

# 1. Introduction

optical propt.

## 1.1 Elementary modes of excitation

12/09/14  
12:04

Subject to ~~an~~ external probes which couple weakly to the nucleus, that is in such a way that the system can

be expressed in terms of the properties of the excitation in the absence of probes, <sup>(Pines and Noziers (1966))</sup> the nucleus reacts <sup>(Bohr and Mottelson 1975)</sup> in terms of single-particle (-hole) motion (one-particle transfer), vibrations (surface, spin, etc) and rotations (Coulomb excitation and inelastic scattering) and pairing vibrations and rotation (two-nucleon transfer reactions) (cf. Figs 1, 2 and 3). 1.1, 1.2 and 1.3

Echoing Heisenberg's requirement that no concept enters the quantal description of a physical system which has not direct relation to experiment, and Landau's result that any weakly excited state of a quantal many-body system may be regarded as an ensemble of weakly interacting elementary modes of excitation, Bohr, Mottelson and coworkers developed a unified description of the nuclear structure in terms of quasiparticles, vibrations and rotations, <sup>both in 3D as well as in space</sup> which was eventually extended to direct nuclear

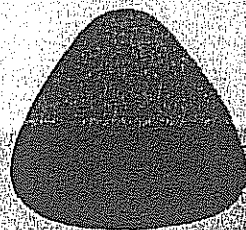
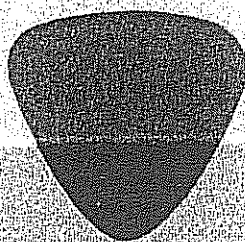
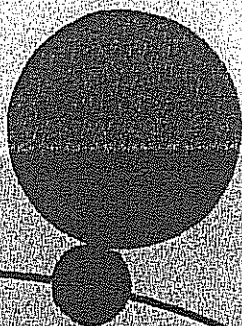
Bohr (1976), Mottelson (1977), Bohr and Mottelson 1975, Bohr, Mottelson (1953), Bes and Broglia 1966, 1977 and refs. therein; and Pines (1958), Belyaev (1959), Nilsson, S.G., Bes and Broglia 1966, 1977 and refs. therein;

cf. also Broglia and Zelevinsky, eds. (1973) and refs. therein

G. Tiana

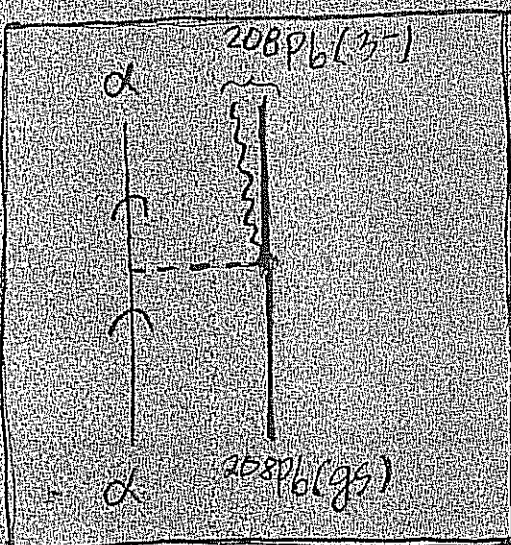
12/09/14 10:47

$^{208}\text{Pb}$

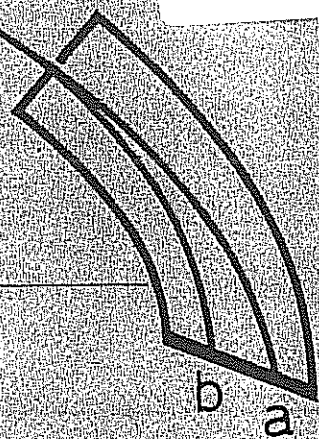


collective (octupole) vibration

projectile

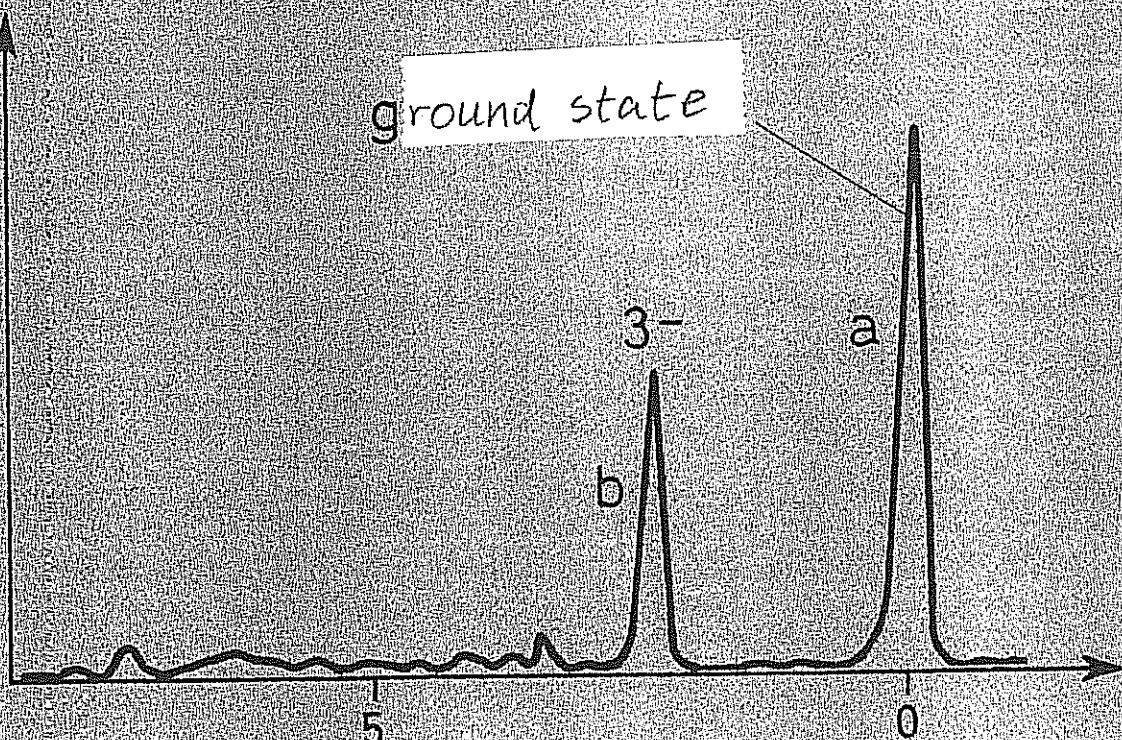


magnet



number  $\alpha$ -particles

ground state



energy loss (MeV)

