The original Lindemann outerion vcompares the atomic fluctuation amplitude (Arz) with the lattice constant a of a crystal. If this ration, which is defined as the disorder parameter AL, reaches acertain value, fluctuations cannot increase without damaging or destroying the crystal lattice. The results of experiments and simulations show that the critical value for AL for simple solids is in the range of 0.10 to 0.15, relatively undependent of the type of substance, the nature of the interaction potential, and the crystal structure (Bilgram 1987; Löwen, 1994; Stillinger 1995), applications of this criterion to an inhomogeneous finite system like a protein in its native state (aperiodic crystal, schrödinger, 1944) requires evaluation of the generalized Lindemann parameter (Stillinger and Stillinger, 1990),

$$\Delta_L = \frac{\sqrt{\sum_i \langle r_i^2 \rangle / N}}{a!}$$

where N is the number of atoms and a' the most probable non-bonded near-neighbor distance, i's the position of atom i, Dri2= (Ti- (Ti)), and (> denotes configurational

Lindemann F.A. (1970) The catalog of molecular vibrational frequencies, Physik, Z. 11,609-612

(at the conditions of measurement of simulations (e.g., biological) averages. The dynamics as a function of the distance from the geometric center of the protein is characterized by defining interior to (int) Linde mann parameter

 $\Delta_{L}^{int}(r_{cut}) = \frac{\sum_{i,r_{i} < r_{cut}} \langle \Delta r_{i}^{2} \rangle / N}{\alpha^{i}}$ 

over the atoms that are within a chosen cutoff distance, reut, from the center of mass of the protein.

Simulations and experimental data for a number of proteins, in particular Barnase, Myoglobin, Crambin and Ribonuclease A madicate \$0.14 as the critical value distinguishing between solid-like and liquid-like behaviour and reut \$\approx 6A. As can be seen from table 1, the interior of a protein is solid-like (\$\Delta\_L \leq 0.14), while its surface is liquid-like (\$\Delta\_L \leq 0.14), while its surface is

liquid-like ( $\Delta_L > 0.14$ ) under phisiological conditions. The beginning of thermal denaturation in the simulations appears to be related to the melting of its interior (i.e.  $\Delta_L^{int} > 0.14$ ), nothat the entire protein becomes liquid-like

like  $\Delta_L \left( \Delta_L^{int} (6\mathring{A}) \right)$  (300K) MD simulations X-ray data Proteins Barnase Crambin Ribonuclease A Myoglobin all atoms 0,21 (0,12) 0.16 (0.11) 0.16 (0,12) 0.16 (0.09) 0.13 (0.10) 0.12 (0.09) 0.12 (0.08) backbone atoms only 0.16 (0.10) 0.19 (0.13) 0.18(0.12) 0.19(0.10) side-chain atoms only 0,25 (0,14)

Table 1. The heavy-atom  $\Delta_L$  ( $\Delta_L^{int}$ ) value, for four proteins at 300K. After 2 hovetal (1999)

\*) Fluctuations, classical (thermal) or quantal imply a probabilistic description, while one can only predict the odds for a given outcome of an experiment, probabilitie themselves evolve in a deterministic foshio Making use of the harmonic oscillator approximation for the single-particle potential (cf. Fig. 2-22 Bohr and Mottelson, 1969) one can write (cf. Eq. (2-130) of the above reference),

$$\frac{A}{R=1} \langle r_R^2 \rangle = \frac{\pi}{M \omega_0} \sum_{R=1}^{A} (N_R + \frac{3}{2}) = \frac{3}{5} A R^2$$

where A = N + 2 is the nuclear mass number, while the nuclear radius  $R = r_0 A'^3$ , with  $r_0 = 1.2 \, \mathrm{fm}$ , the nuclear radius  $R = r_0 A'^3$ , with  $r_0 = 1.2 \, \mathrm{fm}$ , It is of notice that  $N_h$  is the oscillator principal quantum number associated with the stat R (cf. Fig. 2-23 Bohr and Mottels on, 1969).

The average internucleon distance can be determined from the relation (Brink and

Broglia, 2005, App. C)

$$a' = \left(\frac{V}{A}\right)^{1/5} = \left(\frac{4\pi R^3}{A}\right)^{1/3} = \left(\frac{4\pi}{3}\right)^{1/3} \times 1.2 fm.$$

$$\approx 2 fm$$

Thus,

$$\Delta_L = \frac{\sqrt{3}R}{2fm} \approx 2.3, \quad (A \approx 120).$$

While it is difficult to compare crystal, aperiodic finite crystal and atomic nuclei, arguebly, the above value indicates that a nucleus is liquid-like. More precisely, it is made out of a non-Newtonian fluid, which reacts elastically to sudden sollicitations, and plastically to strain. In any case, one expects from A=2,3 that mean free path is long, larger than nuclear dimensions.

## Quantality parameter

In quantum mechanics, the zero-point Rinetic energy, ~ 12/Maz, involved in the localitation of a particle within a volume of rodius a implies that the lowest energy state the particle, may be delocalized becomes the potential energy gain of the retarnical configuration of fixed particles which minimize U is overwhelmed by the quantal lametic energy. Such delocalized quantal fluids essential energy broviole the basis for discussing the state of electrons in atoms, and metals, of the He atoms in the ground state of the He liquids (bot fermionic 3He, and bosonic 4He), and the state of nucleons in the ground state of atomic nuclei &, a (non-newtonian) quantum fluid.

The relative magnitude of the quantal kinetic energy of the localized state compared with the potential energy can be qualitatively characterized by the quantality para-

meter (Nottelson, 1998)

$$K = \frac{\hbar^2}{Ma^2} \frac{1}{|V_0|}$$

where Misthe mass of the undividual particles, while vo and a measure the strength of the attraction and the range corresponding to the minimum of the potential, respectively. When K is small, quantal effects are small and the lowest state of the system

is expected to have a crystalline structure, while for sufficiently large values of K, the system will remain a quantum fluid even in its ground state.

The values of the force parameters and the venilting quantality parameters for several conclused matter systems are collected in Table 2. For mudei we have two sets. One associated with the bone NN-interaction ("So channel),

and another with the induced pairing interaction

00 ≈ R (=1,2 A'3 fm); Vo ≈ -0.5 MeV. It is seen that the transition between quantum liquid and crystalline solid occurs at K ≈ 0.1 (between He and Hz). Thus brucher are expected to display a (non-new-tomian) quantum liquid structure.

					1	
Constituents		May	a ccm7	Vollev)	K	phase T=0
3He		3	2.9(10-8)	8.6 (10-4)	0.19	liquid
4 He		4	2.9(10-8)	8.6 (10-4)	0.14	liquid
H2		a	3.3(10-8)	32 (10-4)	0,06	Golid
1.0		20	3.1(10 <sup>8</sup> )	31 (10-4)	0.007	Solid
nucleons.	bare	1	9 (10-14)	100 (106)	0,5	liquid
a) unit	<u> </u>	1	60(10-1.4)	0.5(106)	2.0	liquid

a) units of nucleon mass b) 150 NN-Argonne VIII

Table 2 Quantality parameter.
After Mottel's on, 1998

The results discussed above, namely that K«1 mplies localization, that is fixed relations between the constituents, and thus spontaneous symmetry breaking, while K>0.14 implies delocalization and thus homogeneity is an example of the fact that while potential energy always prefer special arrangements, fluctuations, classical or quantal, favour symmetry.

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