Exercise 5.1 Write each symbolic sentence in two ways:

- (i) without any symbol, apart from f.
- (ii) with symbols only, using quantifiers.
 - 1. i The value of f at the origin is rational.

ii
$$\exists r \in Q, f(0) = r$$
.

2. i The value of function f at each point is its corresponding point.

ii
$$\forall x \in R, f(x) = x$$
.

3. i The function f is constant.

ii
$$\exists y \in R, \forall x \in R, f(x) = y.$$

4. i The value of function f, for all integers, is zero.

ii
$$\forall x \in Z, f(x) = 0.$$

5. i The zeros of f include all integers.

ii
$$\forall x \in Z, f^{-1}(0) = x$$
.

6. i Both integers and natural numbers have the same image under f.

ii
$$\forall x \in Z, \forall y \in Nf(x) = f(y)$$
.

7. i The rational numbers have no rational value under f.

ii
$$\nexists x \in Q, f(x) \in Q$$

Exercise 5.3 Write each symbolic sentence without symbols, apart from f.

- 1. The zeros of f include all even integers.
- 2. The function f is identically zero for negative values of the argument.
- 3. The composition of the function f with itself is the Identity function.
- 4. The function f is non-zero at the closed interval of zero to one.
- 5. The value of function f is not rational for any natural number.