Fig. 1

1.1

colour  
G.Tiane 12/09/14  
10:45

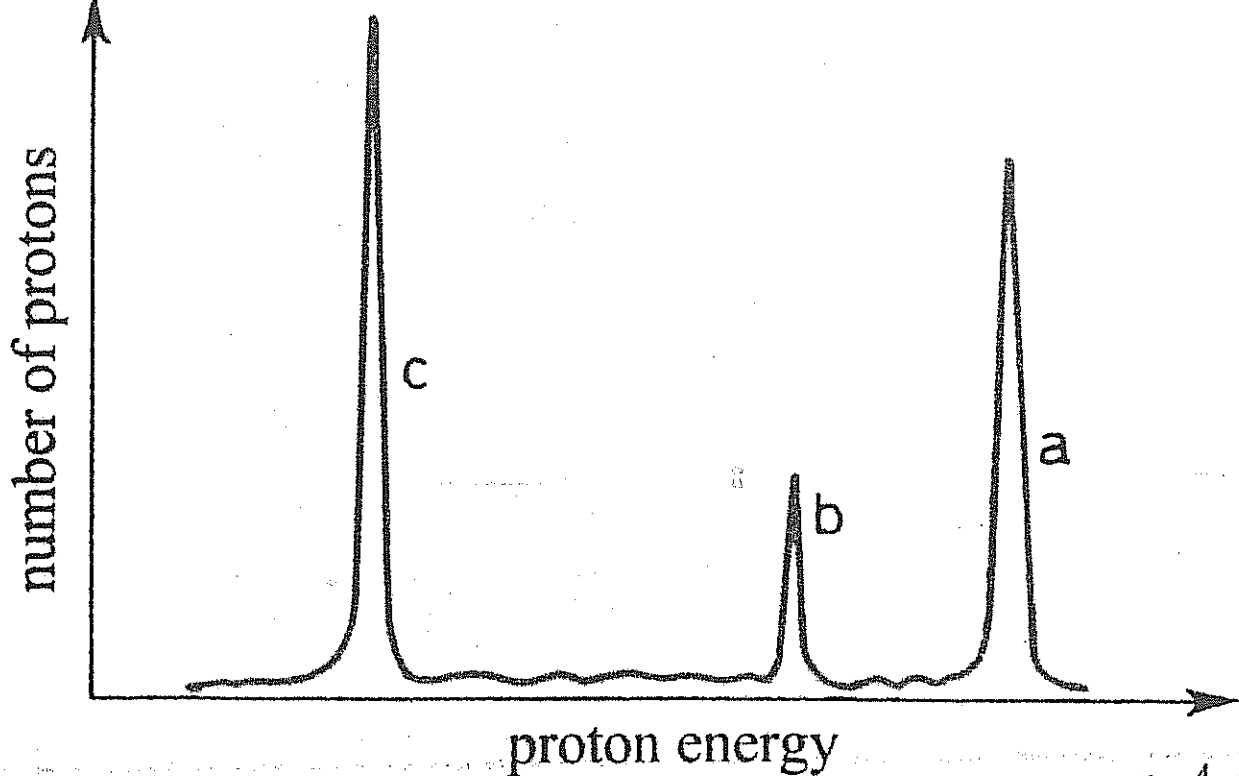
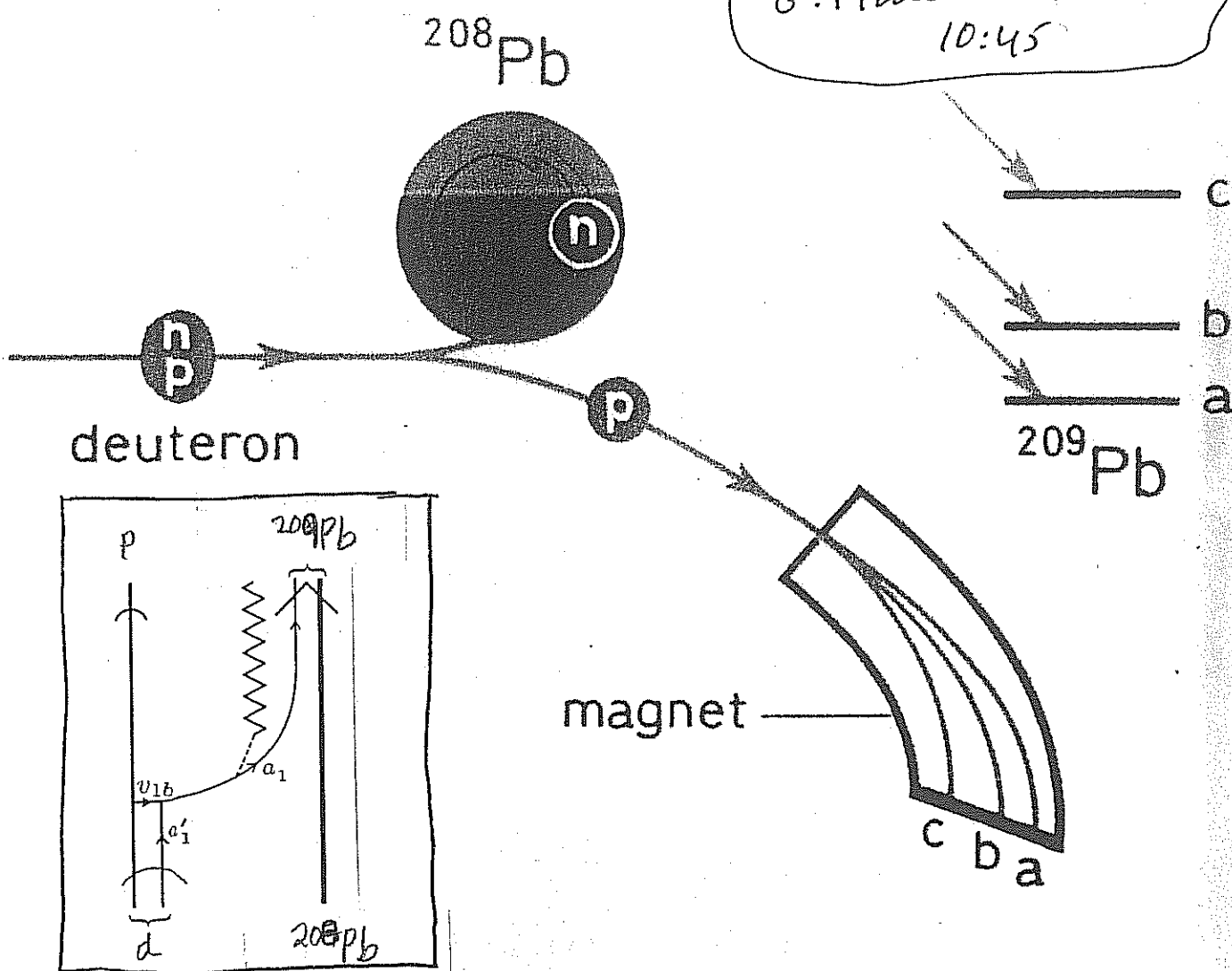
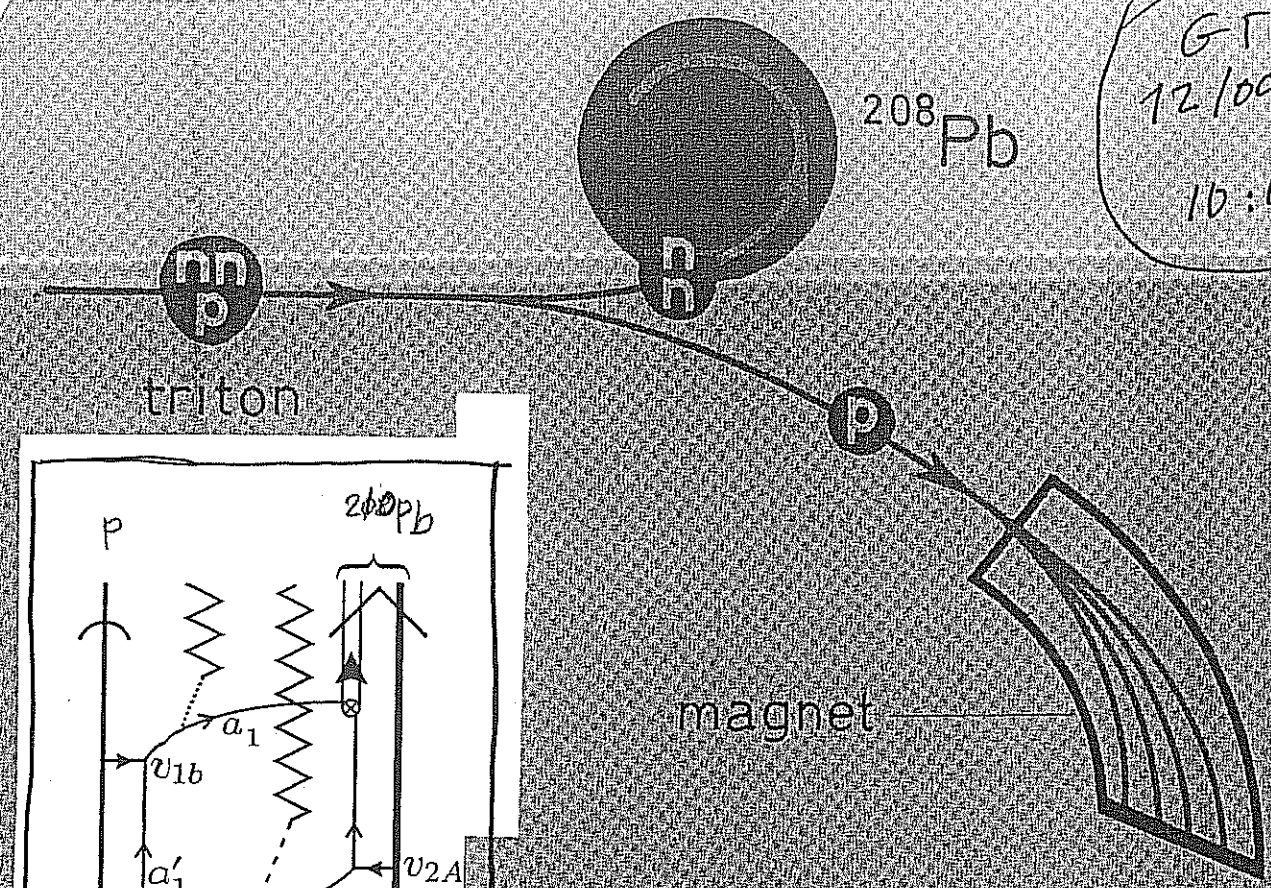


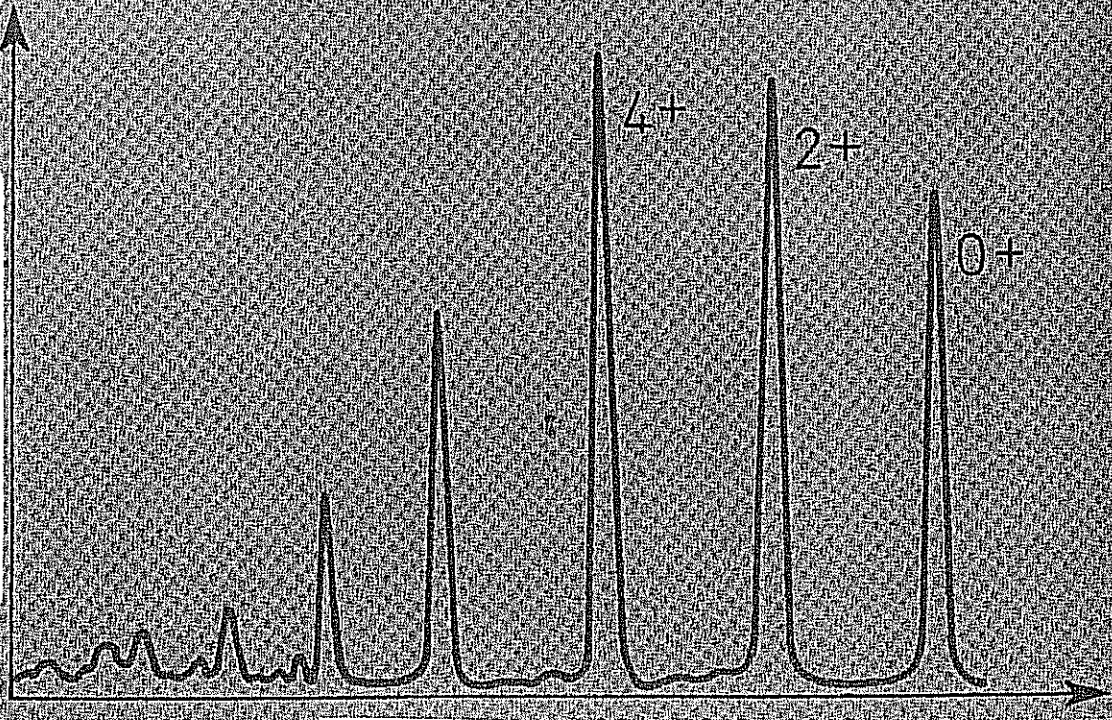
Fig. 2 1.2



GT  
12/09/14  
16:49



number of protons



proton energy

Fig. 3.13

Fig. 1

Schematic representation of ~~elastic~~ elastic (population of the ground state a) an inelastic (lowest octupole vibration 2.65 MeV) processes associated with the reaction  $^{208}\text{Pb}(\alpha, \alpha')^{208}\text{Pb}$ . In the inset the Nuclear Field Theory (NFT) diagram associated with the octupole excitation (S given. a (curved) arrow on a line indicates propagation in the continuum. Outgoing particles are deflected in a spectrograph and recorded in a detector. The corresponding ~~an~~ excitation function is given in the lowest part of the Figure.

Fig. 2

Schematic representation of ~~the~~ one-nucleon transfer reaction  $^{208}\text{Pb}(d, p)^{209}\text{Pb}$  populating the single-particle states of  $^{209}\text{Pb}$ . The energy of the outgoing proton reflects both the Q-value of the reaction and the excitation energy of the final state. For more detail cf. caption to Fig. 1.1 (cf. also ~~Fig. 6.1.1~~ ch. 6 and Fig. 6.1.1)

Fig. 3

Schematic representation of the two-nucleon transfer reaction  $^{208}\text{Pb}(t,p)^{210}\text{Pb}$ , populating the ground state  $0^+$ , and two particle excited states  $2^+$  and  $4^+$ . In the inset it is assumed that the main contribution to the ~~tran~~ process arises from the successive transfer of the nucleons, the jagged curves representing the recoil elementary model taken care of recoil effects (cf. Ch. 7 and Figs 7.C.1 and 7.C.2)

1.2 Sum rules

(These exact and approximate sum rules were

13  
24  
(2)

A quantitative measure of this over-completeness is provided by exact and approximate sum rules that the different observables (cross sections) ~~recorded~~ obtained

~~making use of related to~~ ~~starting from the~~ variety of probes to which the nucleus is subject.

have to fulfil An example of the first type ~~(exact)~~ is the Thomas-Reiche-Kuhn ~~(TRK)~~ sum rule. Of the second ~~(approximate)~~

two nucleon transfer (TNTR) sum rules (cf. Broglia et al 1972; Bayman and

Clement 1972). In both cases they embody particle (pair) number conservation. Charged ~~particle in the first case~~ (electrons in atoms and molecules, effective charges of neutrons and protons in nuclei). Number of Cooper pairs in nuclei in the second.

