$$H = T + v = \underbrace{T + U + V_p}_{\text{mean field}} + (v - U - V_p)$$

Kramers degeneracy $v\bar{v}$ diagonalization $\alpha_{\nu}^{\dagger} = U_{\nu} a_{\nu}^{\dagger} - V_{\nu} a_{\bar{\nu}};$

ground state

$$|\tilde{0}\rangle = \prod_{\nu>0} \alpha_{\nu} \alpha_{\bar{\nu}} |0\rangle \sim \prod_{\nu>0} \left(U_{\nu} + V_{\nu} a_{\nu}^{\dagger} a_{\bar{\nu}}^{\dagger} \right) |0\rangle$$

$$a_{\nu} |0\rangle$$
Ansatz 1: $|\tilde{0}\rangle$ sharp step-funct. occ.

$$|HF\rangle = \prod_{i>0} a_i^{\dagger} a_i^{\dagger} |0\rangle = \prod_i a_i^{\dagger} |0\rangle$$

$$1$$

$$V_{\nu}^2$$
independent motion (for each order)
$$i \quad \varepsilon_F \quad k$$

independent particle motion (fermions)

Ansatz 2: $|\tilde{0}\rangle$ sigmoidal distr. occ.

$$|BCS\rangle = \prod_{\nu>0} \left(U_{\nu} + V_{\nu} a_{\nu}^{\dagger} a_{\bar{\nu}}^{\dagger} \right) |0\rangle$$

$$1 \qquad \qquad \text{independent pair motion (bosons)}$$