha} \Delta_{\alpha} T(\alpha) \quad (\alpha = \pm 2)$ (potential deformation parameters) K_{μ} The specific operator is the electromagnetic multipole operator two-body transfer operator (macroscopic description) $\mathscr{M}(E2, \mu) = \frac{5}{4\pi} Z e R_0^2 K_{\mu}$ $T(\Delta) = \sum_{\nu>0} U_{\nu}(\Delta)V_{\nu}(\Delta)$ (microscopic description) $\mathcal{M}(E2, \mu) = \sum_{\mathbf{r},\omega} \langle \mathbf{r} \mid r^2 Y_{2\mu} \mid \omega \rangle c_{\omega}^+ c_{\mathbf{r}}$ $T(2) = \sum_{r>0} c_r^+ c_{\bar{r}}^+$ It probes the particle-hole particle-particle correlations aspects of the residual interaction. The single-particle potential V is not invariant under gauge transformations rotations in three dimensions $\mathscr{G}(\varphi) = \exp\{-i \mathscr{N} \varphi\}$ $R(\mathbf{n}, \theta) = \exp\{-i\mathbf{I} \cdot \mathbf{n}\theta\}$ number operator: $\mathscr{N} = \sum_{y>0} (c_y + c_y + c_{\bar{y}} + c_{\bar{y}})$ total angular momentum operator: I $\mathscr{G}(\varphi)T(\alpha)\mathscr{G}^{-1}(\varphi) = e^{-i\alpha\varphi}T(\alpha)$ $R(\mathbf{n}, \theta)Q_{\mu}R^{-1}(\mathbf{n}, \theta) = \sum_{\mu'} D_{\mu'\mu}^{\bullet}(\omega)Q_{\mu'}$ $\varphi = \text{gauge angle}$ $\omega = \text{Euler angles}$ T = operator with transfer quantum number α Q = tensor operator of rank two The violation of particle number spherical symmetry defines an intrinsic system of reference in an abstract space the physical three-dimensional space Instead of parametrizing the deformation of the potential by Δa K_{μ} one can use the BCS gap parameter Δ and the angle ϕ β and γ and the angle ω

that defines the orientation of the intrinsic frame of reference.