Physically, they ~~provide with~~ ~~give the~~ (1)

maximum amount of photons (cross section) which the quantal system can absorb from a beam of light (x-rays) shined on it; 2) the ~~area~~ ~~total~~

~~total~~ maximum value of the two-ring area fraction nucleon transfer cross section (fraction of the geometric reaction cross section) exhausted by the final  $(A \pm 2)$  states populated in the process.

(A) from p. (2) b

① 1.2 Sum rules ②<sub>b</sub>  
A quantitative measure of the above mentioned overcompleteness is provided by exact and approximate sum rules the observables (cross sections) associated with the variety of probes to which the nucleus is subject, have to fulfill. An example of the first type (exact) is provided by the Thomas-Reiche-Kuhn (TRK) sum rule. Of the second type (approximate) by two-nucleon transfer (TNTR) sum rules (cf. Broglia et al 1972; Bayman and to p. ②<sub>a</sub> ①

↑  
see refs ch. 2



In other words, <sup>these</sup> sum rules provide: 3  
 a quantitative measure of the single-particle subspace the quantal system under study, in particular the nucleus, uses to induce the antenna-like motion of protons against neutrons; or, to correlate pairs of nucleons moving in time reversal states around the Fermi energy <sup>thus</sup> ~~and~~ providing a sigmoidal distribution of the <sup>level</sup> ~~occupied~~ occupancy.  
 The TRK sum rule can be written as (in the nuclear case) model depends

$$S(E1) = \sum_n |\langle \alpha | F | 0 \rangle|^2 (E_\alpha - E_0) = \frac{9}{4\pi} \frac{\hbar^2 e^2}{2m} \frac{NZ}{A}, \quad \left( \frac{1}{1.1} \right)$$

where  $|\alpha\rangle$  labels the complete set of excited dipole states, which can be reached operating with  $F$  <sup>the dipole operator</sup> on the initial state  $|0\rangle$ . Within this context, each elementary mode of excitation, in the present case of dipole type, defines a cf. app. A  
 ground state. This is in keeping with the fact that they induce specific quantal Zero Point Fluctuations (ZPF) measured by (harmonic approximation) 1,2

$$\langle 0 | F^2 | 0 \rangle = \frac{\hbar \omega}{2c_\alpha} = \frac{\hbar^2}{2D_\alpha} \frac{1}{\hbar \omega_\alpha} \quad (2) \quad \text{(nucleon)}$$

In other words, they perturb the static Fermi sea, that is the set of occupied

# mean field levels of the potential

(4)

$$(k, i, \text{i.e. } \epsilon_i \leq \epsilon_F \text{ and } \epsilon_k > \epsilon_F; \text{ see APP A}) U(r) = \int d^3r' \rho(r') v(|\vec{r} - \vec{r}'|), \quad (3)$$

inducing virtual particle-hole excitations. In the above equation,  $\rho(r)$  is the nuclear density and  $v$  is the nuclear two-body interaction.

In Eq. (1), the quantity

$$(1.1) \quad F = e \sum_n \left( \left( \frac{N-Z}{2A} - t_z \right) r_n Y_{1\mu}(\hat{r}_n) \right), \quad (1.4) \quad (4)$$

is the dipole operator acting both on the  $Z$  protons ( $t_z = -1/2$ ) and on the  $N$  neutrons ( $t_z = +1/2$ ) <sup>of mass  $m_i$</sup>  as indicated by the  $n$ -sum over all nuclear states ( $A = N + Z$ , mass number).

Because  $| \langle \alpha | F | 0 \rangle |^2$  measures the probability <sup>with which</sup> the state  $|\alpha\rangle$  is populated, the  $n$ -sum in (1.1) gives a measure of the maximum energy that the nucleus can absorb from the  $\gamma$ -beam, as can be seen by measuring  $| \langle 0 | F | \alpha \rangle |^2$  in single-particle units <sup>(sp<sup>2</sup>)</sup> (Weisskopf units) <sup>(W)</sup>.

$$B_{sp}(E1; j_1 \rightarrow j_2) = \frac{3}{4} e_{E1}^2 \langle j_1 \frac{1}{2} 10 | j_2 \frac{1}{2} \rangle^2 \times \langle j_2 | r | j_1 \rangle, \quad (5)$$

$$\approx \frac{1}{4\pi} A^{2/3} e_{E1}^2 \text{ fm}^2 = B_W(E1),$$

0.81  
4π

see Eq. 36-38  
ELM 389

where  $(e)_{E1} = (N/A)e$  for neutrons, and, (5)  
 $(e)_{E1} = -(Z/A)e$  for protons, in keeping with  
 the fact that the motion of a ~~re~~ nucleon  
 is associated with a recoil of the rest  
 of the nucleus, since the total center  
 of mass remains at rest in an intrinsic excitation.

(MF) Within this context, independent particle  
 motion in general and the existence of  
 a mean field <sup>(Hartree-Fock (HF) solution)</sup> in particular, can be viewed  
 as the most collective of <sup>all</sup> nuclear phenomena.  
 It is then not surprising that

$$S(E1) = \sum_n |\langle \alpha | F | \tilde{0} \rangle|^2 (E_\alpha - E_0), \quad 1.6$$

$$= \sum_{ki} |\langle k, i | F | g_s(MF) \rangle| (E_{ki} - E_0), \quad (6)$$

provided  $\tilde{0}$  contains the ground state  
 correlations mentioned in connection  
 with Eq(2), and that  $|g_s(MF)\rangle$  those ~~that~~  
 associated with  $\Delta x_n \Delta p_{x_n} \geq \hbar$ , <sup>1.4</sup> ~~moreover~~  
 words, provided <sup>(see Fig. 4)</sup> ~~1.7~~

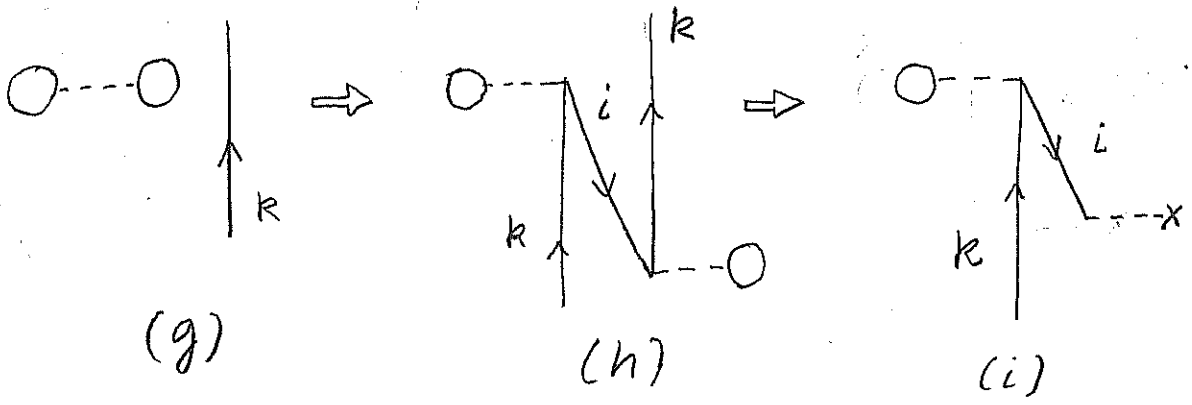
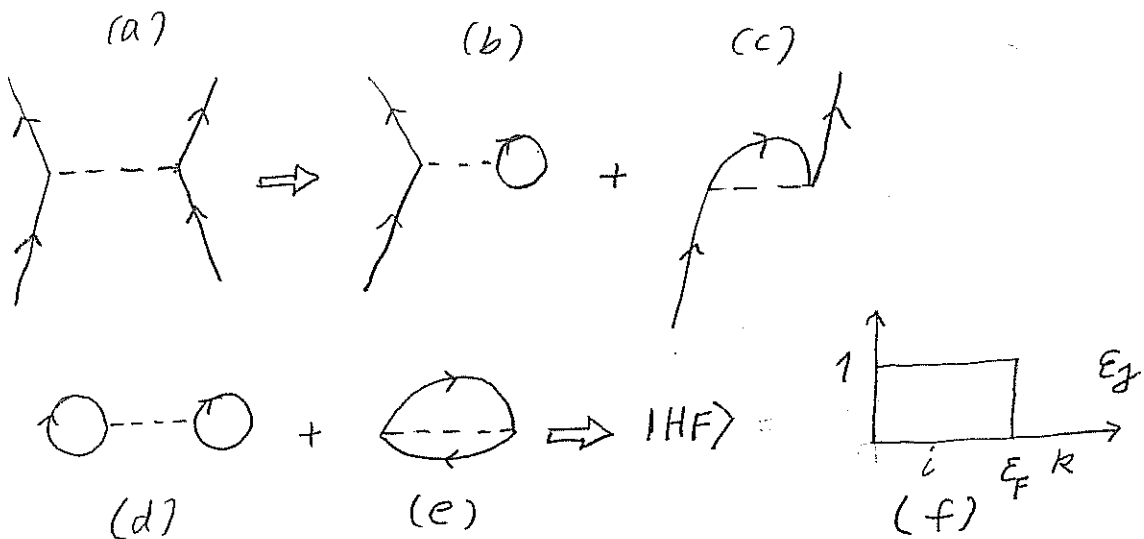
$$|HF\rangle = |g_s(MF)\rangle = \prod_{i \in \text{occup.}} a_i^\dagger |0\rangle \quad (7)$$

where  $|0\rangle$  is the particle vacuum ( $a_i |0\rangle = 0$ ),  
 and  $\prod_a a_i^\dagger |0\rangle = 0$ ,  $a_i^\dagger$  being the creation  
 operator of a dipole correlate particle,  $(\pi_a^\dagger = \sum_{ki} X_{ki}^a a_{ki}^\dagger + Y_{ki}^a (a_{ki}^\dagger)^\dagger)$ ,  
 (-holelike mode)

~~$$E_{\text{corr}} = - \sum_a \hbar \omega_a (\gamma_a^2) = - \sum_a \hbar \omega_a \frac{\hbar \omega_a}{2C_a} = - \sum_a \hbar \omega_a \frac{\hbar^2}{2D_a} \frac{1}{\hbar \omega_a}$$

$$= \boxed{\frac{\hbar^2}{2D_a}} \quad \text{1 coll. state}$$

↑  
Model indep~~



$$\alpha_\nu |HF\rangle = 0 ; \quad \alpha_\nu = \begin{cases} a_k & (E_k > E_F) \\ b_i = (-1)^{\text{phase}} a_i^\dagger & (E_i \leq E_F) \end{cases}$$

(j)

