

5.C.2: Graphical representation of the successive transfer of two nucleons. tails see text.

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$$\bar{a}^{(2)}(\infty) = \frac{1}{i\hbar} \int_{-\infty}^{\infty} dt (\psi^b \psi^B, (V_{bB} - V_{bB})) e^{i\sigma_1} \psi^f \psi^F)$$

$$\times \exp[\frac{i}{\hbar} (E^{bB} - E^{fF}) t + \gamma_1(t)]$$

$$\times \exp[\frac{i}{\hbar} (E^{fF} - E^{aA}) t' + \gamma_2(t)]. \qquad (5.C.7)$$

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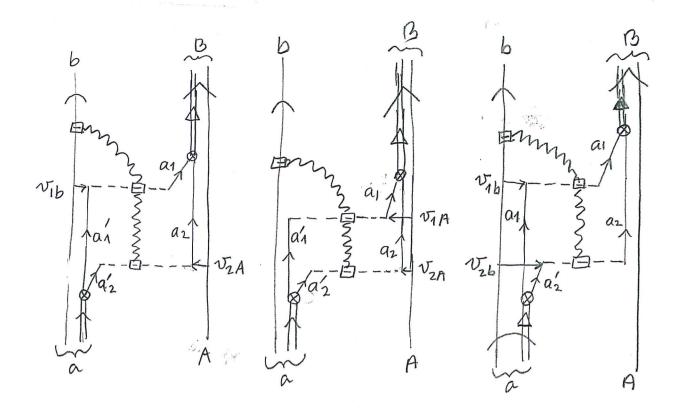
$$\times \exp[\frac{i}{\hbar} (E^{fF} - E^{aA}) t' + \gamma_2(t)]. \qquad (5.C.7)$$

$$\times \exp[\frac{i}{\hbar} (E^{fF} - E^{aA}) t' + \gamma_2(t)]. \qquad (5$$

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See also Sect. D.3 of app. D of Phys. Si pp 28,29,



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			or (11 Li (95) -		
(	i	DL	Theory	Experiment	0 = Ocm
	95 (3/2)	0	6.1	5,7±0,9	20° < 0 < 154.5°
	2,69 MeV (1/2-)	2	0,7	1 ± 0.36	30° < 0 < 100°

Jable 6.1.2

Integrated two-neutron transfer differential cross section associated with the reaction

1H ("Li, "Li(i))" H populating the ground state and the first excited state of 9Li (Tamhata et al (2008), column labeled Experiment), The theoretical values are from Potel et al (2010) (see also Potel et al (2013)) & see Figs. 6.1.3 and 6.8.2);

the quadrupole and dipole collective vibrational states being exchanged between the two halo neutrons, Also shown (left) is the diagram associated with the bare nuclear pairing interaction. dashed line

	$^{11}\mathrm{Li}(p,t)^{9}\mathrm{Li}$											
	V	W	$V_{so}$	$W_d$	$r_1$	$a_1$	$r_2$	$a_2$	$r_3$	<i>a</i> <sub>3</sub>	r <sub>4</sub>	a <sub>4</sub>
p, <sup>11</sup> L $i$ <sup>d</sup> )	63.62	0.33	5.69	8.9	1.12	0.68	1.12	0.52	0.89	0.59	1.31	0.52
$d$ , ${}^{10}\mathrm{Li}^{b)}$	90.76	1.6	3.56	10.58	1.15	0.75	1.35	0.64	0.97	1.01	1.4	0.66
t, <sup>9</sup> Li <sup>c)</sup>	152.47	12.59	1.9	12.08	1.04	0.72	1.23	0.72	0.53	0.24	1.03	0.83

Table 6.1.1: Optical potentials (cf. Tanihata, I. et al. (2008)) used in the calculation of the absolute differential cross sections displayed in Fig. 6.1.3 and Table 6

We are then in presence of a paradigmatic nuclear embodiment of Cooper's model which is at the basis of BCS theory: a single weakly bound neutron pair on top of the Fermi surface of the <sup>9</sup>Li core. But the analogy goes beyond these aspects, and covers also the very nature of the interaction acting between Cooper pair partners. Due to the high polarizability of the system under study and of the small overlap of halo and core single particle wavefunctions, most of the Cooper pair correlation energy stems, according to NFT, from the exchange of collective vibrations, the role of the strongly screened bare interaction being, in his case, minor and (see Sect. 2.6). In other words, we are in the presence of a new realization of the Cooper model in which a totally novel Bardeen–Pines–Prölich–like phonon induced interaction is generated by a self induced collective vibration of the nuclear medium.

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. soft mode

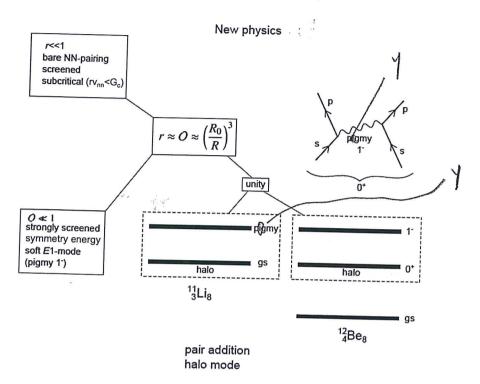


Figure 6.1.4: Schematic representation of a possible realization of halo pair addition mode in terms of the first excited 0<sup>+</sup> state (2.24 MeV) of <sup>12</sup>Be (for details see Sect. 2.6).

state (and the lowest E1-concentration strength state<sup>9</sup>), in other nuclei it may be an excited state which could be observed in a combined L=0, and L=1 two-particle transfer reaction to excited states, or in terms of E1 decay of the bygmy resonance built on top of it. Within this context, it is an open question whether one could expect to find a realization of such a halo pair addition mode in, for example, the first excited  $0^+$  state of  $1^2$ Be (see Fig. 6.1.4).

