

and that the EWSR associated with the ^{11}Li pigmy resonance is $\approx 10\%$ of the total Thomas-Reiche-Kuhn sum rule one can write,

$$0.1 \frac{\hbar^2 A}{2M} = \frac{1}{K_1} [(0.5 \text{ MeV})^2 - (\hbar\omega_{\text{pigmy}})^2],$$

and thus

$$(\hbar\omega_{\text{pigmy}})^2 = (0.5 \text{ MeV})^2 - 0.1 \frac{\hbar^2 A}{2M} K_1,$$

where (see Bortignon et al (1998))

$$K_1 = -\frac{5V_1}{A(5/2)^2} \left(\frac{2}{11}\right) = -\frac{125 \text{ MeV}}{A \times 100 \text{ fm}^2} \left(\frac{2}{11}\right) \approx -\frac{2.5 \text{ fm}^{-2} \text{ MeV}}{A^2},$$

the ratio in parenthesis reflecting the fact that only 2 out of 11 nucleons, slosh back and forth in an extended configuration with little overlap with the other nucleons. One then obtains,

$$\begin{aligned} -0.1 \frac{\hbar^2 A}{2M} K_1 &= 0.1 \times 20 \text{ MeV fm}^2 A \times \frac{2.5}{A^2} \text{ fm}^{-2} \text{ MeV} \\ &\approx 0.45 \text{ MeV} \approx (0.7 \text{ MeV})^2 \end{aligned}$$

Consequently

$$\hbar\omega_{\text{pigmy}} = \sqrt{(0.5)^2 + (0.7)^2} \text{ MeV} \approx 1 \text{ MeV},$$