Fig. 1.4

Schematic representation of the processes characterizing the Hartree-Fock ground state (single-particle vacuum), in terms of Feynman-NFT diagrams. (a) nucleon-nucleon interaction through the bare (instantaneous) NN-potential. (b) Hartree mean field contribution. (c) Fock mean field contribution. (d, e) ground state correlations (ZPF) associated with Hartree and Fock processes. (f) decoupling between occupied and empty state operated by the HF field. (g) nucleon in presence of Hartree ZPF. (h) modification of single-particle state  $k$  due to Hartree ZPF and implying the existence of hole (antiparticle) states ( $b_i$  HF) with quantum numbers time reversed to that of particle states ( $b_i = (-1)^{\text{phase}} a_i$ ). In other words, the  $|HF\rangle$  ground (vacuum) state is filled to the rim ( $\epsilon_F$ ) with  $N$  nucleons. (The system with  $(N-1)$  nucleons can, within the language of (Feynman's) field theory, <sup>be described</sup> in terms of the degrees of freedom of that of the missing nucleon (hole-, antiparticle state). ~~such~~ Such a description is obviously considerably more economic than that corresponding to a wavefunction with  $N-1$  spatial and spin coordinates pairs  $(\vec{r}_i, \sigma_i)$ ,



Relation (6) is a consequence of the fact that  $S(E)$  is proportional to the average value of the double commutator  $[[H, F], F]$  in the ground state of the system ( $|0\rangle$  or  $|HF\rangle$ ). Because  $F$  is a function of only the nucleon coordinates, and assuming  $v(|\vec{r}-\vec{r}'|)$  to be velocity independent, the only contribution to the <sup>(universal)</sup> double commutator arises from the <sup>(kinetic energy)</sup>. Thus, the value (7) is model independent. In other words, this value does not depend on the correlations acting among the nucleons, but on the number of them participating in the motion and thus on the corresponding effective inertia. In fact  $\sum_{\alpha} \hbar \omega_{\alpha} \left( \frac{\hbar \omega_{\alpha}}{2C_{\alpha}} \right) = \sum_{\alpha} \left( \hbar^2 / 2D_{\alpha} \right)$ . It is then not surprising that the TRK sum rule was used in the early stages of quantum mechanics, to determine the number of electrons of atoms.

Let us now go back to two-nucleon transfer <sup>(pairing)</sup> processes. The associated absolute cross sections can be set on <sup>essentially</sup> equal footing with respect to Q-value effects with the help of empirically determined ~~determined~~ global functions (cf. Broglia et al 1972)).

In this way, the theoretical absolute cross sections associated with e.g. the  $A(t,p)A+2$  <sup>population</sup> ~~reaction~~ (we assume ~~that~~ ~~the~~ ~~even~~ ~~N~~ to be even) of ~~the~~ <sup>(with)</sup> final state of spin  $J$  and parity  $(-1)^J$  can be written as

$$\sigma^{(n)}(J=L, Q_0) = \left| \sum_{j_1 j_2} B(j_1 j_2; J_n) S(j_1, j_2; L, Q_0) \right|^2 \quad (8)_{1.8}$$

where

$$S(j_1, j_2; L, Q_0) = \sigma(j_1, j_2; L, Q_0) \quad (9)_{1.9}$$

and

$$B(j_1 j_2; J_n) = \left\langle \Phi_{J_n}(\xi_{A+2}) \left| \left[ \Phi_{J_i=0}(\xi_A) \frac{[a_{j_1}^\dagger a_{j_2}^\dagger]_J}{[(1+\delta(j_1, j_2))]^{1/2}} \right] \right. \right\rangle \quad (10)_{1.10}$$

is the two-nucleon spectroscopic amplitude, ~~the~~  $\Phi_{J_i=0}(\xi_A)$  being the wavefunction describing the ground state of the initial ~~state~~ ~~state~~ (ground state of the ~~initial~~ nucleus,  $\Phi_{J_n}$  that of the final, ~~the~~  $\xi$  labelling the radial and spin relative coordinates. Assuming  $A$  to be a closed shell system, at least in neutrons, and  $J_i=0$ , one can write

$$|0_n^+\rangle = |J=0\rangle = \sum_{j_1 j_2} C^{(n)}(j_1, j_2; J=0) |j_1, j_2; J=0\rangle, \quad (11)_{1.11}$$

where  $n=1, 2, 3, \dots$  labels the ~~final~~ ~~final~~ final nucleus ~~the~~ states of spin  $J=0$  in increasing order.

energy order, making use of the (8)  
completeness relation of the coefficients  
 $c^{(n)}(j, j; J=0)$  one ~~obtains~~ obtains,

$$\sum_n \sigma^{(n)}(J=L=0, Q) = \sum_j \sigma(j, j; L=0, Q) \quad (12)$$

The above equation is quite similar to (6)<sup>1.6</sup>, aside from the fact that the  $Q$ -value effect in (6)<sup>1.6</sup> can be analytically dealt with, ~~while~~ while  $\sigma(Q)$  is a functional of  $Q$ . This is in keeping with the fact that in elastic and inelastic processes the mass partition is equal in both entrance and exit channels. Thus, the intrinsic ~~structure~~ (structure) and the ~~relative motion~~ ~~coordinates~~ ~~can~~ ~~be~~ ~~treated~~ ~~separately~~ ~~this~~ ~~is~~ ~~not~~ ~~the~~ ~~case~~ ~~for~~ ~~transfer~~ ~~processes~~, ~~both~~ ~~intrinsic~~ ~~and~~ ~~reaction~~ ~~coordinates~~ ~~being~~ ~~interweaved~~ ~~through~~ ~~the~~ ~~recoil~~ ~~process~~ ~~(particle - recoil mode coupling)~~.

relative motion (coordinates) ~~can~~ ~~be~~ ~~treated~~ ~~separately~~. This is not the case for transfer processes, both intrinsic and ~~reaction~~ <sup>reaction</sup> coordinates being interweaved through the recoil process (particle - recoil mode coupling). ~~even~~ from a physics point of view

The analogy becomes <sup>(even)</sup> richer ~~physically~~, remembering the fact that in the case of independent particle

cf. Fig. 5 and 6; cf. also App. B.)

in 1.5 and 1.6  $\uparrow$  np (27) - (30)

pure two-particle configurations (9)

$$|0_{n=1}^+\rangle = |j^2(0)\rangle = [a_j^+ a_j^+]_0 |0\rangle, \quad (1.13) \quad a_j |0\rangle = 0$$

the vacuum  $|0\rangle$  contains only independent-particle ZPF ( $\Delta x_k \Delta p_{xk} \geq \hbar$ ), while in the case of collective pairing vibrations, i.e. vibrations which change particle number in two units,

(being)

$$|0_{n=1}^+\rangle = \prod_{n=1}^{(\beta=+2)} |\tilde{0}\rangle = \sum_{k=1}^{n=1} X_k [a_k^+ a_k^+]_0 \prod_{i=1}^{n=1} [a_i a_i]_0, \quad (1.14) \quad (1.15)$$

where  $\beta$  is the transfer quantum number,  $X_k$  and  $[a_i a_i]_0$  are corresponding

and  $\prod_{n=1}^{(\beta=+2)} |\tilde{0}\rangle = 0$ . The ZPF is ~~measured~~ given by  $(\frac{\hbar \omega_{n=1}}{2 C_{n=1}})^{1/2} = (\frac{\hbar^2}{2 D_{n=1}} \frac{1}{\hbar \omega_{n=1}})^{1/2}$  collectively

A further parallel can be achieved by ~~introducing~~ defining two-particle units (1.15) (1.15)

$$\sigma_{2pu}^{\max}(A, L, Q) = \max[\sigma(j_1, j_2; L, Q_0)]$$

where  $\max[\ ]$  indicates that the largest two-particle absolute cross section in the single-particle subspace considered (hot orbital), is to be considered. In this way one can write the relation (42) in dimensionless units. Furthermore, one can define enhancement factors.

It is to be noted that it is to be noted that the

~~percol sound ku dx~~  
two-particle transfer  
Another sum rule has been introduced <sup>(10)</sup>  
in the literature,  
(Bayman and Clement 1972), which  
relates <sup>the difference between</sup> two-nucleon stripping and  
pick-up reactions, with <sup>cross sections</sup> single-  
particle transfer processes. (cf. also  
~~Let us now return~~ Landford and

### 1.3 Couplings between elementary modes

Let us now return to the subject  
<sup>Pauli principle</sup> of the finite overlap existing between  
the elementary modes of nuclear  
excitation. That is, to the fact that  
one is working in a ~~physical~~  
<sup>of states</sup> basis which contains much of the  
physics one likes to describe, but <sup>which has</sup> ~~having~~  
the shortcoming of ~~being non~~  
~~orthogonal~~  
being overcomplete. An orthogona-  
lization ~~protocol~~ <sup>protocol</sup> procedure, like a gene-  
ralized Gram-Schmidt procedure, but  
leading to an effective field theory,  
where the different modes melt together,  
is called for (cf. App. C)

Because the overlaps between elemen-  
tary modes of excitation is proportional  
to their coupling, and in keeping with  
the fact that mean field theory is the  
natural starting point of ~~the~~ nuclear



~~two-particle transfer~~  
(two-particle transfer)

Another ~~sum~~ rule has been introduced <sup>(10)</sup>  
~~in the literature~~

(Bayman and Clement 1972), which  
<sup>the difference between</sup> relates two-nucleon stripping and  
pick-up reactions, with <sup>cross sections</sup> single-  
particle transfer processes. (cf. also  
~~Let us now return~~ Landford and

### 1.3 Couplings between elementary modes

Pauli  
principle

Let us now return to the subject  
of the finite overlap existing between  
the elementary modes of nuclear  
excitation. That is, to the fact that  
one is working in a ~~physical~~  
basis <sup>of states</sup> which contains much of the  
physics one likes to do. <sup>which has</sup>  
the ~~acting~~

~~bein~~

bein  
li za  
ra lize  
leadin  
where  
in call

Pauli  
principle

gona-  
gene-  
rut  
y,  
gether,

Because the overlaps between elemen-  
tary modes of excitation is proportional  
to their coupling, and in keeping with  
the fact that mean field theory is the  
natural starting point of ~~the~~ nuclear

structure calculations, overcoming - (11)  
pleteness of the basis is tantamount  
to the appearance of linear couplings  
between quasiparticles and collective  
modes (cf. App. D and E) (old ch. 5 ~~inelastic~~ scattering)

Basis orthogonalization thus implies  
the diagonalization of the associated  
particle-vibration coupling Hamil-  
tonian  $H_C$ . The rules to do so have  
been cast into a <sup>(graphical)</sup> ~~and~~ ~~effective~~ effective  
field theory, namely the Nuclear Field  
Theory (NFT). In this theory ~~particles~~  
the free fields are allowed to  
interact through ~~four-point~~ four-point vertices  
(bare interaction acting among  
particle lines) and the particle-  
vibration vertices, ~~between particle~~  
~~lines and~~

to be calculated in the HF (HFB)  
approximation (particle lines) and  
in the RPA (QRPA) (vibrations). These  
elementary modes of excitation  
interact through four-point vertices  
(nucleon-nucleon <sup>bare</sup> interaction), and  
through the particle-vibration cou-  
pling vertices.