Single-particle  $s_{1/2}$  and  $p_{1/2}$  states at threshold in neutron drip-line nuclei have been found to lead, within the framework of a bare, short range, pairing interaction scheme to halo anti-pairing effects<sup>10</sup>. The fact that the separation energy of the halo neutrons (halo Cooper pair) of <sup>11</sup>Li(gs) is  $\approx 400$ keV, testifies to the fact that the anti-halo pairing effect is, in this case, overwhelmed by (dynamical) medium polarization effects.

Within this context it is of notice that, again, the interweaving of the different elementary modes of nuclear excitation, pairing and pygmy resonances in the

9Kanungo et al. (2015).

<sup>&</sup>lt;sup>10</sup>Bennaceur, K. et al. (2000), cf. also Hamamoto and Mottelson (2003), Hamamoto, I. and Mottelson (2004).

CHAPTER 6. STRUCTURE WITH TWO NEUTRONS

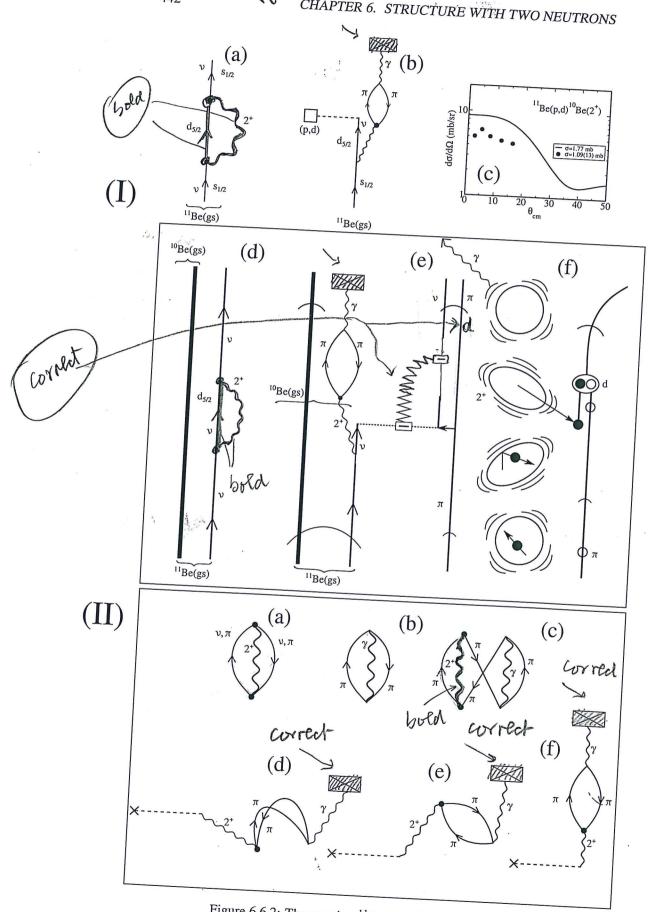


Figure 6.6.2: The reaction  ${}^{11}\text{Be}(p, d){}^{10}\text{Be}(2^+)$ .

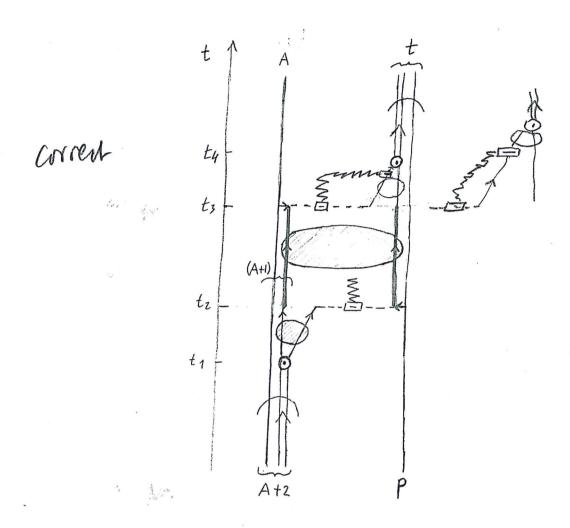


Figure 6.6.3: Diagram describing structure and reaction aspects of the main process through which a Cooper pair (di-neutron) tunnels from target to projectile in the reaction  $(A + 2) + p \rightarrow A + t$ . In order that the two-step process  $(A + 2) + p \rightarrow$  $(A + 1) + d \rightarrow A + t$  takes place, target and projectile have to be in contact at least in the time interval running between  $t_2$  and  $t_3$ . During this time, the two systems create, with local regions of ever so low nucleonic presence, a common density over which the non-local pairing field can be established, and the Cooper pair can be correlated. Even with regions in which the pairing interaction may be zero. Small ellipses (with linear dimensions of the order of the nuclear radius  $R_0$ ) indicate situations in which the two neutron correlation is distorted by the external mean field of a single of the systems involved of the reaction, i.e. A + 2 in the entrance channel, t in the exit one (see e.g. Fig. 2.6.3). The large ellipse (with linear dimensions of the order of the correlation length  $\xi$ ) indicate the region in which the two partners of the Cooper pair correlate over distances of the order of the correlation length  $\xi$ . It is this information that the outgoing particle of a Cooper pair transfer process brings to the detector. In other words, this is the observable Cooper pair in terms of its specific probe, and the reason why the neutrons are described, in the interval  $\Delta t = t_3 - t_1^2$ , in terms of bold face arrowed lines.