

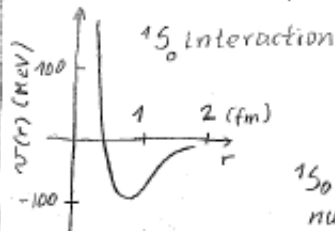
Quantity parameter ratio of quantal kinetic energy of localization and potential energy) box 1

App. 2.9

$$Q = \frac{\hbar^2}{M_n a^2} \frac{1}{|V_0|}; M_n = 0.939 \text{ GeV}/c^2 \quad (\text{neutron mass})$$

$$a \approx 1 \text{ fm (range)}$$

$$V_0 \approx -100 \text{ MeV (depth)}$$



$^1S_0$ : interaction between two nucleons in states of time reversal with  $S=L=0$ , and thus in a singlet state.

(QM: ZPF ( $\Delta p \Delta x \approx \hbar$ ))

$$\left( \frac{\hbar^2}{M_n a^2} \right)$$

constituents	$M/M_n$	$a$ (cm)	$v_0$ (eV)	$Q$	phase ( $T=0$ )	$T_c$
$^3\text{He}$	3	$2.9(-8)$	$8.6(-4)$	0.19	liquid <sup>a)</sup>	
$^4\text{He}$	4	$2.9(-8)$	$8.6(-4)$	0.14	liquid <sup>a)</sup>	
$\text{H}_2$	2	$3.3(-8)$	$32(-4)$	0.06	solid <sup>a)</sup>	
$^{20}\text{Ne}$	20	$3.1(-8)$	$31(-4)$	0.007	solid	
nucleons	1	$9(-14)$	$100(+6)$	$0.5^c$	liquid <sup>a,b)</sup>	

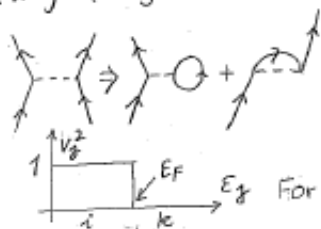
a) liquid (condensed)

b) better, Non-Newtonian solid

c) Nucleus, paradigm of quantal many-body Fermi systems.

(B.R. Mottelson, Elementary features of nuclear structure, Les Houches, Session LXVI, Elsevier (1992))

Fluctuations, quantal or classical, favor symmetry: gases and liquids are homogeneous. Potential energy on the other hand prefers special arrangements: atoms like to be at specific distances from each other (spontaneous breaking of symmetry).



$$U(r) = \int d^3r' P(r') v(|r-r'|)$$

$$P(r) = \sum_i |\psi_i(r)|^2$$

$$U_x = - \sum_i \langle \psi_i^*(r') v(|r-r'|) \psi_i(r) \rangle$$

For  $Q \gg 0.15$  independent-particle motion.