The NFT rules for evaluating  
the effect of these couplings between

fermions and bosons involve a number of restrictions, ~~in keeping with the fact that the collective~~

~~the~~ concerning initial and intermediate states as compared with the usual rules of perturbation theory that are to be used in ~~the~~ evaluating the effect of the original nucleon-nucleon interaction acting in the fermion space. This is in keeping with the fact that the collective modes ~~contain~~ the correlations arising from forwards ~~and~~ and backwards going particle-hole ( $\beta=0$ ) as well as as particle-particle ( $\beta=+2$ ) and hole-hole ( $\beta=-2$ ) bubbles. Furthermore, because these ~~quasi~~ bosons are not elementary but composite fields, ~~made out of~~ made out of pairs of fermions, and thus subject to ~~the~~ the Pauli principle.

~~The general validity~~

~~Nuclear Field Theory~~

The general validity of ~~the~~ NFT rules have been demonstrated

by proving the equivalence existing, to each order of perturbation theory, between the many-body finite nuclear system ~~propagator~~ <sup>calculated</sup> in terms of Feynman diagrams ~~involving~~ <sup>only</sup> the fermionic degrees of freedom, i.e. explicitly respecting Pauli in a complete and ~~not~~ not overcomplete basis, and the propagator constructed in terms of Feynman diagram involving fermion and phonon degrees of freedom (NFT Feynman diagrams) in the case of a general two-body interaction and an arbitrary distribution of single-particle levels.

Concerning the actual ~~existence~~ <sup>(the practical difficulty of</sup> of NFT ~~one can~~ <sup>recognize</sup> ~~that it is~~ <sup>in keeping with the fact that</sup> ~~short of impossible~~ <sup>respecting</sup> the corresponding rules, ~~there is~~ not a single bare NN-force (eventually with 3N and higher order corrections) with which it is possible to generate a mean field ~~and coll~~ (cf. Eq. (3)) and collective modes, that is,

Concerning the actual embodiment of NFT one can recognize the practical difficulties of respecting the corresponding rules. This is in keeping with the fact that there is not a single bare NN-force (eventually with 3N and higher order corrections) with which it is possible to generate a mean field (Eq (3)) <sup>1,3</sup> to determine the single-particle states and, by introducing a periodic time-dependence with the constraint <sup>1,16</sup>

$$\delta U(r) = \int d^3r' \delta \rho(r') v(|\vec{r} - \vec{r}'|), \quad (16)$$

calculate the collective modes associated with the variety of particle-hole ( $\beta=0$ ; density, spin, isospin, etc) and pairing ( $\beta=\pm 2$ ; monopole and multipole pair addition and pair subtraction) channels. If such a low- $k$  well behaved bare force was available one could then diagonalize, within the framework of NFT and to any desired order of perturbation theory the Hamiltonian  $H_c$ ,  
sum

(Schwenk)



(13)<sub>b</sub>

One could argue that one can reach a similar goal by making use of effective interactions, each tailored to provide a sensible description of each of the channels considered. For example a Skyrme interaction (like  $\text{SLy4}$ ) to calculate mean field, single-particle modes, and eventual some  $\beta=0$  modes.

$$\delta U(r) = \int d^3r' \rho(r') v(|\vec{r} - \vec{r}'|), \quad (18) \quad 1.16 \quad (14)$$

~~which, however,~~

~~is not a normalizing factor~~

for all channels (density, spin, isospin, etc) which, once the variety of couplings are carried out to the needed order, infinite ~~for~~ some case, ~~processes if needed~~, provide a quantitative account of the data. In other words, ~~ab initio is ruled out~~ ~~and thus is~~ and thus a common ground state ~~corrected~~ which corrected with the corresponding homogeneous ZPF lead eventually to the "exact" ground state (cf. App. A)

~~On the other hand empirical~~

have been carried out,

On the other hand, empirical ~~rule~~ ~~have been~~ ~~carried out~~, making use of the bare Argonne  $v_{14}$  potential, and of Skyrme <sup>forces</sup> (or Saxon-Woods ~~parametrization~~ ~~parametrizations~~) to determine the mean field and spin-vibrational channels, and multipole-multipole forces with ~~self~~ self-consistent coupling constants for the variety of density ~~vibration~~ vibration channels.

The resulting predictions are, as a rule, able to provide ~~an overall~~ ~~account~~ ~~together with specific reaction software~~, in particular COOPER, ~~of the~~ "complete"

as well as dressed modes

dual origin  
+  $S_N(pit)$  etc

dual  
 $^{11}Li$   
 $^{12}Be$   
anom  
 $2+$   
 $S_N$   
while  
Colo

~~sets~~ sets of experimental data, ~~obtained~~ obtained with the help of Coulomb, inelastic and one- and two-nucleon transfer data, (as can be seen From Figs. ....)

Eggs  
 $\beta_2$

Summing up, ~~the~~ the nuclear structure description ~~provided~~ <sup>given</sup> by the elementary modes of nuclear excitation approach within the framework of NFT, provides a ~~complete~~ <sup>unified</sup> description of the variety of observables. At the same time, each cross section or <sup>essentially</sup> transition probability is connected to all others (see Fig 6)

able to map out the nuclear structure-reaction landscape

landscape  
nuclear  
structure  
landscape



text of Ch. 1 Intr.

Continue in

p. (25)

those associated with

Competition between the variety of ZPF, in particular density ( $\beta=0$ ) and pairing vibrational ( $\beta=\pm 2$ ) modes

Non-orthogonality of the NFT basis  
made out of local elementary modes  
of excitation Appendix E 30/07/14 (1)

The ground state of  $^{210}_{84}\text{Po}_{126}$  can be (16)

viewed as the proton pair addition mode  
of the doubly closed shell nucleus  $^{208}_{82}\text{Pb}_{126}$ ,  
mode displaying  $J^\pi = 0^+$  and  $\beta = +2$

(transfer-) quantum numbers. Within this framework  
expected to be a bona fide proton  
single-particle system ( $\beta = +1$ ), in which  
the  $g_{7/2}$ ,  $d_{5/2}$ ,  $h_{11/2}$ ,  $d_{3/2}$  and  $g_{1/2}$  are  
occupied, the odd proton occupying  $h_{9/2}$ , in  
the ground state, a substate of the  
 $h_{9/2}$  orbital. (one-proton stripping and pick up reactions,  
e.g. with the help of)

This picture can be specifically probed  
through  $^{210}\text{Po}(t, \alpha)^{209}\text{Bi}$  and  $^{208}\text{Pb}(^3\text{He}, d)^{209}\text{Bi}$  transfer processes.

While essentially the full reaction cross

pick-up reaction cross section  
consistent with occupancy (full  $(2j+1)$ ) is  
found in a single peak in the case

$3/2^+$  of the states  $1/2^+$  ( $g_{1/2}$ ) and  $11/2^-$  ( $h_{11/2}$ ),  
two states with essentially equal  
strength and lying close to the  
expected (independent-particle)

energy are observed. These four peaks  
are essentially not excited in the  
stripping process, testifying to their  
essential hole character

(see table E.1)

It is of notice  
that

↑  
footnote

present case, at variance with  
the rest of the monograph,  
we will be made of spectroscopic  
factors

of the end of  
Sect 1.1

2.1

30/07/14 (2)

In an attempt to further clarify the structure of the two  $3/2^+$  resonances made to the inelastic process  $^{209}\text{Bi}(d,d')$ . Both states are excited in the process.

(17)

with a summed cross section consistent with that expected for the  $3/2^+$  member of the  $(h_{9/2} \pi) \otimes 3^-(^{208}\text{Pb})$  positive parity septuplet ( $J = 3/2 - 15/2$ )

~~process through~~ process, the angular distribution of the associated cross sections revealing the  $L=3$ , octupole character (Tables <sup>C.2 and C.3</sup> ~~2 and 3~~) with centroid around 2.6 MeV

(Tables C.2 and C.3) In keeping with the fact that the same experiment reveals a ~~multiplet~~ multiplet (septuplet) of states with summed ~~cross~~  $L=3$  inelastic cross section consistent with that of the lowest collective ( $2.615\text{ MeV}$ ,  $B(E3)/B_{sp} \approx 32$ ) octupole vibration of  $^{208}\text{Pb}$ , one can posit that the two  $3/2^+$  states are a linear combination of the unperturbed ~~states~~ (two-particle)-(one-hole) ~~states~~ (2p-1h) states, (1.C.1)

$$|\alpha\rangle = |d_{3/2}^{-1} \otimes \text{gs}(^{210}\text{Pb}); 3/2^+\rangle \equiv |\uparrow\uparrow\rangle,$$

and

$$|\beta\rangle = |h_{9/2} \otimes 3^-(^{208}\text{Pb}); 3/2^+\rangle \equiv |\uparrow\frac{5}{2}\rangle.$$

(1.C.2)



Because these states lie very close in energy ~~all~~ they mix. According to NFT, the most important contribution <sup>(to this mixing arises)</sup> ~~arising~~ from the process given in Fig. ~~1.C.1~~ C.1

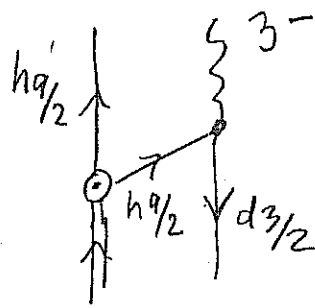


Diagram describing ~~the~~ one of the most important processes coupling the ~~the~~  $2p-1h$  states (1.C.1) and (1.C.2),

The resulting (mixed) <sup>physical</sup> states can be approximately written ~~as~~ (see Bortignon et al 1977 for details) as,

(in)  
Fig 4.7 p. 344

$$|I\rangle = -0.53 |\alpha\rangle + 0.76 |\beta\rangle, \quad (1.C.3)$$

and

$$|III\rangle = \overset{1.02}{\cancel{0.92}} |\alpha\rangle + \overset{0.80}{\cancel{0.71}} |\beta\rangle, \quad (1.C.4)$$

② - ①  $\rightarrow$  (from P. ①<sub>a</sub>)

Let us now calculate the overlap  $\sigma = \langle \alpha | \beta \rangle$  between the basis states  $|\alpha\rangle$  and  $|\beta\rangle$ , that is  $\sigma = \cos \chi$  (cf. Fig. 1.C.2). Following this figure (cf. also caption) one can write,

$$\sqrt{\sigma_I^{tr}} = \cos \phi \quad ; \quad \sqrt{\sigma_{II}^{tr}} = \cos\left(\frac{\pi}{2} - \phi\right) = \sin \phi, \quad (1.C.5)$$

where

$$\sigma^{tr} = \sigma_I^{tr} + \sigma_{II}^{tr} = 1, \quad (1.C.6)$$

in keeping with the fact that the absolute cross sections to the states  $|I\rangle$  and  $|III\rangle$  are normalized in terms of the total cross section.

