$$U(r) = \int d\mathbf{r}' \rho(r') v(|\mathbf{r} - \mathbf{r}'|)$$

$$\rho(r) = \sum_{i} |\varphi(\mathbf{r})|^{2}$$

$$U_{x}(r, r') = -\sum_{i} \varphi_{i}^{*}(\mathbf{r}') v(|\mathbf{r} - \mathbf{r}'|) \varphi_{i}(\mathbf{r})$$