

$$P(y^* | y) = \frac{P(y^*, y)}{K \leftarrow P(y)}$$

می دانیم

$$P(y^*, y) = \frac{1}{K} \frac{1}{(2\pi)^{n/2} |\Sigma|} \left( -\frac{1}{2} (x - \mu)^T \Sigma^{-1} (x - \mu) \right) =$$

مراحل کلی

$$P(y^*, y) = \frac{1}{K_r} \exp \left\{ -\frac{1}{2} \begin{bmatrix} y \\ y^* \end{bmatrix}^T \Sigma^{-1} \begin{bmatrix} y \\ y^* \end{bmatrix} \right\} =$$

$$= \frac{1}{K_r} \exp \left\{ -\frac{1}{2} \begin{bmatrix} y \\ y^* \end{bmatrix}^T \begin{bmatrix} K(x, x) & K(x, x^*) \\ K(x^*, x) & K(x^*, x^*) \end{bmatrix} \begin{bmatrix} y \\ y^* \end{bmatrix} \right\} =$$

$$= \frac{1}{K_r} \exp \left\{ -\frac{1}{2} \left[ y^T K(x, x) + y^{*T} K(x^*, x) + y K(x, x^*) + y^* K(x^*, x^*) \right] \right\}$$

$$= \frac{1}{K_r} \exp \left\{ -\frac{1}{2} \left[ y^T y K(x, x) + y^{*T} y K(x^*, x) + y y^* K(x, x^*) + y^T K(x^*, x^*) y^* \right] \right\}$$

$$= \frac{1}{K_r} \exp \left\{ -\frac{1}{2} \left[ y^{*T} K(x^*, x^*) y^* + 2 y^* K(x, x^*) y \right] \right\}$$

$$K(x, x^*) = K(x^*, x)$$

که اگر باند دوم و عقاب یعنی دساده یعنی به عبارت زیری رسم:

$$= \exp \left( (x - \mu)^T \Sigma^{-1} (y - \mu') \right)$$

$$\mu = -K(x, x) K(x, x^*) y$$

$$\Sigma = K(x, x)$$