In the same way

$$\sqrt{\sigma_I^{oct}} = \cos(\chi - \phi) = \cos \chi \cos \phi + \sin \chi \sin \phi, \quad (1.C.7)$$

and

$$\begin{aligned} \sqrt{\sigma_{II}^{oct}} &= -\cos\left(\pi - \left(\frac{\pi}{2} - \phi + \chi\right)\right) = -\cos\left(\frac{\pi}{2} + (\phi - \chi)\right), \\ &= \sin \phi \cos \chi + \sin \chi \cos \phi. \quad (1.C.8) \end{aligned}$$

(a) as resulting from the calculation of the <sup>(19)</sup><sub>a</sub>  
 diagram displayed in Fig. 1C.1 to all  
 orders with the help of Brillouin-Wigner  
 perturbation theory (diagonalization of  
 the corresponding effective Hamiltonian;  
 cf. p. 316 Bortignon et al 1977).  
 to p. (19) (a)

(b) A simple estimate of the NFT prediction  
 can be made making use of the relations  
 $\langle I|I \rangle = (-0.53)^2 + (0.76)^2 - 2 \times 0.53 \times 0.76 \theta = 1$ ,  
 $\langle II|II \rangle = (1.02)^2 + (0.80)^2 + 2 \times 1.02 \times 0.80 \theta = 1$   
 and  $\langle I|II \rangle = -0.53 \times 1.02 + 0.76 \times 0.80$   
 $+ (-0.53 \times 0.80 + 0.76 \times 1.02) \theta = 0$ , leading  
 to  $\theta = -0.18, -0.42$  and  $-0.19$  respectively  
 and, thus, to the average value of  $-0.26$ .  
 to p. (20) (b)

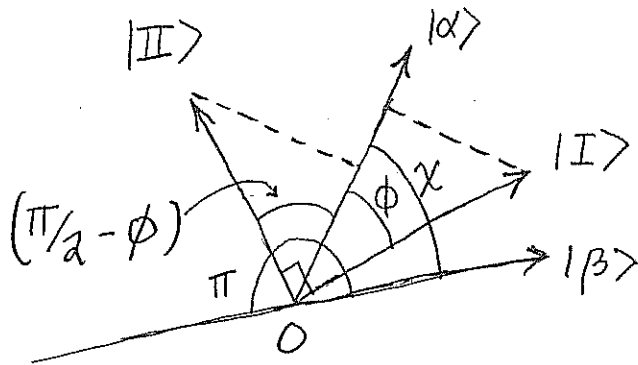


Fig. 1.C.2

Schematic representation of the  $3/2^+$  states entering the NFT calculation of the process displayed in Fig. 1.C.1. The basis state  $|\alpha\rangle$  carries the full  $(t, \alpha)$  transfer strength  $(tr.) \sigma^{tr}$ , while the basis state  $|\beta\rangle$  the full octupole (oct.) strength  $\sigma^{oct}$  (see Tables 1.C.1 - 1.C.3). The overlap between these states is denoted  $\cos \chi$ . The physical states obtained through the <sup>(Feynman)</sup> "orthogonalization process" are denoted  $|I\rangle$  and  $|II\rangle$  (cf. Eqs. (1.C.3) and (1.C.4))

$$|I\rangle = -0.53 |\alpha\rangle + 0.76 |\beta\rangle, (1.C.3)$$

and

$$|II\rangle = -0.92 |\alpha\rangle - 0.71 |\beta\rangle, (1.C.4)$$

Let us now calculate the overlap  $\Theta = \langle \alpha | \beta \rangle$ ,

$$|\alpha\rangle \equiv |d_{3/2} \otimes g_s(210 p_0); 3/2^+\rangle = |\uparrow\uparrow\rangle$$

$$|\beta\rangle \equiv |h_{9/2} \otimes g_s(208 p_6); 3/2^+\rangle = |\uparrow\downarrow\rangle$$

overlap between the basis states  $|\alpha\rangle$  and  $|\beta\rangle$ , that is

$$\Theta = \cos \chi \text{ (cf. Fig. 1.C.2)}$$

The overlap between the states is denoted  $\cos \chi$ .

The physical states obtained through the NFT "orthogonalization process" are denoted  $|I\rangle$  and  $|II\rangle$  (cf. Eqs. (1.C.3) and (1.C.4)).

One can then write

$$\sqrt{\sigma_I^{tr}} = \cos \phi; \quad \sqrt{\sigma_{II}^{tr}} = \cos(\frac{\pi}{2} - \phi) = \sin \phi \quad (1.C.5)$$

$$\sigma^{tr} = \sigma_I^{tr} + \sigma_{II}^{tr} = 1 \quad (1.C.6)$$

in keeping with the fact that the absolute cross sections are normalized in terms of the total cross section.

In the same way

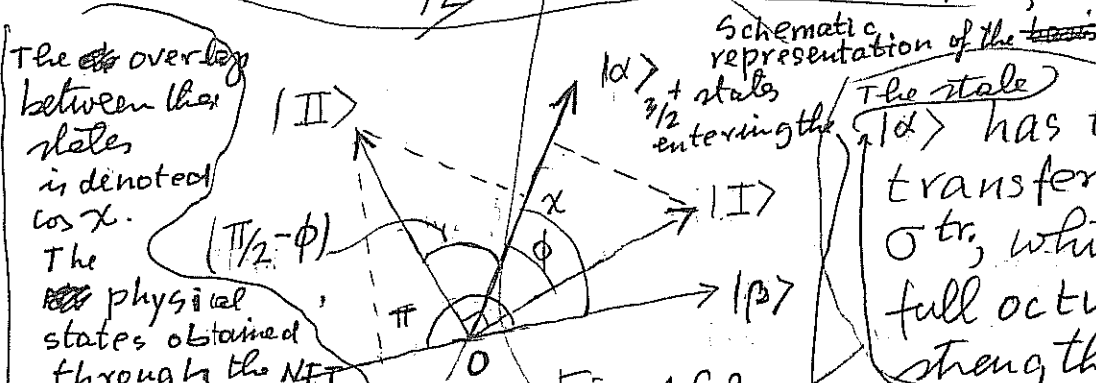
$$\sqrt{\sigma_I^{oct}} = \cos(\chi - \phi) = \cos \chi \cos \phi + \sin \chi \sin \phi \quad (1.C.7)$$

and

$$\begin{aligned} \sqrt{\sigma_{II}^{oct}} &= -\cos(\pi - (\frac{\pi}{2} - \phi + \chi)) = -\cos(\frac{\pi}{2} + (\phi - \chi)) \\ &= -\sin \phi \cos \chi + \sin \chi \cos \phi \quad (1.C.8) \end{aligned}$$

$$\begin{aligned} \sin(a \pm b) &= \sin a \cos b \pm \cos a \sin b \\ \cos(a \pm b) &= \cos a \cos b \mp \sin a \sin b \end{aligned}$$

$$\begin{aligned} \cos(-\chi) &= \cos \chi \\ \sin(-\chi) &= -\sin \chi \end{aligned}$$



Thus

$$\sqrt{\sigma_I^{\text{oct}}} = \cos \chi \sqrt{\sigma_I^{\text{tr}}} + \sin \chi \sqrt{\sigma_{II}^{\text{tr}}} \quad (1.C.9)$$

~~(3)~~  
~~(9)~~  
(20)

and

$$\sqrt{\sigma_{II}^{\text{oct}}} = -\cos \chi \sqrt{\sigma_{II}^{\text{tr}}} + \sin \chi \sqrt{\sigma_I^{\text{tr}}} \quad (1.C.10)$$

Multiplying the above relations by  $\sqrt{\sigma_I^{\text{tr}}}$  and  $\sqrt{\sigma_{II}^{\text{tr}}}$  respectively one obtains,

$$\sqrt{\sigma_I^{\text{tr}} \sigma_I^{\text{oct}}} = \cos \chi \times \sigma_I^{\text{tr}} + \sin \chi \sqrt{\sigma_I^{\text{tr}} \sigma_{II}^{\text{tr}}} \quad (1.C.11)$$

and

$$\sqrt{\sigma_{II}^{\text{tr}} \sigma_{II}^{\text{oct}}} = -\cos \chi \sigma_{II}^{\text{tr}} + \sin \chi \sqrt{\sigma_I^{\text{tr}} \sigma_{II}^{\text{tr}}} \quad (1.C.12)$$

Subtracting the above relations leads to the overlap expression

$$\cos \chi = \frac{-\sqrt{\sigma_I^{\text{tr}} \sigma_I^{\text{oct}}} + \sqrt{\sigma_{II}^{\text{tr}} \sigma_{II}^{\text{oct}}}}{\sigma_I^{\text{tr}} + \sigma_{II}^{\text{tr}}} \quad (1.C.13)$$

Tables 1.C.1-1.C.3

Making use of the values of  $\sqrt{\sigma}$  (cf. Table 4.7 of (Bortignon et al 1977)) one obtains

$$\cos \chi = \frac{\sqrt{1.8 \times 4.2} - \sqrt{2.2 \times 1.1}}{4} = -0.298 \quad (1.C.14)$$

(see Table 4.6 Bortignon et al (1977),  $M_{(3/2)_1(3/2)_2}^{(3/2)_{h9/2}(0^+ d_{3/2})} = -0.271$ )

in overall agreement with the

NFT predictions  $(-0.18 - 0.27 - 0.16)/3 \approx -0.20$

(b)-(b) from P (19) a

~~-0.42 - 0.19~~  $\uparrow$  ~~-0.26~~  
(152)

Of course we can hardly expect  
to obtain the sign to agree with  
the NFT as it is associated with a  
free choice of the axis of reference  
(Fig. <sup>1, C, 2</sup> 6) (note also the fact that  
 $\sigma$  is well defined, ~~but~~ <sup>while</sup>  $\sqrt{\sigma}$  is  
undetermined by an overall sign).

(4) (6)  
(21)

Non-orthogonality N.F.T. (elementary modes of excitation) ~~base~~

$$|3/2_1\rangle \approx -0.53 \left| \begin{array}{c} \uparrow \downarrow \\ d_{3/2} \end{array} \right\rangle + 0.76 \left| \begin{array}{c} \uparrow \\ h_{9/2} \end{array} \right\rangle$$

(4) 7  
(22)

$$|3/2_2\rangle = -0.92 \left| \begin{array}{c} \uparrow \downarrow \\ d_{3/2} \end{array} \right\rangle - 0.71 \left| \begin{array}{c} \uparrow \\ h_{9/2} \end{array} \right\rangle$$

alternative

Another way to work out the overlap  $\theta = \langle I | J \rangle$  can be determined from the normalization condition of the states by the states  $|I\rangle$  and  $|J\rangle$ .

$$\langle I | I \rangle \approx (0.53)^2 + (0.76)^2 - 2 \times 0.53 \times 0.76 \theta = 1 \quad (1.c.15)$$

Thus,  $0.859 - 0.806 \theta = 1 \quad (1.c.16)$

And

$$\theta = -\frac{0.141}{0.806} \approx -0.18 \quad (1.c.17)$$

Libro 10  
Lough

NRIR

Similarly,

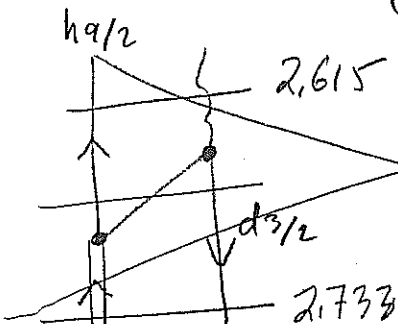
$$\langle II | II \rangle \approx (0.92)^2 + (0.71)^2 + 2 \times 0.92 \times 0.71 \theta = 1$$

leading to  $1.351 + 1.306 \theta = 1 \quad (1.c.19)$

and

$$\theta = \frac{-0.306}{1.351} \approx -0.27 \quad (1.c.20)$$

From state info, neglecting the term proportional to  $\theta$  one obtains,



$M_{1,2} = -0.271$   
 See Table 4.6  
 [Phys. Rep.]

