Multi cell LSTM

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1 Introduction

In this document we formulate new extension of long short-term memory (LSTM) recurrent neural network.

1.1 Conventional LSTM

Let $x_t \in \mathbb{R}^{D_x}$ be input vectors. LSTM state $(c_t, h_t)^T$ is defined by:

$$\begin{aligned}
i_t &= \sigma(W^i x_t + U^i h_{t-1} + b^i) \\
f_t &= \sigma(W^f x_t + U^f h_{t-1} + b^f) \\
o_t &= \sigma(W^o x_t + U^o h_{t-1} + b^o) \\
\tilde{c}_t &= \tanh(W^c x_t + U^c h_{t-1} + b^c)^{,} \\
c_t &= f_t \bullet c_{t-1} + i_t \bullet \tilde{c}_t \\
h_t &= o_t \bullet \tanh(c_t),
\end{aligned} \tag{1}$$

Where i_t, f_t, o_t are calles input, forget and output gates, $\tilde{c}_t$ - candidate cell vector, c_t - cell vector, and h_t - hidden state vector. All aforementioned variables are D_h- dimensional. By $\bullet$ we denote element-wise multiplication. Parameter count of LSTM is:

$$N = 4 \cdot D_h \cdot (D_x + D_h + 1), \tag{2}$$

and state is defined by $2D_h$ variables. c_t may be interpreted as internal memory of LSTM, while h_t - represent its content, exposed by the output gate.

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1.2 Multi cell LSTM

The internal memory of LSTM, c_t, shares the same dimension with h_t. However, according to our intuition c_t should be able to store more information than h_t. We hypothesise, that extension of c_t may increase effectiveness of LSTM approach. We suggest multi-cell variant of LSTM (MCLSTM) with D_p cells, assembled into $D_h \times D_p$ matrix C_t. Internal attention p_t controls importance weights of individual cells (columns of C_t).

$$\begin{aligned}
i_t &= \sigma(W^i x_t + U^i h_{t-1} + b^i) \in \mathbb{R}^{D_h} \\
f_t &= \sigma(W^f x_t + U^f h_{t-1} + b^f) \in \mathbb{R}^{D_h} \\
o_t &= \sigma(W^o x_t + U^o h_{t-1} + b^o) \in \mathbb{R}^{D_h} \\
p_t &= \text{softmax}(W^p x_t + U^p h_{t-1} + b^p) \in \mathbb{R}^{D_p} \\
\tilde{C}_t &= \tanh(W^c x_t + U^c h_{t-1} + b^c) 1^T \in \mathbb{R}^{D_h \times D_p} \\
C_t &= (f_t p_t^T) \bullet C_{t-1} + (i_t p_t^T) \bullet \tilde{C}_t \in \mathbb{R}^{D_h \times D_p} \\
h_t &= \frac{1}{D_p} o_t \bullet (\tanh(C_t) 1) \in \mathbb{R}^{D_h}
\end{aligned}, \tag{3}$$

Parameter count of multi cell LSTM is:

$$N = (4 \cdot D_h + D_p) \cdot (D_x + D_h + 1), \tag{4}$$

and state is defined by $D_h(D_p + 1)$ variables.

The implementation of MCLSTM can be downloaded from: `https://github.com/povidanius/multi_cell_lstm`