Quadrupole Pairing States of higher energy correspond to β and γ vibrations. pairing vibrations. B(E2) values Two-particle transfer reactions among members of the ground state rotational superfluid band are proportional to the square of the intrinsic static quadrupole moment Qo whereas transitions from the ground state band to an excited band have $B(E2; I_t \to I_f) = |\langle K_f | \mathcal{M}(E2, \nu) | K_t \rangle|^2 \langle I_t K_t 2K_f - K_t | I_f K_f \rangle^2$ $\sigma(g.s. \rightarrow p.v.) \approx |\langle p.v. | T(\Delta) | g.s. \rangle|^2$ Typical values for strongly distorted nuclei are $B(E2; 2^+ \to 0^+) \approx 100 B_{ep}$ $\sigma(g.s.(A) \rightarrow g.s.(A+2)) \approx 50 \sigma_{sp}$ $B(E2; 2'^+ \rightarrow 0^+) \approx 3 B_{ep}$ $\sigma(g.s.(A) \rightarrow p.v.(A + 2)) \approx 1 \sigma_{2p}$ For small values of χ G the system has $Q_0 = 0$ $\Delta = 0$ and the system displays a typical phonon spectrum. Angular momentum The number of particles is conserved and each phonon carries $I^{\pi} = 2^+$ has $\alpha = \pm 2$ It corresponds to oscillations of Δ around $\Delta_{eq} = 0$. of the surface around $Q_0 = 0$. The energy is given by $\mathcal{S}_Q = (n + \frac{5}{2}) \hbar \omega_Q$ $\mathcal{E}_p = (n+1) \hbar \omega_p$ n = number of pairing phonons n = number of quadrupole phonons ω_p = frequency of the pairing mode ω_{σ} = frequency of the quadrupole mode The microscopic RPA wave function of a one-phonon state is given by $=\sum_{\omega,\gamma}\left\{\frac{\langle\omega\parallel r^{2}Y_{1}\parallel\gamma\rangle}{\varepsilon_{\omega}+\varepsilon_{\gamma}-\hbar\omega_{q}}\left[c_{\omega}^{+}c_{\nu}\right]^{2}+\frac{\langle\omega\parallel r^{2}Y_{1}\parallel\gamma\rangle}{\varepsilon_{\omega}+\varepsilon_{\gamma}+\hbar\omega_{q}}\left[c_{\nu}^{+}c_{\omega}\right]^{2}\right\}\left|\tilde{0}\rangle_{q}\right\}$ $=\sum_{\omega,\gamma}\left\{\frac{\langle\omega\parallel r^{2}Y_{1}\parallel\gamma\rangle}{\varepsilon_{\omega}+\varepsilon_{\gamma}-\hbar\omega_{q}}\left[c_{\omega}^{+}c_{\nu}\right]^{2}+\frac{\langle\omega\parallel r^{2}Y_{1}\parallel\gamma\rangle}{\varepsilon_{\omega}+\varepsilon_{\gamma}+\hbar\omega_{q}}\left[c_{\nu}^{+}c_{\omega}\right]^{2}\right\}\left|\tilde{0}\rangle_{q}\right\}$ $=\sum_{\omega,\gamma}\left\{\frac{\langle\omega\parallel r^{2}Y_{1}\parallel\gamma\rangle}{\varepsilon_{\omega}+\varepsilon_{\gamma}-\hbar\omega_{q}}\left[c_{\omega}^{+}c_{\nu}\right]^{2}+\frac{\langle\omega\parallel r^{2}Y_{1}\parallel\gamma\rangle}{\varepsilon_{\omega}+\varepsilon_{\gamma}+\hbar\omega_{q}}\left[c_{\nu}^{+}c_{\omega}\right]^{2}\right\}\left|\tilde{0}\rangle_{q}\right\}$ $|2^{+}\rangle = \Gamma_{2+}^{+} |\tilde{0}\rangle_{0}$ c,+ creates a "Mayer-Jensen" particle. Because of the conservation of number of particles angular momentum at least two-phonons are required to build an excited state in the nucleus Ao a $J^{\pi} = 0^+$ state $|0'^{+}\rangle = \Gamma_{\alpha}^{+}\Gamma_{r}^{+} |\tilde{0}\rangle_{n}$ $|0'^{+}\rangle = [\Gamma_{2+}^{+}\Gamma_{2+}^{+}]^{\circ} |\tilde{0}\rangle_{\sigma}$ The cross section ratio The electromagnetic transition probabilities $\frac{\sigma(g.s.(A_0-2)\to p.v.(A_0))}{\sigma(g.s.(A_0-2)\to g.s.(A_0))}\approx 1$ $\frac{B(E2; 0'^+ \to 2^+)}{B(E2; 2^+ \to 0^+)} \approx 1$ $\sigma(g.s.(A_0-2) \rightarrow g.s.(A_0)) \approx 10 \sigma_{2p}$ and $B(E2; 2^+ \rightarrow 0^+) \approx 20 B_{sp}$ $\sigma(g.s.(A_0) \rightarrow 0'(A_0 + 2)) \approx 0$ $B(E2; 2'^+ \to 0^+) \approx 0$ where A_0 represents the closed-shell system.