Finally,

$$\langle I | II \rangle \approx \langle 3/2_1 | 3/2_2 \rangle = 0 = (0.53 \times 0.92) - (0.76 \times 0.71) + 2(-0.53 \times (-0.71) - 0.92 \times 0.76) \theta$$

$$= -0.052 - 0.323 \theta = 0 \quad (1.c.22)$$

leading to  $\theta = -\frac{0.052}{0.323} \approx -0.16 \quad (1.c.23)$

Ortho



	$E_x$ (MeV)	$S(t, \alpha)$ (2j+1)	$S(^3\text{He}, d)$
$3/2^+$	2.49	$1.8 \pm 0.3$	$< 0.01$
$3/2^+$	2.95	$2.2 \pm 0.3$	$< 0.01$
$1/2^+$	2.43	1.8 (2)	$< 0.02$
$11/2^-$	3.69	10.0 (12)	$< 0.05$

87.8

single-particle transfer

✓ Table 1.C.1 ~~Relative~~ Experimental values of the energy and of the relative cross sections associated with low-lying states of  $^{209}\text{Bi}$  ~~as formulated in~~

the reaction  $^{210}\text{Po}(t, \alpha)^{209}\text{Bi}$

		$\frac{\sigma(^{209}\text{Bi}(9/2^-, g.s.) \rightarrow ^{209}\text{Bi}(3/2^+; E))}{\sigma(^{208}\text{Pb}(g.s.) \rightarrow (3^-; 2.615 \text{ MeV}))}$
$3/2$	2.49	$0.041 \pm 0.003$
$3/2$	2.95	$0.011 \pm 0.002$

✓ Table 1.C.2 Relative inelastic octupole cross sections associated with the inelastic excitation of the two lowest-lying  $3/2^+$  states of  $^{209}\text{Bi}$  (after Bortignon et al 1977 and refs. therein)

	$E_n$ (MeV)		$\frac{\sigma(nq_1 \rightarrow 3/2^+)}{\sigma(0^+ \rightarrow 3^-)}$ (%)		$S(t, d)$		$S(^3\text{He}, d)$	
	Theory	Exp	Theory	Exp	Theory	Exp.	Theory	Exp
$3/2$	<del>3.76</del> 2.480	2.494	3.76	$4.2 \pm 0.3$	1.83	$1.8 \pm 0.3$	0.02	$< 0.01$
$3/2$	<del>2.956</del> 3.125	2.95	1.56	$1.1 \pm 0.2$	2.25	$2.2 \pm 0.3$	$10^{-5}$	$< 0.01$

✓ Table 1.C.3

Resume of NFT prediction of the structure and reaction properties of the lowest-lying  $3/2^+$  state of  $^{209}\text{Bi}$  in comparison with the experimental data (after Bortignon et al 1977 and refs. therein; see also Tables 1.C.2 and 1.C.2).

✓ Table 2 C.2 (total)

The ~~total~~ inelastic cross section  $\sigma_{\text{oct}}$  associated with the octupole vibrational state of  $^{208}\text{Pb}$  can be written ~~as~~ in terms of that associated with a single magnetic substate  $\sigma'$  as  $\sigma_{\text{oct}} = 7\sigma'$ . That associated with the multiplet  $(h_{9/2} \otimes 3^-)_{J^+}$  ( $J = 3/2 - 15/2$ ) as  $\sigma_{\text{oct}} = 70\sigma'$ ;

in keeping with the fact that the  $h_{9/2}$  state has 10 magnetic substates. Thus, the strength associated with the  $3/2$  channel

is  $4/70 = 0.057$ , to be compared with the observed (percentage) summed strength  $0.053 \pm 0.003 (= 0.042 \pm 0.003 \pm 0.011 \pm 0.002)$  associated with the  $2.45 \text{ MeV}$  and

✓ Table 4 C.1 the  $2.95 \text{ MeV } 3/2^+$  state; see Bortignon et al (1977).

~~Single-particle~~ Single-particle strength associated with the single-particle transfer reactions  $^{210}\text{Po}(\alpha, d)^{209}\text{Bi}$  and  $^{208}\text{Pb}(^3\text{He}, d)^{209}\text{Bi}$  (cf. Bortignon et al 1977).

✓ Table 3 C.3 et al 1977).

Summary of NFT calculations predictions ~~and for the two lowest  $3/2^+$~~  concerning the structure of the two lowest  $3/2^+$  state of  $^{209}\text{Bi}$ , in comparison with the experimental data (see Bortignon et al 1977)

Table 4.7 of

$$X = \frac{G(2J+1)}{D} = G N(\epsilon) = \lambda$$

those associated

appendix 1

Competition between the variety of ZPF, in particular density ( $\beta=0$ ) and pairing ( $\beta=\pm 2$ ) modes

(26)  
(25)

The ~~single particle~~ <sup>vibrational</sup> dressing through the ~~vibrations~~

~~Vibron~~ (Nilsson-like)

Particle-hole like vibrations, like e.g. quadrupole vibrations, induce dynamical distortions of the mean field which break virtually the  $(2j+1)$  magnetic degeneracy of levels with two-fold ~~degenerate~~ (Kramer's) degenerate levels, thus ~~effectively~~ reducing the ~~Density~~ of states (DOS) around the Fermi energy

Fig 1

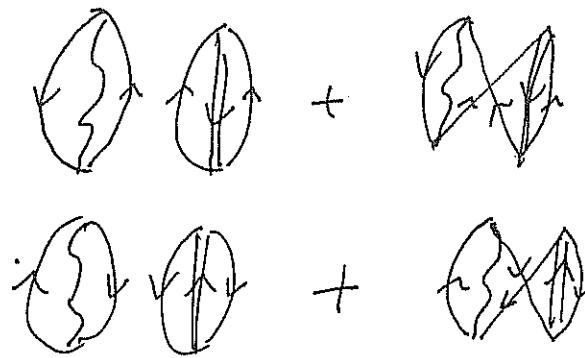
Fig 1: A schematic representation of the ~~interweaving~~ of single-particle motion and collective vibrations has on pairing correlations

Pairing vibrations smooth out the sharp discontinuity at the Fermi energy ~~for~~ displayed by ~~non-interaction~~ closed shell systems, thus effectively concentrating in an effective single  $j$ -shell through dynamical  $U_j V_j$  weighting factors, the global degeneracy of levels ~~around~~ in the interval  $\epsilon$  energy region

$$\Sigma_F \pm E_{corr}(\beta = \pm 2) (\text{Fig 1(g)}) \quad 1.6$$

ZPF ~~is~~ induced by ~~particle-hole~~  
 particle-hole like and by  
 pairing modes conjugate with each  
 other, through Pauli's principle

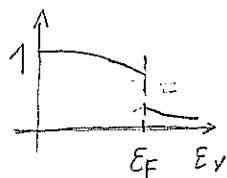
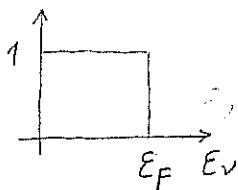
(17)  
 26



~~X = GPR~~  
~~etc~~

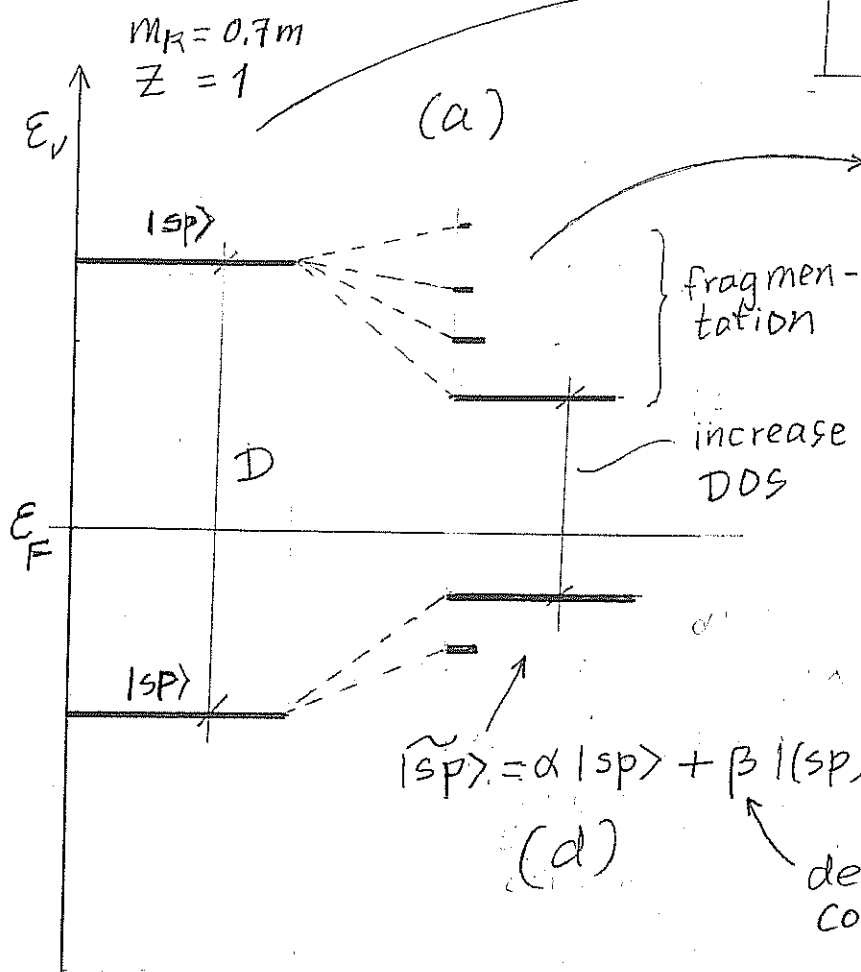
thus leading to a single ground  
 state containing all the dressed,  
 renormalized ZPF (cf. App. A)

(20) 2



$$X = \frac{G 2 \Omega}{D} = G N(0)$$

(b)



