where $|0\rangle$ is the vacuum state and a_j^{\dagger} creates a particle in the orbital j with time-reversal properties $\tau a_{j_m}^{\dagger} \tau^{-1} = (-1)^{j+m} a_{j-m}^{\dagger}$. The amplitudes α_j are determined by the secular equation

$$(2\varepsilon_{j}-E)\alpha_{j}=\sum_{j'}(j+\frac{1}{2})^{\frac{1}{2}}(j'+\frac{1}{2})^{\frac{1}{2}}G(j',j',j,j)\,\alpha_{j'},$$

Fig. 2.13,1

single-particle energy associated with the j-orbital. If we retegrals (*) G(j', j', j, j) by an average value G, the eigenvalues E e dispersion relation

$$\frac{1}{G} = \sum_{\mathbf{j}} \frac{\mathbf{j} + \frac{1}{2}}{2\varepsilon_{\mathbf{j}} - E} = \sum_{\mathbf{j}} \sum_{\mathbf{m} \geq \mathbf{0}} \frac{1}{2\varepsilon_{\mathbf{j}} - E} \equiv F(E) \; .$$

The nature of the solution is illustrated in fig. 1. When E goes from a value smaller to a value larger than $2\varepsilon_i$, F(E) decreases from ∞ to $-\infty$. As E passes through the origin to negative values, F(E) decreases from ∞ to zero. The eigenvalues E are given by the intersection of F(E) with the line $F(E) = G^{-1}$.

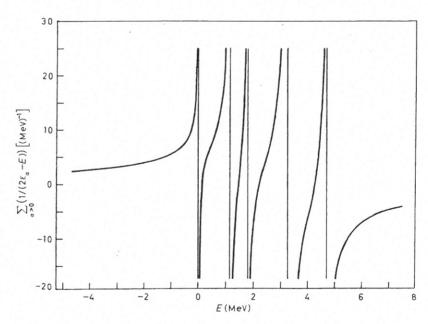


Fig. 1. – Dispersion relation (1.3) for $^{206}{\rm Pb}.$ The single-hole states available to the two neutrons are $p_{1/2}(0),\,f_{5/2}(0.57),\,p_{3/2}(0.89),\,i_{13/2}(1.63),\,f_{7/2}(2.34)$ (from ref. [12]). The label α denotes the quantum numbers (j,m).

^(*) For a contact interaction, $G(j',j',j,j) = -(V_0/4\pi) \int u_{j'}^{*2}(r) u_j^2(r) r^2 dr$.