(c)

$$\tilde{X} = \tilde{G} \tilde{N}(0)$$

$$\tilde{G} = Z^2 (G + G_{ind})$$

$$\tilde{N}(0) = N(0)/Z$$

$$\tilde{X} = Z (G + G_{ind}) N(0)$$

$H_{MF}$

NFT

(g)



(e)

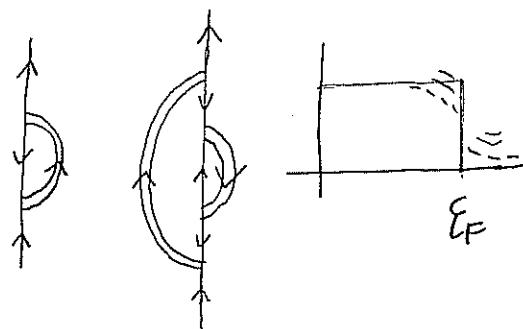
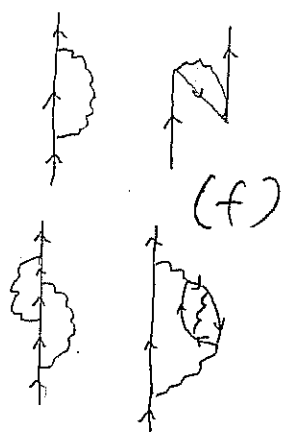


Fig. 1.6

Fig. A

Fig. A 1.6

(; (e), (f))

(1/2)

(26)

bold face

(as measured by  $1/2$ )

Schematic representation of some of the consequences the interweaving of the elementary modes of excitation with varied transfer quantum number ( $\beta = 0, \pm 1, \pm 2$ ) have in the (mainly single-particle) nuclear spectrum, in particular pair correlations, as measured by the (two-level) dimensionless parameter  $X = G^2 \Omega / D = G N(0)$ , product of the bare coupling constant  $G$  and the density of states (DOS) at the Fermi energy (ratio of single-particle degeneracy  $2\Omega = (2j+1)$ , and the single-particle energy separation), Coupling with surface modes (f) reduce the effective value of  $D$  leading to an increase of  $N(0)$  but, at the same time decreases, through the breaking of the single-particle strength, the single-particle content of each level (as measured by  $z$ ). The eventual increase of  $X$ , as reflected by  $\bar{X}$ , results from a delicate balance of the two effects eventually overwhelmed by the induced pairing interaction resulting from the exchange of collective ( $\beta=0$ ) vibration between pair of nucleons

moving in time reversal state,  
and by the dynamical smoothing  
of the Fermi energy by the coupling  
of nyle-particle states to  $\beta = \pm 2$   
pairing vibration (g).

${}^1\text{H}({}^{11}\text{Li}, {}^9\text{Li}(1/2^-)){}^9\text{H}$

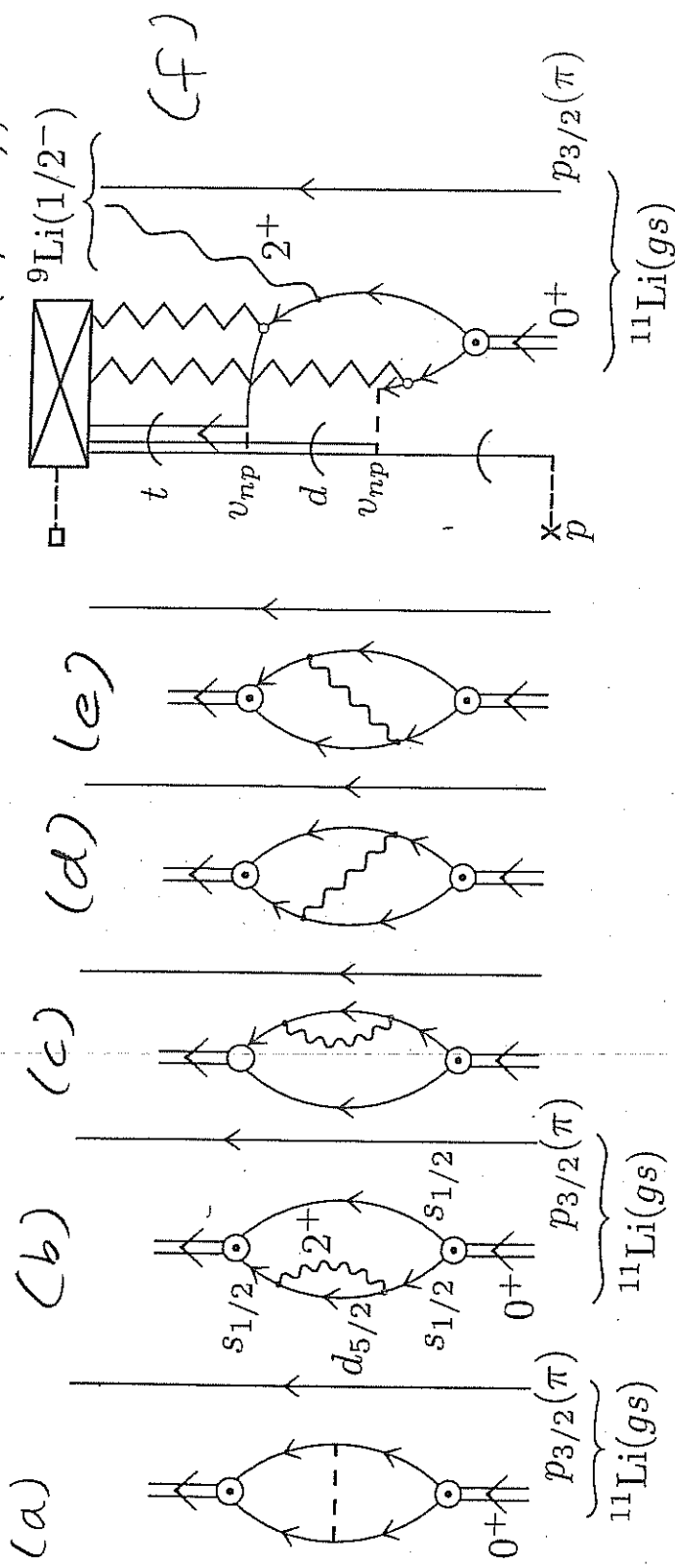


Fig 1.5

1.5  
#  
Fig. 1.5  
Tato



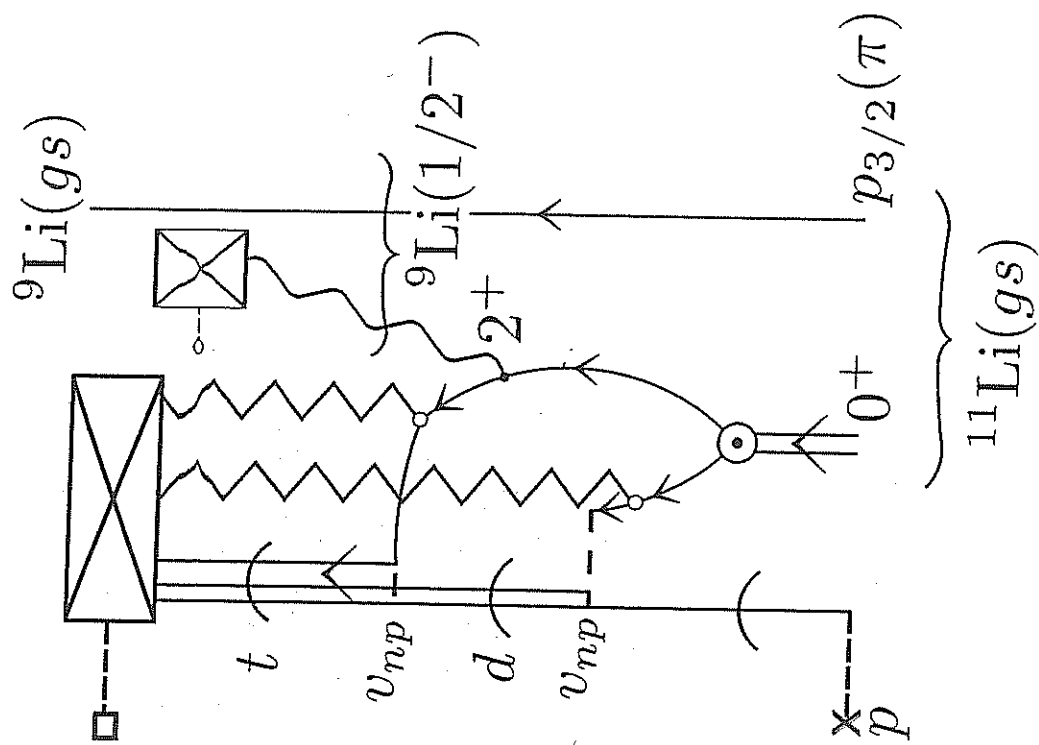
Caption to Fig. 4 <sup>5</sup> <sup>9</sup>Li pair addition mode  
 (doubled arrowed line) (28)

Lowest order, NFT diagrams associated with the processes gluing the <sup>11</sup>Li to the core <sup>9</sup>Li through the exchange of the core quenching role phonon. Single arrowed lines describe the nucleon independent-particle motion of neutrons ( $1s_{1/2}$ ,  $d_{5/2}$ , etc) as well as of protons ( $p_{3/2}(\pi)$ ).

(a) Bare interaction, four-point vertex (horizontal dashed line); (b,c) self energy, effective mass process dressing the  $s_{1/2}(v)$  single-particle state; (d,e) vertex correction (induced interaction) renormalizing the pair addition mode coupling vertex with which it couples to the fermion (dotted open circle); (f) NFT diagrams describing the reaction ~~the reaction~~

$^1\text{H}(^9\text{Li}, ^9\text{Li}(1/2^-; 2.69\text{MeV}))^3\text{H}$  populating the first excited state of <sup>9</sup>Li.

The jagged line is the recoil phonon carrying asymptotically to the detector the momentum mismatch associated with the transfer process. In this case of successive transfer, one for each transferred neutron ( $^{11}\text{Li}(gs) + p \rightarrow ^{10}\text{Li} + d \rightarrow ^9\text{Li}(1/2^-) + t$ )



Variety of pv-  
coupling vertices  
(NFT)

- ⊙ pair
- surface
- recoil

(Fig. 1.6)

Fig 1.6

Tato

Fig 13<sup>6</sup>

(30)

Gedanken  $\gamma$ -ray coincidence  
experiment  $^1\text{H}(^7\text{Li}, ^9\text{Li})^3\text{H}$  and

$^9\text{Li}(\text{gs}) + \gamma(E2: 2.69\text{MeV})$ . In this case, the  
virtual self-energy and vertex  
correction processes ~~due to the~~

becomes real ~~asymptot~~

~~by intervening the~~ through the  
action of the (pit) external field.

Thus, it is not only the recoil phonons  
which have asymptotic wavefunction,  
but also the quadrupole vibration,  
which is ~~not~~ ~~revealed~~ measured  
by the  $\gamma$ -detector. For detail see  
Caption Fig. d.

4